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Topology matching

for fully automatic similarity estimation of 3D shapes

- 1 M. Hilaga et al., ACM SIGGRAPH, 2001.
- 1 Geometry-based and topology-based approach
- 1 For each vertex of the object, calculate a sum of the geodesic distance from this vertex to others
- 1 Reeb graph, where each node represents a region according to the value
- 1 Construct multi-resolutional Reeb graph by grouping adjacent regions











Design issues

- 1 Correctness, discrimination
- 1 Efficiency, automation
- 1 Robustness
 - 1 Similarity transformation: translation, rotation and scaling
 - 1 Connectivity changes: re-meshing, sub-division and simplification
 - 1 Model degeneracy: missing, wrongly oriented normals, intersecting, disjoint and overlapping polygons
 - 1 Noise, deformation, etc.
- 1 Scope
 - 1 Static objects
 - 1 Not for articulated creatures













- Translation and scaling roughly in 3D space
- The error in translation and scaling will be diminished by 2D image matching



















Zernike polynomials of order p, with repetition q

 $Vpq(r, \theta) = R_{pq}(r) e^{jq\theta}$

 $\begin{array}{ll} R_{pq}(r)^{=\sum^{(p-|q|/2)}_{k=0}} & (-1)^{k}(p\text{-}k)!/\{k!((p+|q|/2\text{-}k)!(p-|q|)/2\text{-}k)!\} & r^{p\text{-}2k} \end{array}$

$$\begin{split} R_{00}(r) &= 1, \quad R_{11}(r) = r, \\ R_{20}(r) &= 2r^2\text{-}1, \quad R_{22}(r) = r^2 \\ R_{31}(r) &= 3r^3\text{-}2r, \quad R_{33}(r) = r^3 \end{split}$$

Trace contour for rendered image

- 1 Erosion operation to connect the separated parts
- 1 Thinning, but don't remove the rendered pixels





Retrieval from a large database

- Iterative early rejection of non-relevant 3D models
- 1 Only parts of the images and coefficients are compared
- 1 6 iterations in total
 - 1 1st~5th iteration: Zernike moment
 - 1 6th iteration: Fourier descriptor
 - 1 The threshold of removing models is set as the mean of the similarity























Timing statistics in computing the similarity matrix

- 1 The average time is 0.0013 second to compare two shape descriptors
- 1 The average storage is 4700 bytes for a single shape descriptor
- 1 The average time is 3.25 seconds to compute each shape descriptor
- 1 on a PC with Pentium 4 CPU 2.4GHz, 256MB RAM and NVIDIA GeForce 2 MX





