DRAFT — NOT FOR DISTRIBUTION LITERATURE SURVEY, VERSION 1

Dynamics of Credit Expansions and Contractions

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1 Relation to previous work

2 Some references

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3 Sketch of an idea

I argue that our monetary flow model cannot be easily subsumed within the usual DSGE model by considering the continuous-time limit of both.

- The continuous-time limit of the usual DSGE model is considered in [12], where, as might be expected, it is shown to lead to an ordinary differential equation of standard type and low dimension (actually, eight).
- In the continuous-time limit our monetary flow model leads to a *delay-differential* equation (DDE), also called differential equations of the *retarded* type. This results from the fact that the delays in the loan array are on a larger scale from the update increment (period), and remain macroscopic when the differential limit is taken.
- In general DDEs have an infinite number of eigenvalues and lead to dynamic behavior that is inherently more complex than standard differential equations of low dimension. For example, a first-order DDE with a single delay can easily lead to oscillatory behavior. Erneux [29] provides a good introduction and survey.
- DDEs are used to model a macroeconomic system in [13], where rare poisson shocks are modeled. As they put it in their motivation, "... the simple awareness of large and rare 'Poisson jumps' leads to an adjustment of households' optimal consumption plans. One crucial difference to business cycle shocks is that an econometrician may not observe rare events for a longer period, and thus households might appear to be irrational." A similar justification can be made for the long delays that naturally result from loan contracts.

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