

Administrative Information http://www.cs.princeton.edu/courses/archive/fall02/cs341/ Professor: Moses Charikar moses@cs.princeton.edu 305 CS building, 8-7477 Secretary: Mitra Kelly mkelly@cs.princeton.edu 323 CS Building, 8-4562 Teaching Assistants: Adriana Karagiozova karagioz@cs.princeton.edu 414 CS Building, 8-5388 Renato Werneck 5-5135 rwerneck@princeton.edu

Administrative Information

- Required text: Invitation to Discrete Mathematics
 Jiri Matousek and Jaroslav Nesetril
- Reference: Discrete Mathematics and its Applications Kenneth Rosen
- All handouts posted on web page
- · Class mailing list
- Homeworks assigned every Wed., due in class next Wed.
- Grading:
 - 9-10 homeworks (80%), take-home final (20%)
- Collaboration policy

Discussion Sessions/Office Hours

4

- Discussion Sessions in addition to office hours (perhaps)
- · Times announced next week on basis of student choices
- My office hours for next week: Tue, 2:00-4:00 pm

3

What is Discrete Mathematics ?

- Mathematics dealing with finite sets
- Topics: counting, combinatorics, graph theory, probability
- Goals:

Develop mathematical maturity Foundation for advanced courses in Computer Science

- Flavor of questions:
- How many valid passwords on a computer system ?

5

- What is the probability of winning a lottery ?
- What is the shortest path between two cities ?

Toy problems as illustrations

• Puzzle:

Three houses, three wells: Can we connect each house to each well by pathways so that no two pathways cross ?

• Real world problem:

VLSI: Given placement of components of circuit on a board, is it possible to connect them along a board so that no two wires cross ?

Proof techniques	
	7

Evidence vs. Proof

 $p(n) = n^2 + n + 41$ Claim: $\forall n \in \mathbb{N}, p(n)$ is prime 6





Evidence vs. Proof

• Euler's conjecture (1769):

 $a^4 + b^4 + c^4 = d^4$ has no solution for *a*,*b*,*c*,*d* positive integers

Counterexample: 218 years later by Noam Elkies:

 $95800^4 + 217519^4 + 414560^4 = 422481^4$

Example courtesy: Prof. Albert R. Meyer's lecture slides for MIT course 6.042, Fall 02

11















Strong Induction example

- Show that if n is an integer greater than 1, n can be written down as a product of primes
- P(n): n can be written down as a product of primes
- Basis Step: P(2) is true, 2=2
- Inductive Step: Assume P(j) is true for all $j \le k$ Need to show that P(k+1) is true
- Case 1: k+1 is prime, P(k+1) is true
- Case 2: $k+1 = a \cdot b$

By induction hypothesis, both a and b can be written as a product of primes.

Proof by contradiction

