Why Data Structures?

Goal: deal with large amounts of data.
- Organize data so that it is easy to manipulate.
- Time and space efficient.

Basic computer memory abstraction.
- Indexed sequence of bits.
- Address = index.

Need higher level abstractions to bridge gap.
- Array.
- STRUCT.
- Linked list.
- Binary tree.
- Database.
- ...

C Representation of C Students

```c
#include <stdio.h>

struct student {
    char name[16];
    int grade;
};

int main(void) {
    struct student t;
    struct student x = {"Bill Gates", 60};
    struct student y = {"Steve Jobs", 70};
    if (x.grade > y.grade)
        t = x;
    else
        t = y;
    printf("Better student: %s\n", t.name);
    return 0;
}
```

Structs

Fundamental data structure.
- HETEROGENEOUS collection of values (possibly different type).
  - Database records, complex numbers, linked list nodes, etc.
- Store values in FIELDS.
- Associate NAME with each field.
- Use struct name and field name to access value.

Built into C.
- To access `rate` field of structure `x` use `x.rate`
- Basis for building "user-defined types" in C.
Typedef
User definition of type name.
- Put type descriptions in one place - makes code more portable.
- Avoid typing `struct` - makes code more readable.

```c
typedef int Grade;
typedef char Name[16];
struct student {
    Name name;
    Grade grade;
};
typedef struct student Student;

Student x = {"Bill Gates", 60};
```

A Data Type: Points
Define structures for points in the plane, and operations on them.

```c
#include <math.h>
typedef struct {
    double x;
    double y;
} Point;
double distance(Point a, Point b) {
    double dx = a.x - b.x;
    double dy = a.y - b.y;
    return sqrt(dx*dx + dy*dy);
}
Point randomPoint(double s) {
    Point p;
p.x = randomDouble(s);
p.y = randomDouble(s);
    return p;
}
```

Another Data Type: Circles
 Define structures for points in the plane, and operations on them.

```c
#include <math.h>
define PI 3.1415

typedef struct {
    Point center;
    double radius;
} Circle;
int inCircle(Point p, Circle c) {
    return distance(p, c.center) <= c.radius;
}
double area(Circle c) {
    return PI * c.radius * c.radius;
}
int intersectCircles(Circle c, Circle d) {
    return distance(c.center, d.center) <= c.radius + d.radius;
}
```

Using Data Types: Estimating π
Monte Carlo estimate of π.
- Generate N random points in 2 x 2 square.
- Determine fraction that lie in unit circle.
- On average $\pi / 4$ fraction should lie in circle.
- Use $4 \times$ fraction as estimate of $\pi$.

```c
#define N 100000

int main(void) {
    int i, cnt = 0;
    Point p = {1.0, 1.0};
    Circle c;
    c.center = p; c.radius = 1.0;
    for (i = 0; i < N; i++) {
        p = randomPoint(2.0);
        if (inCircle(p, c))
            cnt++;
    }
    printf("pi = %f\n", 4.0*cnt/N);
    return 0;
}
```
Standard Data Type Implementation

Data type:
- Set of values and collection of operations on those values.

Example (built-in): int, double, char.

Example (user defined): complex numbers.
- Set of values: $4 + 2i$, $1.3 - 6.7i$, etc.
- Operations: add, multiply, show, etc.

Separate implementation from specification.
- INTERFACE: specifies allowed operations.
- IMPLEMENTATION: provides code for operations.
- CLIENT: uses data type as black box.

Complex Number Data Type

Create data structure to represent complex numbers.
- See Sedgewick 4.8.
- Store in rectangular form: real and imaginary parts.

typedef struct {
    double re;
    double im;
} Complex;

Interface lists allowable operations on complex data type.
- Name interface with .h extension.

typedef struct {
    double re;
    double im;
} Complex;

Complex COMPLEXadd (Complex a, Complex b);
Complex COMPLEXmult (Complex a, Complex b);
Complex COMPLEXpow (Complex a, Complex b);
Complex COMPLEXconj (Complex a);
double COMPLEXabs (Complex a);
double COMPLEXreal (Complex a);
double COMPLEXimag (Complex a);
Complex COMPLEXinit (double x, double y);
void COMPLEXshow (Complex a);

Complex Number Data Type: Interface

store in rectangular form

can't reuse +, * symbols

function prototypes

COMPLEX.h
**Complex Number Data Type: Client**

Client program uses interface operations to calculate something:

```c
#include <stdio.h>
#include "COMPLEX.h"

int main(void) {
    Complex a, b, c;
    a = COMPLEXinit( 5.0, 6.0);
    b = COMPLEXinit(-2.0, 3.0);
    c = COMPLEXmult(a, b);
    COMPLEXshow(a);
    printf(" * ");
    COMPLEXshow(b);
    printf(" = ");
    COMPLEXshow(c);
    printf("\n");
    return 0;
}
```

Client can use interface:

(5 + 6i) * (-2 + 3i) = -28 + 3i

**Complex Number Data Type: Another Client**

Redo Mandelbrot with equivalent complex number update:

```c
#define MAXIT 255
#include "COMPLEX.h"

int mand(Complex z) {
    int i = 0;
    Complex c = z;
    while (COMPLEXabs(c) <= 2.0 && i < MAXIT) {
        c = COMPLEXadd(COMPLEXmult(c, c), z);
        i++;
    }
    return i;
}
```

**Complex Number Data Type: Implementation**

Write code for interface functions.

```c
#include <stdio.h>
#include <math.h>
#include "COMPLEX.h"

Complex COMPLEXadd(Complex a, Complex b) {
    Complex t;
    t.re = a.re + b.re;
    t.im = a.im + b.im;
    return t;
}

Complex COMPLEXmult(Complex a, Complex b) {
    Complex t;
    t.re = a.re * b.re - a.im * b.im;
    t.im = a.re * b.im + a.im * b.re;
    return t;
}
```

Write code for interface functions.

```c
double COMPLEXabs(Complex a) {
    return sqrt(a.re * a.re + a.im * a.im);
}

void COMPLEXshow(Complex a) {
    printf("%f + %f i\n", a.re, a.im);
}

Complex COMPLEXinit(double x, double y) {
    Complex t;
    t.re = x;
    t.im = y;
    return t;
}
```

Implementation and client need to agree on interface:

Function in math library:

```
```
Compilation

Client and implementation both include COMPLEX.h

Compile jointly.
\%gcc client.c complex.c -lm

Or compile separately.
\%gcc -c complex.c
\%gcc -c client.c
\%gcc client.o complex.o -lm

Unx
\% gcc126 client.c complex.c
\% a.out
(5.00 + 6.00 i) * (-2.00 + 3.00 i) = (-28.00 + 3.00 i)

Client, Interface, Implementation

Client  couchpotato.c
Interface  "TV.h"
Implementation  tvplasma.c

client needs to know how to use interface
implementation needs to know what interface to implement

Implementation and client need to agree on interface ahead of time.

Can Change Implementation

Can use alternate representation of complex numbers.
  - Store in polar form: modulus and angle.

\[ z = x + i y = r (\cos \theta + i \sin \theta) = re^{i\theta} \]

typedef struct {
  double r;
  double theta;
} Complex;

Alternate Interface

Interface lists allowable operations on complex data type.

COMPLEX.h

```c
typedef struct {
  double r;
  double theta;
} Complex;
```

Complex COMPLEXadd (Complex a, Complex b);
Complex COMPLEXmult (Complex a, Complex b);
Complex COMPLEXpow (Complex a, Complex b);
Complex COMPLEXconj (Complex a);
double COMPLEXabs (Complex a);
double COMPLEXreal (Complex a);
double COMPLEXimag (Complex a);
Complex COMPLEXinit (double x, double y);
void COMPLEXshow (Complex a);
```
Alternate Implementation

Write code for interface functions.

```c
#include "COMPLEX.h"
#include <math.h>
#include <stdio.h>

Complex COMPLEXabs(Complex a) {
    return a.r;
}

Complex COMPLEXmult(Complex a, Complex b) {
    Complex t;
    t.r = a.r * b.r;
    t.theta = a.theta + b.theta;
}
```

Some interface functions are now faster and easier to code.

Alternate Implementation

Write code for interface functions.

```c
Complex COMPLEXadd(Complex a, Complex b) {
    Complex t;
    double x, y;
    x = a.r * cos(a.theta) + b.r * cos(b.theta);
    y = a.r * sin(a.theta) + b.r * sin(b.theta);
    t.r = sqrt(x*x + y*y);
    t.theta = arctan(y/x);
    return t;
}
```

Others are more annoying.

Multiple Implementations

Usually, several ways to represent and implement a data type.

How to represent complex numbers: rectangular vs. polar?

- Depends on application.
- Rectangular are better for additions and subtractions.
  - no need for arctangent
- Polar are better for multiply and modulus.
  - no need for square root
- Get used to making tradeoffs.

This example may seem artificial.

- Essential for many real applications.
- Crucial software engineering principle.

Rational Number Data Type

See Assignment 3.

- You will create data type for Rational numbers.
- Add associated operations to Rational number data type.

```c
typedef struct {
    int num;
    int den;
} Rational;
```

- Simple version relatively easy to implement.
- Improved implementation staves off overflow by:
  - reducing fractions
  - order of computation
Conclusions

Basic computer memory abstraction.
- Indexed sequence of bits.
- Address = index.

Need higher level abstractions to bridge gap.
- Array.
  - homogeneous collection of values
- Struct.
  - heterogeneous collection of values

Data type.
- Set of values and collection of operations on those values.

Client-interface-implementation paradigm.
- Consistent way to implement data types.

Can Change Implementation

Complex multiplication.
- \( (a + bi)(c + di) = x + yi \)

<table>
<thead>
<tr>
<th>Naïve</th>
<th>Gauss</th>
</tr>
</thead>
<tbody>
<tr>
<td>( x = ac - bd )</td>
<td>( x_1 = (a + b)(c + d) )</td>
</tr>
<tr>
<td>( y = bc + ad )</td>
<td>( x_2 = ac )</td>
</tr>
<tr>
<td></td>
<td>( x_3 = bd )</td>
</tr>
<tr>
<td></td>
<td>( x = x_1 - x_3 )</td>
</tr>
<tr>
<td></td>
<td>( y = x_1 - x_2 - x_3 )</td>
</tr>
</tbody>
</table>

\( 4 \) multiplications, \( 2 \) additions

<table>
<thead>
<tr>
<th>Gauss</th>
</tr>
</thead>
<tbody>
<tr>
<td>( x_1 = (a + b)(c + d) )</td>
</tr>
<tr>
<td>( x_2 = ac )</td>
</tr>
<tr>
<td>( x_3 = bd )</td>
</tr>
<tr>
<td>( x = x_1 - x_3 )</td>
</tr>
<tr>
<td>( y = x_1 - x_2 - x_3 )</td>
</tr>
</tbody>
</table>

\( 3 \) multiplications, \( 5 \) additions

complex.c (everything else as before)

```c
Complex COMPLEXmult(Complex a, Complex b) {
    Complex t;
    double x1 = (a.re + a.im) \* (b.re + b.im);
    double x2 = a.re \* b.re;
    double x3 = a.im \* b.im;
    t.re = x2 - x3;
    t.im = x1 - x2 - x3;
    return t;
}
```

Pass By Value, Pass By Reference

Arrays and structs are passed to functions in very DIFFERENT ways.

Pass-by-value:
- int, float, char, struct
- a COPY of value is passed to function

```c
void mystery(Point a) {
    a.y = 17.0;
}
Point a = {1.0, 2.0};
mystery(a);
printf("%4.1f\n", a.y);
```

Unix

```
% a.out
1.0
```

Pass-by-reference:
- arrays
- function has direct access to array elements

```c
void mystery(double a[]) {
    a[1] = 17.0;
}
double a[] = {1.0, 2.0};
mystery(a);
printf("%4.1f\n", a[1]);
```

Unix

```
% a.out
17.0
```