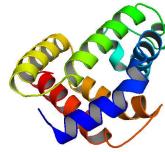


## Protein Structure Determination II



Scott McAllister  
Princeton University  
CS597A, Fall 2005



## Protein Structure Prediction

### Amino acid sequence [PDB: 1q4sA ]

MHRTSGNSHATGGNLPDVASHYPVATEGTLDGTVFVIDEMTPERATASVEVTDLRQRWGLVHGGAYCALAEMLA  
TEAVTAVHEKGMMAVGGSNHTSFRRPVKEGHRAEAVRHAGSTTWFWDVSLRDDAGRLCAVSSMSIAVRPRD

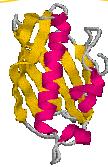
### Helical structure

MHRTSGNSHATGGNLPDVASHYPVATEGTLDGTVFVIDEMTPERATASVEVTDLRQRWGLVHGGAYCALAEMLA  
TEAVTAVHEKGMMAVGGSNHTSFRRPVKEGHRAEAVRHAGSTTWFWDVSLRDDAGRLCAVSSMSIAVRPRD

### Beta strand and sheet structure

MHRTSGNSHATGGNLPDVASHYPVATEGTLDGTVFVIDEMTPERATASVEVTDLRQRWGLVHGGAYCALAEMLA  
TEAVTAVHEKGMMAVGGSNHTSFRRPVKEGHRAEAVRHAGSTTWFWDVSLRDDAGRLCAVSSMSIAVRPRD

### 3D Protein Structure



## Outline

- Notable Methods
- ASTRO-FOLD Framework
  - $\alpha$ -helix Prediction
  - $\beta$ -sheet Prediction
  - Interhelical contact prediction
  - Derivation of Restraints
  - Generation of additional distance bounds
  - Tertiary Structure Prediction
- Results
- Discussion

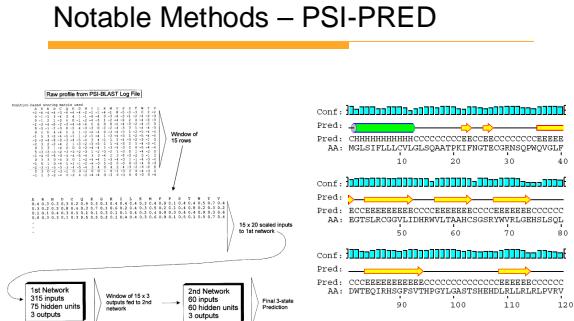


## Notable Methods – PSI-PRED

### Notable Methods – PSI-PRED

- Prediction of Secondary Structure
- 3 stages:
  - Generation of a sequence profile
    - PSI-BLAST on non-redundant database
    - Creates PSSM for later input
  - Prediction of initial secondary structure
    - Neural network (Feed forward, back propagation)
  - Filtering of the predicted structure
- Web server:  
<http://bioinf.cs.ucl.ac.uk/psipred>

Jones, DT. *J. Mol. Biol.* (1999)



Jones, DT. *J. Mol. Biol.* (1999)

## Notable Methods - RAPTOR

- Fold recognition method as optimization problem
- Scoring function that accounts for
  - mutation
  - environment
  - gaps
  - secondary structure
  - pairwise interactions

Xu, J and M. Li. *J. Bioinf Comput Biol.* (2003)

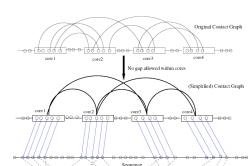


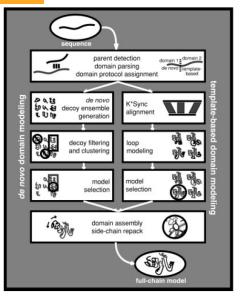
Fig. 1. Template contact graph and its version of collapsed contacts and arcs. A dashed arc represents a native contact that is not in the original contact graph, representing an interaction between the two connected residues. A dashed arc means that if two query sequence residues are connected by an arc in the original contact graph, they are not connected by an arc in the collapsed contact graph. The collapsed contact graph is used to calculate the energy function. The interaction score between two segments of the query sequence is calculated by summing the interaction scores of two separate native contacts that are aligned by two intersected template contacts.

$$\min W_m E_m + W_s E_s + W_p E_p + W_g E_g + W_{ss} E_{ss}$$



## Notable Methods – Robetta

- Combines template-based and ab initio approach
  - Uses template if available, otherwise starts with ab initio
- Also includes methods to detect domains and model loops



D. Chivian et al. *Proteins*. (2003)

## Notable Methods – Skolnick

- Combine aspects of comparative modeling/fold recognition/ab initio
- Apply clustering algorithm to select among conformers

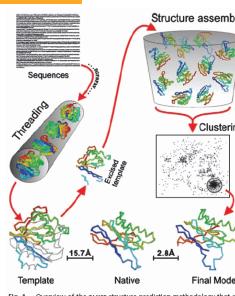


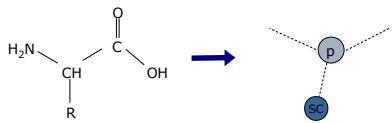
Fig. 1. Overview of the Nasus structure prediction methodology that consists of template identification by thermonexx threading algorithm (6), CAS fragment assembly, and fold selection by smexx clustering (18). The entire process for *Lay6* is shown as an example.



Zhang, Y. and J. Skolnick. *PNAS*. (2004)

## Notable Methods - UNRES

- United Residue approach
- Represent each protein as unified peptide group and unified side chain



- Minimize with this coarse force field, then refine a detailed atomistic force field

Liwo, et al. *J. Comput Chem*. (1997a,b)



## Notable Methods – PREDICT

- Method for the structure prediction of membrane proteins, especially GPCRs
- Does NOT rely on homology to rhodopsin
- Approach
  - Generation of a large number of protein "decoys"
  - Simultaneous optimization and scoring of decoys
    - Optimization includes helix orientations, helix vertical alignments, helix positions, π-stacking of aromatic residues, helical tilts

Shacham, S. *Proteins*. (2004)



## Notable Methods – Available Servers

- 3D Jury (consensus)
  - <http://bioinfo.pl>
- 3D-pssm/phyre
  - <http://www.sbg.bio.ic.ac.uk/~3dpssm/>
- 123D+
  - <http://123d.ncicrf.gov/run123D+.html>
- FFAS03
  - <http://ffas.ljcrf.edu/ffas-cgi/cgi/ffas.pl>
- FOREST
  - <http://abs.cit.nih.gov/foresst2/>

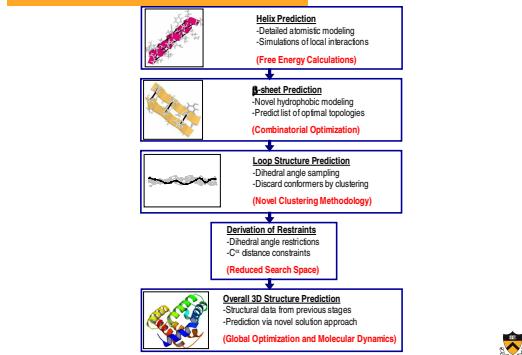


## Notable Methods – Available Servers

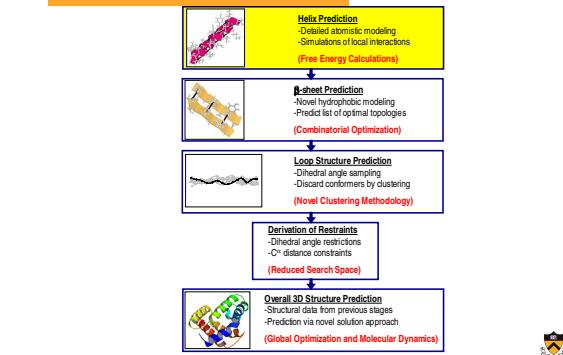
- 3GenesilicoD Jury (consensus)
  - <http://genesilico.pl/meta/>
- PredictProtein
  - <http://cubic.bioc.columbia.edu/predictprotein>
- mGenTHREADER/PSIPRED
  - <http://bioinf.cs.ucl.ac.uk/psipred/psiform.html>
- Robetta
  - <http://robbetta.bakerlab.org>



## ASTRO-FOLD



## ASTRO-FOLD



## Helix Formation

- Physical characteristics
  - Well-defined backbone and hydrogen bonding patterns
- Physical understanding
  - Local forces: Hierarchical folding
  - Non-local forces: Hydrophobic collapse
- Experimental Evidence
  - Helix formation occurs rapidly
  - Sequence is sufficient to identify initiation/termination

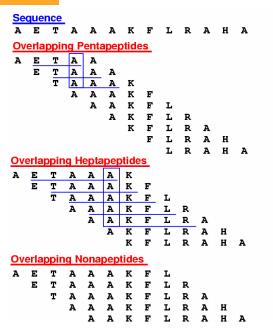


Klepeis, JL and Floudas, CA. *J. Comput. Chem.* (2002)



## Dividing the problem

- Decompose sequence into smaller, overlapping oligopeptides
- Captures local interactions
- Free energy calculations on oligopeptides combined to yield overall prediction



Klepeis, JL and Floudas, CA. *J. Comput. Chem.* (2002)



## Helix Prediction – Key Ideas

### Overlapping oligopeptides

Decompose polypeptide to identify local sites of helix formation and termination

### Ensemble of low energy states

Calculate properties of proteins using data from many low energy states rather than a single state

### Free energy calculations Klepeis & Floudas 2000

Model proteins using detailed energy calculations including entropic and solvation contributions

### Deterministic global optimization Floudas 2000

Predict low energy states using powerful global optimization approaches such as aBB

Klepeis, JL and Floudas, CA. *J. Comput. Chem.* (2002)

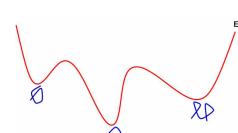


## Generating an ensemble

- Create low energy states and the global minimum state



- Formulated as a nonconvex optimization problem
  - requires global optimization techniques



Klepeis, JL and Floudas, CA. *J. Comput. Chem.* (2002)



## Overall Gibbs Free Energy

- Potential**  
Scheraga & coworkers  

$$\sum_{i \in \text{MB}} c_i \left[ \left( \frac{r_{ij}^2}{r_{ci}} \right)^{12} - \left( \frac{r_{ij}^2}{r_{ci}} \right)^6 \right] + \sum_{i \in \text{MB}, j \in \text{SA}} c_{ij} \left[ \left( \frac{r_{ij}^2}{r_{ci}} \right)^{12} - \left( \frac{r_{ij}^2}{r_{ci}} \right)^6 \right] + \sum_{i \in \text{MB}} \frac{332}{D \pi r_{ci}^2} q_i q_j + \sum_{k \in \text{GB}} \frac{A_k}{2} (1 \pm \cos \alpha_k \phi_k)$$
- Entropic**  

$$-\frac{k_B}{2} \ln [\text{Det}(H_{\text{vac},\gamma})]$$
- Cavity**  
Honig & coworkers  
1988, 1993, 1995  
  

$$F_{\text{cavity}} = \gamma(SA) + b$$
- Polarization**  
Honig & coworkers  
1988, 1993, 1995  
  

$$F_{\text{solv}} = F_{\text{polar}}(\varepsilon=80) + F_{\text{polar}}(\varepsilon=1)$$
- Ionization**  
Honig & coworkers  
1988, 1993, 1995  
  

$$F_{\text{ioniz}} (\text{pH}) = kT \ln Z$$

Klepeis, JL and Floudas, CA. *J. Comput. Chem.* (2002)

$$\begin{aligned} F_{\text{vac}} &= - \\ TS_{\text{vac}} &+ \\ F_{\text{cavity}} &+ \\ F_{\text{solvation}} &+ \\ F_{\text{ionization}} & \end{aligned}$$



## Helix Formation Probability

- Calculate probability of conformer  $i$  from free energy

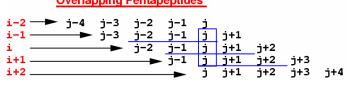
$$p_i = \frac{\exp[-\beta(F_o - F_i)]}{\sum_j \exp[-\beta(F_o - F_j)]}$$

- Use to calculate probability of cluster formation for particular oligopeptide

$$p_{\text{AAA}} = \sum_{i \in \text{AAA}} p_i$$

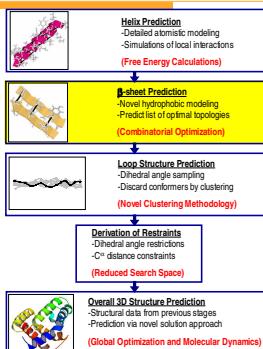
Sequence  
j-4 → j-3 → j-2 → j-1 → j → j+1 → j+2 → j+3 → j+4

Overlapping Pentapeptides



Klepeis, JL and Floudas, CA. *J. Comput. Chem.* (2002)

## ASTRO-FOLD



Klepeis, JL and Floudas, CA. *Biophys J.* (2003)

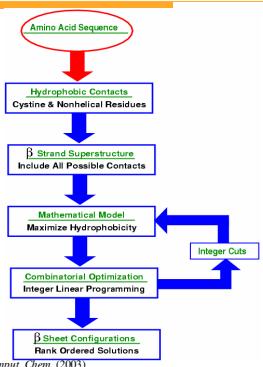
## β-sheet Formation

- Major challenge for protein structure prediction
  - β-strand location not accurate
  - Topology prediction not reliable
- Physical understanding
  - Local forces not as important
  - Non-local forces (hydrophobic collapse) dominate
- Experimental evidence
  - Hydrophobic collapse proceeds rapidly



Klepeis, JL and Floudas, CA. *J. Comput. Chem.* (2003)

## β-sheet Prediction Flowchart



Klepeis, JL and Floudas, CA. *J. Comput. Chem.* (2003)

## β-sheet Prediction

- Residue-based aspect
  - Identify set of residues  $i$ , and the associated hydrophobicity,  $H_i$
  - Binary variables introduced for residue-residue contact



- Strand-based aspect
  - Identify set of strands  $s_i$ , and the associated weight  $S_{s_i}$
  - Binary variables introduced for strand-strand contacts



Klepeis, JL and Floudas, CA. *J. Comput. Chem.* (2003)

## B-sheet Formulation: Key Concepts

### Binary variables

0-1 variables are used to characterize residue-to-residue and strand-to-strand contacts

### Linear objective function

Objective is to maximize the hydrophobic potential as controlled by the binary variables

### Linear constraints

Constraints account for different combinations of residue and strand contacts (e.g., parallel/antiparallel)

### Integer cuts

Iterative addition of these constraints allow for the generation of a ranked list of optimal solutions

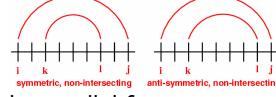
Klepeis, JL and Floudas, CA. *J. Comput. Chem.* (2003)



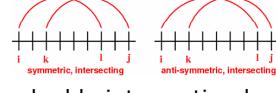
Klepeis, JL and Floudas, CA. *J. Comput. Chem.* (2003)

## $\beta$ -sheet Constraints

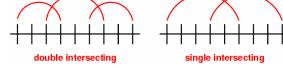
### Allowable antiparallel forms



### Allowable parallel forms



### Disallow double intersecting loops



Klepeis, JL and Floudas, CA. *J. Comput. Chem.* (2003)



## $\beta$ -sheet Objective Function

### Maximizing hydrophobic potential

$$\max \sum_i \sum_{j, P(i) + 2 < P(j)} (H_i + H_j + H_{ij}^{\text{add}}) y_{ij}$$

$$+ \sum_{si} \sum_{sj, Q(si) < Q(sj)} (S_{si} + S_{sj}) w_{si,sj}$$

$$y_{ij} = \begin{cases} 1 & \text{if } i, j \text{ form contact} \\ 0 & \text{if } i, j \text{ do not form contact} \end{cases} \quad \forall i < j$$

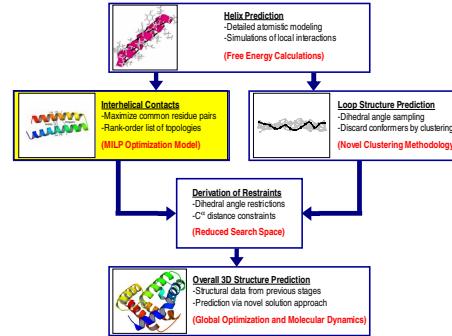
$$w_{si,sj} = \begin{cases} 1 & \text{if } si, sj \text{ form contact} \\ 0 & \text{if } si, sj \text{ do not form contact} \end{cases} \quad \forall si < sj$$

Klepeis, JL and Floudas, CA. *J. Comput. Chem.* (2003)



Klepeis, JL and Floudas, CA. *J. Comput. Chem.* (2003)

## ASTRO-FOLD for $\alpha$ -helical Bundles



McAllister, SR and Floudas, CA. *Proceedings, BIOMAT Conference* (2005).



## Dataset Selection

### Protein Sources

- 229 PDBSelect25<sup>1</sup> database
- 62 CATH<sup>2</sup> database
- 20 Zhang et al.<sup>3</sup>
- 7 Huang et al.<sup>4</sup>

### Restrictions

- No  $\beta$ -sheets, at least 2  $\alpha$ -helices
- No highly similar sequences

### Dataset

- 318 proteins in the database set

McAllister, SR, et al. (submitted 2005)

<sup>1</sup>Hobohm, U. and C.Sander. *Prot Sci* 3 (1994) 522.

<sup>2</sup>Orengo, C.A. et al. *Structure* 5 (1997) 1093.

<sup>3</sup>Zhang, C. et al. *PNAS* 99 (2002) 3581.

<sup>4</sup>Huang, E.S. et al. *J Mol Biol* 290 (1999) 267.



## Probability Development

### Contact Types

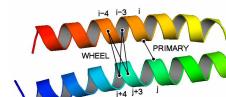
#### ▪ PRIMARY contact

- Minimum distance hydrophobic contact between 4.0 Å and 10.0 Å

#### ▪ WHEEL contact

- Only WHEEL position hydrophobic contacts between 4.0 Å and 12.0 Å

### Classified as parallel or antiparallel contacts



McAllister, SR, et al. (submitted 2005)



## Model Overview

- Formulation: Maximize interhelical residue-residue contact probabilities
  - Binary variable  $y_{m,n}^A$  indicates antiparallel helical contact
  - Binary variable  $w_{i,j}^{m,n}$  indicates residue contact
- Goal: Produce a rank-ordered list of the most likely helical contacts
  - Contacts used to restrict conformational space explored during protein tertiary structure prediction

McAllister, SR, et al. (submitted 2005)



## Pairwise Model Objective

- Level 1 Objective
  - Maximize probability of pairwise residue-residue contacts

$$\begin{aligned} \max & \quad \sum_m \sum_n y_{mn}^a \cdot \sum_i \sum_j w_{ij}^{mn} \cdot p_{ij;mn}^a \\ & + \sum_m \sum_n y_{mn}^p \cdot \sum_i \sum_j w_{ij}^{mn} \cdot p_{ij;mn}^p \\ & y_{mn}^a, y_{mn}^p, w_{ij}^{mn} = \{0, 1\} \end{aligned}$$

McAllister, SR, et al. (submitted 2005)



## Pairwise Model Constraints

- Level 1 Constraints
  - At most one contact per position

$$\sum_{j:j>i} w_{ij} + \sum_{j:j< i} w_{ij} \leq 1$$

- Helix-helix interaction direction

$$y_{mn}^a + y_{mn}^p \leq 1 \quad \forall(m, n)$$

- Linking interaction variables

$$w_{ij}^{mn} \leq y_{mn}^a + y_{mn}^p$$

$$y_{mn}^a + y_{mn}^p - \sum_i \sum_j w_{ij}^{mn} \leq 0$$

McAllister, SR, et al. (submitted 2005)



## Pairwise Model Constraints

- Level 1 Constraints
  - Limit helical kinks

$$w_{ij}^{mn} + w_{i'j'}^{mn} \leq 1 \quad \forall(i, i', j, j') : |diff(i, i')| - |diff(j, j')| \leq 2$$

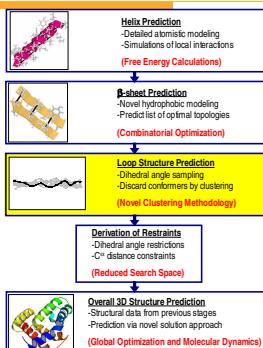
or either  $|diff(i, i')| \leq 5$  or  $|diff(j, j')| \leq 5$



McAllister, SR, et al. (submitted 2005)



## ASTRO-FOLD



Klepeis, JL and Floudas, CA. *Biophys J.* (2003)



## Loop Prediction - Methodology

### Create ensemble by dihedral angle sampling

- extracted  $p(\phi, \psi)$  from  $\sim 2500$  loops
- sampled  $p(\phi, \psi)$  at  $5^\circ \times 5^\circ$  resolution
- created ensembles of 2000 conformers for each loop



### Structure optimization with first principles force field

- Dunbrack rotamer library
- ECEPP/3 force field for structure optimization

### Clustering to identify conformers that are close to native

Mönnigmann, M. and Floudas, CA. *Proteins.* (2005)



## Loop Prediction – New Use of Clustering

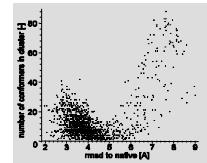
- Clustering has been used **before** to
  - **Group** conformers
  - **Select** conformers that represent groups
- **New use** of clustering
  - **Discard** conformers that are far from native
- First steps of approach
  - Choose RMSD threshold  $t$
  - Calculate pairwise RMSD values for the ensemble
  - For each conformer, record number of conformers with  $\text{RMSD} \leq t$

Mönnigmann, M. and Floudas, CA. *Proteins.* (2005)



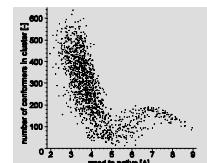
## Loop Prediction – Clustering Example

- threshold  $\approx 3.0\text{\AA}$
- large clusters for small RMSDs unfortunately also for large RMSDs
- not always advisable to consider centroid of largest cluster



Mönnigmann, M. and Floudas, CA. *Proteins.* (2005)

- threshold  $\approx 3.5\text{\AA}$
- increasing threshold shows that clusters with large RMSDs are small basins only
- large clusters with small RMSDs survive



## Loop Prediction – Clustering Example

- threshold  $\approx 4.0\text{\AA}$
  - for sufficiently large threshold distribution is monotonous
  - tail with large RMSDs becomes apparent
- 
- threshold  $\approx 4.5\text{\AA}$
  - distribution more conservative the larger threshold
  - for sufficiently large threshold clusters of conformers with large RMSDs can be discarded

Mönnigmann, M. and Floudas, CA. *Proteins.* (2005)



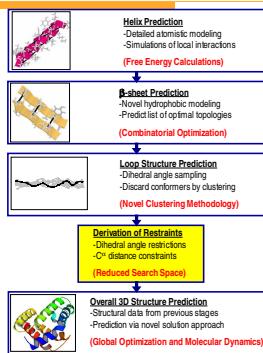
## Loop Prediction – Clustering Algorithm

1. Choose threshold  $t$ , choose critical cluster size  $N_{crit}$
2. Calculate cluster sizes  $N_i$  for all conformers in ensemble
3. If  $N_i > N_{crit}$  for all  $i$ , stop
4. Discard conformers that generate clusters of size  $N_i < N_{crit}$
5. Go back to step 2

Mönnigmann, M. and Floudas, CA. *Proteins.* (2005)



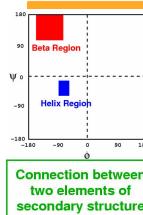
## ASTRO-FOLD



Klepeis, JL and Floudas, CA. *Biophys J.* (2003)



## Derivation of Restraints

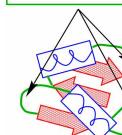


### Dihedral angle restraints

- Backbone **dihedral angles** restrained according to classification of residue as either helix or strand

### Distance restraints

- $C^{\alpha}-C^{\alpha}$  distance restraints for **hydrogen bond network of helix** (residues  $i$  and  $i+4$ )
- $C^{\alpha}-C^{\alpha}$  distance restraints for **predicted interhelical contacts**



Klepeis, JL and Floudas, CA. *Biophys J.* (2003)



### Bounds on loop residues

- Based on **dihedral angle deviation** of **best identified conformer** from loop clustering analysis



## Hybrid Algorithm Motivation

- o  $\alpha$ BB Features
  - n Global minimum guarantee
  - n Rigorous upper and lower bounds
  - n Rigorous termination
  - n Slow performance
- o CSA Features
  - n Stochastic global minimum search
  - n Provides upper bound on solution
  - n Heuristic termination
  - n Faster performance

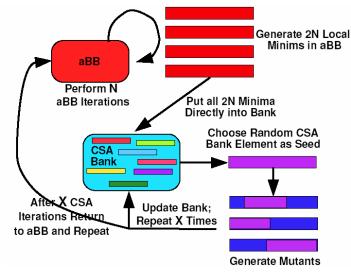
Klepeis, JL, et al. *Biophys J.* (2003)



## Alternating Hybrids

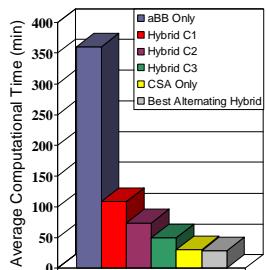
- o Approach
  - n Use output of a series of  $\alpha$ BB runs to fill the CSA bank
  - n A number of CSA iterations are performed before refilling the bank with additional  $\alpha$ BB solutions

Klepeis, JL, et al. *Biophys J.* (2003)



## Hybrid Performance

- o Runs on met-enkephalin
  - n Hybrids identified global minimum structure (rigorous)
  - n Best alternating hybrid faster than CSA only!

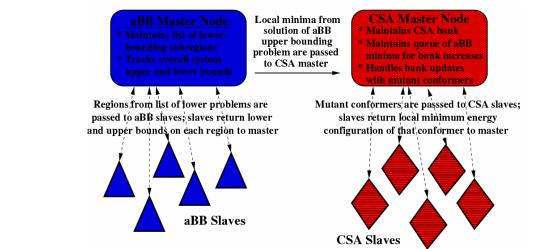


Klepeis, JL, et al. *Biophys J.* (2003)

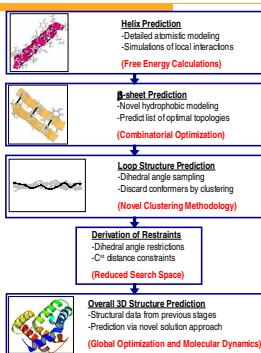


## Parallelization

- o Protein runs scale as  $(N_{\text{res}})^{2-4}$
- o Implement as distributed method
  - n Two "master" nodes:  $\alpha$ BB and CSA



## ASTRO-FOLD



Klepeis, JL and Floudas, CA. *Biophys J.* (2003)



## Secondary Structure Prediction Results

- o Applied to a number of CASP5 targets

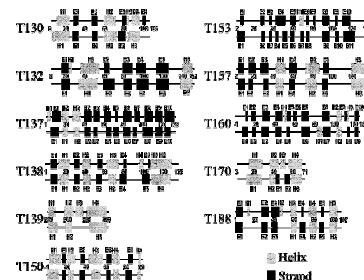


FIGURE 11. Comparison of predictions for beta-sheets and strands versus experimental observations. For each target, the gray line represents the secondary structure content of the experimentally determined structure, and the colored line identifies the subsequent prediction made.

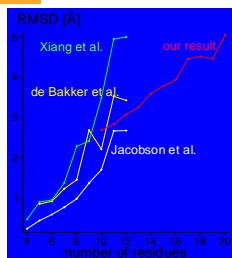
Klepeis, JL and Floudas, CA. *Biophys J.* (2003)



## Loop Prediction – Results Comparison

- Comparison difficult
  - flexible stem residues
  - fixed stems in all previous results
- we solve harder problem
  - number of residues includes 3+3 stem residues in our case
  - stem residues have tighter probability distributions

- Results of comparison
  - Jacobson et al. result with fixed stems better
    - use information on stem geometry, if available
  - new method results in very favorable slope
  - new method is better than or only slightly worse than methods for fixed stems



Münningmann, M. and Floudas, CA. *Proteins*. (2005)



## Tertiary Structure Prediction Results

- Successful on a number of small protein systems
- Able to address difficult structures from CASP5 targets

Protein	# of AA	RMSD
1gb1	56	4.2
bpti	58	4.1
3d2	63	5.4
r69	68	6.2
t59	75	5.4
t114	87	4.5
t105	95	5.8
t52	101	6.9

Klepeis, JL and Floudas, CA. *Biophys J*. (2003)

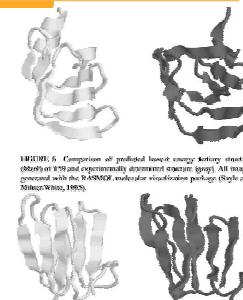
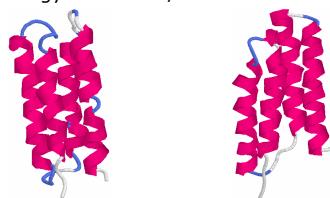


FIGURE 6: Comparison of predicted lowest energy tertiary structure (left) of T142 and experimentally determined structure (right). All images generated with the RASMOL molecular visualization package (Steyn and Miersch-Wilke, 1998).



## Results – Blind Structure Prediction

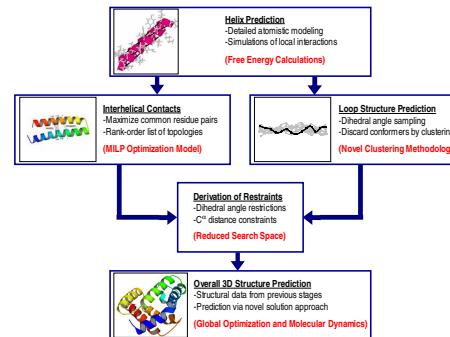
- PDB:1p68 (Prof. M. Hecht, Princeton Univ.)
- No information about secondary/tertiary structure
- $\alpha$ -helix: 5-21, 30-49, 56-75, 80-100
- Distance restraints: 63 intrahelical
- Best energy: -846 kcal/mol      RMSD: 5.1 Å



Klepeis, JL, et al. *Proteins*. (2005)



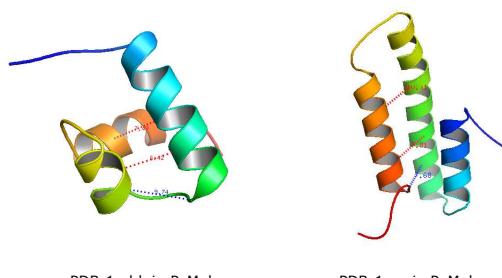
## ASTRO-FOLD for $\alpha$ -helical Bundles



McAllister SR and Floudas, CA. *Proceedings, BIOMAT Conference* (2005).



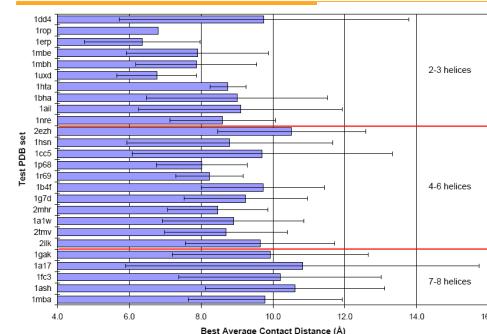
## Results – 2-3 helix bundles



McAllister et al. (submitted 2005)



## Results – Contact Prediction Summary



McAllister et al. (submitted 2005)

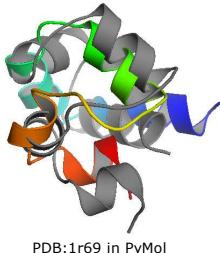


## Results – Tertiary Structure Prediction

### o PDB:1r69

- 63 amino acid protein
- Top 5 conformers

Conformer	Energy (kcal/mol)	RMSD (Å)
1	-358.77	6.05
2	-351.92	7.95
3	-347.71	6.72
4	-337.80	5.88
5	-337.52	8.04
157	-210.13	4.68



■ +/- 20° on dihedral angles of loop predictions

McAllister SR and Floudas, CA. *Proceedings, BIOMAT Conference* (2005).

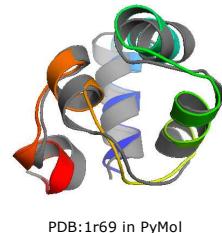


## Results – Tertiary Structure Prediction

### o PDB:1r69

- 63 amino acid protein
- Top 5 conformers

Conformer	Energy (kcal/mol)	RMSD (Å)
1	-381.54	3.72
2	-376.10	3.40
3	-375.17	4.45
4	-363.77	2.03
5	-356.85	4.91



■ +/- 10° on dihedral angles of experimental loops

McAllister SR and Floudas, CA. *Proceedings, BIOMAT Conference* (2005).



## Discussion

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