Week 6 Precept

1. Left Leaning Red-Black Trees

   (a) Consider the following 2-3 Tree.

   ![2-3 Tree Diagram]

   Draw the corresponding red-black tree.

   (b) Consider the following red-black tree. Does this tree satisfy LLRB invariants? If not, draw the new tree after fixing the links. Just draw the links that were changed (if any)

   ![Red-Black Tree Diagram]
(c) Consider the new red-black tree drawn in Part(b). Draw the resulting red-black tree after inserting key H and then draw it again after inserting key T. The new tree must be a valid red-black tree.

(共生) Consider the new red-black tree drawn in Part(b). Draw the resulting red-black tree after inserting key H and then draw it again after inserting key T. The new tree must be a valid red-black tree.

(d) LLRB construction
Given the keys $A < B < C < D < E < F < G$, insert them into a LLRB in the given order showing rotations and flips after each operation. Draw the LLRB after each character insertion.
2. Algorithm Design Question
An array $b$ is called a Circular Shift of array $a$, if $b$ is obtained by rotating a sorted array $a$ clockwise as shown below.

(a) Assume that the array $b$ consists of $N$ comparable keys, no two of which are equal. Array $a$ is not provided. Design an efficient algorithm to determine the minimum value of array $a$. Briefly describe your algorithm, using crisp and concise prose.

(b) Design an efficient algorithm to find any given key in array $b$. You can use your algorithm in part (a) to help solve this problem. Briefly describe your algorithm, using crisp and concise prose.
3. Midterm Preparation

The following topics will be covered in the midterm exam. Be sure to read lecture notes, review assignments, blackboard exercises. The exam page is available at url http://www.cs.princeton.edu/courses/archive/fall15/cos226/exams/midterm-info-fall.html
You can find information about the exam location, review sessions and office hours before midterm.

(a) Union-Find: quick-find, quick-union, weighted quick-union
(b) Elementary Data structures: resizing arrays, linked lists, stacks, queues
(c) Elementary Sorting Algorithms: insertion sort, selection sort, Knuth shuffle
(d) Linearithmic sorting algorithms: mergesort, bottom-up mergesort quicksort, 3-way quicksort, quickselect
(e) Priority Queues: binary heaps, heapsort
(f) Binary Search and BST’s: sequential search, binary search, BSTs
(g) kd-trees: kd-trees, interval search trees, 2-3 trees, left-leaning red-black BSTs
(h) Hashing (NOT COVERED): separate chaining, linear probing