An Introduction to Typed Assembly Language

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Acknowledgments

- These notes started as a lecture given by Greg Morrisett, July 2001 [10] and have since been extended and edited.
- They give readers a simple introduction to many of the core elements of the Cornell Typed Assembly Language project.
 - Contributors: G. Morrisett, K. Crary, N. Glew, D.
 Grossman, T. Jim, C. Hawblitzel, M. Hicks, L. Hornof,
 R. Samuels, F. Smith, D. Walker, S. Weirich, S. Zdancewic
 - See http://www.cs.cornell.edu/talc
- Suggested Reading
 - G. Morrisett, D. Walker, K. Crary, N. Glew. From System-F to Typed Assembly Language. [13]
 - G. Morrisett, K. Crary, N. Glew, D. Walker. Stack-Based Typed Assembly Language. [12]
- A more complete bibliography appears at the end of these notes.

Safety through Types

- An architecture for safe mobile code:
 - Download code and typing annotations from untrusted code producer
 - Verify untrusted code using trusted type checker
 - Link verified code into extensible system & run without error
- Security hinges on an understanding of programming language structure
 - We must be able to reason precisely about what programs do.
 - We must be able to define the "good" and "bad" behaviors.
 - We must be able to identify and rule out (mechanically) those programs that might exhibit "bad" behaviors.
- Typed Assembly Language (TAL) is the language technology we will use to accomplish the goals.

Outline

- TAL-0: Assembly Language Control Flow and Basic Types
- TAL-1: Parametric Polymorphism
- TAL-2: Stack Types
- Type-Directed Compilation: From Tiny to TAL-2
- TAL-3: Data Structures
- TAL-4: Dependency
- TAL-5: Modularity and Linking
- References

What Is TAL?

• In theory:

- An idealized RISC-style assembly language and formal operational semantics for a simple abstract machine
- A formal type system (collection of type systems) that captures properties of processor register state, stack and memory
- Rigorous proofs demonstrate that TAL enforces important safety guarantees in assembly language programs

• In practice [20, 11]:

- A type checker for almost all of the Intel Pentium IA32 architecture
- Tools for assembly, disassembly, and linking of TAL binaries (a pair of machine code segment and types segment)
- A prototype compiler for a safe imperative language (Popcorn)
- These notes concentrate on the development of the theory of TAL and type-directed compilation. This presentation streamlines the formal work from past papers.

Example Assembly Language Program

High-level code:

Assembly language code:

```
	extcolor{\%} r_1 holds n, r_2 holds a, r_{31} holds return address 	extcolor{\%} which expects the result in r_1
```

```
fact: ble r_1, L2 % if n \leq 0 goto L2 mul r_2, r_2, r_1 % a := a 	imes n sub r_1, r_1, 1 % n := n-1 jmp fact % goto fact L2: mov r_1, r_2 % result := a jmp r_{31} % jump to return address
```

TAL-0

Syntax of a simple RISC-like assembly language.

- Registers: $r \in \{r1, r2, r3, \ldots\}$
- Labels: $L \in Identifier$
- Integers: $n \in [-2^{k-1}..2^{k-1})$
- Blocks: $B := jmp v \mid i; B$
- $\bullet \ \text{Instrs:} \ i ::= \mathit{aop}\ r_d, r_s, v \mid \mathit{bop}\ r, v \mid \mathsf{mov}\ r, v$
- Operands: $v := r \mid n \mid L$
- ullet Arithmetic Ops: $aop ::= add \mid sub \mid mul \mid \cdots$
- Branch Ops: $bop := beq | bgt | \cdots$

TAL-0 Abstract Machine

- Model evaluation as a transition function mapping machine states to machine states: $\Sigma \longmapsto \Sigma$
- Machine: $\Sigma = (H, R, B)$
- H is a partial map from labels to basic blocks B.
- R maps registers to values (ints n or labels L). Notation:

$$R(n) = n$$

 $R(L) = L$
 $R(r) = v$ if $R = \{\dots, r \mapsto v, \dots\}$

• B is a basic block (corresponding to the current program counter.)

Operational Semantics

$$(H,R,\operatorname{mov} r_d,v;B)\longmapsto (H,R[r_d:=R(v)],B)$$

$$(H,R,\operatorname{add} r_d,r_s,v;B)\longmapsto (H,R[r_d:=n],B)$$
 where $n=R(v)+R(r_s)$
$$(H,R,\operatorname{jmp} v)\longmapsto (H,R,B)$$
 where $R(v)=L$ and $H(L)=B$
$$(H,R,\operatorname{beq} r,v;B)\longmapsto (H,R,B)$$
 where $R(r)\neq 0$
$$(H,R,\operatorname{beq} r,v;B)\longmapsto (H,R,B')$$
 where $R(r)=0,R(v)=L,\operatorname{and} H(L)=B'$

The other instructions (sub, bgt, etc.) follow a similar pattern.

Error Conditions

- The abstract machine is *stuck* if there is no transition from the current state to some next state.
- The stuck states define the "bad" things that may happen.
- Our type system will ensure that the machine never gets stuck.
- Example stuck states:
 - $(H, R, \text{add } r_d, r_s, v; B)$ and r_s or v aren't ints
 - -(H, R, jmp v) and v isn't a label, or
 - -(H, R, beq r, v:B) and r isn't an int or v isn't a label
- To distinguish between integers and labels, we require a type system.

Types

Basic types:

- $\tau ::= int \mid \Gamma \rightarrow \{ \}$
- $\Gamma ::= \{r_1:\tau_1, r_2:\tau_2, \ldots\}$

Code types:

- Code labels have type $\{r_1:\tau_1,r_2:\tau_2,\ldots\} \to \{\}$.
- The order that register names appear in a code type is irrelevant
- To jump to code with this type, register r_1 must contain a value of type τ_1 , register r_2 must contain . . .
- Intuitively, code labels are functions that take a record of arguments
- The function never returns the code block always ends with a jump to another label

Example Program with Types

```
% r_1 holds n, r_2 holds a, r_{31} holds return address % which expects the result in r_1 fact: \quad \{r_1 : int, r_2 : int, r_{31} : \{r_1 : int\} \rightarrow \{\ \}\} \rightarrow \{\ \} ble r_1, L2 % if n \leq 0 goto L2 mul r_2, r_2, r_1 % a := a \times n sub r_1, r_1, 1 % n := n-1 jmp fact % goto fact L2: \quad \{r_2 : int, r_{31} : \{r_1 : int\} \rightarrow \{\ \}\} \rightarrow \{\ \} mov r_1, r_2 % result := a jmp r_{31} % jump to return address
```

Mis-typed Program

```
\begin{array}{lll} \textit{fact:} & \{r_1 : int, r_{31} : \{r_1 : int\} \to \{\;\}\} \to \{\;\} \\ & \text{ble} \, r_1, L2 \\ & \text{mul} \, r_2, r_2, r_1 & \text{\% ERROR! } \, r_2 \, \, \text{doesn't have a type} \\ & \text{mov} \, r_1, r_3 \\ & \text{jmp} \, L1 & \text{\% ERROR! no such label} \\ \\ L2 : & \{r_2 : int, r_{31} : \{r_1 : int\} \to \{\;\}\} \to \{\;\} \\ & \text{mov} \, r_{31}, r_2 \\ & \text{jmp} \, r_{31} & \text{\% ERROR! } \, r_{31} \, \, \text{is not a label} \\ \end{array}
```

Type Checking Basics

- We need to keep track of:
 - the types of the registers at each point in the code (type-states)
 - the types of the labels on the code
- Heap Types: Ψ will map labels to label types.
- Register Types: Γ will map registers to types.

Typing Operands

• integer literals are ints:

$$\Psi ; \Gamma \vdash n : int$$

• lookup register types in Γ :

$$\Psi ; \Gamma \vdash r : \Gamma(r)$$

• lookup label types in Ψ :

$$\Psi;\Gamma \vdash L:\Psi(L)$$

Subtyping

- Our program will never crash if the register file contains more values than necessary to satisfy some typing precondition
- In other words, a register file type with more components is a *subtype* of a register file containing fewer components.

$$\{r_1:\tau_1,\ldots,r_{i-1}:\tau_{i-1},r_i:\tau_i\} \leq \{r_1:\tau_1,\ldots,r_{i-1}:\tau_{i-1}\}$$

- Notice the similarity to record subtyping: a record with more fields is a subtype of a record with fewer fields.
- On the other hand, label type subtyping works in the opposite direction. A label that only requires r_1 and r_2 to contain integers may be used as a label that requires r_1 , r_2 and r_3 to contain integers.
- Label types, like ordinary function types, obey *contravari*ant subtyping rules in their argument types:

$$\frac{\Gamma' \le \Gamma}{\Gamma \to \{\} \le \Gamma' \to \{\}}$$

- Subtyping is also reflexive and transitive
- A subsumption rule allows a value to be used at a supertype:

$$\frac{\Psi; \Gamma \vdash v : \tau_1 \quad \tau_1 \leq \tau_2}{\Psi; \Gamma \vdash v : \tau_2}$$

Typing Instructions

• The judgment for instructions looks like:

$$\Psi \vdash i : \Gamma_1 \to \Gamma_2$$

- Γ_1 describes the registers on input to the instruction (a typing precondition)
- Γ_2 describes the registers on output (a typing postcondition)
- Ψ is invariant. The types of heap objects will not change as the program executes (at least for now,...).

Typing Instructions

• Arithmetic operations:

$$\frac{\Psi; \Gamma \vdash r_s : int \quad \Psi; \Gamma \vdash v : int}{\Psi \vdash aop \, r_d, r_s, v : \Gamma \rightarrow \Gamma[r_d := int]}$$

• Conditional branches:

$$\frac{\Psi ; \Gamma \vdash r : int \quad \Psi ; \Gamma \vdash v : \Gamma \to \{\ \}}{\Psi \vdash bop \ r, v : \Gamma \to \Gamma}$$

• Data movement:

$$\frac{\Psi ; \Gamma \vdash v : \tau}{\Psi \vdash \mathsf{mov}\, r, v : \Gamma \to \Gamma[r_d := \tau]}$$

Basic Block Typing

• All basic blocks end in the jump instruction:

$$\frac{\Psi; \Gamma \vdash v : \Gamma \to \{\ \}}{\Psi \vdash \mathsf{jmp}\, v : \Gamma \to \{\ \}}$$

Since a jmp never returns/falls through to the following instruction, we may choose the return context arbitrarily. For simplicity, we choose {} and make that the return context for all blocks.

• Instruction sequences:

$$\frac{\Psi \vdash i : \Gamma_1 \to \Gamma_2 \quad \Psi \vdash B : \Gamma_2 \to \{\}}{\Psi \vdash i ; B : \Gamma_1 \to \{\}}$$

• Subtyping is an admissible rule for basic blocks:

Lemma: Admissibility of Basic Block Subtyping If $\Psi \vdash B : \Gamma_2 \to \{\}$ and $\Gamma_1 \leq \Gamma_2$ then $\Psi \vdash B : \Gamma_1 \to \{\}$.

Proof: By induction on the typing derivation for basic blocks and instructions.

Machine Typing

• Heap typing:

$$\frac{\mathrm{Dom}(H) = \mathrm{Dom}(\Psi) \quad \forall L \in \mathrm{Dom}(H).\Psi \vdash H(L) : \Psi(L)}{\vdash H : \Psi}$$

• Register file typing:

$$\frac{\forall r \in \mathsf{Dom}(\Gamma).\Psi; \{\,\} \vdash R(r) : \Gamma(r)}{\Psi \vdash R : \Gamma}$$

• Machine typing:

$$\frac{\vdash H: \Psi \quad \Psi \vdash R: \Gamma \quad \Psi \vdash B: \Gamma \rightarrow \{\,\}}{\vdash (H, R, B)}$$

Type Safety

We have designed the type system so that it satisfies the following property:

• Theorem: Type Safety. If $\vdash \Sigma$ and $\Sigma \longmapsto^* \Sigma'$ then Σ is not stuck.

Proof by induction on the length of the instruction sequence, following Wright and Felleisen [26] and Harper [7].

- (Preservation) Each step in evaluation preserves typing.
- (Progress) If a state is well-typed then it is not stuck.

Corollaries:

- All jumps are to valid labels (control-flow safety)
- All arithmetic is done with integers (not labels)

Proof: Canonical Forms

Before proving Progress and Preservation, we must be able to characterize the *shape* and *properties* of a value based upon its *type*.

Lemma: Canonical Forms. If $\vdash H : \Psi$ and $\Psi \vdash R : \Gamma$ and $\Psi ; \Gamma \vdash v : \tau$ then

- $\tau = int \text{ implies } R(v) = n.$
- $\tau = \{r_1:\tau_1,\ldots,r_n:\tau_n\} \to \{\} \text{ implies } R(v) = L.$ Moreover, $H(L) = B \text{ and } \Psi \vdash B : \{r_1:\tau_1,\ldots,r_n:\tau_n\} \to \{\}$

Proof: By induction on the value typing derivation. [Exercise: fill in the details.]

Proof: Progress

Lemma: Progress. If $\vdash \Sigma_1$ then there exists a Σ_2 such that $\Sigma_1 \longmapsto \Sigma_2$.

Proof: By cases on the form of the code block in Σ_1 .

Example case: $\Sigma_1 = (H, R, \text{jmp } v)$. We are given the derivation:

$$\frac{\vdash H: \Psi \quad \Psi \vdash R: \Gamma \quad \Psi \vdash \mathsf{jmp}\, v: \Gamma \to \{\ \}}{\vdash (H, R, \mathsf{jmp}\, v)}$$

By inspection of the typing rules for blocks, the third premise above must be a derivation that ends in the jump rule:

$$\frac{\Psi; \Gamma \vdash v : \Gamma}{\Psi \vdash \mathtt{jmp}\, v : \Gamma \to \{\ \}}$$

By Canonical Forms, R(v) = L and $L \in Dom(H)$. Therefore, the operational rule for jumps applies and Σ_1 is not stuck: $(H, R, jmp v) \longmapsto (H, R, H(L))$

Proof: Preservation

Lemma: Preservation. If $\vdash \Sigma_1$ and $\Sigma_1 \longmapsto \Sigma_2$ then $\vdash \Sigma_2$. Proof: By cases on the form of Σ_1 .

Example case: $\Sigma_1 = (H, R, jmp v)$. We are given the derivation:

$$\frac{ \vdash H : \Psi \quad \Psi \vdash R : \Gamma \quad \Psi \vdash \mathsf{jmp}\,v : \Gamma \to \{\ \}}{\vdash (H, R, \mathsf{jmp}\,v)}$$

and the operational rule must be:

$$(H, R, jmp v) \longmapsto (H, R, B)$$

where $R(v) = L$ and $H(L) = B$

Hence, we must prove that $\vdash (H, R, B)$. As in the proof of Progress, we may deduce that the third premise of the typing derivation ends in an application of the jump rule:

$$\frac{\Psi; \Gamma \vdash v : \Gamma \to \{\ \}}{\Psi \vdash \mathsf{jmp}\, v : \Gamma \to \{\ \}}$$

Therefore, by Canonical Forms, we know

$$\Psi \vdash B : \Gamma \rightarrow \{ \}$$

and hence

$$\frac{\vdash H : \Psi \quad \Psi \vdash R : \Gamma \quad \Psi \vdash B : \Gamma \rightarrow \{\ \}}{\vdash (H, R, B)}$$

Proof Summary

- The Type Safety theorem is relatively straightforward to prove using Canonical Forms, Progress and Preservation lemmas.
- Proofs almost always reveal flaws in initial design and clearly specify the properties that the language enforces.
- As we scale the programming language up, these proof techniques are remarkably robust. However, the proofs quickly become very detailed and tedious.
- Open research problem: How can we automate generation of these proofs? Some initial results from Schürmann and Pfenning [17, 14].

Scaling It up

The simple abstract machine and type system can be scaled up in many directions:

- more primitive types and options (e.g., floats, jal, complex instruction set operations, etc.) [20]
- a control stack for procedures [12]
- more polymorphism [13]
- a module system, link checker and dynamic linker [5]
- memory-allocated values (e.g., tuples and arrays) and explicit memory management [24, 19, 25, 23]
- objects for object-oriented programming [4]
- types for concurrency control
- dependent types for expressing more complex access control and security properties [22, 27]
- intentional type analysis [3, 2]

Over the next few lectures we will work through many of these topics.

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TAL-1: Polymorphism

- Changes to types:
 - Add type variables to types: α
 - * Type variables are treated abstractly
 - * Allow code reuse
 - * As we'll see they come in handy elsewhere...
 - Label types can be polymorphic:

$$\forall \alpha, \beta, \{r_1 : \alpha, r_2 : \beta, r_3 : \{r_1 : \beta, r_2 : \alpha\} \rightarrow \{\}\} \rightarrow \{\}$$

- * Describes a function that swaps the values in registers r_1 and r_2 , for values of any two types.
- * Register r_3 contains the return address which expects the values to be swapped.
- Changes to operands:
 - To jump to polymorphic functions, we explicitly instantiate type variables, calling for a new form of operand: $v[\tau]$
 - We write $v[\tau_1, \ldots, \tau_n]$ for $v[\tau_1] \cdots [\tau_n]$.

Example Polymorphism

Callee-Saves Registers

- A common register-allocation strategy:
 - When calling a function, save the contents of some registers (caller-saves registers) onto the stack. When the function returns, restore the contents of these registers from the stack.
 - Allow the callee to save (and restore) the contents of other designated registers (callee-saves registers).
 - If the callee does not use all registers, the cost of saving and restoring is not incurred.
- Correctness criterion: the callee must return to the caller with the same values in the callee-saves registers

Callee-saves Registers Example

```
callee: \forall \alpha. \{r_1 : int, r_5 : \alpha, r_{31} : \{r_1 : int, r_5 : \alpha\} \rightarrow \{\}\} \rightarrow \{\}
                          	exttt{	iny X} save register r_5
          \mathtt{mov}\,r_4,r_5
                                \% use register r_5 for other work
          mov r_5, 7
          add r_1, r_1, r_5
                                	extstyle % 	extstyle % 	extstyle % 	extstyle % 	extstyle <math>	extstyle r_5
          \mathtt{mov}\,r_5,r_4
          jmp r_{31}
                                 % will need r_5 callee returns
caller: mov r_5, 255
          mov r_1, 5
          \mathtt{mov}\,r_{31}, L
          jmp \ callee[int] % callee[int]:
                                 \{r_1: int, r_5: int, r_{31}: \{r_1: int, r_5: int\} \rightarrow \{\}\}
L: \{r_1: int, r_5: int\} \rightarrow \{\}
          mul r_3, r_1, r_5
```

Callee-saves Registers Bug

- We can actually prove formally that *callee* preserves the values of its callee-saves registers. This fact is a property of *callee*'s polymorphic type! (See Reynolds [15] and Crary [1])
- Moral: polymorphism can be used for more than just code reuse. It can force a procedure to "behave well" in some circumstances.

Operational Semantics

- In order to prove our Type Preservation result, we must make a couple of minor changes in our operational semantics.
 - Heaps H now map labels to type-labeled blocks:

$$H(L) = \forall \alpha_1, \dots, \alpha_n. \Gamma \rightarrow \{ \}.B$$

- Type variables $\alpha_1, \ldots, \alpha_n$ appear free both in Γ and B
- Control-flow operations substitute arguments types for type variables:

$$(H, R, jmp \ v[\tau_1, \dots, \tau_n]) \longmapsto (H, R, B[\tau_1/\alpha_1, \dots, \tau_n/\alpha_n])$$

where $R(v) = L$ and $H(L) = \forall \alpha_1, \dots, \alpha_n.\Gamma \rightarrow \{\}.B$

$$(H, R, \text{beq } r, v[\tau_1, \dots, \tau_n]; B) \longmapsto (H, R, B'[\tau_1/\alpha_1, \dots, \tau_n/\alpha_n])$$

where $R(r) = 0, R(v) = L$, and $H(L) = \forall \alpha_1, \dots, \alpha_n.\Gamma \rightarrow \{\}.B'$

Polymorphic Typing

• Since types may now contain variables, we must ensure they only contain properly declared variables. The following judgment states that a type is well-formed (ie: it makes sense):

$$\frac{Free Vars(\tau) \subseteq \Delta}{\Delta \vdash \tau}$$

where
$$\Delta = \alpha_1, \ldots, \alpha_n$$

• We also modify the operand and instruction typing judgments to account for the type variables in scope:

$$\Psi; \Delta; \Gamma \vdash v : \tau$$

$$\Psi; \Delta \vdash i : \Gamma_1 \to \Gamma_2$$

Polymorphic Typing

• We have a typing rule for our new sort of operand

$$\frac{\Psi; \Delta; \Gamma \vdash v : \forall \alpha_1, \alpha_2, \dots, \alpha_n. \Gamma' \to \{ \} \quad \Delta \vdash \tau}{\Psi; \Delta; \Gamma \vdash v[\tau] : (\forall \alpha_2, \dots, \alpha_n. \Gamma' \to \{ \})[\tau/\alpha_1]}$$

• We change heap typing slightly in order to introduce the bound type variables:

$$\forall L \in \mathsf{Dom}(H).\Psi; \alpha_1, \dots, \alpha_n \vdash B : \Gamma \to \{ \}$$

$$H(L) = \forall \alpha_1, \dots, \alpha_n.\Gamma.B \qquad \text{(for all } L)$$

$$\Psi(L) = \forall \alpha_1, \dots, \alpha_n. \to \{ \}$$

$$\vdash H : \Psi$$

Type Safety

- The type safety proof follows the same Progress and Preservation formula as before.
- We need one central addition to the proof: The Substitution Lemma.

If
$$\Psi; \alpha_1, \ldots, \alpha_n \vdash B : \Gamma \to \{\}$$
 and $\vdash \tau_i$ for $i = 1..n$ then $\Psi; \cdot \vdash B[\tau_1/\alpha_1, \ldots, \tau_n/\alpha_n] : \Gamma[\tau_1/\alpha_1, \ldots, \tau_n/\alpha_n] \to \{\}$

• Exercise: Prove the Substitution Lemma and Preservation for TAL-1.

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The Run-time Stack

- Almost every compiler uses a *stack*
 - A consecutive sequence memory addresses with one end designated the top
 - Values are stored on the stack and later retrieved
 - The compiler can grow the stack to store more values and later shrink the stack, explicitly deallocating the topmost values.

• Uses:

- To store temporary values/result of intermediate computations when we run out of registers
- To store the return address and local variables of recursive functions before a recursive function call.

TAL-2: Add a stack

• Machine states:

$$- M ::= (H, R, S, B)$$

• Stacks are modelled as a list of values:

$$-S ::= \min \mid v :: S$$

• New instructions:

$$i ::= \mathtt{salloc}\, n \mid \mathtt{sfree}\, n \mid \mathtt{sld}\, r_d, n \mid \mathtt{sst}\, r_s, n$$

- Error conditions:
 - If we free too much or read/write locations too deep in the stack, the machine will get stuck

Remarks

- The stack operations have a 1-to-1 correspondence with RISC instructions.
- \bullet A designated register sp points to the top of the stack.
 - salloc corresponds to subtracting n from a stackpointer register (e.g. $\operatorname{sub} sp, sp, n$)
 - sfree corresponds to adding n to the stack pointer (e.g. add sp, sp, n)
 - sst corresponds to writing a value into offset n from the stack pointer (e.g. st sp(n), r)
 - sld corresponds to reading a value from offset n relative to the stack pointer (e.g. ld r, sp(n))
- CISC-like instructions (e.g. push/pop)can be synthesized.
 - push v =salloc 1; sst v, 1
 - pop r = sld r, 1; sfree 1

Simple Stack-Based Program

L1:

RA:

 $jmp r_{31}$

• A recursive version of the factorial function:

```
factrec(n) =
           if n \leq 0 then
           else
                n*factrec (n-1)
factrec: % r_1 holds argument n, r_{31} holds return address
         \% which expects the result in r_1
                          % n > 0, goto L1
         bgt r_1, L1
        mov r_1, 1
                          % n \leq 0, return 1
         jmp r_{31}
         salloc 2
                          % allocate space for frame
                   % save return address
         \mathtt{sst}\,r_{31},1
         \mathtt{sst}\,r_1,2
                          	exttt{\%} save n
         \mathrm{sub}\, r_1, r_1, 1 % n := n-1
         \mathtt{mov}\, r_{31}, RA % return address := RA
         jmp factrec % do recursive call, result in r_1
         % result in r_1
                  	extcolored{\%} restore n into r_2
         \operatorname{sld} r_2, 2
         sld r_{31}, 1 % restore return address
```

 $exttt{mul } r_1, r_1, r_2 \qquad exttt{ % result } := n * fact(n-1)$

% return

Semantics for Stack Operations

- As before, the operational semantics maps machine states to machine states.
- After a sequence of new locations have been allocated at the top of the stack, they will initially be filled with garbage.
 - The junk value? models uninitialized/garbage stack slots.
 - It is introduced exclusively for the operational semantics. Programmers will not manipulate junk.

$$(H,R,S,\mathtt{salloc}\,n;B)\longmapsto (H,R,\overbrace{?::\cdots::?}^n::S,B)$$

$$(H, R, v_1 :: \cdots :: v_n :: S, \mathtt{sfree}\, n; B) \longmapsto (H, R, S, B)$$

$$(H, R, S, \operatorname{sld} r, n; B) \longmapsto (H, R[r := v_n], S, B)$$

where $S = v_1 :: \cdots :: v_n :: S'$

$$(H, R, S_1, \operatorname{sst} r, n; B) \longmapsto (H, R, S_2, B)$$
where $S_1 = v_1 :: \cdots :: v_{n-1} :: v_n :: S'$
and $S_2 = v_1 :: \cdots :: v_{n-1} :: R(r) :: S'$

Typing the Stack

• Stack types:

$$-\sigma ::= \mathtt{nil} \mid \tau :: \sigma \mid \rho$$

- The nil type represents the empty stack.
- The type $\tau :: \sigma$ represents a stack v :: S where τ is the type of v and σ is the type of S.
- The type ρ is a stack type variable that describes some unknown "tail" in the stack.
- Register file types contain a special register sp that is mapped to the type of the current stack:

$$\{sp:int::\rho,r_1:int,\ldots\}$$

• In addition, we'll let label types be polymorphic over stack types:

$$\forall \rho. \{ sp: int :: \rho, r_1: int \} \rightarrow \{ \}$$

• Type contexts may now contain stack variables:

$$\Delta ::= \cdot \mid \Delta, \alpha \mid \Delta, \rho$$

• Junk values have junk type: ?

Stack Instruction Typing

As before, instruction typing judgments have the form

$$\Psi : \Delta \vdash i : \Gamma_1 \rightarrow \Gamma_2$$

• Stack allocation:

$$\overline{\Psi ; \Delta \vdash \mathtt{salloc}\, n : \Gamma[sp := \sigma] \to \Gamma[sp := \underbrace{? :: \cdots :: ?}_{n} :: \sigma]}$$

• Stack free:

$$\overline{\Psi; \Delta \vdash \mathtt{sfree}\, n : \Gamma[sp := \tau_1 :: \cdots :: \tau_n :: \sigma] \to \Gamma[sp := \sigma]}$$

• Stack load:

$$\frac{\Gamma(sp) = \tau_1 :: \cdots :: \tau_n :: \sigma}{\Psi; \Delta \vdash \operatorname{sld} r, n : \Gamma \to \Gamma[r := \tau_n]}$$

• Stack store:

$$\frac{\Psi; \Delta; \Gamma \vdash v : \tau \quad \Gamma(sp) = \tau_1 :: \cdots :: \tau_n :: \sigma}{\Psi; \Delta \vdash \mathtt{sst}\, v, n : \Gamma \to \Gamma[sp := \tau_1 :: \cdots :: \tau :: \sigma]}$$

Typing Factree (Bug)

```
type \tau_{\rho} = \{r_1 : int, sp : \rho\} \rightarrow \{\}
factrec \forall \rho. \{sp : \rho, r_1 : int, r_{31} : \tau_{\rho}\} \rightarrow \{\}
            bgt r_1, L1[\rho]
            mov r_1, 1
            jmp r_{31}
L1: \forall \rho. \{ sp : \rho, r_1 : int, r_{31} : \tau_{\rho} \} \rightarrow \{ \}
            salloc 2 % sp:?::?::\rho
            \operatorname{sst} r_{31}, 1 % sp: \tau_{\rho} :: ? :: \rho
            \operatorname{sst} r_1, 2 % sp: \tau_{\rho}:: int:: \rho
            \mathtt{sub}\,r_1,r_1,1
            \operatorname{mov} r_{31}, RA[\rho] \quad \% \quad r_{31} : \{ sp : \tau_{\rho} :: int :: \rho, r_{1} : int \} \to \{ \ \}
            jmp factrec[	au_{
ho} :: int :: 
ho]
RA: \forall \rho. \{sp : \tau_{\rho} :: int :: \rho, r_1 : int\} \rightarrow \{\}
            \mathtt{sld}\,r_2,2 % r_2:int
                                     r_{31}: 	au_{
ho}
            \mathsf{sld}\,r_{31},1
            \mathtt{mul}\, r_1, r_1, r_2
                           % ERROR! sp:	au_{
ho}::int::
ho
            jmp r_{31}
```

Typing Factree Corrected

```
type \tau_{\rho} = \{r_1 : int, sp : \rho\} \rightarrow \{\}
factrec \forall \rho. \{sp: \rho, r_1: int, r_{31}: \tau_{\rho}\} \rightarrow \{\}
            bgt r_1, L1[\rho]
            mov r_1, 1
             jmp r_{31}
        \forall \rho. \{sp: \rho, r_1: int, r_{31}: \tau_{\rho}\} \rightarrow \{\}
L1:
             salloc 2
             \mathtt{sst}\,r_{31},1
             \mathtt{sst}\,r_1,2
             \operatorname{\mathsf{sub}} r_1, r_1, 1
            \operatorname{mov} r_{31}, RA[\rho]
             jmp factrec[	au_{
ho} :: int :: 
ho]
            \forall \rho. \{ sp : \tau_{\rho} :: int :: \rho, r_1 : int \} \rightarrow \{ \}
RA:
             \mathtt{sld}\,r_2,1 % r_2:int
                                        r_{31}: 	au_{
ho}
             \operatorname{sld} r_{31}, 2
            mul r_1, r_1, r_2
                                    % sp: \rho
             sfree 2
             jmp r_{31}
```

Another Example

• The callee can't mess with the caller's stack frame:

```
\begin{array}{l} caller: \ \forall \rho'. \{sp: \tau_{code} :: \rho'\} \to \{ \ \} \\ & \text{salloc 1} \\ & \text{mov } r_1, 17 \\ & \text{sst } r_1, 1 \\ & \text{mov } r_{31}, RA[\rho'] \\ & \text{jmp } callee[\tau_{code} :: \rho'] \\ callee: \ \forall \rho. \{sp: int :: \rho, r_{31} : \{sp: \rho, r_1 : int\} \to \{ \ \} \} \to \{ \ \} \\ & \text{sld } r_1, 1 \\ & \text{add } r_1, r_1, r_1 \\ & \text{sst } r_1, 2 \\ & \text{sfree 1} \\ & \text{jmp } r_{31} \\ \\ RA: \ \ \forall \rho'. \{sp: \tau_{code} :: \rho', r_1 : int\} \to \{ \ \} \\ \dots \end{array}
```

• Polymorphism protects the stack.

The Theorems Carry Over

- Typing ensures we don't get stuck.
 - e.g. try to write off the end of the stack
 - But it doesn't ensure the stack stays within some quota
- With a bit more complication, we can deal with exceptions (See Morrisett et al. [12])

Things to Note

- We didn't have to bake in a notion of procedure call/return. Jumps were good enough.
 - Side effect: tail calls are a non-issue.
- Polymorphism and polymorphic recursion are crucial for encoding standard procedure call/return.
- When combined with the callee-saves trick, we can code up calling conventions.
 - Arguments on stack or in registers?
 - Results on stack or in registers?
 - Return address? Caller pops? Callee pops?
 - Caller saves? Callee saves?
- It's the orthogonal combination of typing features that makes things scale well.

Values of Different Size

- In high-level languages such as ML, all values have uniform size
 - The natural native representations of high-level values may have different sizes (64-bit floats vs. 32-bit integers).
 - To handle the size mismatch, an ML compiler will box floating-point values (represent them as a 32-bit pointer to a float).
- In low-level languages, we must handle values with non-uniform size.
 - There is no assembly language compiler to insert boxing coercions!
 - We must know how much space a value takes up on the stack so the type checker can verify that stack access is done properly.
 - We must know which values are small enough to fit into (32-bit) registers.
 - In summary, we need a function that computes the size of an object with type τ :

$$\begin{array}{lll} \mathtt{size}(int) & = & 1 \\ \mathtt{size}(float) & = & 2 \\ \mathtt{size}(\forall \alpha_1, \dots, \alpha_n.\Gamma \rightarrow \{\ \}) & = & 1 \\ \mathtt{size}(?_{32}) & = & 1 \\ \mathtt{size}(?_{64}) & = & 2 \end{array}$$

- But how do we compute the size of an abstract type α ?

Kinds and Types

- Solution: we classify all types according to the size of the objects that inhabit them.
- Generally, when we need to establish properties of types, we will use a system of kinds
- Kinds classify types just as types classify expressions.
- Here, a kind can specify the size of the values in a particular type:

$$\kappa ::= \mathtt{Sz}(i) \mid \mathtt{T}$$

• Type contexts Δ map type variables to their kinds:

$$\Delta ::= \cdot \mid \Delta, \alpha :: \kappa$$

Kinds and Types

• A judgment assigns each type a kind that reflects its size:

$$\overline{\Delta \vdash int :: Sz(1)}$$
 $\overline{\Delta \vdash float :: Sz(2)}$

$$\frac{\Delta \vdash \tau :: \mathtt{Sz}(i) \qquad \Delta \vdash \sigma :: \mathtt{Sz}(j)}{\Delta \vdash (\tau :: \sigma) :: \mathtt{Sz}(i+j)}$$

$$\overline{\Delta, \alpha :: \kappa \vdash \alpha :: \kappa}$$

$$\frac{\Delta \vdash \tau :: \mathtt{Sz}(i)}{\Delta \vdash \tau :: \mathtt{T}} \qquad \frac{\Delta \vdash \tau :: \mathtt{T}}{\Delta \vdash \tau :: \sigma :: \mathtt{T}}$$

• Modified stack load:

$$\begin{split} \Gamma(sp) &= \tau_1 :: \cdot \cdot \cdot :: \tau_m :: \sigma \\ \Delta \vdash (\tau_1 :: \cdot \cdot \cdot :: \tau_{m-1} :: \mathtt{nil}) :: \mathtt{Sz}(n-1) & \Delta \vdash \tau_m :: \mathtt{Sz}(1) \\ \hline \Psi ; \Delta \vdash \mathtt{sld}\, r, n : \Gamma \rightarrow \Gamma[r := \tau_m] \end{split}$$

- The load selects object m off the stack
- That object must fit inside a register (have kind Sz(1))
- x86 fld (load value onto floating point stack) will be similar but require the object have kind Sz(2)

Outline

- TAL-0: Assembly Language Control Flow and Basic Types
- TAL-1: Parametric Polymorphism
- TAL-2: Stack Types
- Type-Directed Compilation: From Tiny to TAL-2
- TAL-3: Data Structures
- TAL-4: Dependency
- TAL-5: Modularity and Linking
- References

Certified Code Systems

- A complete system for certified code contains three parts:
 - A strongly-typed source programming language.
 - A type-preserving compiler.
 - A strongly-typed target language.
- TAL will serve as our target language
- In this lecture, we will
 - Develop a very simple strongly-typed source language.
 - Explore the compilation process.

Source language: Tiny

- A simply-typed functional language.
 - Integer expressions
 - Conditionals
 - Recursive functions
 - Function pointers (no closures)
 - A strong type system
- An example program:

Tiny Syntax

• Types:

$$\tau ::= int \mid \tau_1 \to \tau_2$$

• Expressions:

$$e ::= x \mid f \mid n \mid e_1 + e_2 \mid e_1 \mid e_2 \mid \text{if } e_1 = 0 \text{ then } e_2 \text{ else } e_3 \mid \text{let } x = e_1 \text{ in } e_2$$

• Function declarations:

$$d ::= \operatorname{fun} f(x:\tau_1) : \tau_2 = e$$

• Programs:

$$P ::= \mathtt{letrec}\ d_1\ \cdots\ d_n\ \mathtt{in}\ e$$

A Tiny Type System

• Type checking occurs in a context Φ which maps function variables f and expression variables x to types

Expressions:

$$\overline{\Phi \vdash x : \Phi(x)}$$

$$\overline{\Phi \vdash f : \Phi(f)}$$

$$\overline{\Phi \vdash n : int}$$

$$\frac{\Phi \vdash e_1 : int \quad \Phi \vdash e_2 : int}{\Phi \vdash e_1 + e_2 : int}$$

$$\frac{\Phi \vdash e_1 : \tau_1 \to \tau_2 \quad \Phi \vdash e_2 : \tau_1}{\Phi \vdash e_1 \ e_2 : \tau_2}$$

$$\frac{\Phi \vdash e_1 : int \quad \Phi \vdash e_2 : \tau \quad \Phi \vdash e_3 : \tau}{\Phi \vdash \text{if } e_1 = 0 \text{ then } e_2 \text{ else } e_3 : \tau}$$

$$\frac{\Phi \vdash e_1 : \tau_1 \quad \Phi, x : \tau_1 \vdash e_2 : \tau_2}{\Phi \vdash \mathsf{let} \, x = e_1 \, \mathsf{in} \, e_2 : \tau_2}$$

Typing Tiny Programs

Declarations:

$$\frac{\Phi, x : \tau_1 \vdash e : \tau_2}{\Phi \vdash \text{fun } f(x : \tau_1) : \tau_2 = e : (f : \tau_1 \to \tau_2)}$$

Programs:

$$\Phi = f_1: au_{1,1} o au_{1,2}, \dots, f_n: au_{n,1} o au_{n,2} \ \Phi \vdash d_i: (f_i: au_{i,1} o au_{i,2}) \quad \Phi \vdash e: int \ \vdash ext{letrec } d_1 \, \cdots \, d_n \, ext{in} \, e$$

- All Tiny programs return an integer as their final result
- Exercise: verify that the factorial program is well-typed

Type-Preserving Compilation

- A compiler for a realistic language normally consists of a series of type-preserving transformations
 - After each transformation, we can type check the code to help detect compilers.
- Every transformation in type-preserving compiler has two parts:
 - A type translation from source types to target types
 - A term translation from source types and terms to target terms
- The compiler described here is derived from the original implementation of our Popcorn compiler [20, 11].

The Type Translation

- The type translation $(\mathcal{T}[\cdot])$ maps Tiny types to TAL types
- Integers:

$$\mathcal{T}[int] = int$$

- Function types:
 - The translation of function types fixes the *calling convention* that the compiler will use.
 - * The caller pushes the argument and then the return address onto the stack.
 - * The callee pops the argument and return address. The result is placed in register r_a .

$$\mathcal{T}\llbracket\tau_1 \to \tau_2\rrbracket = \forall \rho. \{sp : \mathcal{K}\llbracket\tau_2, \rho\rrbracket :: \mathcal{T}\llbracket\tau_1\rrbracket :: \rho\} \to \{\}$$

where

$$\mathcal{K}[\![\tau,\sigma]\!] = \{sp : \sigma, r_a : \mathcal{T}[\![\tau]\!]\} \to \{\}$$

Expression Translation

- To keep the translation simple, we will use the stack extensively:
 - The values of all expression variables are kept on the stack
 - * M maps expression variables to stack offsets
 - * I(M) increments the stack offset associated with each variable in the domain of M
 - To compute the value of an expression, we first compute the values of its subexpressions and push them on the stack.
 - We return the value of an expression in the register r_a
- In all, we use 3 registers and the stack
- The shape formal translation is $\mathcal{E}[\![e]\!]_{M,\sigma} = J$ where J is a sequence of labels (and their types) and instructions.
- For each function f, we assume there is a TAL label L_f
- T(e) is the source type of expression e
 - Technically, we should thread the Tiny typing context Φ through the translation to make it possible to construct the type of an expression e. For the sake of brevity, we elide this detail.

Expression Translation

• Expression variables:

$$\mathcal{E}[\![x]\!]_{M,\sigma} = \operatorname{sld} r_a, M(x)$$

• Function variables:

$$\mathcal{E}[\![f]\!]_{M,\sigma} = \operatorname{mov} r_a, L_f$$

• Integer constants:

$$\mathcal{E}\llbracket n \rrbracket_{M,\sigma} = \operatorname{mov} r_a, n$$

• Addition:

$$egin{aligned} \mathcal{E}\llbracket e_1 + e_2
bracket_{M,\sigma} &= \ \mathcal{E}\llbracket e_1
bracket_{M,\sigma} & ext{push } r_a \ \mathcal{E}\llbracket e_2
bracket_{\mathbf{I}(M),int::\sigma} & ext{pop } r_t \ ext{add } r_a, r_t, r_a \end{aligned}$$

Expression Translation

• Function Call:

$$\mathcal{E}\llbracket e_1 \ e_2
bracket_{M,\sigma} = \ \mathcal{E}\llbracket e_1
bracket_{M,\sigma} \ ext{push } r_a \ \mathcal{E}\llbracket e_2
bracket_{\mathrm{I}(M),\mathcal{T}\llbracket au_1
ightarrow au_2
bracket_{:::\sigma} \ ext{pop } r_t \ ext{push } r_a \ ext{push } L_r[
ho] \ ext{jmp } r_t[\sigma] \ L_r : orall
bracket_{\mathcal{T}(2),\sigma} \ ext{where } \mathtt{T}(e_1) = au_1
ightarrow au_2 \ ext{and } L_r ext{ is fresh}$$

• Conditional:

$$\mathcal{E}[\![if\ e_1 = 0\ then\ e_2\ else\ e_3]\!]_{M,\sigma} = \ \mathcal{E}[\![e_1]\!]_{M,\sigma} \ bneq\ r_a, L_{else}[
ho] \ \mathcal{E}[\![e_2]\!]_{M,\sigma} \ jmp\ L_{end}[
ho] \ L_{else}: orall
ho. \{sp:\sigma\} \ \mathcal{E}[\![e_3]\!]_{M,\sigma} \ jmp\ L_{end}[
ho] \ L_{end}: orall
ho. \mathcal{K}[\![au,\sigma]\!] \ where\ T(e_2) = au \ and\ L_{else}, L_{end}\ are\ fresh$$

• Exercise: Translate the let-expression

Program Translation

• Function translation:

```
\begin{split} \mathcal{F} \llbracket \text{fun } f(x : & \tau_1) : \tau_2 = e \rrbracket = \\ L_f : \mathcal{T} \llbracket \tau_1 \to \tau_2 \rrbracket \\ \mathcal{E} \llbracket e \rrbracket_{[x : = 2], \mathcal{K} \llbracket \tau_2, \rho \rrbracket :: \mathcal{T} \llbracket \tau_1 \rrbracket :: \rho} \\ \text{pop } r_t \\ \text{sfree } 1 \\ \text{jmp } r_t \end{split}
```

• Program translation:

```
egin{aligned} \mathcal{P} \llbracket 	ext{letrec } d_1 & \cdots & d_n 	ext{ in } e 
bracket = \ & \mathcal{F} \llbracket d_1 
bracket & \cdots & \ & \mathcal{F} \llbracket d_n 
bracket & \ & \mathcal{E} \llbracket e 
bracket \cdot \mathcal{K} \llbracket int, 
ho 
bracket : 
ho 
bracket & \ & \mathsf{pop} \ r_t & \ & \mathsf{jmp} \ r_t \end{aligned}
```

- To run the program, jump to L_{main} after pushing the return address on the stack.
- Expect the program result in register r_a .

Example: Compiling Fact

• Recall the fact function in Tiny:

```
letrec  \begin{aligned} & \text{fun } fact \; (n{:}int) : int = \\ & \text{if } n = 0 \; \text{then} \; 1 \; \text{else} \; n * fact (n-1) \end{aligned} \\ & \text{in} \\ & fact \; 6 \end{aligned}
```

Example: Compiling Fact

```
L_{fact}: \forall \rho. \{ sp : \mathcal{K}[[int]] :: int :: \rho \}
                                           % load argument
           \operatorname{sld} r_a, 2
          bneq r_a, L_{else}[
ho] % n=0?
          \operatorname{mov} r_a, 1
                                           % return 1
           jmp L_{end}
L_{else}: \forall \rho. \{ sp : \mathcal{K} \llbracket int \rrbracket :: int :: \rho \}
           \operatorname{sld} r_a, 2
                                            % begin multiplication (load n)
          push r_a
                                           % begin fact call sequence
          \operatorname{\mathsf{mov}} r_a, L_{fact}
          push r_a
                                           % begin subtraction (load n)
           \operatorname{sld} r_a, 4
          push r_a
          mov r_a, 1
          pop r_t
                                           n-1
           \operatorname{\mathsf{sub}} r_a, r_t, r_a
                                           % load L_{fact}
          pop r_t
          \operatorname{\textsf{push}} L_r[\rho]
          jmp r_t[int :: \mathcal{K}[int, \rho]] :: int :: \rho]
     \forall \rho. \{sp: int :: \mathcal{K}\llbracket int, \rho \rrbracket :: int :: \rho, r_a: int \}
L_r:
                                           % load n
          pop r_t
                                           n * fact(n-1)
          \operatorname{mul} r_a, r_t, r_a
           jmp L_{end}[\rho]
L_{end}: \forall \rho. \{sp : \mathcal{K}[[int, \rho]] :: int :: \rho, r_a : int\}
                                            % pop return address
          pop r_t
                                            % throw away argument
           sfree 1
                                            % return
           jmpr_t
```

Optimizations

- Almost any compiler will produce better code than ours!
 - But how many compilers can you fit on three slides?
- Our type system makes it possible to generate much better code and to implement many standard optimizations:
 - Instruction selection optimizations
 - Common subexpression elimination
 - Register allocation
 - Redundant load and store elimination
 - Instruction scheduling optimizations
 - Strength reduction
 - Loop-invariant removal
 - Tail-call optimizations
 - And others.
- As demonstrated by the TIL/TILT compilers, types do not interfere with most common optimizations [21]

Instruction Selection

- Design principal: instruction sequences with the same operational behavior should have the same static behavior.
 - Unattainable in general, but something to strive for.
- We can synthesize the typing rule for push from a stack allocation and store since push v = salloc 1; sst v, 1
 - First, we write down the typing rules for the sequence, specialized to specific operands:

$$\frac{\overline{\Psi;\Delta\vdash \mathtt{salloc}\,1:\Gamma[sp:=\sigma]\to\Gamma[sp:=?::\sigma]}\quad \mathcal{D}}{\Psi;\Delta\vdash\mathtt{salloc}\,1;\mathtt{sst}\,v,1:\Gamma[sp:=\sigma]\to\Gamma[sp:=\tau::\sigma]}$$

$$\mathcal{D} = \frac{\Psi; \Delta; \Gamma[sp := ? :: \sigma] \vdash v : \tau}{\Psi; \Delta \vdash \mathtt{sst}\, v, 1 : \Gamma[sp := ? :: \sigma] \rightarrow \Gamma[sp := \tau :: \sigma]}$$

- Then we extract the premises at the leaves of the derivation, removing the intermediate states:

$$\frac{\Psi;\Delta;\Gamma[sp:=?::\sigma]\vdash v:\tau}{\Psi;\Delta\vdash\operatorname{push} v:\Gamma[sp:=\sigma]\to\Gamma[sp:=\tau::\sigma]}$$

Instruction Selection

- Since $\operatorname{push} v$ is statically equivalent to $\operatorname{salloc} 1$; $\operatorname{sst} v, 1$, a compiler writer can always replace one with the other
 - To optimize instruction encoding size
 - To optimize execution efficiency
 - To enable other optimizations

• Example:

```
push 7 push 8 push 9
```

Can be replaced by:

```
salloc 1
sst 7, 1
salloc 1
sst 8, 1
salloc 1
sst 9, 1
```

Which can be further reduced to:

```
\begin{array}{c} \mathtt{salloc}\, 3 \\ \mathtt{sst}\, 7, 1 \\ \mathtt{sst}\, 8, 1 \\ \mathtt{sst}\, 9, 1 \end{array}
```

Tail-Call Optimizations

- A crucial optimization for functional languages
- Applies when the final operation in a function f is a function call to g
- Rather than have f push the return address and engage in the normal calling sequence, f will pop all of its temporary values and jump directly to g, never to return
- Example:

Without tail-call optimization:

```
L_f : \\ \forall \rho. \{sp : \mathcal{K}[\![\tau_{return}, \rho]\!] :: \tau_{f-arg} :: \rho, r_a : \tau_{g-arg}\} \rightarrow \{\ \} \\ \text{salloc 2} \\ \text{sst } L_r \qquad \text{% push return address} \\ \text{sst } r_a, 2 \qquad \text{% push argument} \\ \text{jmp } L_g[\tau_{raddr} :: \tau_{f-arg} :: \rho] \\ \\ L_r : \qquad \forall \rho. \{sp : \tau_{raddr} :: \tau_{f-arg} :: \rho, r_a : \tau_{ret}\} \rightarrow \{\ \} \\ \text{pop } r_t \qquad \text{% pop return address} \\ \text{sfree 1} \qquad \text{% throw away } f \text{'s argument} \\ \text{jmp } r_t \qquad \text{% return} \\ \end{cases}
```

With tail-call optimization:

What optimizations can't we handle?

The version of TAL discussed so far provides no mechanisms for the following source of optimizations:

- Optimizations that alter the code stream: run-time code generation, run-time code optimization
 - Smith, Hornoff, Jim, and Morrisett have designed a system for safe run-time code generation (see Smith's thesis [18])
- Various stack-allocation strategies
 - Our type system can't represent pointers deep into the stack
 - Morrisett et al. [12] extend the stack typing discipline, but more work needs to be done here
- Optimizations that rely upon properties of values that are not reflected in the type structure:
 - Arithmetic properties of integers (eg: n = 17), which are useful for reasoning about arrays and pointer arithmetic (coming in a following section)
 - Aliasing properties of pointers in heap-allocated data structures (coming in a following section)

Properties of the Compiler

- Our compiler is type-preserving: If P is a well-typed Tiny program: $\vdash P$ then the compiled program is also well-typed: $\vdash \mathcal{P}[\![P]\!] : \Psi$ for some Ψ .
- The proof would proceed by induction on the structure of the program P.
- Each optimization phase and compiler transformation respects this property.
- To detect errors in our compiler's implementation we can run the compiler and type check the output.

Practical Compiler Issues

- As you translate from a high-level language to a low-level TAL-like language, the types must encode the structural information lost in the translation
- Result: by the time we have compiled to assembly, the types encode lots of data
- Careful engineering is required to enable efficient code size and type checking time
 - The Popcorn Compiler (PII266):
 - Object code: 0.55MB, 39 modules
 - Naive encoding: 4.50MB, checking time: 750s
 - Optimized encoding: 0.27MB, checking time: 22s
 - Checking time scales linearly with code size
 - Likely more optimization possible

Popcorn Example

• Source Type:

$$int \rightarrow bool$$

• TAL Type:

```
All a:T,b:T,c:T,r1:S,r2:S,e1:C,e2:C.
    {ESP: {EAX:bool, M:e1+e2, EBX:a, ESI:b, EDI:c,
        ESP:int::r1@{EAX:exn,ESP:r2,M:e1+e2}::r2}::int::r1@
        {EAX:exn,ESP:r2,M:e1+e2}::r2,
        EBP: sptr{EAX:exn,ESP:r2,M:e1+e2}::r2,
        EBX:a, ESI:b, EDI:c, M:e1+e2}
```

• Types for higher-order functions can require pages to write them down!

Compressing Types

- Gzip:
 - Effective for reducing binary size over the wire
 - No help during verification
- Tailor types to the language being compiled/the compiler
 - eg: fix the calling convention
 - Restricts interoperability/language and compiler evolution
- Higher-order type constructors
 - Fairly effective, useful for compiler debugging/code readability
- Hash-cons (ie: use graphs to represent types)
 - Highly effective, fast type equality
 - A significant engineering investment
- Type reconstruction/type inference
 - Can be very efficient with respect to both space and time
 - Must take care to avoid increasing trusted computing base
- See Grossman and Morrisett [6] for a survey of techniques used in our implementation.

Summary of Type-Directed Compilation

- Type-directed and type-preserving compilation provides an *automatic* way to generate certifiable low-level code
- We can prove that the compiler produces well-typed assembly code from any well-typed source language program
- Programmers can program as they normally do in their favorite strongly typed high-level language
- Constructing a type-preserving compiler takes more work initially but the result is more robust:
 - Compiler writers must transform both types and terms
 - Special care must be taken to compress type information
 - Type checking intermediate program representations can detect compiler errors
- Most conventional compiler optimizations are naturally type-preserving, so using a typed target language has little impact (if any) on compiler performance

Outline

- TAL-0: Assembly Language Control Flow and Basic Types
- TAL-1: Parametric Polymorphism
- TAL-2: Stack Types
- Type-Directed Compilation: From Tiny to TAL-2
- TAL-3: Data Structures
- TAL-4: Dependency
- TAL-5: Modularity and Linking
- References

Data Structures

- The register file and stack give us some local storage for word-sized values
 - Stack space can be recycled for values of different types
 - Critical trick: can't create pointers to these values
 - The trick prevents code from seeing two different views of the stack (through different pointers/aliases). It is simple to ensure that the single view of the stack is accurate.
- What about aggregates?
 - eg: tuples, records, arrays, objects, datatypes, etc.
 - TAL puts these "large" values in the heap and refers to them via pointers.
 - This introduces aliasing and the potential for multiple views/access pathes for the same data structure
 - Recycling heap memory is not as easy

TAL-3: Add Tuples

- Let heap H map labels to either blocks of code or tuples of values: $\langle v_1, \ldots, v_n \rangle$
- The values v_i are either integers or labels
- The labels are abstract (no pointer arithmetic)
- Tuple instructions:
 - Allocate tuple: malloc r_d, n
 - Load from k^{th} component of the tuple: $1d r_d, r_s(k)$
 - Store into k^{th} component of the tuple: st $r_d(k), r_s$
- Tuple types: $\langle \tau_1, \ldots, \tau_n \rangle$

Tuple Operational Semantics

• Allocation:

$$(H, R, v_1 :: \cdots :: v_n :: S, \mathtt{malloc} r_d, n; B) \longmapsto (H[L : \langle v_1, \dots, v_n \rangle], R[r_d := L], S, B)$$

where L is a fresh label (ie: not in $Dom(H)$)

• Load:

$$(H, R, S, \operatorname{1d} r_d, r_s(k); B) \longmapsto (H, R[r_d := v_k], S, B)$$

where $H(R(r_s)) = \langle v_1, \dots, v_n \rangle$ and $1 \leq k \leq n$

• Store:

$$(H[L = \langle v_1, \dots, v_n \rangle], R, S, \operatorname{st} r_d(k), r_s; B) \longmapsto (H[L = \langle v_1, \dots, v_{k-1}, R(r_s), v_{k+1}, \dots, v_n \rangle], R, S, B)$$
where $R(r_d) = L$

Tuple Typing

• Allocation:

$$\frac{\Gamma(sp) = \tau_1 :: \tau_2 :: \cdots :: \tau_n :: \sigma}{\Psi; \Delta \vdash \mathtt{malloc}\, r_d, n : \Gamma \to \Gamma[sp := \sigma, r_d := \langle \tau_1, \tau_2, \dots, \tau_n \rangle]}$$

• Load:

$$\frac{\Psi; \Delta; \Gamma \vdash r_s : \langle \tau_1, \dots, \tau_n \rangle \quad 1 \leq k \leq n}{\Psi; \Delta \vdash \operatorname{1d} r_d, r_s(k) : \Gamma \to \Gamma[r_d := \tau_k]}$$

• Store:

$$\frac{\Psi; \Delta; \Gamma \vdash r_d : \langle \tau_1, \dots, \tau_n \rangle \quad \Psi; \Delta; \Gamma \vdash r_s : \tau_k \quad 1 \leq k \leq n}{\Psi; \Delta \vdash \mathsf{st}\, r_d(k), r_s : \Gamma \to \Gamma}$$

Remarks

- The load and store operations correspond to conventional RISC instructions.
- The malloc instruction does not.
 - Typically, this would be implemented by a call into the run-time to atomically allocate and initialize the tuple.
 - Atomic allocation and initialization interferes with our ability to compile common C-style programming idioms
 - Interferes with instruction selection and scheduling
 - The advantage is a simple design where we need not reason about pointers and aliasing.
- There's no way to explicitly deallocate heap memory
 - TAL relies upon a garbage collector to reclaim all heap storage.
 - Remember, the garbage collector is another element of our trusted computing base.
- The types of tuples are *invariant*.
 - You can't update a component in the tuple with a value of a different type
 - The same is true for code and other heap objects
- In summary, TAL has the memory model of a *high-level* programming language

Arrays

• Hard issues:

- Need to allocate and initialize storage of unknown size.
- Each array subscript operation must be in bounds.
- In general, this implies we need size information at run time.
- Simple solution: special operations:
 - new_array r_a, r_{size}, r_{item}
 - asub $r_{item}, r_a(r_i)$
 - aupd $r_a(r_i), r_{item}$
 - The disadvantage is that this fixes array representations and makes interoperation with other languages difficult/costly. There is some overhead to performing the array-bounds checks.

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TAL-4: A Refined Memory Model

- Machine states now have the form $(H_U; H_M; S; R; B)$ where H_M is memory managed explicitly by the TAL program
- In order to check programs that explicitly manage memory (as most C programs do) we will reason about the shape of memory using a simple logic
- $C ::= \{\ell \mapsto \langle \tau_1, \ldots, \tau_n \rangle\} \mid \mathbf{1} \mid C_1 \otimes C_2 \mid \epsilon$
- ϵ is a logic variable
- ullet is a label: either a label variable ϕ or a concrete label L
- We also introduce a new type of managed pointers: $S(\ell)$
 - Only label L has type S(L)
 - When two labels have type $S(\phi)$, we do not know which labels they are, but we do know that they are the same label (they are *aliases*)

Well-formed Stores

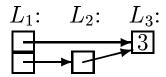
- The judgment $\Psi \vdash H : C$ states that a heap H is well-formed and is described by the formula C.
- We specify a nondeterministic merge of two stores H_1 and H_2 using the notation $H_1 \bowtie H_2$. It requires that the domains of the stores H_1 and H_2 be disjoint.

$$\overline{\Psi dash \{\,\} : \mathbf{1}}$$

$$\frac{\Psi \vdash H_1 : C_1 \quad \Psi \vdash H_2 : C_2}{\Psi \vdash H_1 \bowtie H_2 : C_1 \otimes C_2}$$

$$\frac{\Psi; \cdot \vdash v_i : \tau_i \quad \text{for } 1 \le i \le n}{\Psi \vdash \{L \mapsto \langle v_1, \dots, v_n \rangle\} : \{L \mapsto \langle \tau_1, \dots, \tau_n \rangle\}}$$

• Example:



$$\{L_1 \mapsto \langle S(L_3), S(L_2) \rangle\} \otimes \{L_2 \mapsto \langle S(L_3) \rangle\} \otimes \{L_3 \mapsto \langle int \rangle\}$$

Using Store Types

- New instructions:
 - mmalloc ϕ, r, n
 - free r
- Our old load and store instructions will have overloaded typing rules
- Code types are extended with an extra field to describe the shape the store must have before we jump to the code:
 - $\{hp: C, sp: \sigma, r_1: \tau_1, \dots, r_n: \tau_n\} \to \{\}$

Examples

An error:

```
foo: \quad \forall \epsilon, \rho. \{hp: \epsilon, sp: \rho, r_1: int, \\ r_{31}: \{hp: \epsilon, sp: \rho, r_1: int\} \rightarrow \{\ \}\} \rightarrow \{\ \} \\ \text{mmalloc} \ \phi, \mathbf{r}_2, \mathbf{n} \quad \text{\%} \ hp: \epsilon \otimes \{\phi \mapsto \langle ?, ? \rangle\}, r_2: S(\phi) \\ \text{mov} \ r_7, r_2 \qquad \text{\%} \ r_7: S(\phi) \\ \text{st} \ r_7[1], r_1 \qquad \text{\%} \ hp: \epsilon \otimes \{\phi \mapsto \langle int, ? \rangle\} \\ \text{st} \ r_2[2], r_1 \qquad \text{\%} \ hp: \epsilon \otimes \{\phi \mapsto \langle int, int \rangle\} \\ \text{jmp} \ r_{31} \qquad \text{\%} \ \text{ERROR!} \ \text{Memory leak}.
```

Heap Logic: Details

- To type check code, we must use the entailment relation from our heap logic: $C \vdash C'$
- More generally, entailment has the form $L \vdash C$ where L is a sequence of assumptions C
- This logic is a tiny fragment of *linear logic* and the sequent calculus rules follow.

$$\overline{\cdot \vdash \mathbf{1}}$$

$$\frac{L, L' \vdash C}{L, \mathbf{1}, L' \vdash C}$$

$$\frac{L, C, C', L' \vdash C''}{L, C \otimes C', L' \vdash C''}$$

$$\frac{L \vdash C \quad L' \vdash C'}{L \bowtie L' \vdash C \otimes C'}$$

$$\overline{\{\phi \mapsto \langle \tau_1, \dots, \tau_n \rangle\} \vdash \{\phi \mapsto \langle \tau_1, \dots, \tau_n \rangle\}}$$

$$\overline{\epsilon \vdash \epsilon}$$

• These rules are *sound* with respect to our heap model and entailment is *decidable*. Prove these facts as an exercise.

Subtyping

• We fold the logic into our type system by extending the subtyping relation:

$$\frac{C \vdash C'}{\Gamma[hp := C] \le \Gamma[hp := C']}$$

New Judgments and Block Typing

• Extended instruction typing judgment:

$$\Psi; \Delta \vdash i : \Gamma \to [\Delta']\Gamma'$$

- may be read as "given a managed heap type Ψ and the type variables Δ , instruction i has register file precondition Γ and there exist types Δ' such that the postcondition Γ' will be satisfied upon execution of the instruction.
- The block typing judgment is as before:

$$\Psi; \Delta \vdash B : \Gamma \to \{\}$$

• But the rules for stringing together instructions change slightly:

$$\frac{\Psi; \Delta \vdash i : \Gamma \to [\Delta']\Gamma' \quad \Psi; \Delta, \Delta' \vdash B : \Gamma' \to \{\}}{\Psi; \Delta \vdash i; B : \Gamma \to \{\}}$$

• The rule for typing jumps does not change, but remember that register file typings now contain more information (the type of the managed heap).

$$\frac{\Psi; \Gamma \vdash v : \Gamma \to \{\ \}}{\Psi \vdash \mathsf{jmp}\, v : \Gamma \to \{\ \}}$$

$$\frac{\Gamma(hp) = C \quad \Gamma' = \Gamma[hp := C \otimes \{\phi \mapsto \overbrace{\langle ?, \dots, ? \rangle}^n\}][r := S(\phi)]}{\Psi; \Delta \vdash \mathsf{mmalloc}\; \phi, \mathtt{r}, \mathtt{n} : \Gamma \to [\phi]\Gamma'}$$

$$\Psi ; \Delta ; \Gamma dash r : S(\ell)$$

$$\Gamma(hp) = C \otimes \{\ell \mapsto \langle au_1, \dots, au_n \rangle\} \qquad \Gamma' = \Gamma[hp := C]$$

$$\Psi ; \Delta dash free \ r : \Gamma \to [\]\Gamma'$$

$$\begin{split} \Psi; \Delta; \Gamma \vdash r_d : S(\ell) & \quad \Psi; \Delta; \Gamma \vdash r_s : \tau \\ \Gamma(hp) = C \otimes \{\ell \mapsto \langle \tau_1, \dots, \tau_k, \dots, \tau_n \rangle\} \\ \Gamma' = \Gamma[hp := C \otimes \{\ell \mapsto \langle \tau_1, \dots, \tau, \dots, \tau_n \rangle\}] \\ \hline \Psi; \Delta \vdash \mathsf{st}\, r_d(k), r_s : \Gamma \to [\,]\Gamma' \end{split}$$

$$\frac{\Psi; \Delta; \Gamma \vdash r_d : \tau_k \quad \Psi; \Delta; \Gamma \vdash r_s : S(\ell)}{\Gamma(hp) = C \otimes \{\ell \mapsto \langle \tau_1, \dots, \tau_k, \dots, \tau_n \rangle\}}$$
$$\frac{\Psi; \Delta \vdash \operatorname{1d} r_d, r_s(k) : \Gamma \to []\Gamma}$$

The store type may not match a given instruction precondition syntactically, so we must introduce the following rule to prove the store has the form required at different program points.

$$\frac{\Gamma \le \Gamma'}{\Psi; \Delta; \Gamma \vdash i : \Gamma \to []\Gamma'}$$

Comments

- Singleton types allow us to identify pointers and their aliases.
- Label polymorphism allows us to abstract away from the specific name of a label but retain the aliasing structure of the heap
- Heap polymorphism allows us to abstract away from the size and shape of a portion of the heap
- With recursive and existential types, we can encode linear lists and trees. (See Walker and Morrisett [25])
- We can extend our type system to incorporate a Turingcomplete logic provided we annotate our programs with explicit proofs of the entailment relation. (See Reynolds [16] and Ishtiaq and O'Hearn [9])

Arrays

- Often, using some simple arithmetic facts we can prove that an array access is in bounds at compile time, eliminating the need for a check at run time
- Following Xi, Pfenning and Harper ([28, 27]), we may extend the type checker with a (classical) logic for reasoning about arithmetic, just as we used a (linear) logic for reasoning about the heap
- Arithmetic expressions:

$$a := i \mid n \mid a_1 +_{32} a_2 \mid a_1 -_{32} a_2 \mid a_1 \times_{32} a_2 \mid a_1 \times a_2 \mid \cdots$$

- -i is a 32-bit number variable
- -n is a 32-bit constant
- All expressions have machine semantics
- Logical connectives:

$$P ::= p \mid \mathtt{true} \mid \mathtt{false} \mid a_1 \leq_u a_2 \mid P_1 \supset P_2 \mid P_1 \land P_2 \mid \neg P \mid \cdots$$

- New types:
 - Singleton integers: S(a)
 - Array types: $\tau \ array(a)$

Refined Operand Typing

• New type contexts:

$$\Delta ::= \cdot \mid \Delta, \alpha :: \kappa \mid \Delta, P$$

- New operands: v[proof]
 - -v must be code with a logical precondition: $\forall [P, \Delta'].\Gamma'$
 - -v[proof] has type $\forall [\Delta'].\Gamma'$ provided that proof is a proof of P in the current context:

$$\frac{\Psi;\Delta;\Gamma\vdash v:\forall [P,\Delta'].\Gamma'\to\{\ \}\quad \Delta\vdash proof:P\ \mathtt{true}}{\Psi;\Delta;\Gamma\vdash v[proof]:\forall [\Delta'].\Gamma'\to\{\ \}}$$

- For the sake of brevity, we will omit such proofs from our examples (alternatively, we could assume that a theorem prover is able to reconstruct the proof without help)
- we write instead

$$v[\cdot]$$

• We give constant integers a more refined type:

$$\Psi$$
; Δ ; $\Gamma \vdash n : S(n)$

Refined Instruction Typing

• Instruction typing judgment:

$$\Psi; \Delta \vdash i : \Gamma \to [\Delta']\Gamma'$$

• Addition:

$$\frac{\Psi;\Delta;\Gamma\vdash r_2:S(a_2)\quad \Psi;\Delta;\Gamma\vdash r_3:S(a_3)}{\Psi;\Delta\vdash\operatorname{add} r_1,r_2,r_3:\Gamma\to\Gamma[r_1:=S(a_2+_{32}a_3)]}$$

• Array access:

$$\Psi ; \Delta ; \Gamma \vdash r_2 : \tau \; array(a) \qquad \Psi ; \Delta ; \Gamma \vdash r_3 : S(a_3) \ \Delta \vdash a_3 \leq_u a \; {\sf true} \ \Psi ; \Delta \vdash {\sf ld} \; r_1, r_2(r_3) : \Gamma \rightarrow \Gamma[r_1 := \tau]$$

- As with operands, we could annotate load instructions with a *proof* of the arithmetic inequality above:

$$\operatorname{ld} r_1, r_2(r_3)[proof]$$

• Conditional branches

$$\begin{array}{c} \Psi; \Delta; \Gamma \vdash v : \forall [P].\Gamma \rightarrow \{\ \} & \Psi; \Delta; \Gamma \vdash r : S(a) \\ \Delta, a \leq 0 \vdash P \text{ true} \\ \hline \\ \Psi; \Delta \vdash \text{ble} \, r, v : \Gamma \rightarrow [a > 0]\Gamma \end{array}$$

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Separate Compilation and Linking

- TAL provides mechanisms that allow program parts to be compiled separately, checked for compatibility and linked together to form an executable
- Such functionality is important in almost any programming environment but indispensable in a setting of mobile code and extensible systems
- TAL provides facilities for static linking (all components are assembled before executing the program)
 - See Glew and Morrisett [5]
- TAL also provides facilities for dynamic linking (components are loaded into a running program)
 - See Hicks, Weirich and Crary [8]
- Here, we concentrate on static linking

Linking Diagram

Example

fact_e.tali:

VAL factrec:
$$\forall \rho. \{ sp : \rho, r_1 : int, r_{31} : \{ r_1 : int, sp : \rho \} \rightarrow \{ \} \} \rightarrow \{ \} \}$$

fact.tal:

EXPORT fact_e.tali

$$factrec: \qquad \forall \rho. \{sp: \rho, r_1: int, \\ r_{31}: \{r_1: int, sp: \rho\} \rightarrow \{\ \}\} \rightarrow \{\ \} \\ \operatorname{sub} r_3, r_1, 1 \\ \operatorname{ble} r_3, L1[\rho] \\ \operatorname{jmp} r_{31}$$

 $L1: \qquad \forall \rho. \{sp: \rho, r_1: int, r_3: int, \\ r_{31}: \{r_1: int, sp: \rho\} \rightarrow \{\ \}\} \rightarrow \{\ \} \\ \text{salloc 2} \\ \text{sst } r_{31}, 0$

. . .

Example Continued

```
stdio_e.tali:
{\bf TYPE}\; \mathit{file}
VAL fprintf: · · ·
main_i.tali:
TYPE file
VAL fprintf: · · ·
VAL factrec: ...
main_e.tali:
VAL main: · · ·
main.tal:
IMPORT main_i.tali
EXPORT main_e.tali
main: \cdots
                 \mathtt{jmp}\,factrec
```

Comments

- At the assembly language level:
 - Each implementation file (.tal file) defines a collection of types and values.
 - Each implementation file also declares a collection of imports and exports
 - Each interface file (.tali file) declares a collection of values with their types and types with their kinds.
 - Our convention is that foo_i.tal files contain the imports needed by foo.tal and foo_e.tal files contain the exports
- At the machine code level:
 - tal files are replaced by .o files, which contain binary code and data and .to files, which contain a compressed binary representation of the associated typing annotations

Link Checking

- Before linking, we check:
 - If one file imports a value labeled *foo* and the other file exports a value labeled *foo*, does *foo* have the type expected by the importing file?
 - Similarly, do import and export type declarations with the same name have the same kind (in our simple case: do stack types match stack types and ordinary types match ordinary types)?
 - Are there any import/export name clashes?
 - Note that unexported labels will not clash with labels from other files since they alpha-vary
- Before attempting execution, we check:
 - Are there any remaining types or values to import?

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