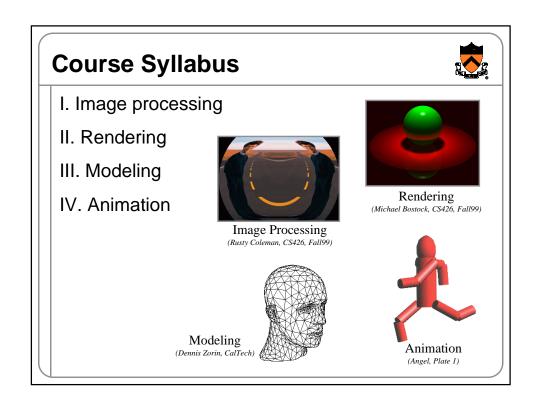
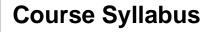


Subdivision Surfaces

Thomas Funkhouser Princeton University C0S 426, Fall 2000







- I. Image processing
- II. Rendering
- **III. Modeling**
- IV. Animation





Image Processing







Modeling (Dennis Zorin, CalTech)



Modeling



- How do we ...
 - Represent 3D objects in a computer?
 - Construct 3D representations quickly/easily?
 - Manipulate 3D representations efficiently?









Different representations for different types of objects

3D Object Representations



- Raw data
 - Voxels
 - Point cloud
 - Range image
 - Polygons
- Surfaces
 - Mesh
 - Subdivision
 - Parametric
 - Implicit

- Solids
 - Octree
 - BSP tree
 - CSG
 - Sweep
- High-level structures
 - Scene graph
 - Skeleton
 - Application specific

Equivalence of Representations



- Thesis:
 - Each fundamental representation has enough expressive power to model the shape of any geometric object
 - It is possible to perform all geometric operations with any fundamental representation!
- Analogous to Turing-Equivalence:
 - All computers today are turing-equivalent, but we still have many different processors

Computational Differences



- Efficiency
 - ∘ Combinatorial complexity (e.g. O(n log n))
 - Space/time trade-offs (e.g. z-buffer)
 - Numerical accuracy/stability (degree of polynomial)
- Simplicity
 - Ease of acquisition
 - Hardware acceleration
 - Software creation and maintenance
- Usability
 - Designer interface vs. computational engine

3D Object Representations



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Surfaces



- What makes a good surface representation?
 - Accurate
 - Concise
 - Intuitive specification
 - Local support
 - Affine invariant
 - Arbitrary topology
 - Guaranteed continuity
 - Natural parameterization
 - Efficient display
 - Efficient intersections



H&B Figure 10.46

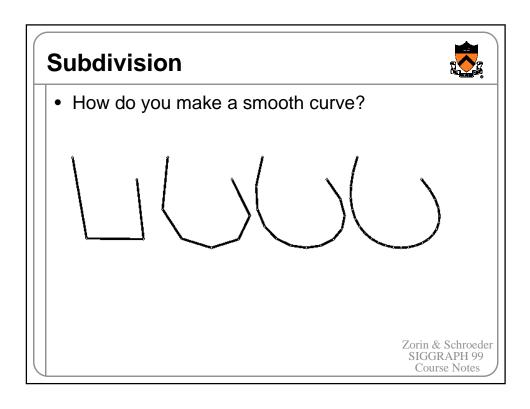
Subdivision Surface

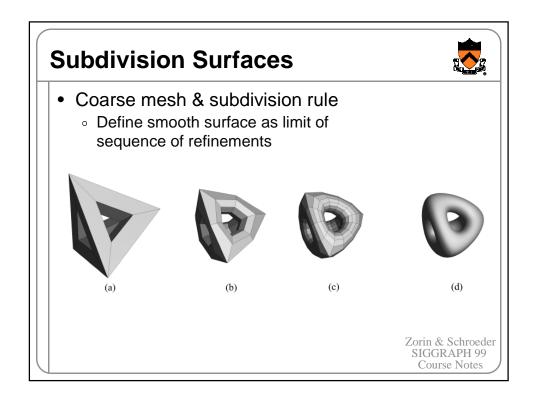


- Properties:
 - Accurate
 - Concise
 - Intuitive specification
 - Local support
 - Affine invariant
 - Arbitrary topology
 - Guaranteed continuity
 - Natural parameterization
 - Efficient display
 - Efficient intersections



Pixar

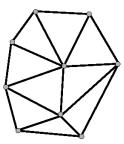


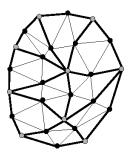


Key Questions



- How refine mesh?
 - Aim for properties like smoothness
- How store mesh?
 - Aim for efficiency for implementing subdivision rules



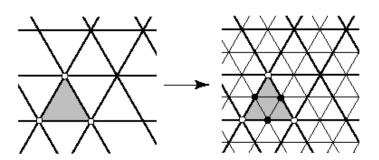


Zorin & Schroeder SIGGRAPH 99 Course Notes

Loop Subdivision Scheme



- How refine mesh?
 - Refine each triangle into 4 triangles by splitting each edge and connecting new vertices

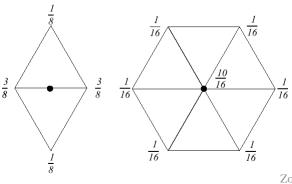


Zorin & Schroeder SIGGRAPH 99 Course Notes

Loop Subdivision Scheme



- How position new vertices?
 - Choose locations for new vertices as weighted average of original vertices in local neighborhood

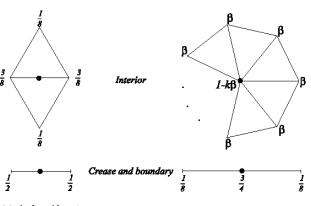


Zorin & Schroeder SIGGRAPH 99 Course Notes

Loop Subdivision Scheme



• Different rules for boundaries:



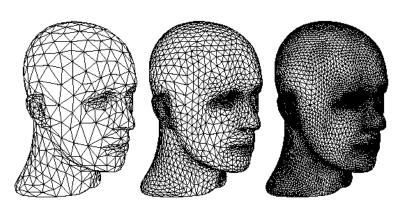
a. Masks for odd vertices

b. Masks for even vertices

Zorin & Schroeder SIGGRAPH 99 Course Notes







Limit surface has provable smoothness properties!

Zorin & Schroeder SIGGRAPH 99 Course Notes

Subdivision Schemes

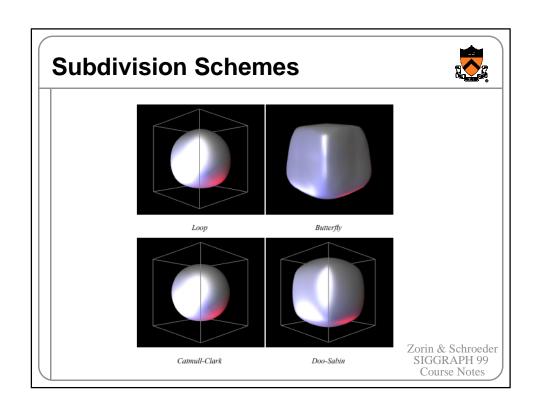


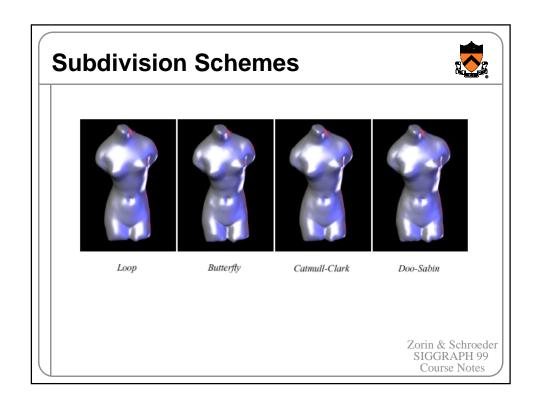
- There are different subdivision schemes
 - Different methods for refining topology
 - Different rules for positioning vertices» Interpolating versus approximating

Face split		
	Triangular meshes	Quad. meshes
Approximating	Loop (C^2)	Catmull-Clark (C2)
Interpolating	Mod. Butterfly (C1)	Kobbelt (C1)

Vertex split	
Doo-Sabin, Midedge (C1)	
Biquartic (C2)	

Zorin & Schroeder SIGGRAPH 99 Course Notes

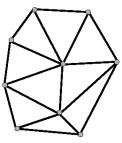




Key Questions



- How refine mesh?
 - Aim for properties like smoothness
- How store mesh?
 - Aim for efficiency for implementing subdivision rules



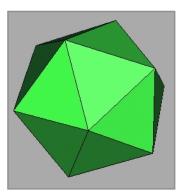


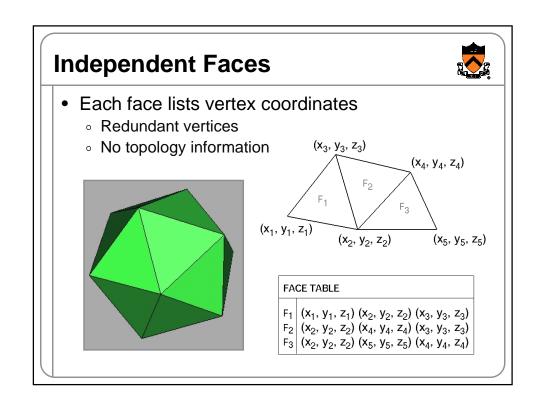
Zorin & Schroeder SIGGRAPH 99 Course Notes

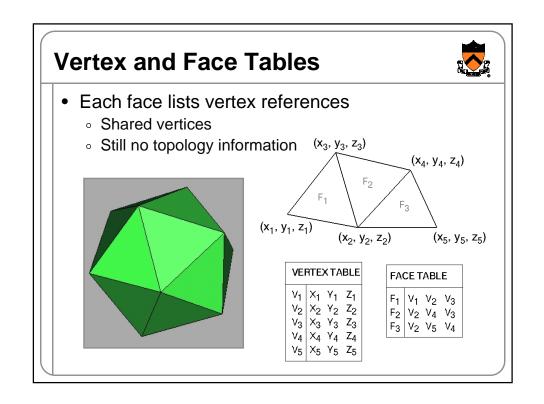
Polygon Meshes

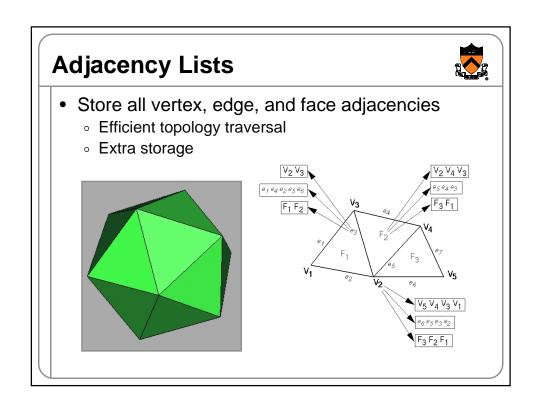


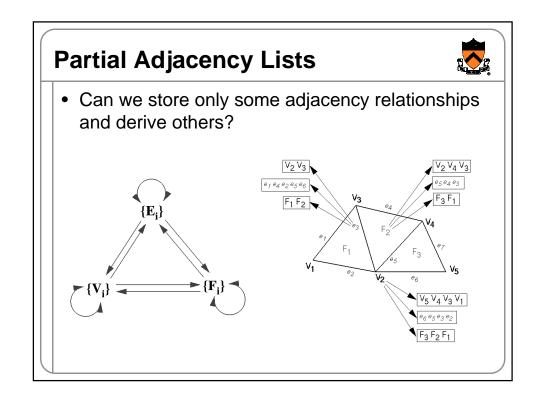
- Mesh Representations
 - Independent faces
 - Vertex and face tables
 - Adjacency lists
 - Winged-Edge

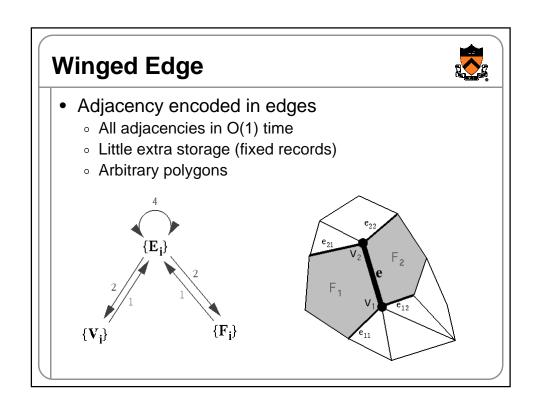


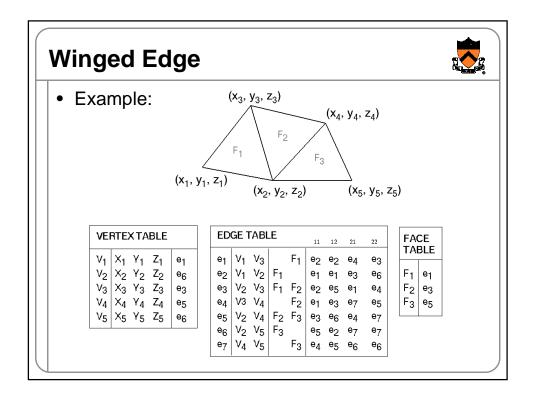








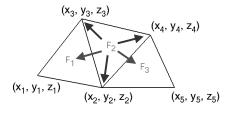




Triangle Meshes



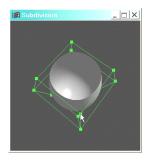
- Relevant properties:
 - Exactly 3 vertices per face
 - Any number of faces per vertex
- Useful adjacency structure for Loop subdivision:
 - Do not represent edges explicitly
 - Faces store refs to vertices and neighboring faces
 - Vertices store refs to adjacent faces and vertices

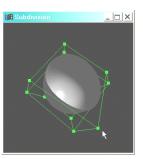


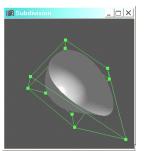
Assignment 4

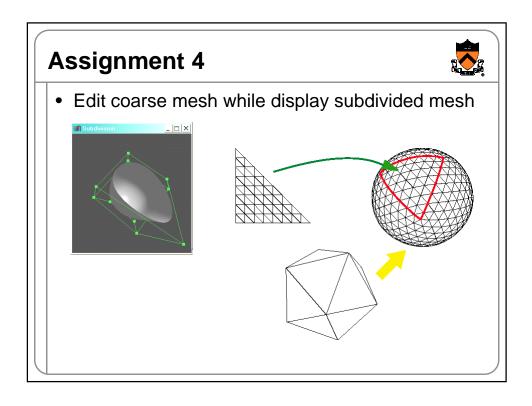


- Interactive editing of subdivision surfaces
 - Loop subdivision scheme
 - Partial adjacency list mesh representation
 - Interactive vertex dragging





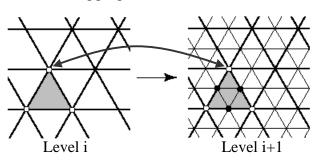




Assignment 4



- Store hierarchy of meshes
 - Full triangle mesh at every level
 - Vertices store references to counterparts one level up and one level down
 - Enables efficient re-positioning of mesh vertices after interactive dragging



Summary



- Advantages:
 - Simple method for describing complex surfaces
 - Relatively easy to implement
 - Arbitrary topology
 - Smoothness guarantees
 - Multiresolution



- Intuitive specification
- Parameterization
- Intersections



