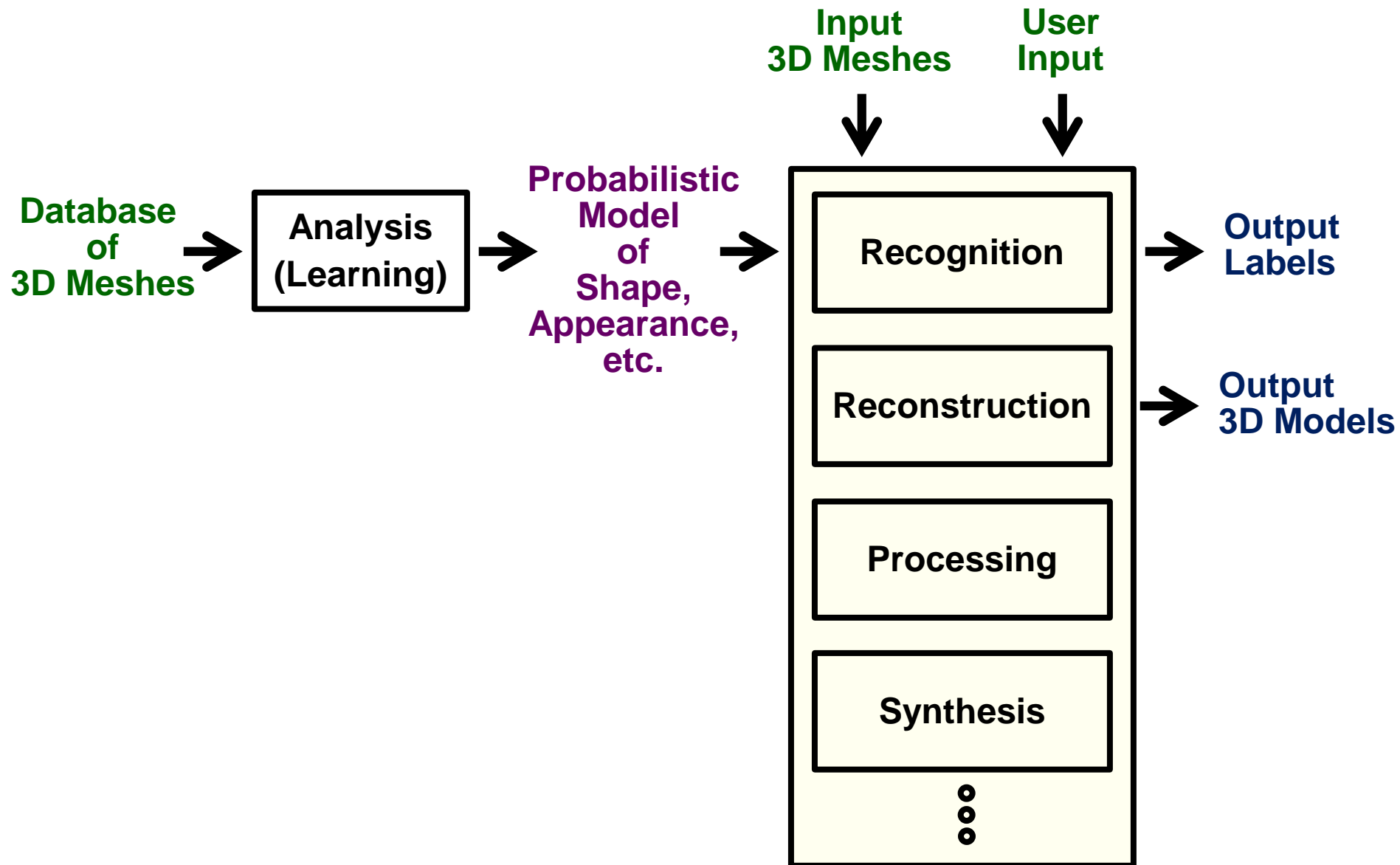




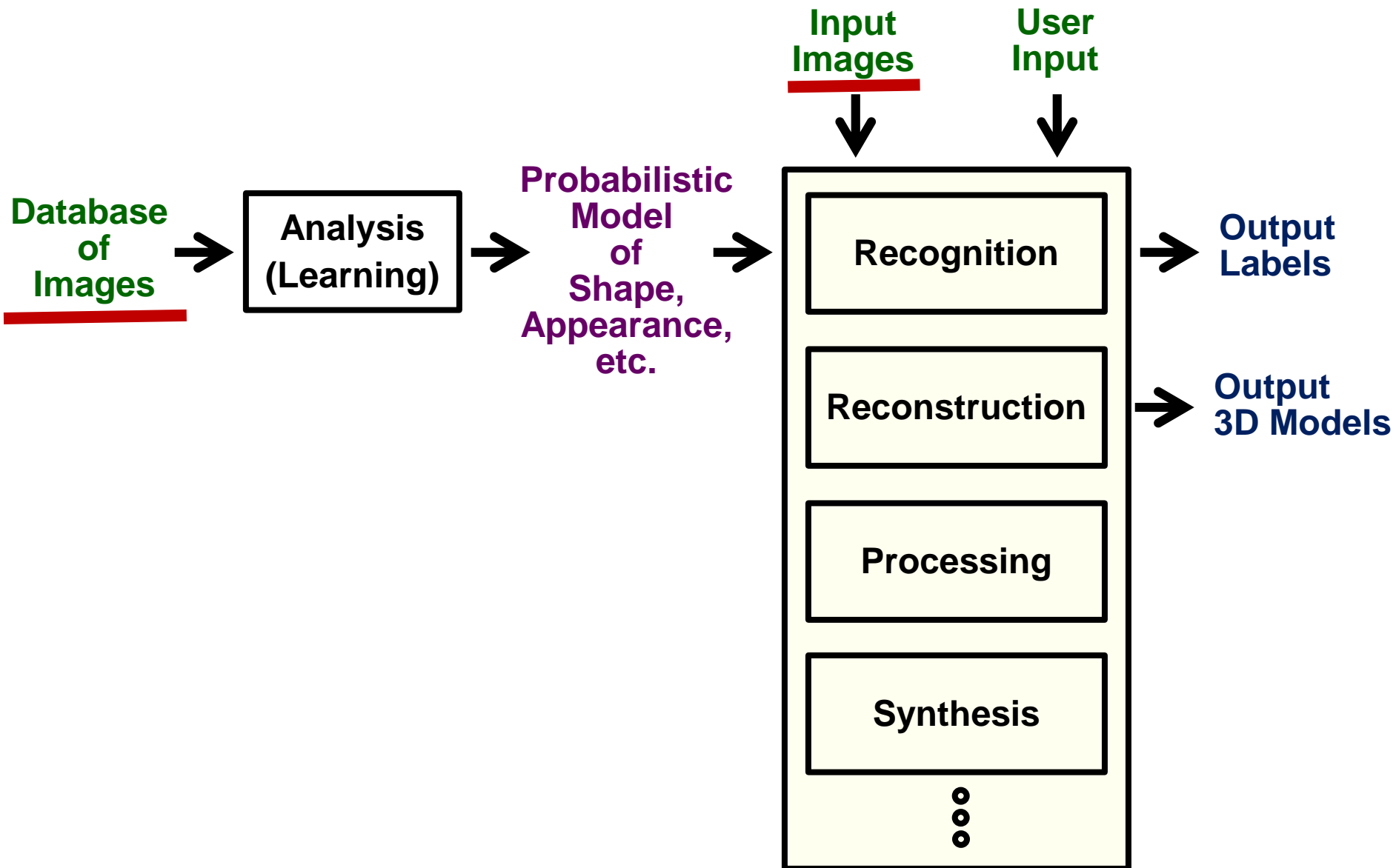
# Learning Probabilistic Models from Collections of 3D Meshes

Sid Chaudhuri, Steve Diverdi, Matthew Fisher,  
Pat Hanrahan, Vladimir Kim, Wilmot Li, Niloy Mitra,  
Daniel Ritchie, Manolis Savva, and Thomas Funkhouser

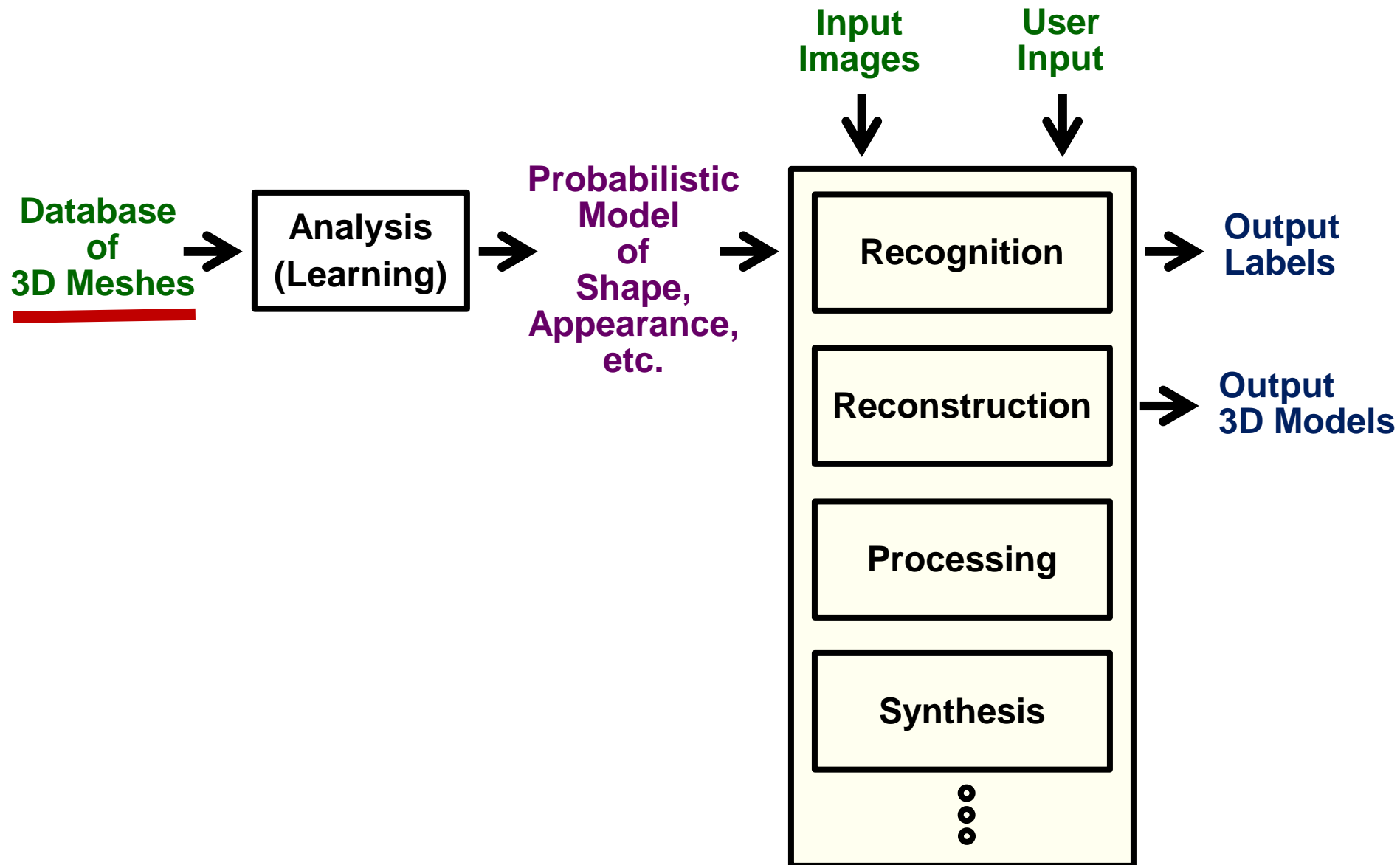
# 3D Shape Analysis



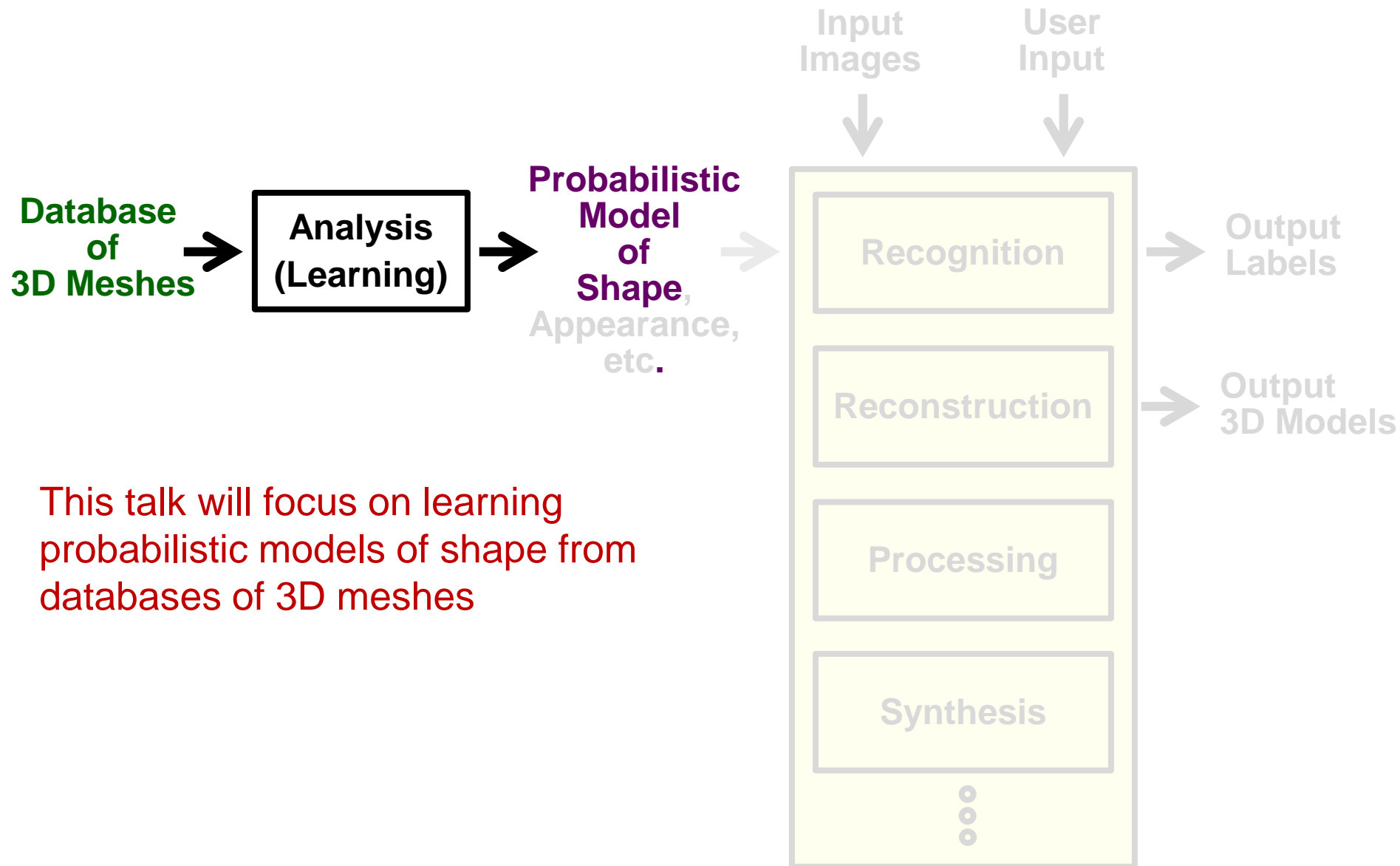
# Computer Vision



# 3D Shape Analysis for Computer Vision?



# Focus of This Talk



# Why 3D Shape Analysis?

Why analyze 3D meshes rather than images/scans?

- No noise
- No lighting
- No perspective
- No occlusions
- No pose estimation
- Easier segmentation
- Enough availability
- Large variety



Trimble 3D Warehouse

# Why 3D Shape Analysis?

Why analyze 3D meshes rather than images/scans?

- No noise
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- Easier segmentation
- Enough availability
- Large variety

➤ Quality?



Trimble 3D Warehouse

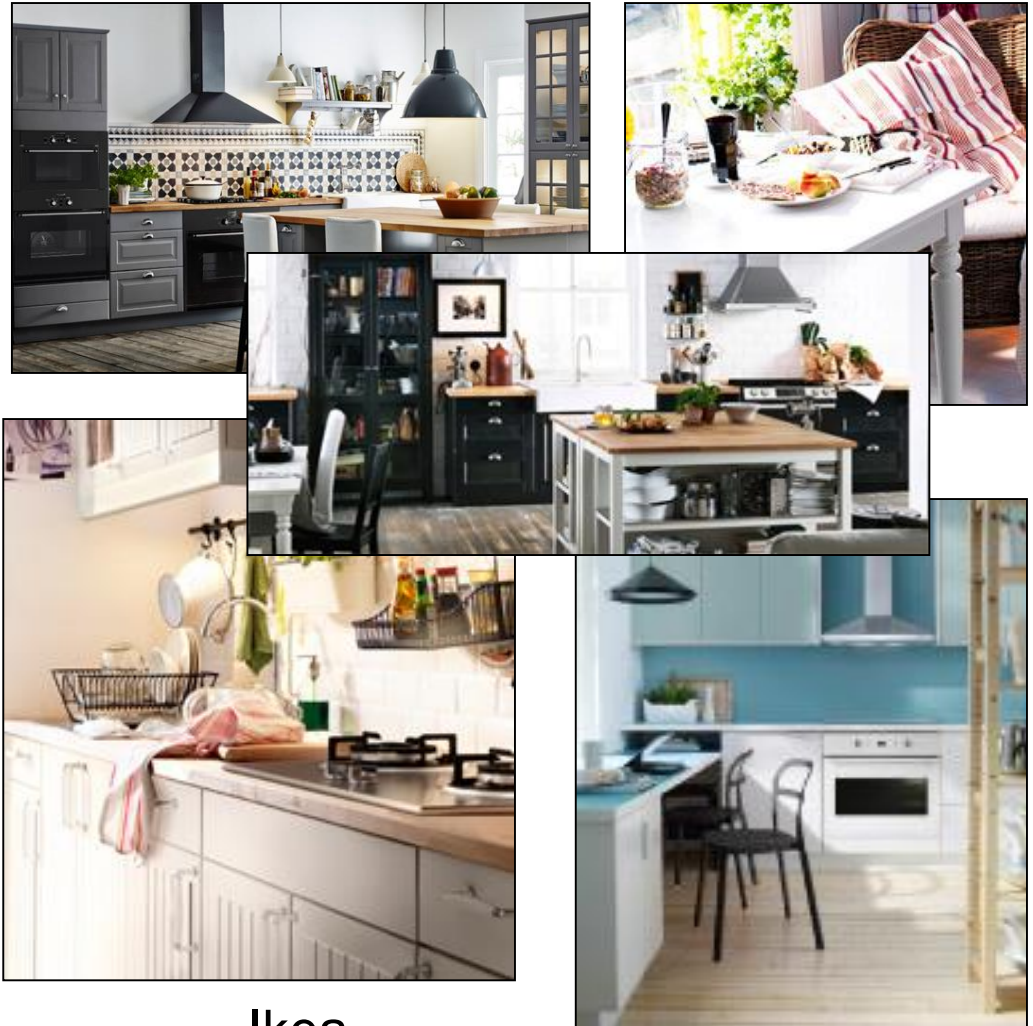


# Why 3D Shape Analysis?

Why analyze 3D meshes rather than images/scans?

- No noise
- No lighting
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- No occlusions
- No pose estimation
- Easier segmentation
- Enough availability
- Large variety

➤ Quality?



Ikea



# Related Work

---

## Using databases of meshes for scene understanding

- Fitting 3D meshes to images
  - Lai 2009, Xu 2011, Satkin 2013, Aubry 2014, etc.
- Fitting 3D meshes to range scans
  - Nan 2012, Shen 2012, Kim 2012, Song 2014, etc.
- Using 3D meshes to learn parameters
  - Zhao 2013, etc.

## Analyzing databases of meshes

- Consistent segmentation, labeling, correspondence, ...
  - Golovinskiy 2009, Sidi 2011, Kim 2013, Mitra 2013, etc.
- Learning probabilistic models
  - Chaudhuri 2010, Kalogerakis 2012, Fisher 2012, Kim 2013, etc.

# Outline of Talk

---

Introduction

Learning probabilistic models from 3D collections

- Part-based templates
- Generative model

Conclusions

# Outline of Talk

---

Introduction

Learning probabilistic models from 3D collections

➤ Part-based templates

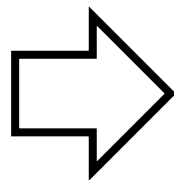
- Generative model

Conclusions

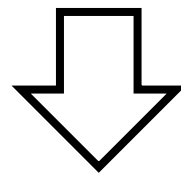
# Goal for This Project



Database of 3D meshes  
representing an object class

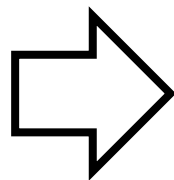


Probabilistic  
Model of Shape

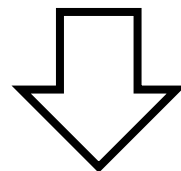


Consistent part segmentations,  
labels, and correspondences

# Goal for This Project



Probabilistic  
Model of Shape



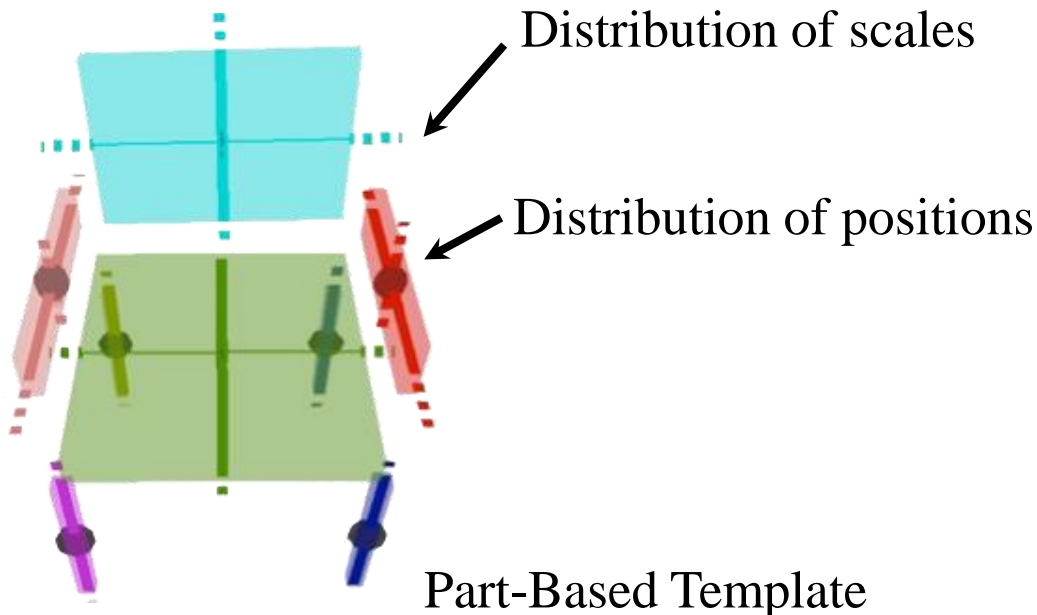
Consistent part segmentations,  
labels, and correspondences

## Challenge

Need to discover  
segmentations, labels,  
correspondences, and  
deformation modes  
all together

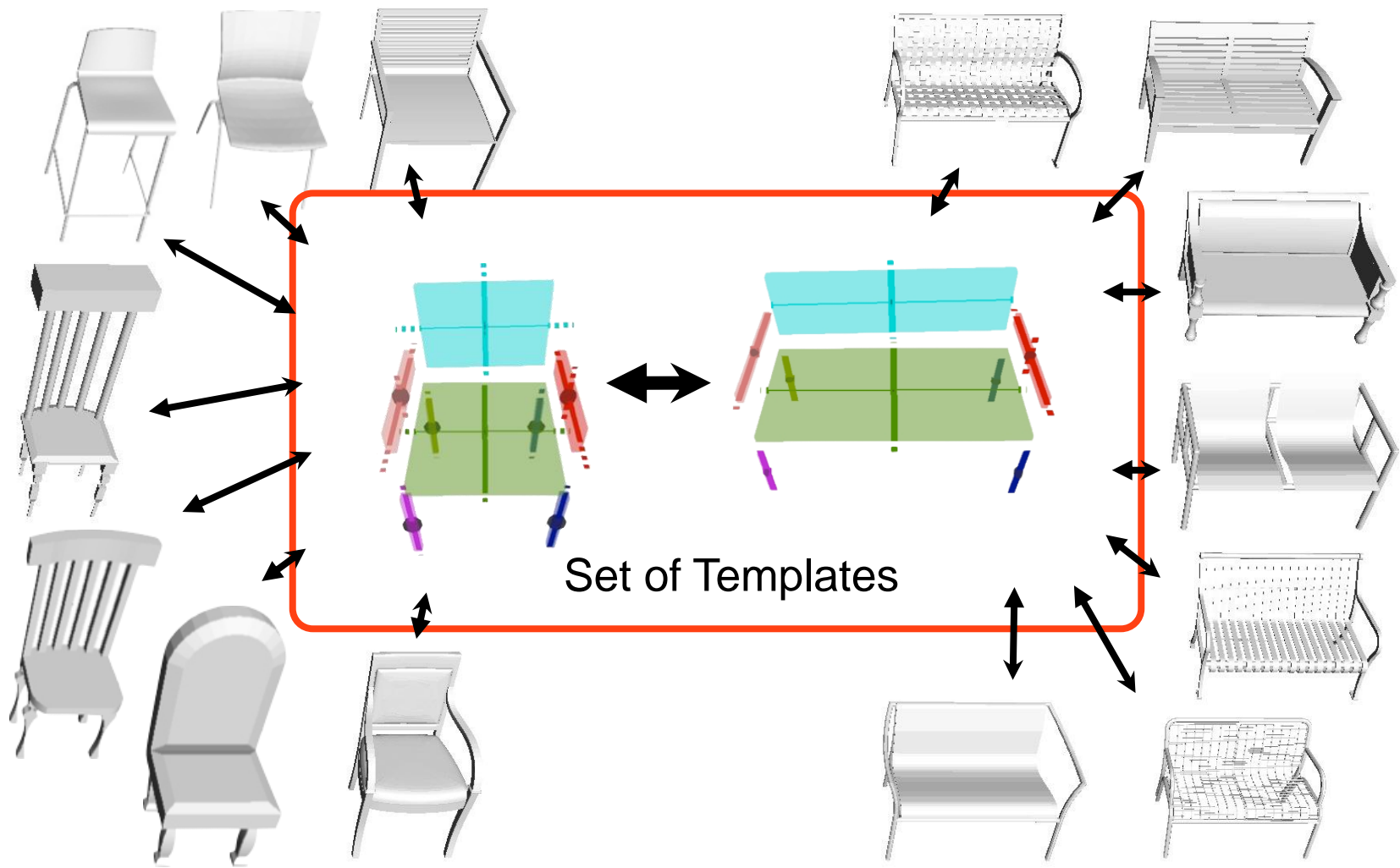
# Part-Based Templates

Represent object class by part-based templates where each template has a set of parts, and each part has probability distributions for its shape, position, and anisotropic scales



# Template Learning and Fitting

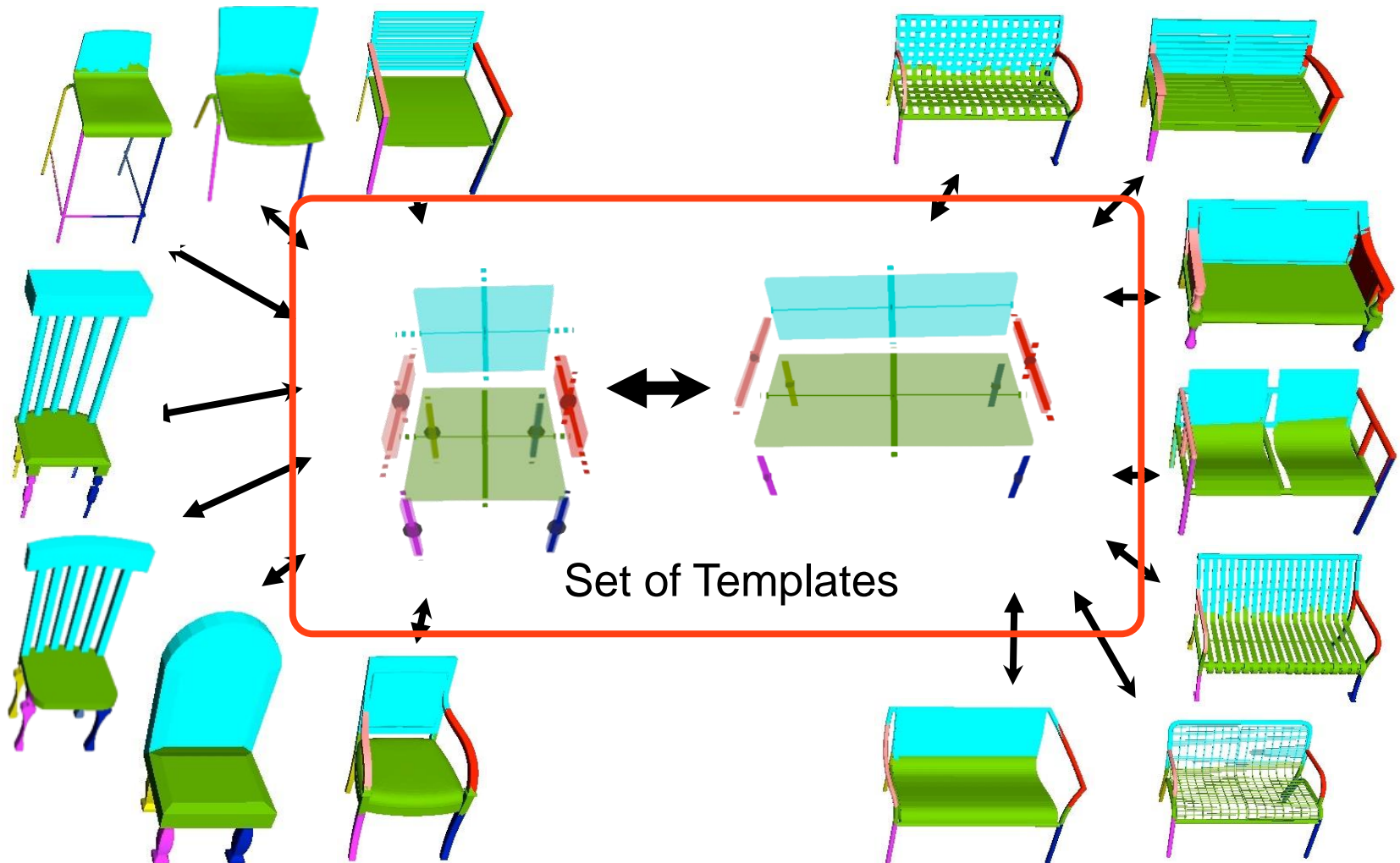
Aim to learn a set of corresponding templates that provides a good fit to every mesh in the database





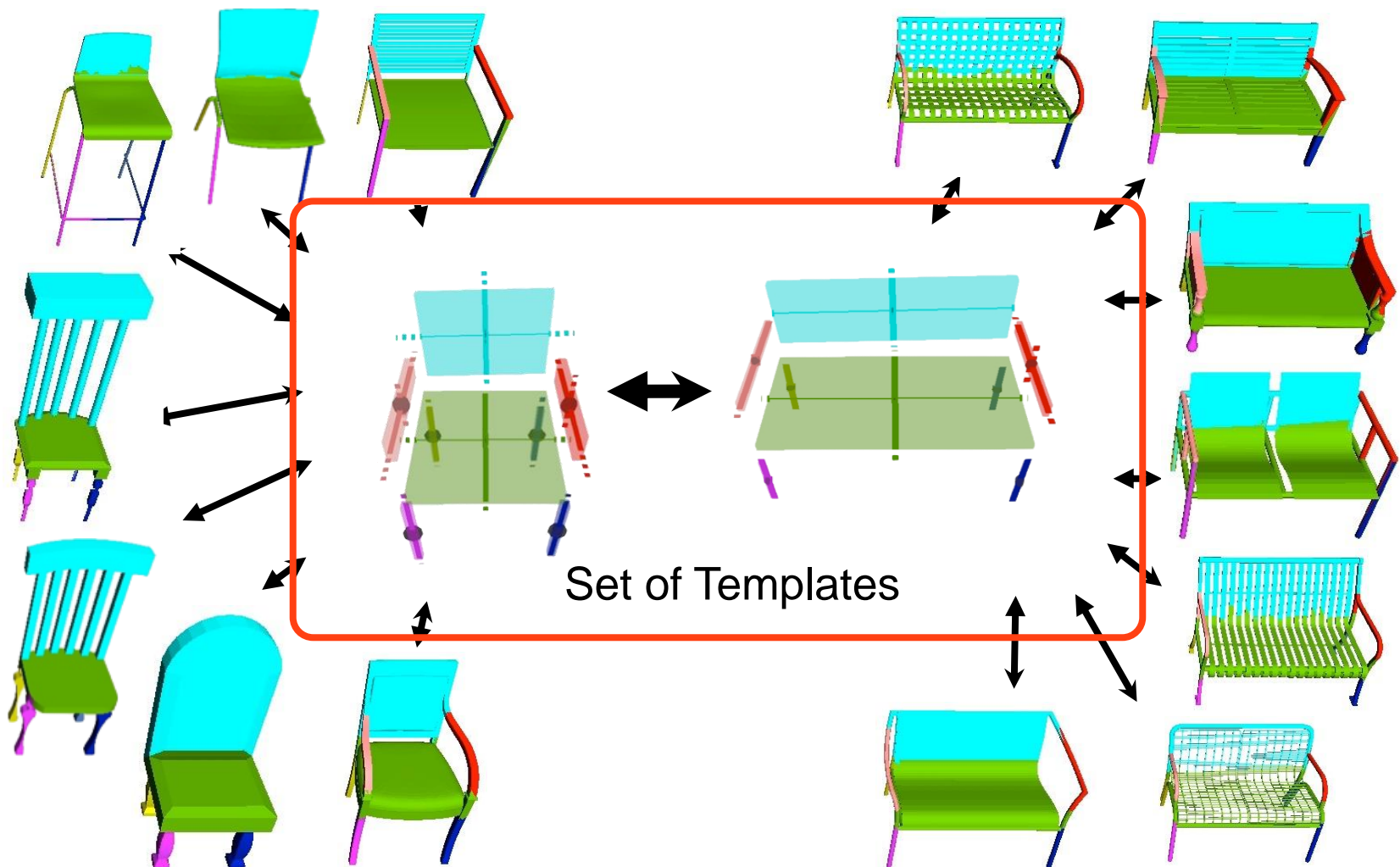
# Template Learning and Fitting

Aim to learn a set of corresponding templates that provides a good fit to every mesh in the database



# Template Learning and Fitting

Aim to learn a set of corresponding templates that provides a good **fit** to every mesh in the database



# Template Fitting Problem

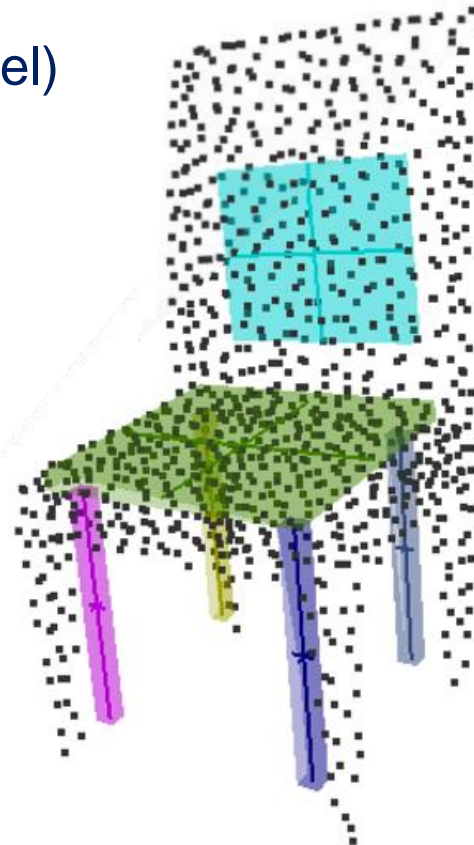
For a given template and mesh, aim to minimize:

$$E = E_{\text{data}} + \gamma E_{\text{deform}} + \beta E_{\text{smooth}}$$

- $E_{\text{data}}$  (template  $\leftrightarrow$  shape distance + local shape features)
- $E_{\text{deform}}$  (plausibility of template deformation)
- $E_{\text{smooth}}$  (close & similar regions get same label)

Unknowns are:

- Point segmentations and labels
- Point correspondences
- Part center positions
- Part anisotropic scales

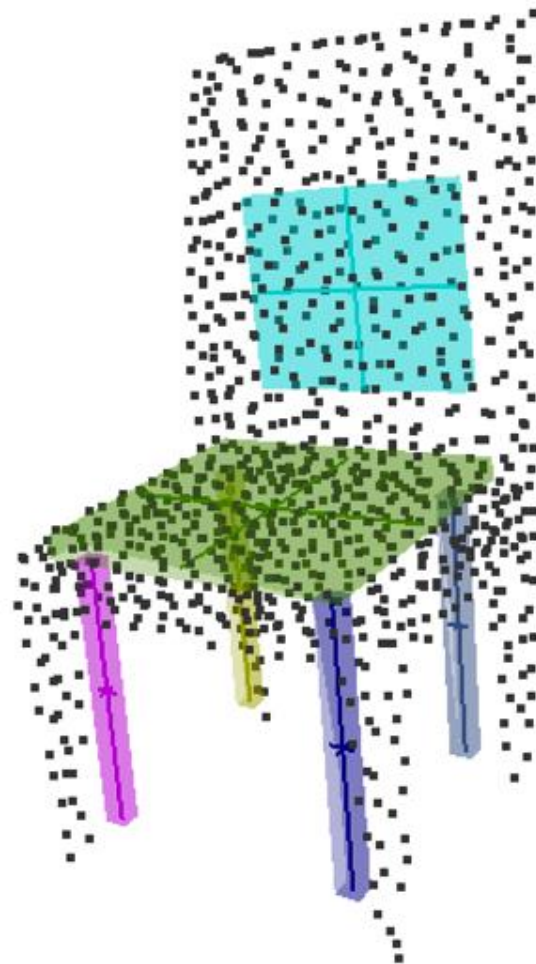


# Template Fitting Algorithm

Solve by iteratively minimizing different energy terms:

- Segmentation and labeling
- Point correspondence
- Part-aware deformation

$$E = E_{\text{data}} + \gamma E_{\text{deform}} + \beta E_{\text{smooth}}$$

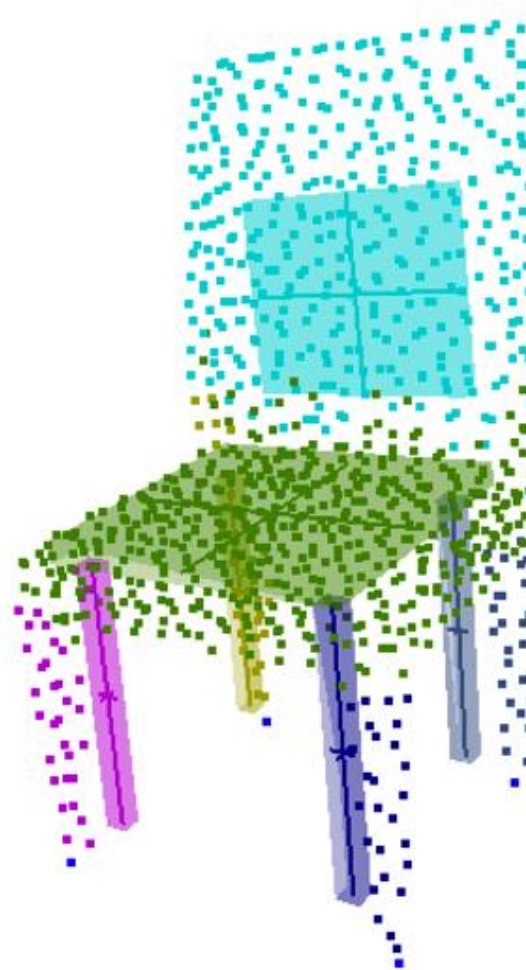


# Template Fitting Algorithm

Solve by iteratively minimizing different energy terms:

- Segmentation and labeling
  - Point correspondence
  - Part-aware deformation

$$E = \underline{E_{\text{data}}} + \gamma E_{\text{deform}} + \underline{\beta E_{\text{smooth}}}$$



Solve with graph cut [Boykov 2001]

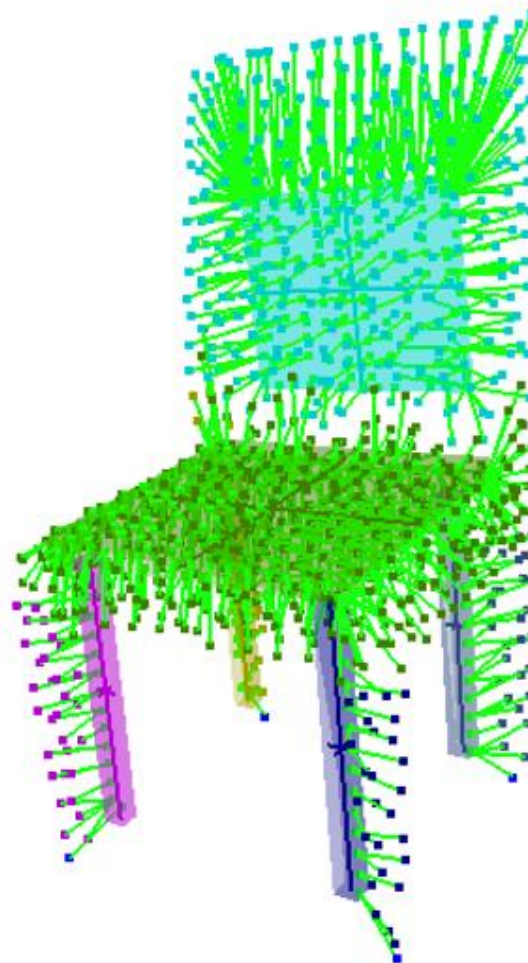


# Template Fitting Algorithm

Solve by iteratively minimizing different energy terms:

- Segmentation and labeling
  - Point correspondence
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$$E = \underline{E_{\text{data}}} + \gamma E_{\text{deform}} + \beta E_{\text{smooth}}$$



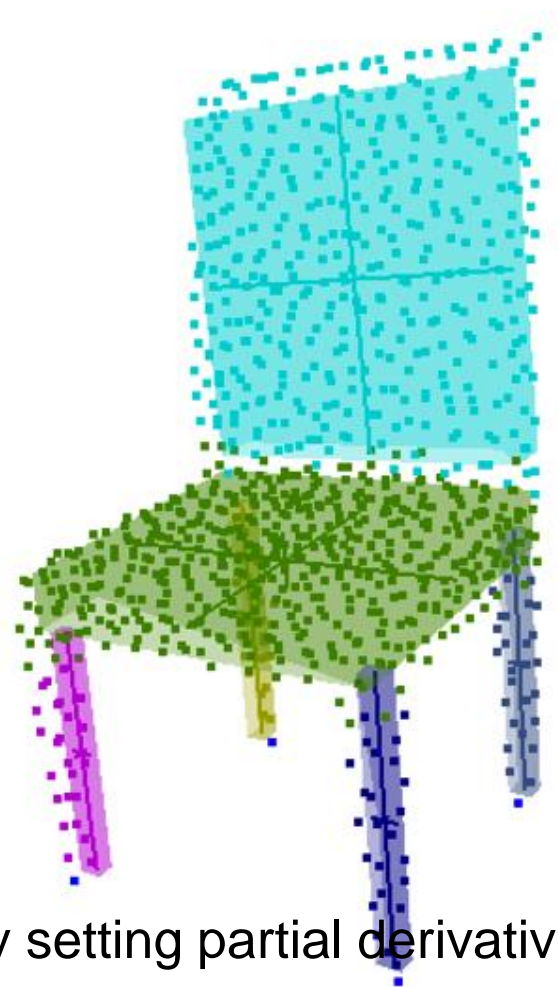
Solve with part-aware closest points

# Template Fitting Algorithm

Solve by iteratively minimizing different energy terms:

- Segmentation and labeling
- Point correspondence
- Part-aware deformation

$$E = \underline{E_{\text{data}}} + \gamma \underline{E_{\text{deform}}} + \beta E_{\text{smooth}}$$

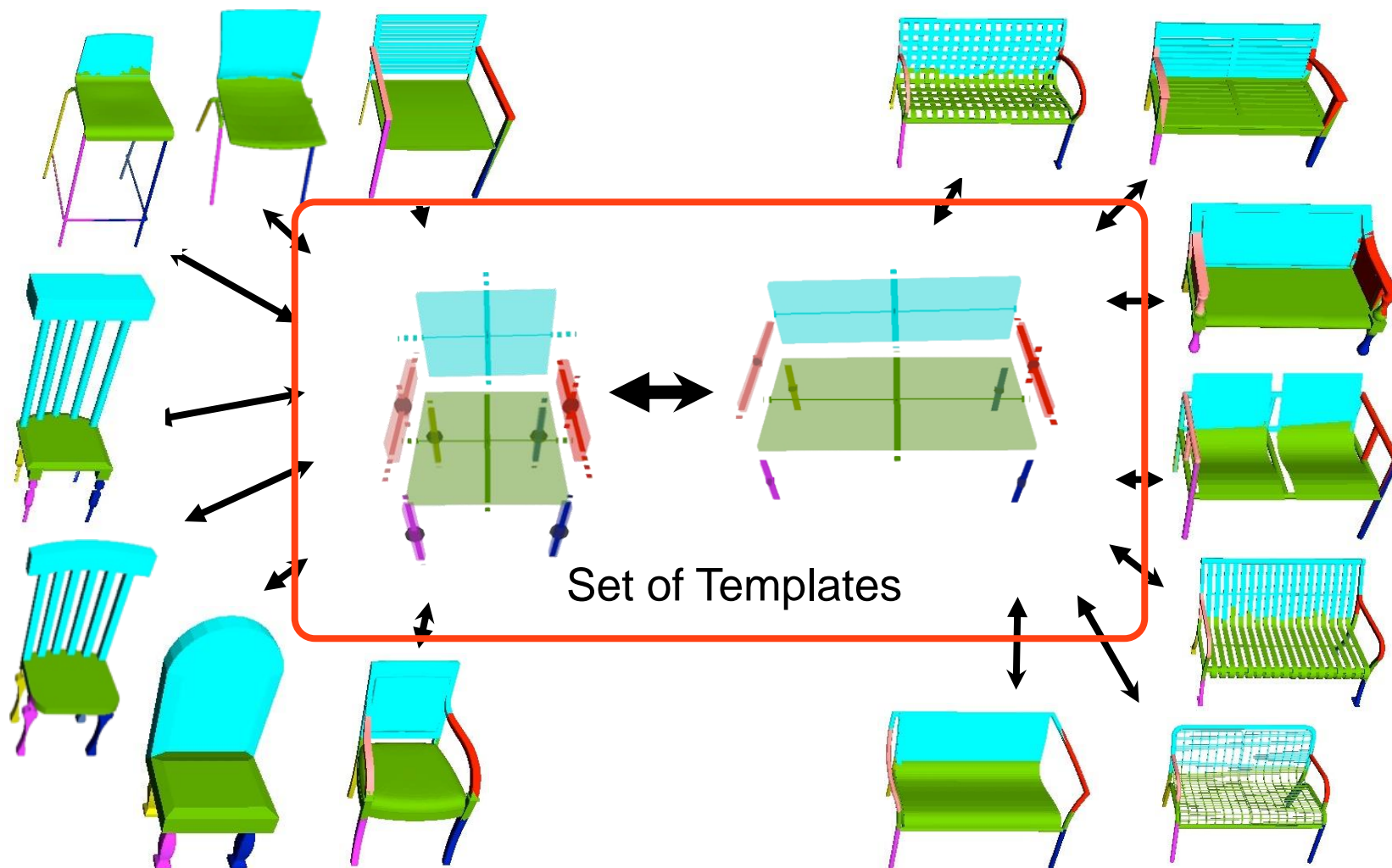


Solve for positions and scales of each part by setting partial derivatives to zero.



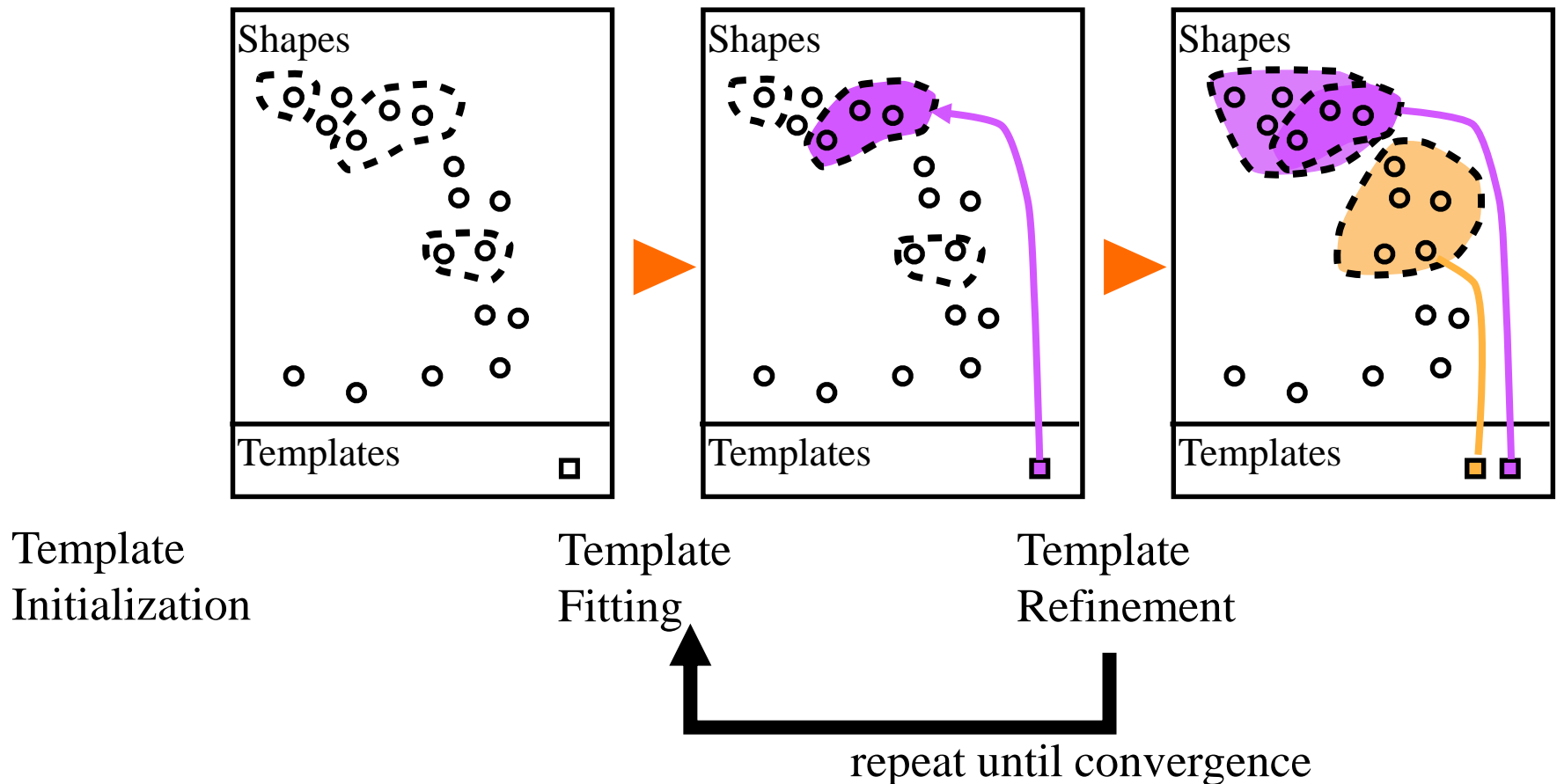
# Template Learning Problem

Aim to **learn** a set of corresponding templates that provides a good fit to every mesh in the database

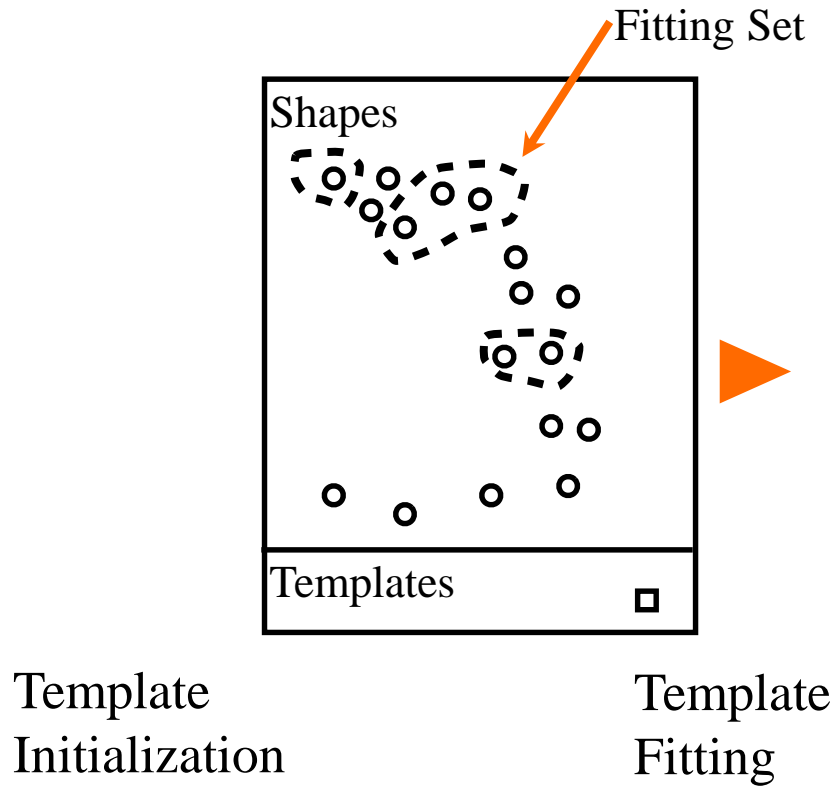


# Template Learning Algorithm

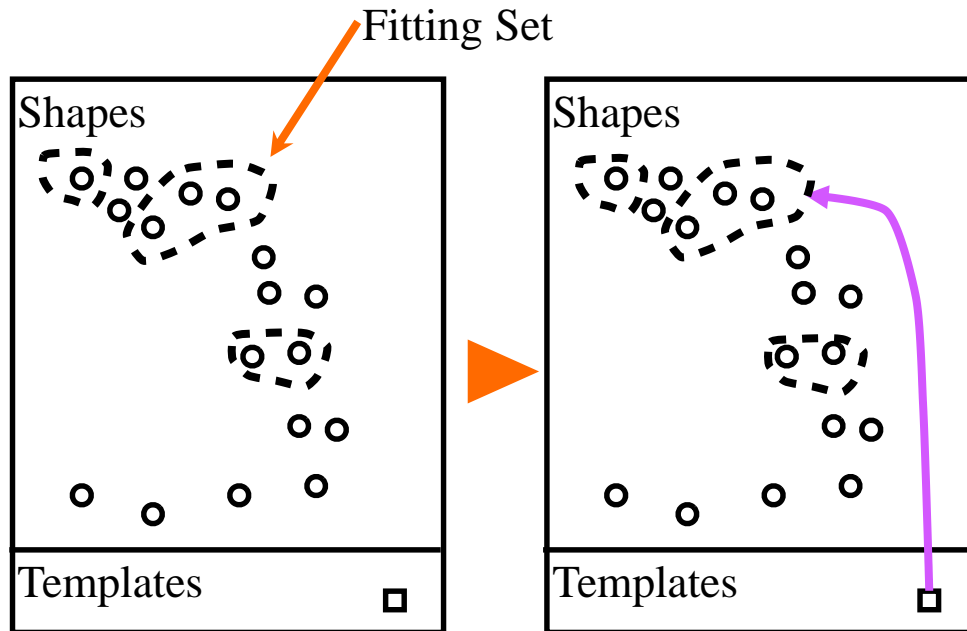
Iteratively grow a set of templates with each optimized to fit a different cluster of meshes



# Template Learning Algorithm



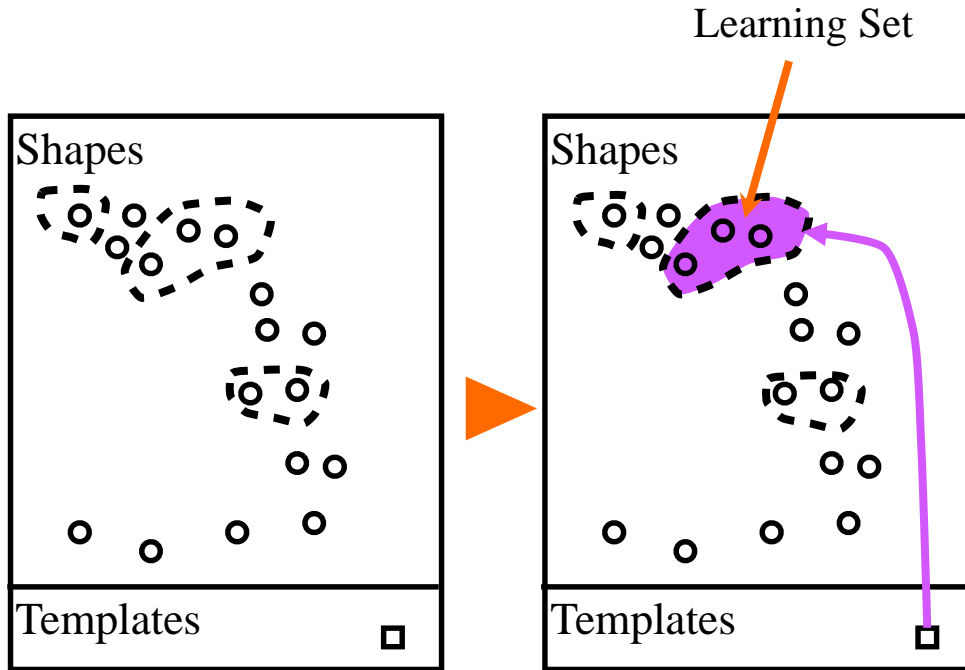
# Template Learning Algorithm



Template  
Initialization

Template  
Fitting

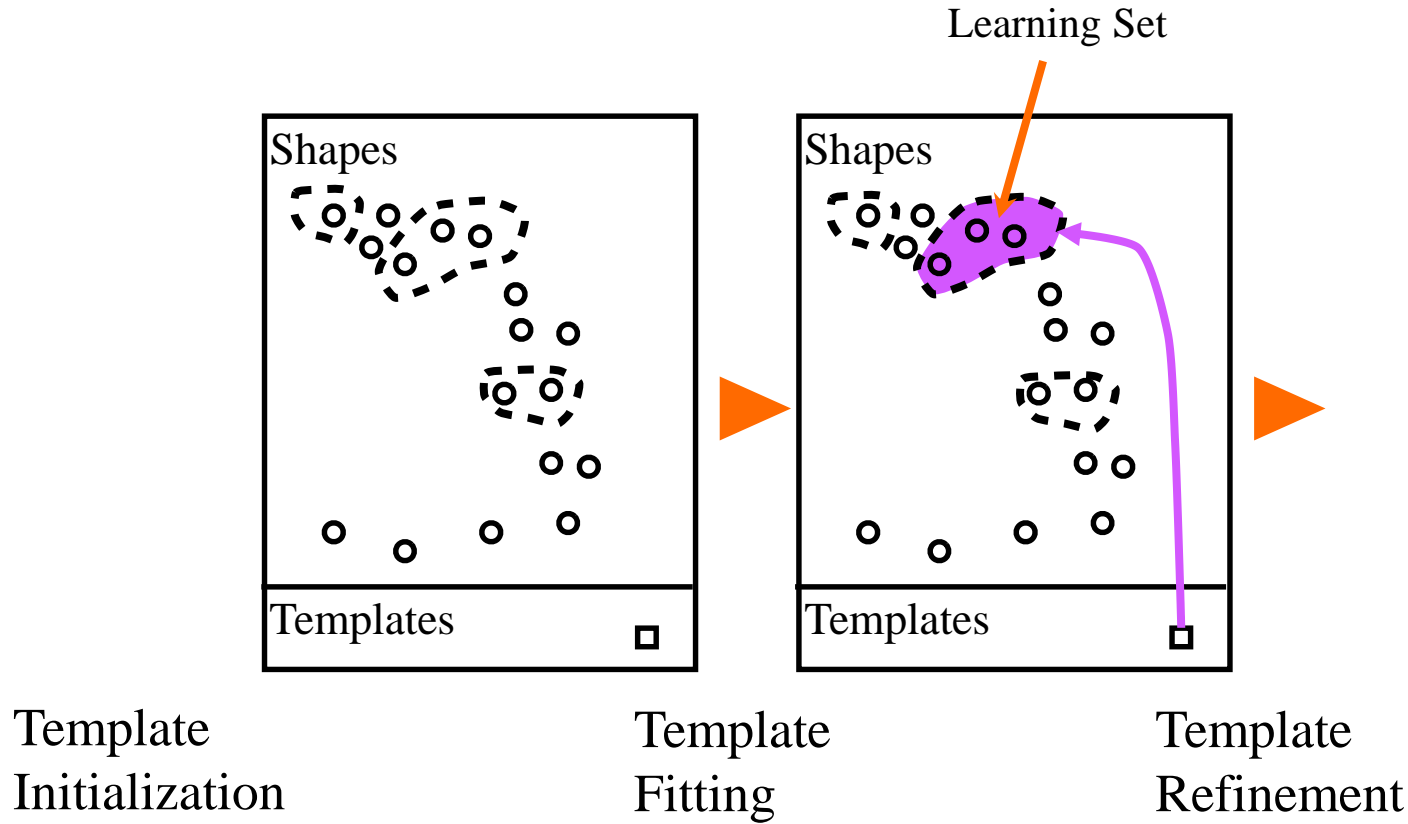
# Template Learning Algorithm



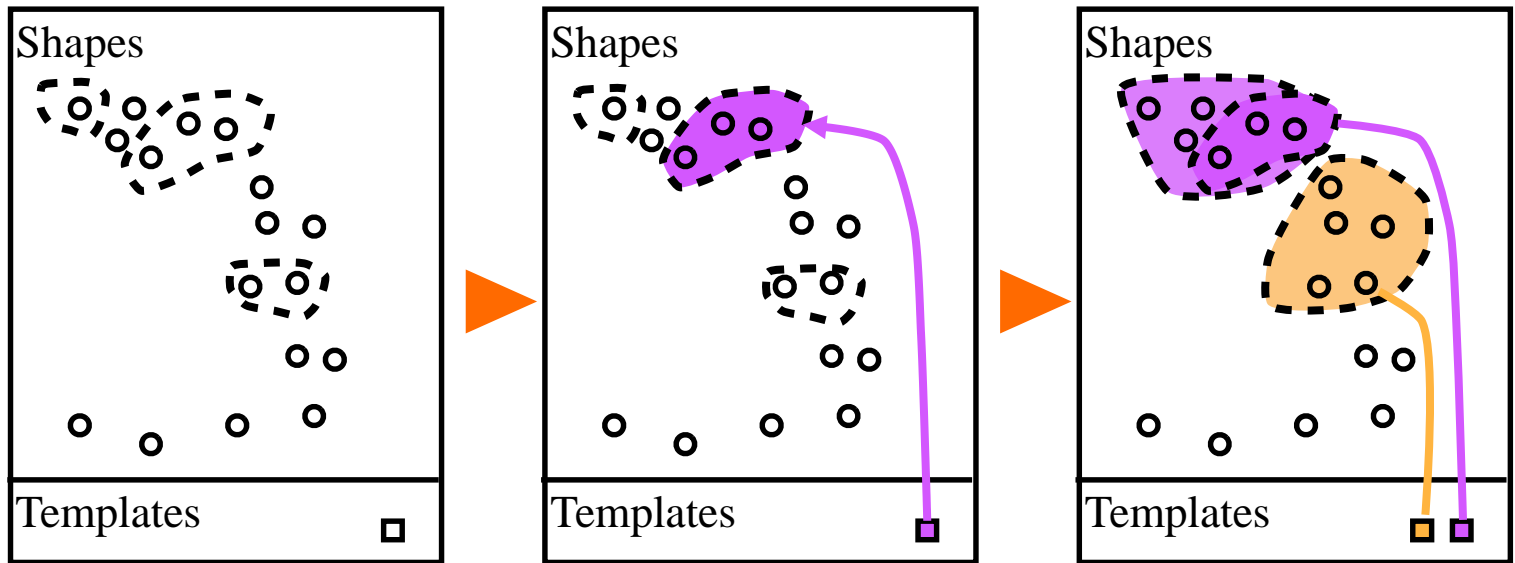
Template  
Initialization

Template  
Fitting

# Template Learning Algorithm



# Template Learning Algorithm



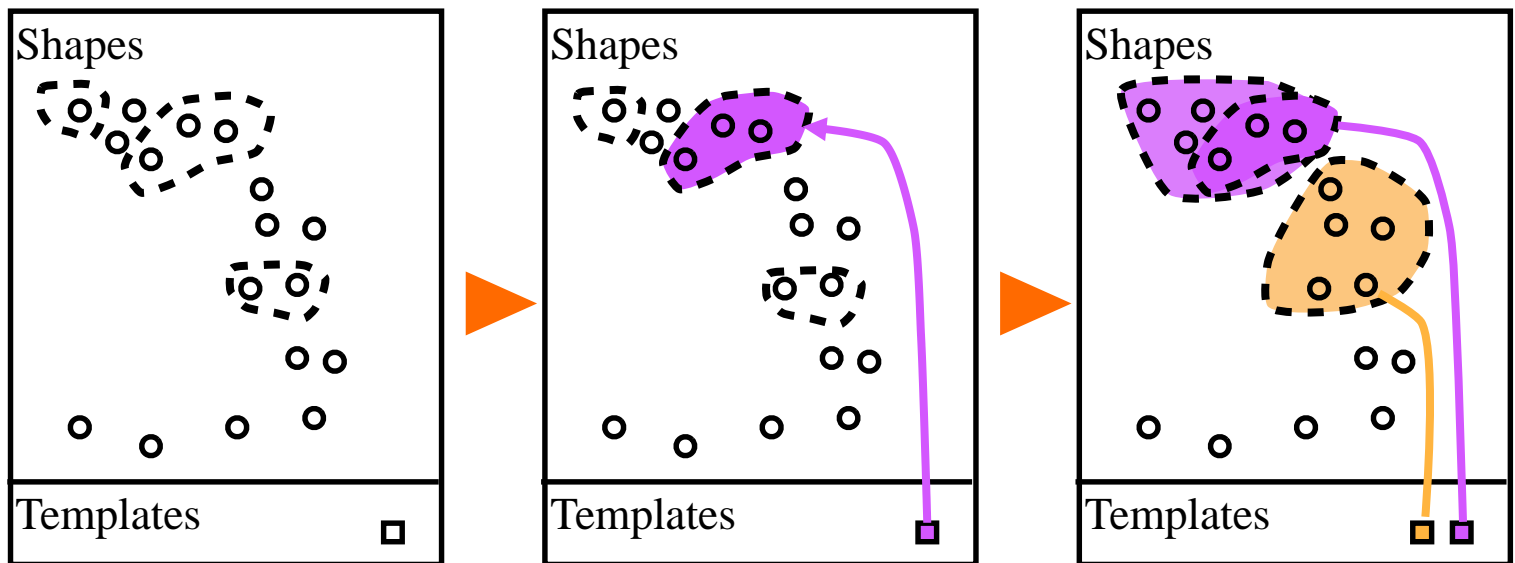
Template  
Initialization

Template  
Fitting

Template  
Refinement



# Template Learning Algorithm



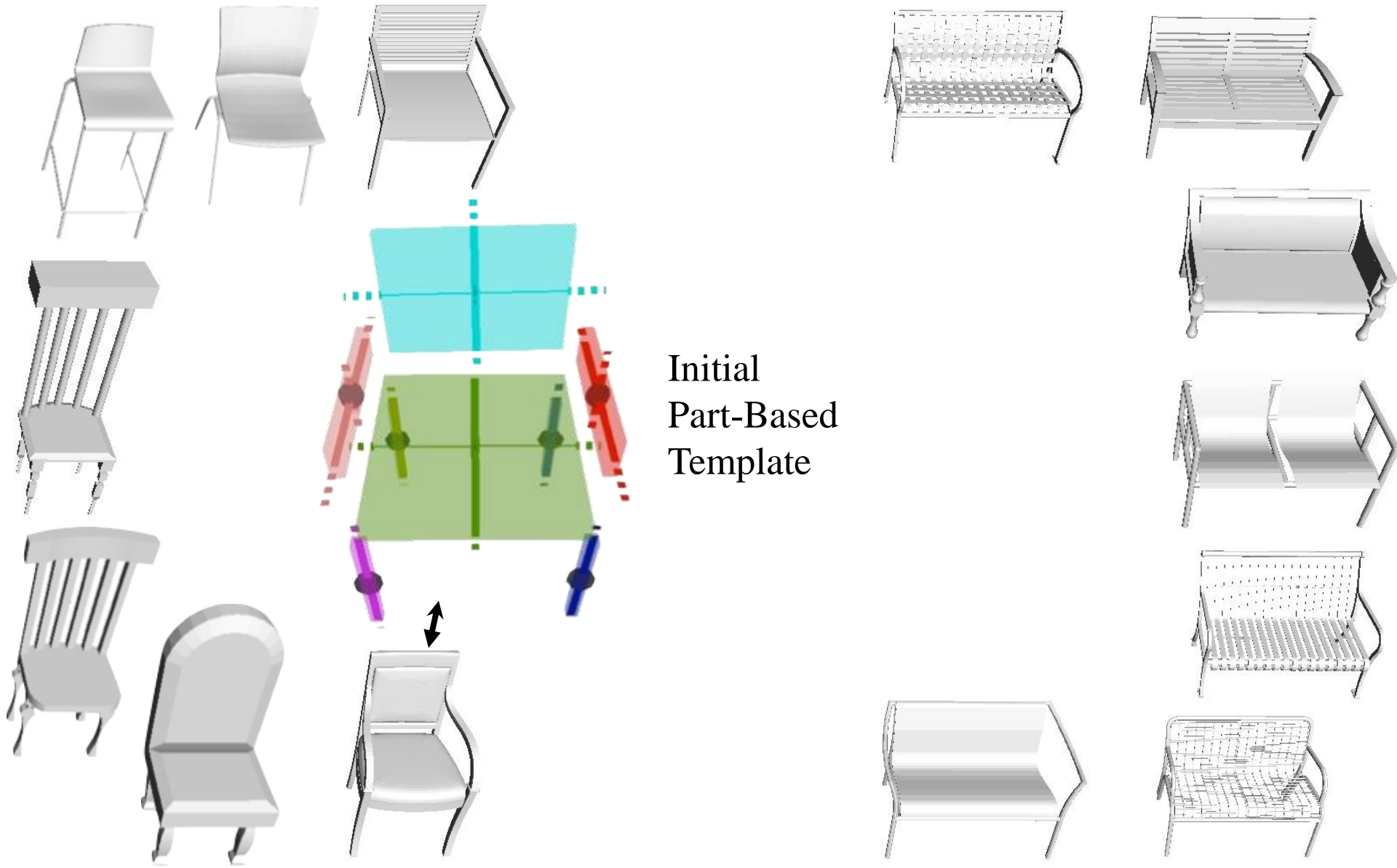
Template  
Initialization

Template  
Fitting

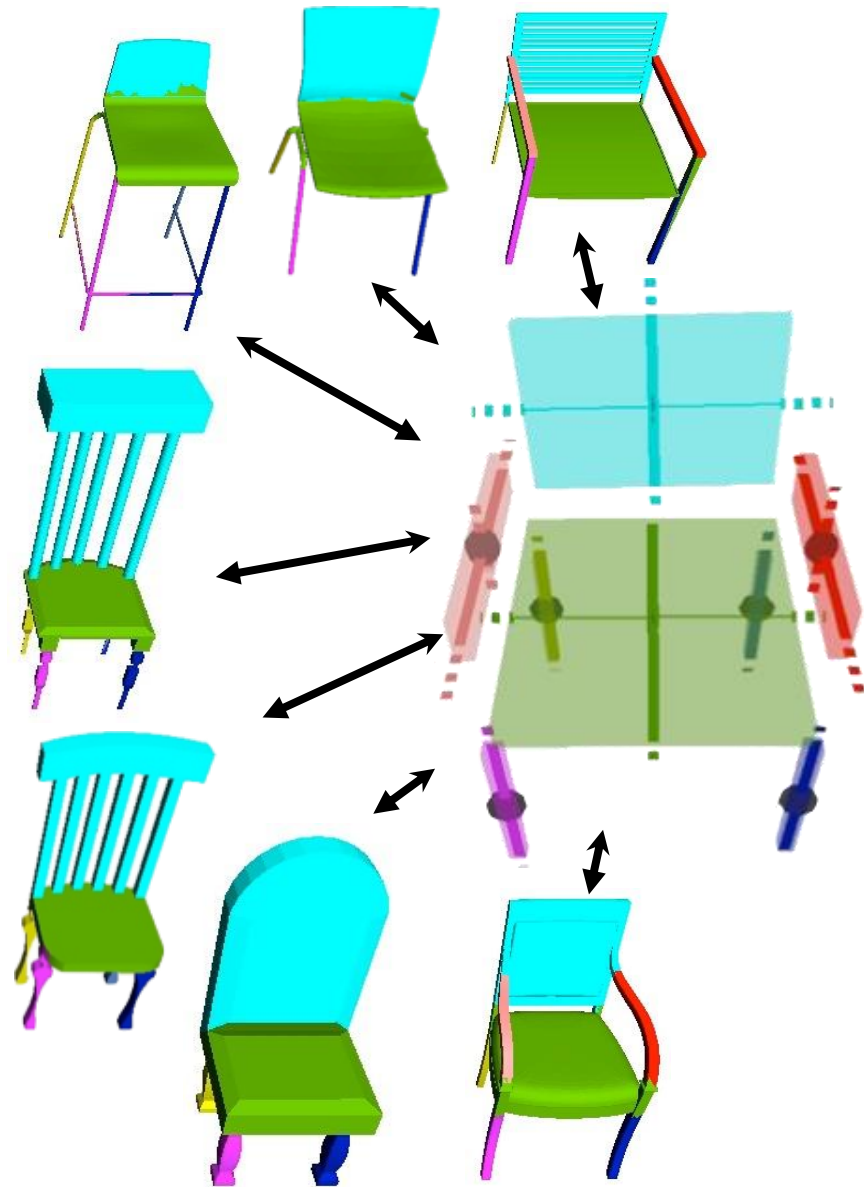
Template  
Refinement

repeat until convergence

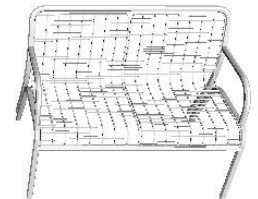
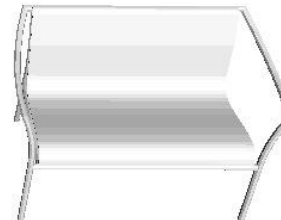
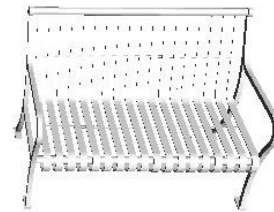
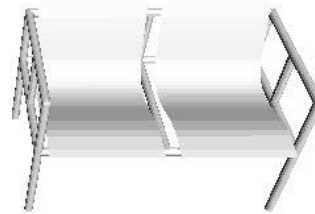
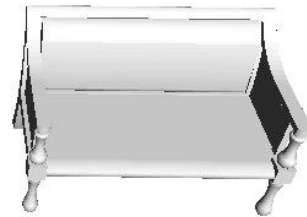
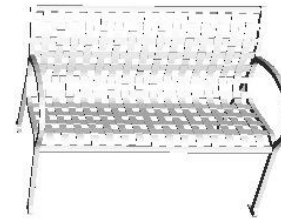
# Template Learning Example



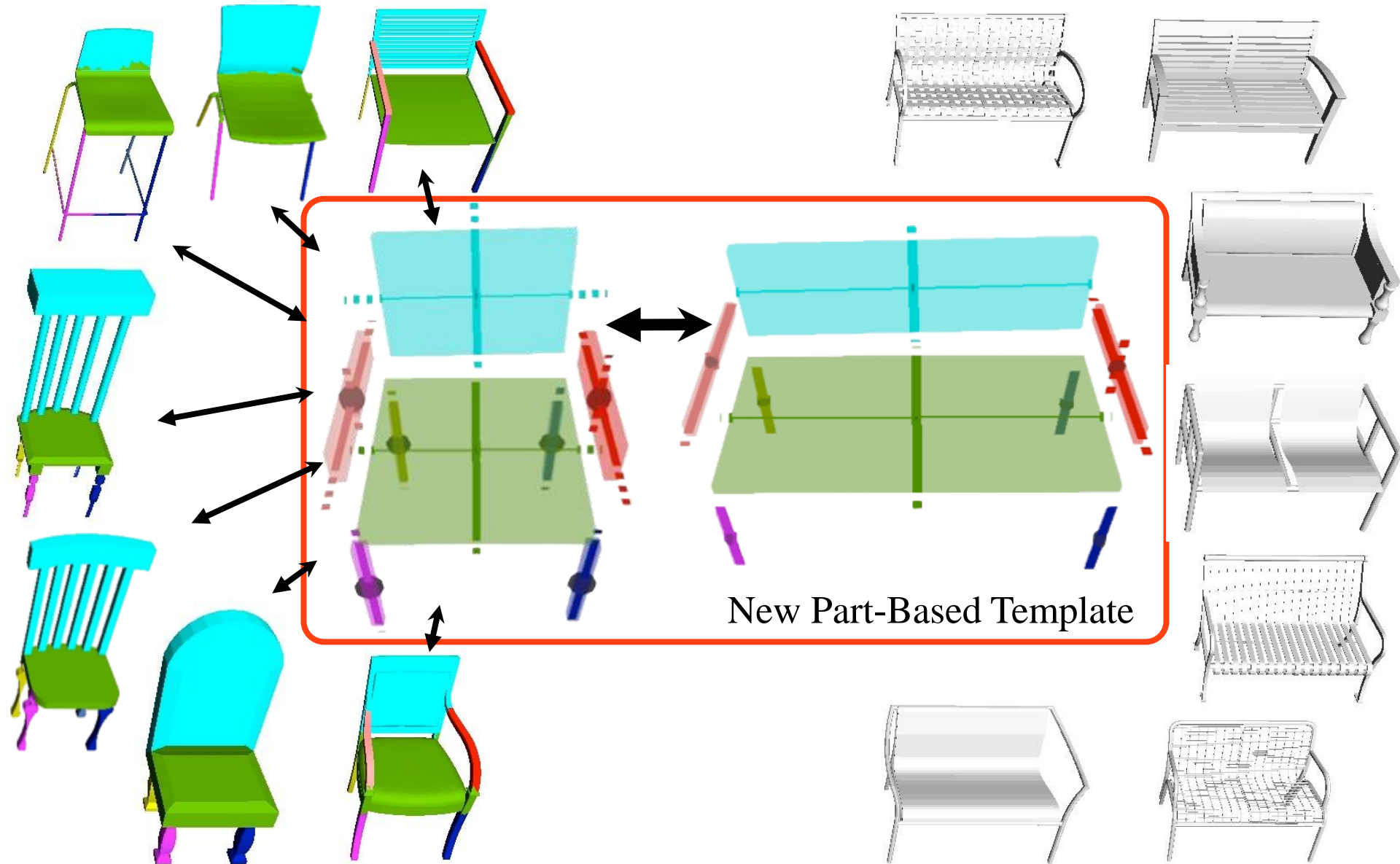
# Template Learning Example



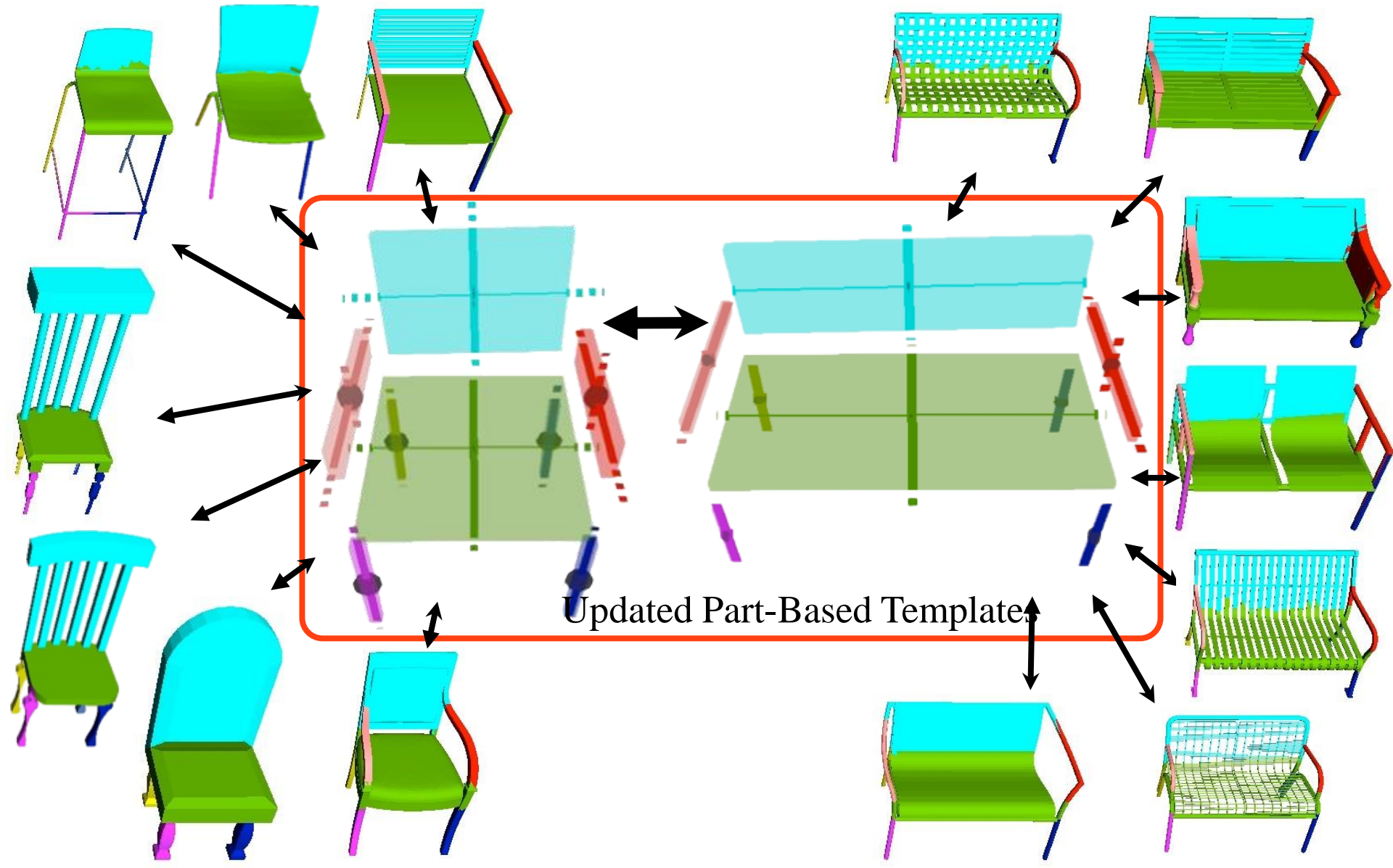
Updated  
Part-Based  
Template



# Template Learning Example



# Template Learning Example





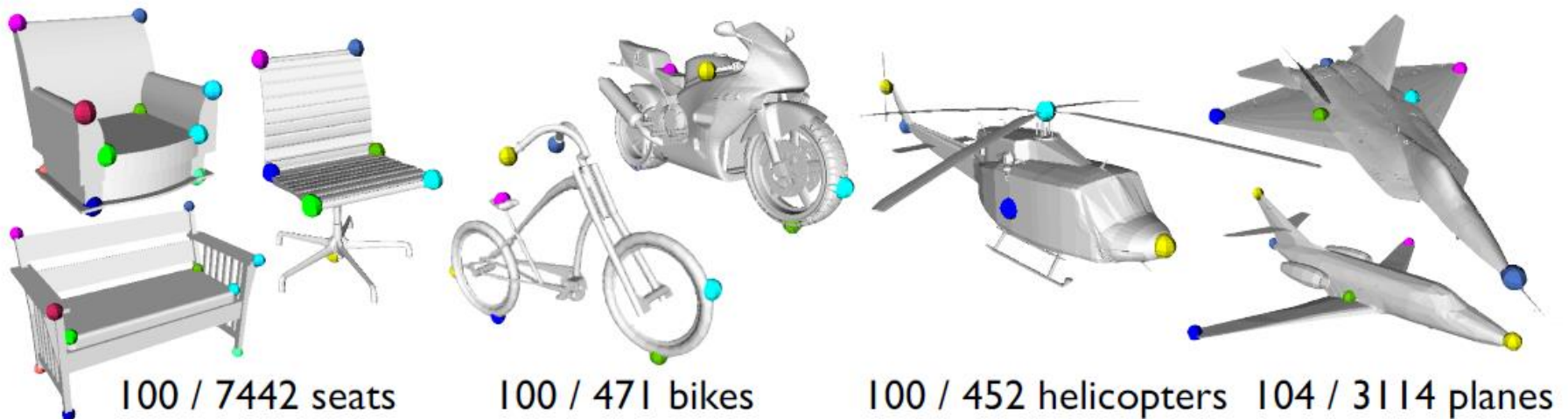
# Template Learning and Fitting Results

## Data sets:

- Crawl SketchUp Warehouse for collections by keyword
- Eliminate outliers with Mechanical Turk
- Specify manual correspondences for subset of models

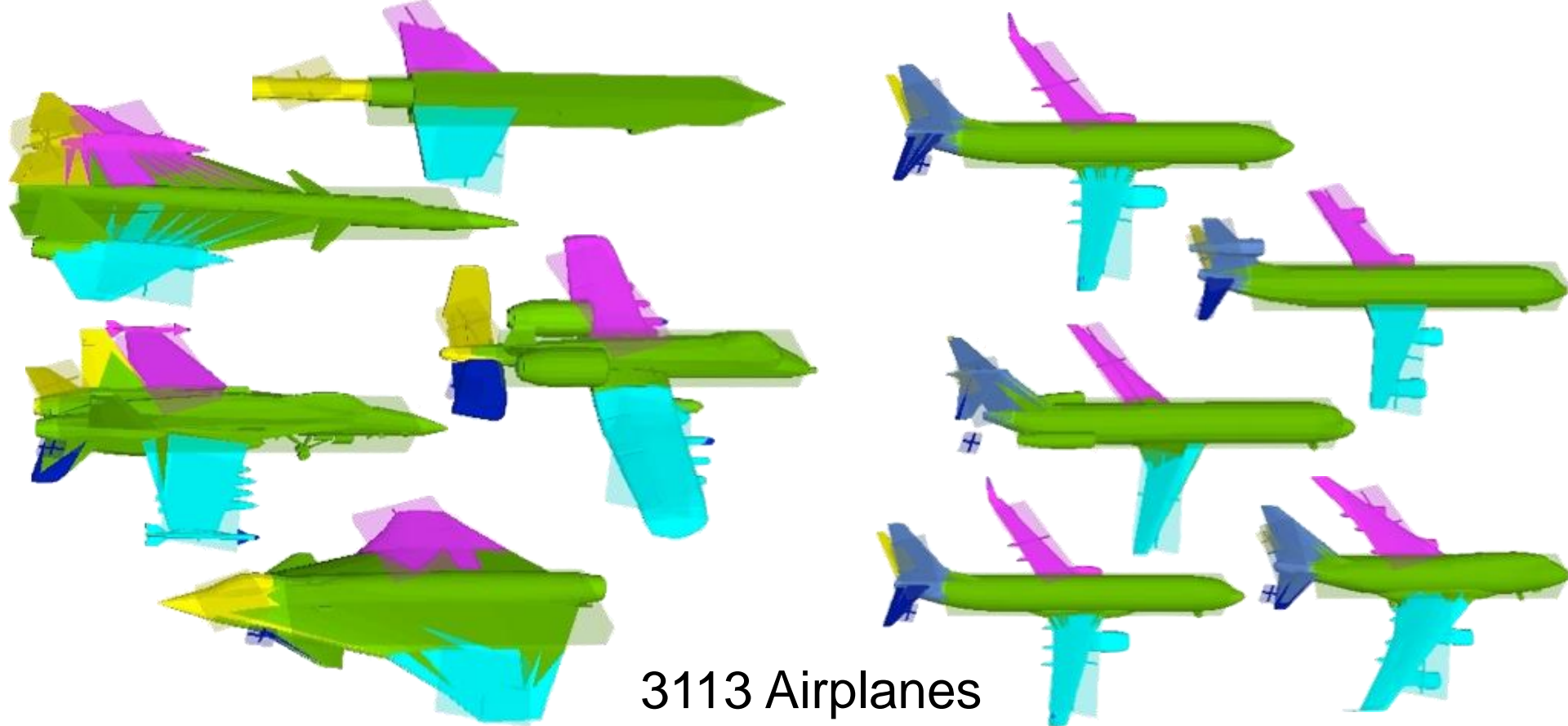
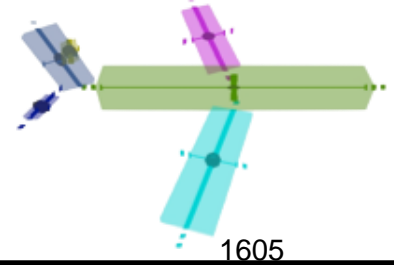
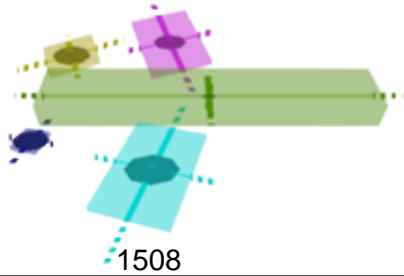
## Experiments:

- Solve for part-based templates for collection
- Evaluate correspondences & segmentations



# Template Learning and Fitting Results

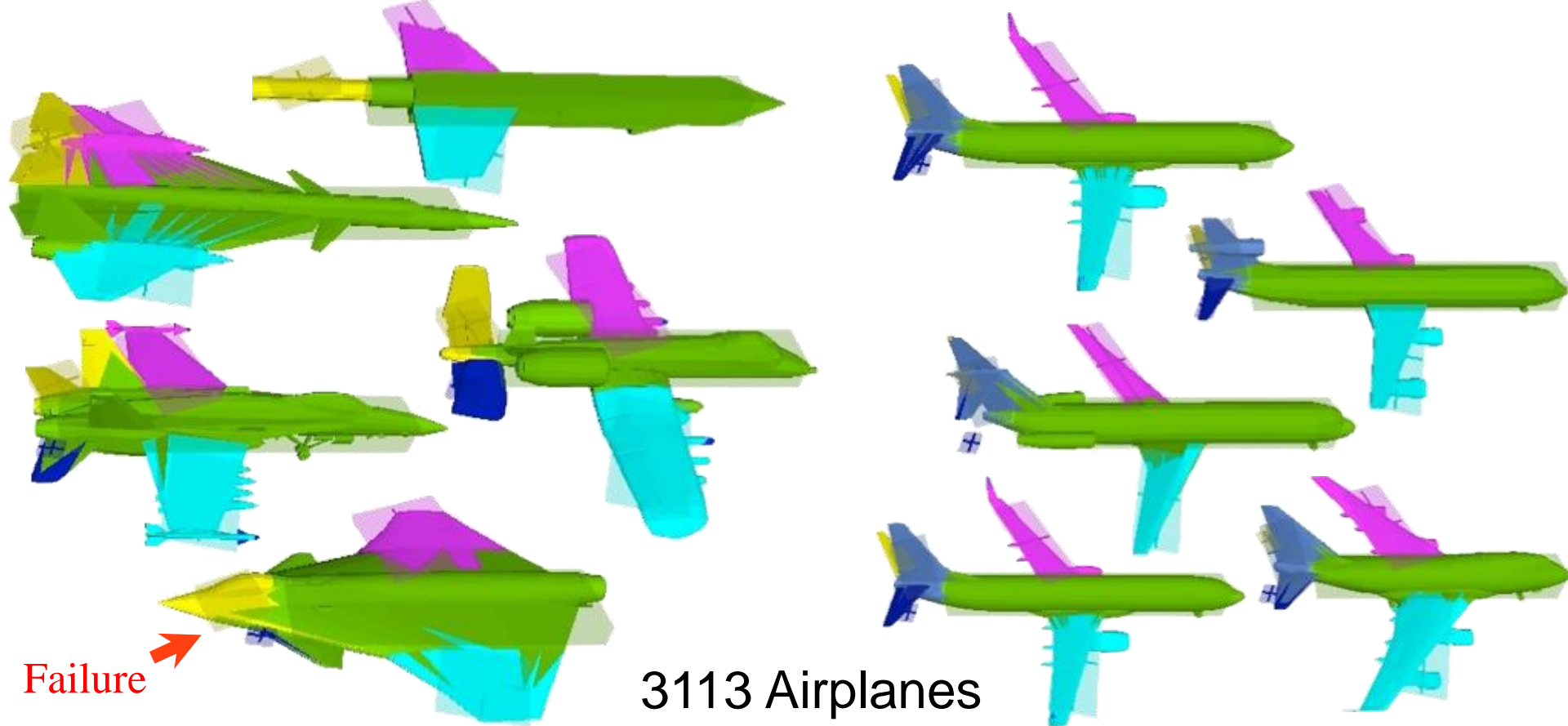
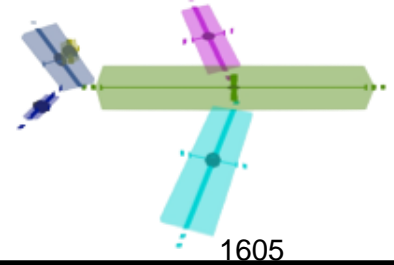
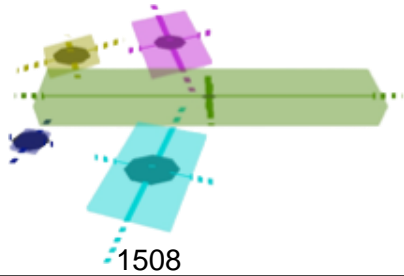
2 Templates





# Template Learning and Fitting Results

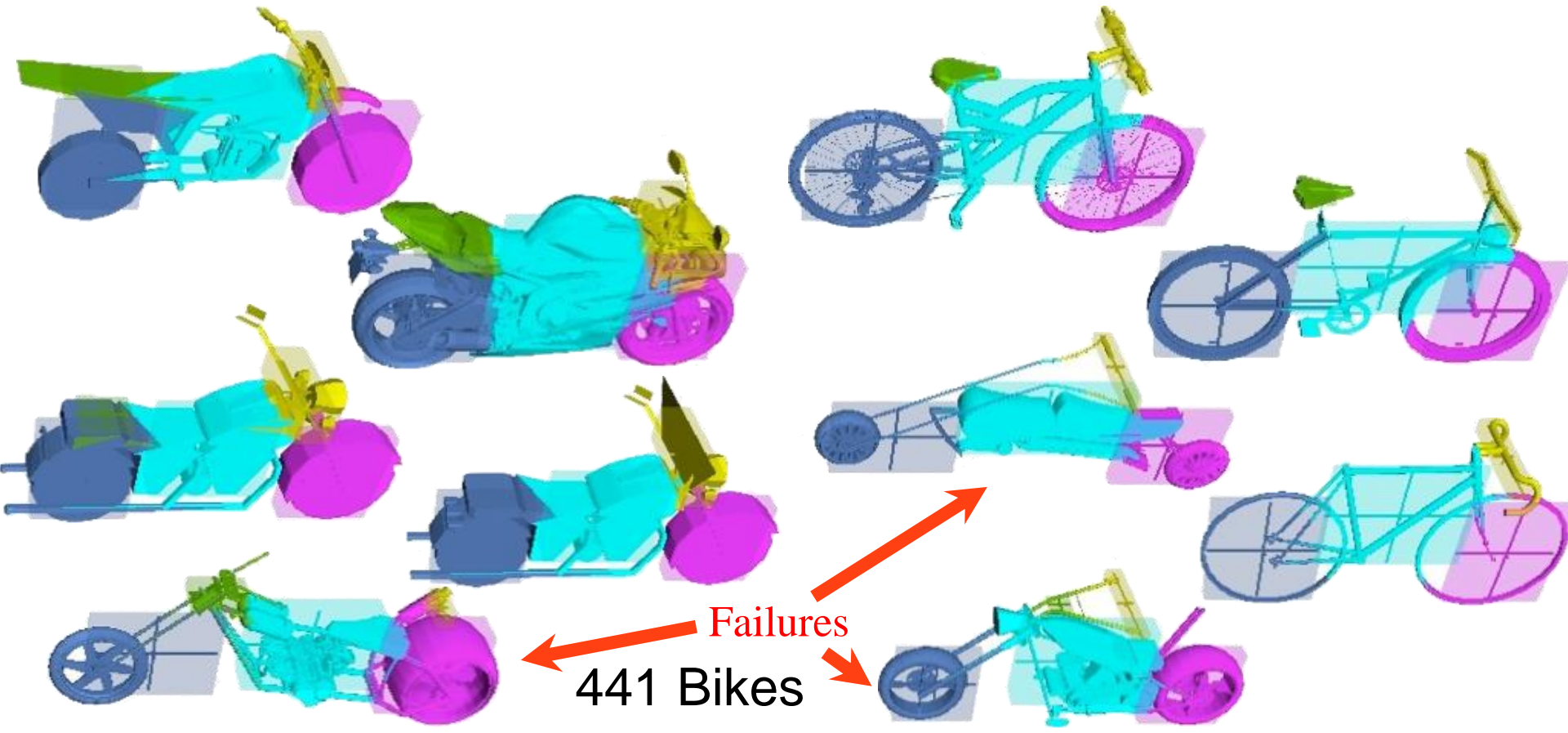
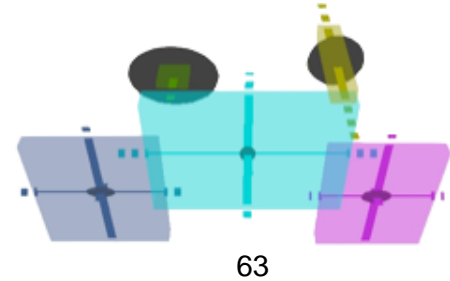
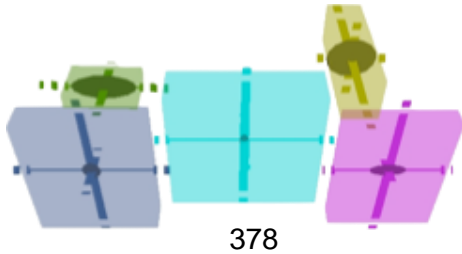
2 Templates





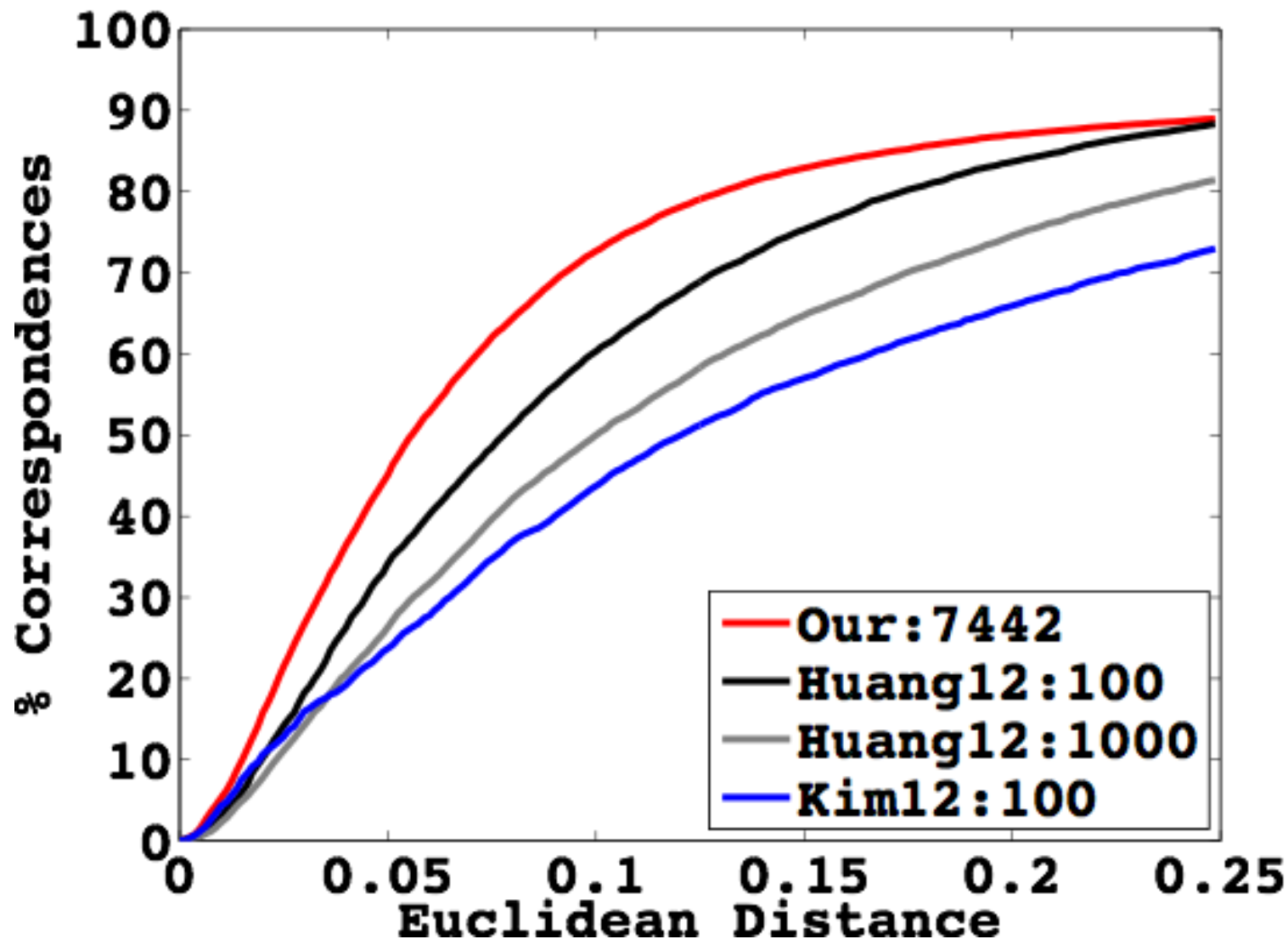
# Template Learning Results

2 Templates




# Surface Correspondence Results

Correspondence benchmark (7442 seats)



# Surface Segmentation Results

Co-segmentation benchmark [Sidi et al, 2011]

Class	Hu	Our	 within 2% or ours is better
Chairs	89.6	97.6	
Lamps	90.7	95.2	
FourLegged	88.7	86.9	
Goblets	99.2	97.6	
Vase	80.2	81.3	
Guitars	98.0	88.5	
Candelabra	93.9	82.4	

# Outline of Talk

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Introduction

Learning probabilistic models from 3D collections

- Part-based templates

- Generative model

Conclusions



# Goal for This Project

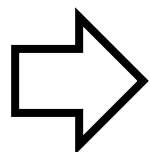


Exemplar  
scenes

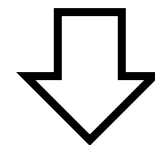
+



Database  
of Scenes

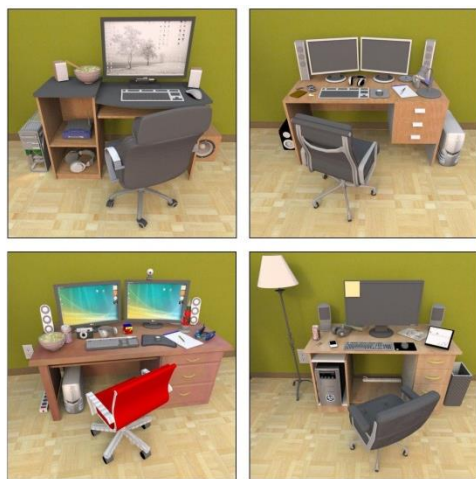


Probabilistic  
Model of Shape



Synthesized novel scenes

# Goal for This Project

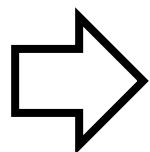


Exemplar  
scenes

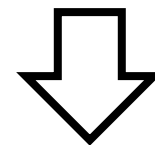
+



Database  
of Scenes



Probabilistic  
Model of Shape



## Challenge

Need to learn a model  
with great generality  
from few examples



Synthesized novel scenes



# Contextual Object Categories

Define categories of objects based on their contexts in a scene rather than basic functions

- Learned from examples by clustering of objects with similar spatial neighborhoods



Some Contextual Object Categories

# Generative Model

Represent the probability of a scene  $S$  by a generative model based on category cardinalities ( $c$ ), support hierarchy topology relationships ( $t$ ), and spatial arrangement relationships ( $a$ )

$$P(S) = P(c, t, a) = P(a/t, c) P(t/c) P(c)$$



Exemplar scenes

# Generative Model Details

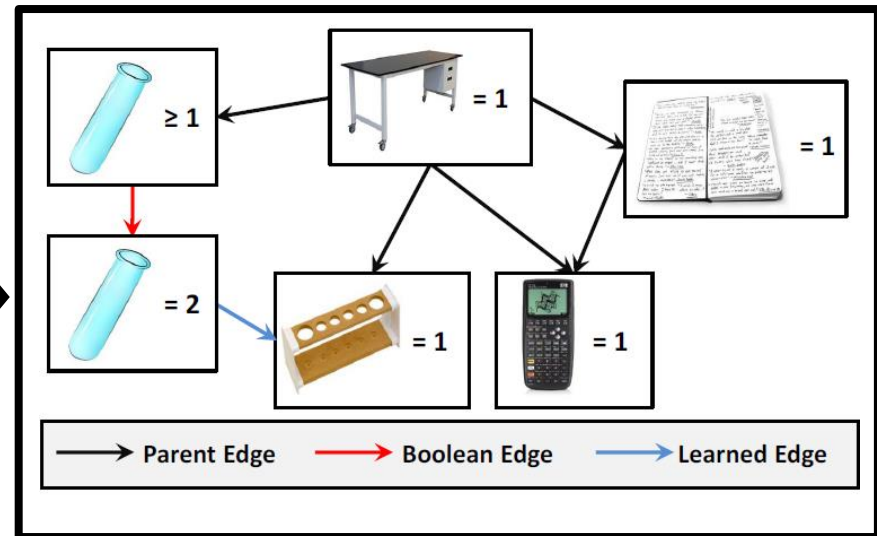
Category cardinalities:  $P(c)$

- Represent with Bayesian network
- Boolean random variables (# desks > 1?)
- Add support surface constraints



Lab table	Test tube rack	Test tube	Notebook	Calculator
1	1	2	0	0
1	0	1	0	1
1	0	0	1	1

Object frequencies in target scenes  
+ support constraints



# Generative Model Details

---

Support relationships:  $P(t/c)$

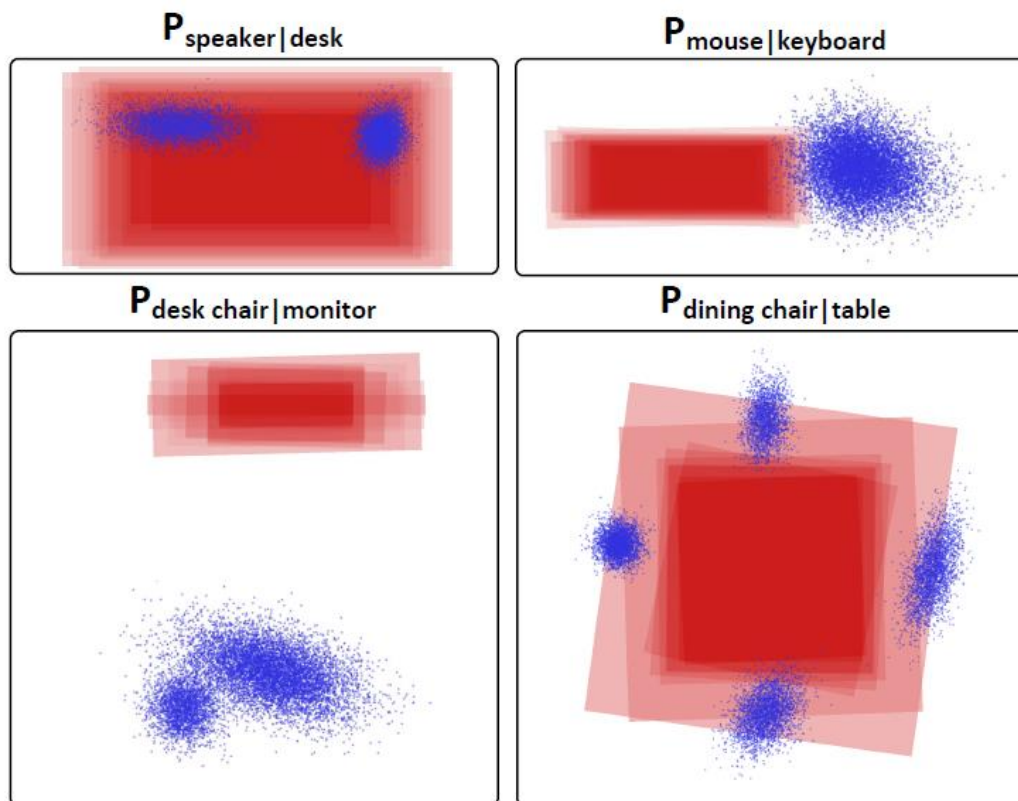
- Boolean random variables (desk supports keyboard?)
- Learn frequencies for pairs of categories
- Total probability is product over all objects in scene

$$P(t|c) = \prod_o P(C(o), C(\text{support}(o)))$$

# Generative Model Details

Spatial arrangements:  $P(a/t,c)=R(a,t,c)S(a,t,c)$

- Random variables for relative positions and orientations
- Pairwise distributions of spatial relationships

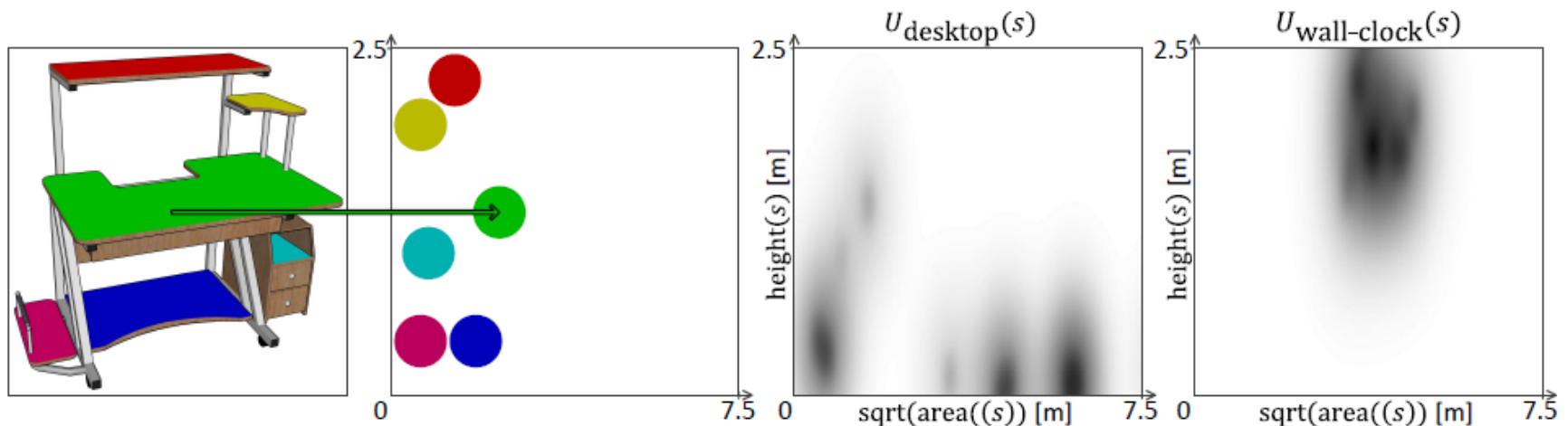


Distributions of spatial relationships for pairs of object categories

# Generative Model Details

Spatial arrangements:  $P(a/t, c) = R(a, t, c) S(a, t, c)$

- Random variables for relative positions and orientations
- Pairwise distributions of spatial relationships
- Feature distributions for positions on support surfaces



Distributions of geometric features of support surfaces



# Scene Synthesis

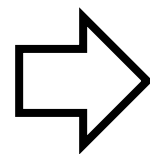


Exemplar  
scenes

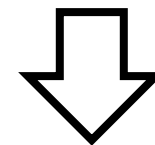
+



Database  
of Scenes

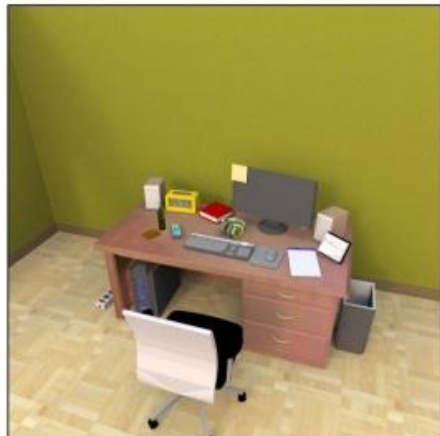


Probabilistic  
Model of Shape



Synthesized novel scenes

# Scene Synthesis Results

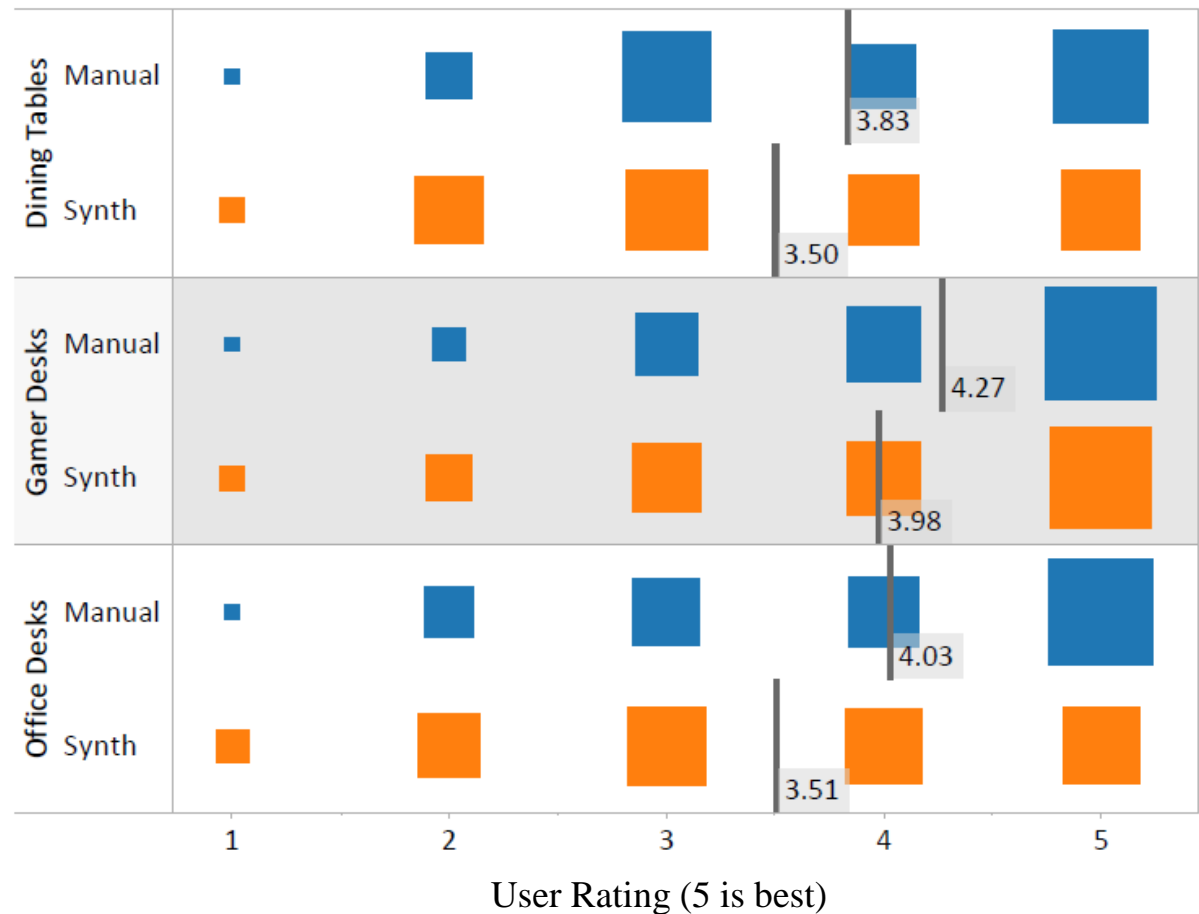


Synthesized novel scenes



# Scene Synthesis Results

User study suggests that people find our synthesized scenes almost as good as manually created ones



# Outline of Talk

---

Introduction

Learning probabilistic models from 3D collections

- Part-based templates
- Generative model

➤ **Conclusions**

# Conclusions

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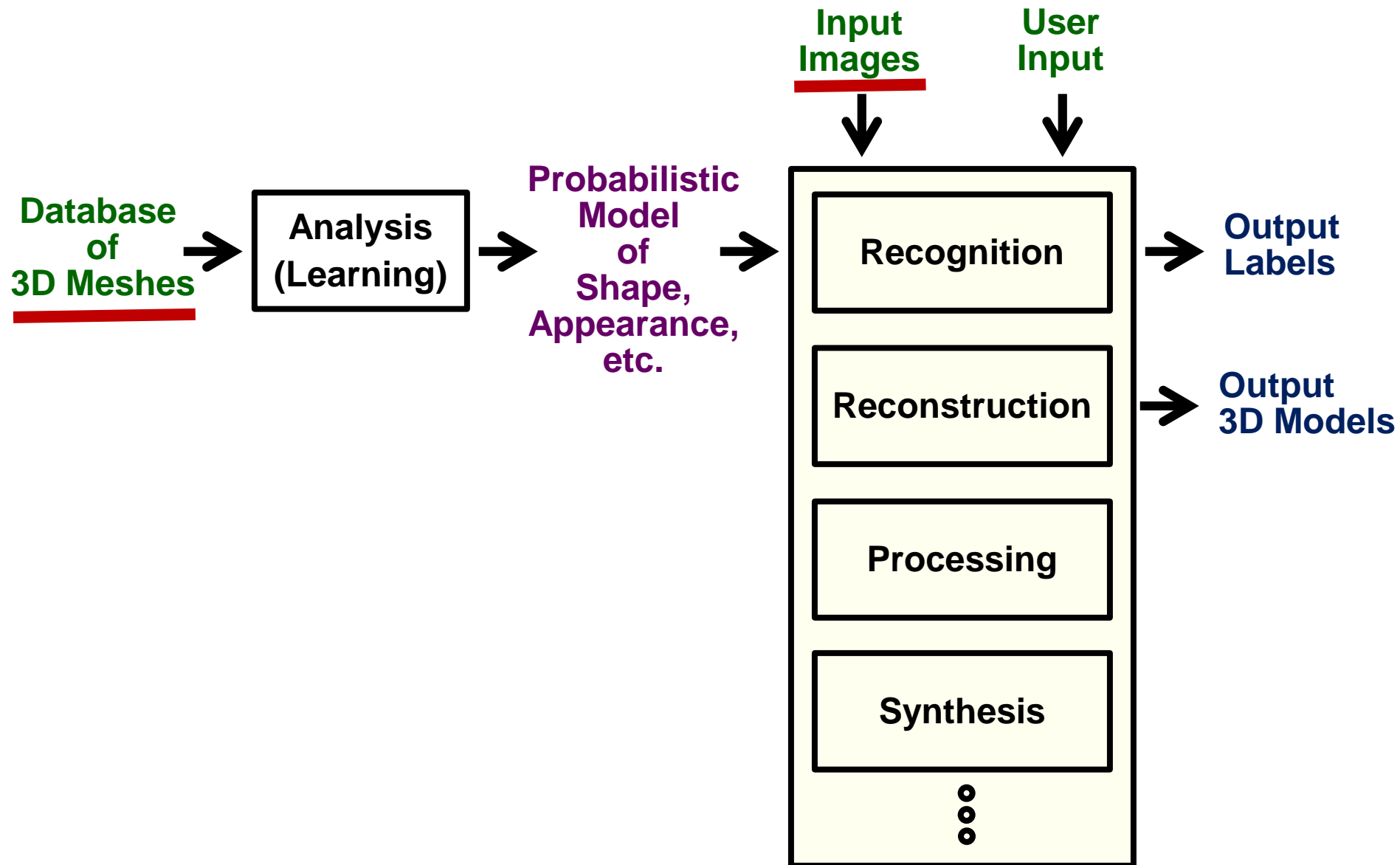
## Main result:

- Probabilistic models can be learned from collections of 3D meshes

## Future work:

- It will be interesting to see if these models can be used effectively to understand scans and images

# 3D Shape Analysis for Computer Vision?



# Acknowledgments

---

## People:

- Sid Chaudhuri, Steve Diverdi, Matthew Fisher, Pat Hanrahan, Vladimir Kim, Wilmot Li, Niloy Mitra, Daniel Ritchie, Manolis Savva

## Funding:

- NSF, NSERC, Intel, Adobe, Google

## Data sets:

- Trimble 3D Warehouse

**Thank You!**