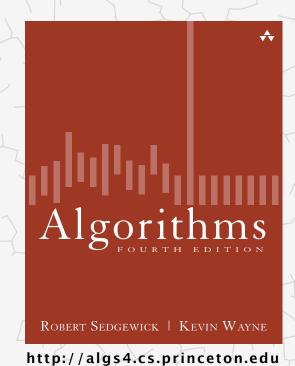
Algorithms



5.3 SUBSTRING SEARCH

- introduction
- brute force
- Knuth-Morris-Pratt
- Boyer-Moore
- ▶ Rabin-Karp



- introduction
- brute force
- Knuth-Morris-Pratt
- Boyer-Moore
- Rabin-Karp

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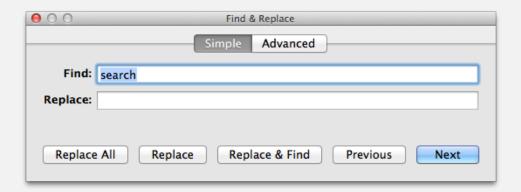
Substring search

Goal. Find pattern of length M in a text of length N.



Goal. Find pattern of length M in a text of length N.





Goal. Find pattern of length M in a text of length N.



Computer forensics. Search memory or disk for signatures, e.g., all URLs or RSA keys that the user has entered.



http://citp.princeton.edu/memory

Goal. Find pattern of length M in a text of length N.



Identify patterns indicative of spam.

- PROFITS
- LOSE WE1GHT
- herbal Viagra
- There is no catch.
- This is a one-time mailing.
- This message is sent in compliance with spam regulations.





Electronic surveillance.



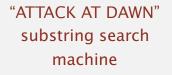


Need to monitor all internet traffic. (security)

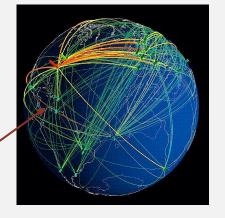
> Well, we're mainly interested in



"ATTACK AT DAWN"



found



No way! (privacy)

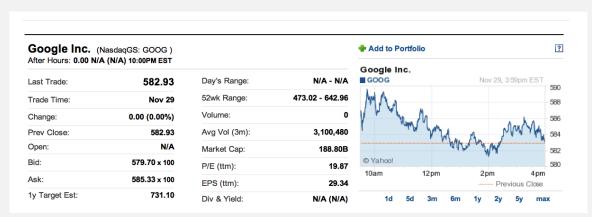


OK. Build a machine that just looks for that.



Screen scraping. Extract relevant data from web page.

Ex. Find string delimited by and after first occurrence of pattern Last Trade:.



http://finance.yahoo.com/q?s=goog

```
Last Trade:

class= "yfnc_tablehead1">
width= "48%">
Trade Time:

class= "yfnc_tablehead1"
width= "48%">
```

Screen scraping: Java implementation

Java library. The index0f() method in Java's string library returns the index of the first occurrence of a given string, starting at a given offset.

```
public class StockQuote
   public static void main(String[] args)
      String name = "http://finance.yahoo.com/q?s=";
      In in = new In(name + args[0]);
      String text = in.readAll();
      int start = text.index0f("Last Trade:", 0);
      int from = text.index0f("<b>", start);
      int to = text.indexOf("</b>", from);
      String price = text.substring(from + 3, to);
      StdOut.println(price);
               % java StockQuote goog
               582.93
               % java StockQuote msft
               24.84
```



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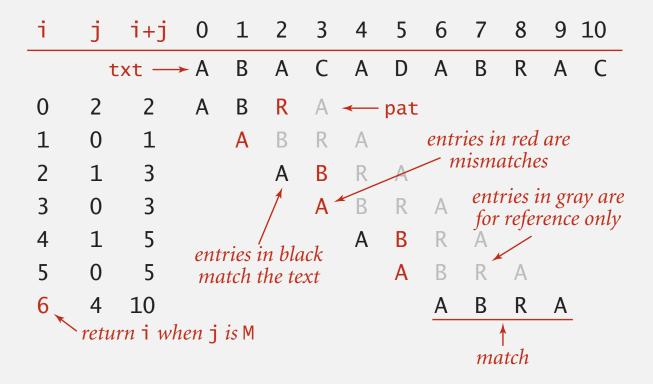
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Brute-force substring search

Check for pattern starting at each text position.



Brute-force substring search: Java implementation

Check for pattern starting at each text position.

```
      i
      j
      i+j
      0
      1
      2
      3
      4
      5
      6
      7
      8
      9
      10

      A
      B
      A
      C
      A
      D
      A
      B
      R
      A
      C

      4
      3
      7
      A
      D
      A
      C
      R

      5
      0
      5
      A
      D
      A
      C
      R
```

```
public static int search(String pat, String txt)
{
  int M = pat.length();
  int N = txt.length();
  for (int i = 0; i <= N - M; i++)
  {
    int j;
    for (j = 0; j < M; j++)
        if (txt.charAt(i+j) != pat.charAt(j))
            break;
    if (j == M) return i;  index in text where pattern starts
}
  return N;  not found
}</pre>
```

Brute-force substring search: worst case

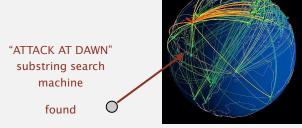
Brute-force algorithm can be slow if text and pattern are repetitive.

Worst case. $\sim MN$ char compares.

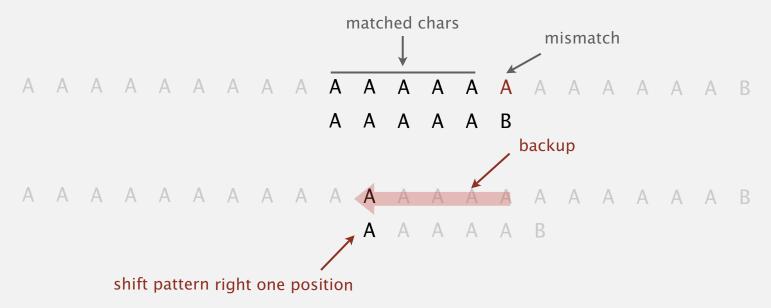
Backup

In many applications, we want to avoid backup in text stream.

- Treat input as stream of data.
- Abstract model: standard input.



Brute-force algorithm needs backup for every mismatch.



Approach 1. Maintain buffer of last *M* characters.

Approach 2. Stay tuned.

Brute-force substring search: alternate implementation

Same sequence of char compares as previous implementation.

- i points to end of sequence of already-matched chars in text.
- j stores # of already-matched chars (end of sequence in pattern).

```
      i
      j
      0
      1
      2
      3
      4
      5
      6
      7
      8
      9
      10

      A
      B
      A
      C
      A
      D
      A
      B
      R
      A
      C

      7
      3
      A
      D
      A
      C
      R

      5
      0
      A
      D
      A
      C
      R
```

```
public static int search(String pat, String txt)
{
  int i, N = txt.length();
  int j, M = pat.length();
  for (i = 0, j = 0; i < N && j < M; i++)
  {
    if (txt.charAt(i) == pat.charAt(j)) j++;
    else { i -= j; j = 0; }
  }
  if (j == M) return i - M;
  else    return N;
}</pre>
```

Algorithmic challenges in substring search

Brute-force is not always good enough.

Theoretical challenge. Linear-time guarantee. — fundamental algorithmic problem

Practical challenge. Avoid backup in text stream. ← often no room or time to save text

Now is the time for all people to come to the aid of their party. Now is the time for all good people to come to the aid of their party. Now is the time for many good people to come to the aid of their party. Now is the time for all good people to come to the aid of their party. Now is the time for a lot of good people to come to the aid of their party. Now is the time for all of the good people to come to the aid of their party. Now is the time for all good people to come to the aid of their party. Now is the time for each good person to come to the aid of their party. Now is the time for all good people to come to the aid of their party. Now is the time for all good Republicans to come to the aid of their party. Now is the time for all good people to come to the aid of their party. Now is the time for many or all good people to come to the aid of their party. Now is the time for all good people to come to the aid of their party. Now is the time for all good Democrats to come to the aid of their party. Now is the time for all people to come to the aid of their party. Now is the time for all good people to come to the aid of their party. Now is the time for many good people to come to the aid of their party. Now is the time for all good people to come to the aid of their party. Now is the time for a lot of good people to come to the aid of their party. Now is the time for all of the good people to come to the aid of their party. Now is the time for all good people to come to the aid of their attack at dawn party. Now is the time for each person to come to the aid of their party. Now is the time for all good people to come to the aid of their party. Now is the time for all good Republicans to come to the aid of their party. Now is the time for all good people to come to the aid of their party. Now is the time for many or all good people to come to the aid of their party. Now is the time for all good people to come to the aid of their party. Now is the time for all good Democrats to come to the aid of their party.

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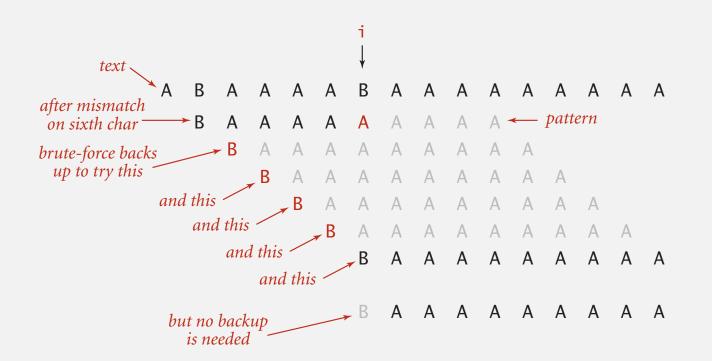
http://algs4.cs.princeton.edu

Knuth-Morris-Pratt substring search

Intuition. Suppose we are searching in text for pattern BAAAAAAAAA.

- Suppose we match 5 chars in pattern, with mismatch on 6th char.
- We know previous 6 chars in text are BAAAAB.
- Don't need to back up text pointer!

assuming { A, B } alphabet



Knuth-Morris-Pratt algorithm. Clever method to always avoid backup. (!)

Deterministic finite state automaton (DFA)

DFA is abstract string-searching machine.

- Finite number of states (including start and halt).
- Exactly one transition for each char in alphabet.
- Accept if sequence of transitions leads to halt state.

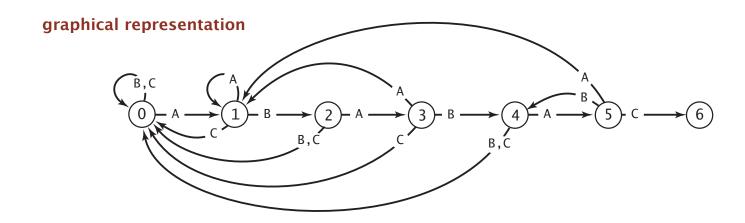
internal representation

	j	0	1	2	3	4	5
<pre>pat.charAt(</pre>	j)	Α	В	Α	В	Α	C
	Α	1	1	3	1	5	1
dfa[][j]	В	0	2	0	4	0	4
<pre>pat.charAt(dfa[][j]</pre>	C	0	0	0	0	0	6

If in state j reading char C:

if j is 6 halt and accept

else move to state dfa[c][j]

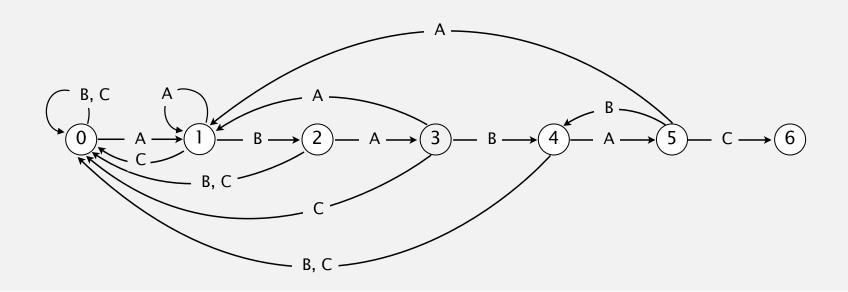


DFA simulation demo

A A B A C A A B A B A C A A



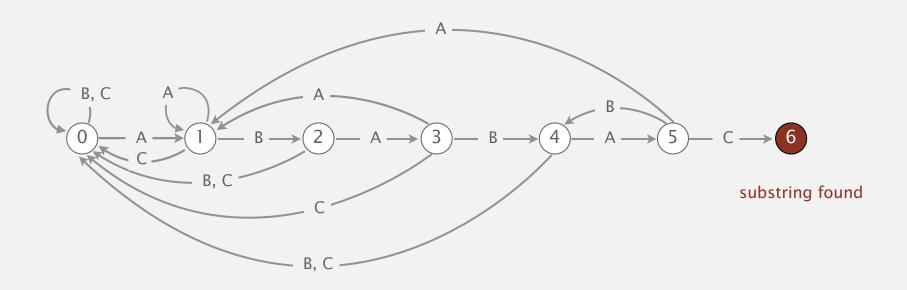
						4	5
pat.charAt	(j)	Α	В	Α	В	Α	С
	Α	1	1	3	1	5	1
dfa[][j]	В	0	2	0	4	0	4
	C	0	0	0	0	0	6



DFA simulation demo



		0	1	2	3	4	5
<pre>pat.charAt(j) </pre>		A	В	Α	В	А	С
	Α	1	1	3	1	5	1
dfa[][j]	В	0	2	0	4	0	4
	C	0	0	0	0	0	6

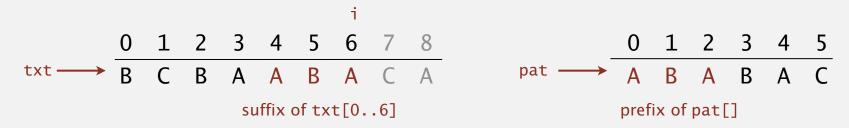


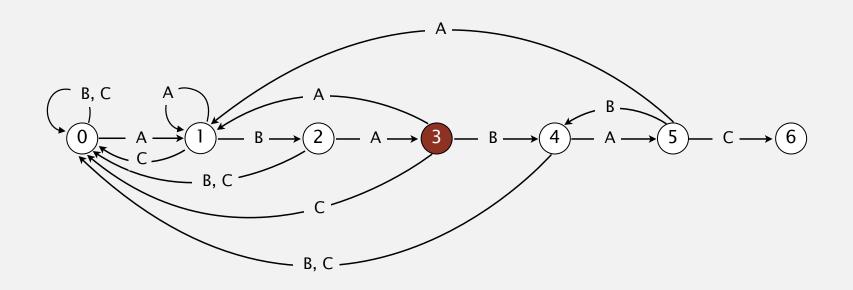
Interpretation of Knuth-Morris-Pratt DFA

- Q. What is interpretation of DFA state after reading in txt[i]?
- A. State = number of characters in pattern that have been matched.

length of longest prefix of pat[]
that is a suffix of txt[0..i]

Ex. DFA is in state 3 after reading in txt[0..6].





Knuth-Morris-Pratt substring search: Java implementation

Key differences from brute-force implementation.

- Need to precompute dfa[][] from pattern.
- Text pointer i never decrements.

Running time.

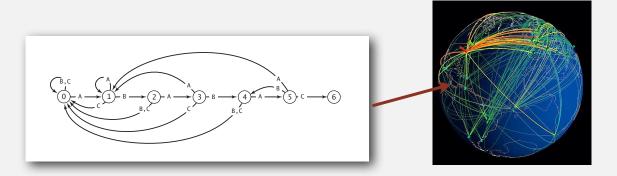
- Simulate DFA on text: at most N character accesses.
- Build DFA: how to do efficiently? [warning: tricky algorithm ahead]

Knuth-Morris-Pratt substring search: Java implementation

Key differences from brute-force implementation.

- Need to precompute dfa[][] from pattern.
- Text pointer i never decrements.
- Could use input stream.

```
public int search(In in)
{
   int i, j;
   for (i = 0, j = 0; !in.isEmpty() && j < M; i++)
        j = dfa[in.readChar()][j];
   if (j == M) return i - M;
   else       return NOT_FOUND;
}</pre>
```



Knuth-Morris-Pratt construction demo

Include one state for each character in pattern (plus accept state).



Constructing the DFA for KMP substring search for ABABAC

0

- (1)
- (2)

(3)

(4)

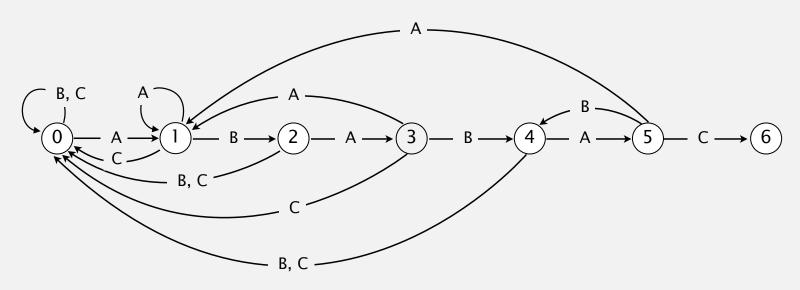
(5)

(6)

Knuth-Morris-Pratt construction demo

		0	1	2	3	4	5
pat.charAt	(j)	A	В	Α	В	Α	C
	Α	1	1	3	1	5	1
dfa[][j]	В	0	2	0	4	0	4
	C	0	0	0	0	0	6

Constructing the DFA for KMP substring search for $\ A\ B\ A\ B\ A\ C$



Include one state for each character in pattern (plus accept state).

0

- (1)
- (2)

(3)

(4)

5

(6)

Match transition. If in state j and next char c == pat.charAt(j), go to j+1.

first j characters of pattern
have already been matched

have already been matched

match transition. If in state j and next char c == pat.charAt(j), go to j+1.

now first j+1 characters of pattern have been matched



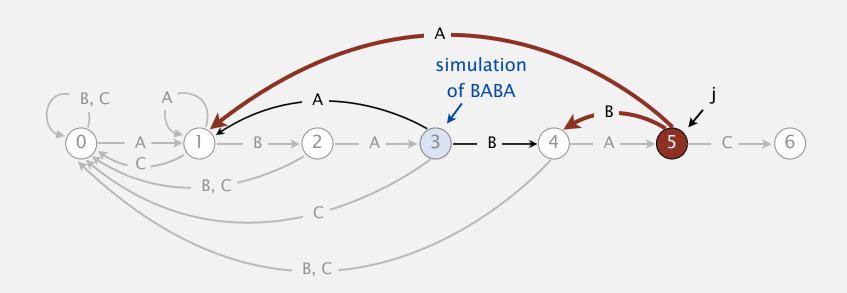


Mismatch transition. If in state j and next char c != pat.charAt(j), then the last j-1 characters of input are pat[1..j-1], followed by c.

To compute dfa[c][j]: Simulate pat[1..j-1] on DFA and take transition c. still under construction (!) Running time. Seems to require *j* steps.

Ex.
$$dfa['A'][5] = 1;$$
 $dfa['B'][5] = 4$
simulate BABA; simulate BABA;
take transition 'A' take transition 'B'
 $= dfa['A'][3]$ $= dfa['B'][3]$

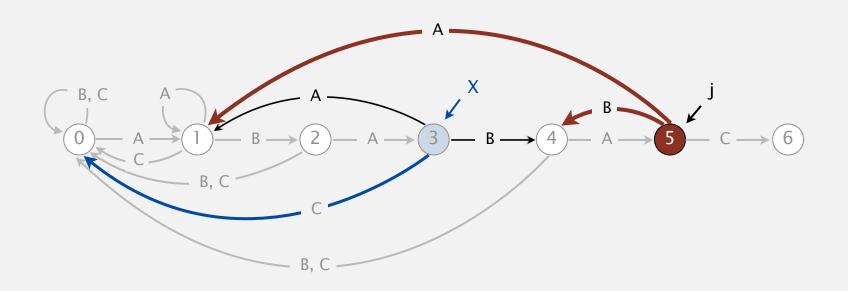




Mismatch transition. If in state j and next char c != pat.charAt(j), then the last j-1 characters of input are pat[1..j-1], followed by c.

To compute dfa[c][j]: Simulate pat[1..j-1] on DFA and take transition c. Running time. Takes only constant time if we maintain state *X*.

Ex.
$$dfa['A'][5] = 1;$$
 $dfa['B'][5] = 4;$
from state X, from state X,
take transition 'A' take transition 'B'
 $= dfa['A'][X]$ $= dfa['B'][X]$



Knuth-Morris-Pratt construction demo (in linear time)

Include one state for each character in pattern (plus accept state).



Constructing the DFA for KMP substring search for ABABAC

- 0
- (1)

(2)

(3)

 $\left(4\right)$

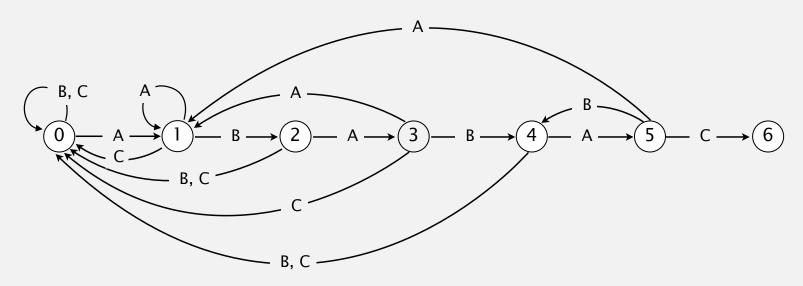
(5)

(6)

Knuth-Morris-Pratt construction demo (in linear time)

		0	1	2	3	4	5
pat.charAt	(j)	A	В	Α	В	Α	С
						5	
dfa[][j]	В	0	2	0	4	0	4
	C	0	0	0	0	0	6

Constructing the DFA for KMP substring search for ABABAC



Constructing the DFA for KMP substring search: Java implementation

For each state j:

- Copy dfa[][X] to dfa[][j] for mismatch case.
- Set dfa[pat.charAt(j)][j] to j+1 for match case.
- Update x.

Running time. M character accesses (but space/time proportional to RM).

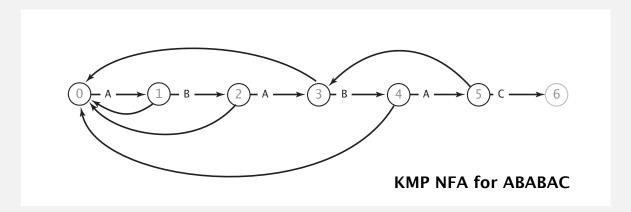
KMP substring search analysis

Proposition. KMP substring search accesses no more than M+N chars to search for a pattern of length M in a text of length N.

Pf. Each pattern char accessed once when constructing the DFA; each text char accessed once (in the worst case) when simulating the DFA.

Proposition. KMP constructs dfa[][] in time and space proportional to RM.

Larger alphabets. Improved version of KMP constructs nfa[] in time and space proportional to M.



Knuth-Morris-Pratt: brief history

- Independently discovered by two theoreticians and a hacker.
 - Knuth: inspired by esoteric theorem, discovered linear algorithm
 - Pratt: made running time independent of alphabet size
 - Morris: built a text editor for the CDC 6400 computer
- Theory meets practice.

SIAM J. COMPUT. Vol. 6, No. 2, June 1977

FAST PATTERN MATCHING IN STRINGS*

DONALD E. KNUTH[†], JAMES H. MORRIS, JR.[‡] AND VAUGHAN R. PRATT¶

Abstract. An algorithm is presented which finds all occurrences of one given string within another, in running time proportional to the sum of the lengths of the strings. The constant of proportionality is low enough to make this algorithm of practical use, and the procedure can also be extended to deal with some more general pattern-matching problems. A theoretical application of the algorithm shows that the set of concatenations of even palindromes, i.e., the language $\{\alpha\alpha^R\}^*$, can be recognized in linear time. Other algorithms which run even faster on the average are also considered.



Don Knuth



Jim Morris



Vaughan Pratt

introduction

brute force

▶ Knuth-Morris-Pratt

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Rabin-Karp

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Robert Boyer

J. Strother Moore

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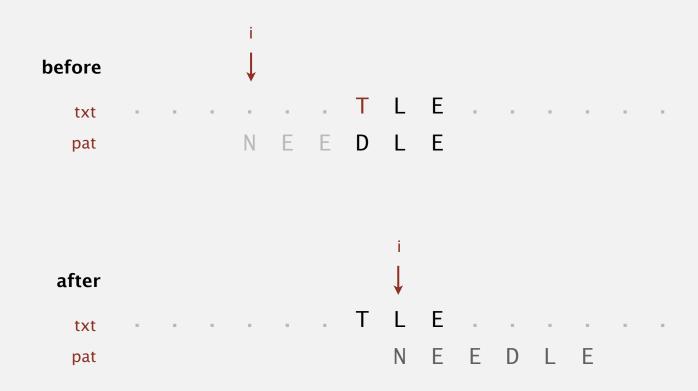
Intuition.

- · Scan characters in pattern from right to left.
- Can skip as many as M text chars when finding one not in the pattern.



Q. How much to skip?

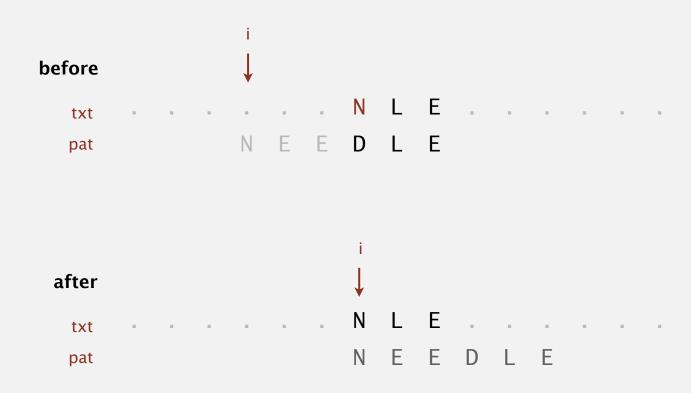
Case 1. Mismatch character not in pattern.



mismatch character 'T' not in pattern: increment i one character beyond 'T'

Q. How much to skip?

Case 2a. Mismatch character in pattern.



mismatch character 'N' in pattern: align text 'N' with rightmost pattern 'N'

Q. How much to skip?

txt

Case 2b. Mismatch character in pattern (but heuristic no help).

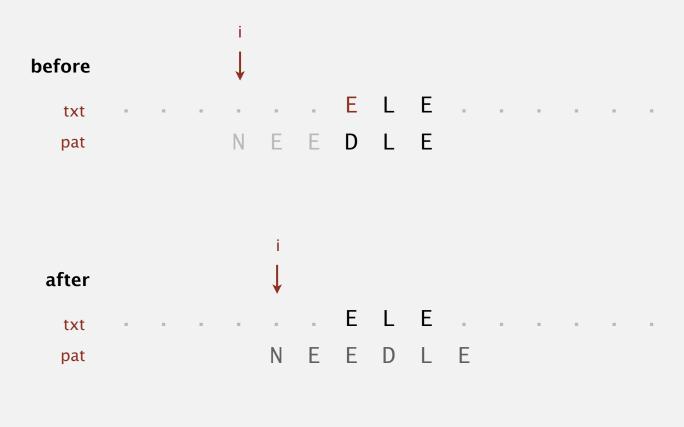


pat N E E D L E

mismatch character 'E' in pattern: align text 'E' with rightmost pattern 'E'?

Q. How much to skip?

Case 2b. Mismatch character in pattern (but heuristic no help).



mismatch character 'E' in pattern: increment i by 1

- Q. How much to skip?
- A. Precompute index of rightmost occurrence of character c in pattern (-1 if character not in pattern).

```
right = new int[R];
for (int c = 0; c < R; c++)
    right[c] = -1;
for (int j = 0; j < M; j++)
    right[pat.charAt(j)] = j;</pre>
```

```
      N
      E
      E
      D
      L
      E

      C
      0
      1
      2
      3
      4
      5
      right[c]

      A
      -1
      -1
      -1
      -1
      -1
      -1
      -1
      -1

      B
      -1
      -1
      -1
      -1
      -1
      -1
      -1
      -1
      -1

      C
      -1
      -1
      -1
      -1
      -1
      -1
      -1
      -1
      -1

      D
      -1
      -1
      -1
      -1
      3
      3
      3
      3

      E
      -1
      -1
      -1
      -1
      3
      3
      3
      3

      E
      -1
      -1
      1
      2
      2
      2
      5
      5

      ...
      -1
      -1
      -1
      -1
      -1
      4
      4
      4

      M
      -1
      -1
      -1
      -1
      -1
      -1
      -1
      -1
      -1

      N
      -1
      0
      0
      0
      0
      0
      0
      0

      ...
      -1
      -1
      -1
      -1
```

Boyer-Moore skip table computation

Boyer-Moore: Java implementation

```
public int search(String txt)
   int N = txt.length();
   int M = pat.length();
   int skip;
   for (int i = 0; i \leftarrow N-M; i \leftarrow skip)
      skip = 0;
      for (int j = M-1; j >= 0; j--)
                                                       compute
      {
                                                      skip value
         if (pat.charAt(j) != txt.charAt(i+j))
             skip = Math.max(1, j - right[txt.charAt(i+j)]);
             break:
                                  in case other term is nonpositive
      if (skip == 0) return i; ← match
   return N;
```

Boyer-Moore: analysis

Property. Substring search with the Boyer-Moore mismatched character heuristic takes about $\sim N/M$ character compares to search for a pattern of length M in a text of length N.

Worst-case. Can be as bad as $\sim MN$.

i:	skip	0	1	2	3	4	5	6	7	8	9
	txt—	→ B	В	В	В	В	В	В	В	В	В
0	0	Α	В	В	В	В		pat			
1	1		Α	В	В	В	В				
2	1			Α	В	В	В	В			
3	1				Α	В	В	В	В		
4	1					Α	В	В	В	В	
5	1						Α	В	В	В	В

Boyer-Moore variant. Can improve worst case to $\sim 3~N$ character compares by adding a KMP-like rule to guard against repetitive patterns.

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Boyer-Moore

Rabin-Karp



Michael Rabin, Turing Award '76

Dick Karp, Turing Award '85

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Rabin-Karp fingerprint search

Basic idea = modular hashing.

- Compute a hash of pattern characters 0 to M-1.
- For each i, compute a hash of text characters i to M + i 1.
- If pattern hash = text substring hash, check for a match.

```
pat.charAt(i)
i
    2 6 5 3 5 % 997 = 613
                 txt.charAt(i)
      1 2 3 4 5 6 7 8 9 10 11 12 13 14 15
                   2 6 5 3 5 8 9 7 9 3
    3 1 4 1 5 % 997 = 508
0
       1 4 1 5 9 % 997 = 201
1
         4 1 5 9 2 % 997 = 715
2
3
            1 5 9 2 6 % 997 = 971
4
               5 9 2 6 5 % 997 = 442
                                          match
                 9 2 6 5 3 % 997 = 929
                   2 6 5 3 5 % 997 = 613
6 \leftarrow return i = 6
```

Efficiently computing the hash function

Modular hash function. Using the notation t_i for txt.charAt(i), we wish to compute

$$x_i = t_i R^{M-1} + t_{i+1} R^{M-2} + \dots + t_{i+M-1} R^0 \pmod{Q}$$

Intuition. *M*-digit, base-*R* integer, modulo *Q*.

Horner's method. Linear-time method to evaluate degree-*M* polynomial.

```
// Compute hash for M-digit key
private long hash(String key, int M)
{
  long h = 0;
  for (int j = 0; j < M; j++)
     h = (R * h + key.charAt(j)) % Q;
  return h;
}</pre>
```

Efficiently computing the hash function

Challenge. How to efficiently compute x_{i+1} given that we know x_i .

$$x_i = t_i R^{M-1} + t_{i+1} R^{M-2} + ... + t_{i+M-1} R^0$$

 $x_{i+1} = t_{i+1} R^{M-1} + t_{i+2} R^{M-2} + ... + t_{i+M} R^0$

Key property. Can update hash function in constant time!

$$x_{i+1} = (x_i - t_i R^{M-1}) R + t_{i+M}$$

current subtract multiply add new value leading digit by radix trailing digit (can precompute R^{M-1})

Rabin-Karp substring search example

```
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15
     3 1 4 1 5 9 <mark>2 6 5 3 5</mark> 8 9 7 9 3
     3 % 997 = 3
     3 \quad 1 \quad \% \quad 997 = (3*10 + 1) \ \% \quad 997 = 31
     3 \quad 1 \quad 4 \quad \% \quad 997 = (31*10 + 4) \ \% \quad 997 = 314
 2
     3 \quad 1 \quad 4 \quad 1 \quad \% \quad 997 = (314*10 + 1) \ \% \quad 997 = 150
 3
     3 1 4 1 5 % 997 = (150*10 + 5) % 997 = 508 ^{RM} ^{R}
           4 \ 1 \ 5 \ 9 \ \% \ 997 = ((508 + 3*(997 - 30))*10 + 9) \% \ 997 = 201
 5
 6
            4 1 5 9 2 \% 997 = ((201 + 1*(997 - 30))*10 + 2) \% 997 = 715
               1 5 9 2 6 \% 997 = ((715 + 4*(997 - 30))*10 + 6) \% 997 = 971
 7
                   5 \quad 9 \quad 2 \quad 6 \quad 5 \quad \% \quad 997 = ((971 + 1*(997 - 30))*10 + 5) \% \quad 997 = 442
 8
                      9 \quad 2 \quad 6 \quad 5 \quad 3 \quad \% \quad 997 = ((442 + 5*(997 - 30))*10 + 3) \% \quad 997 = 929
 9
```

Rabin-Karp: Java implementation

```
public class RabinKarp
  private long patHash; // pattern hash value
  private int M; // pattern length
  private long Q;  // modulus
  private int R;  // radix
  private long RM; // R^{\wedge}(M-1) \% Q
  public RabinKarp(String pat) {
     M = pat.length();
     R = 256;
                                                            a large prime
     Q = longRandomPrime();
                                                            (but avoid overflow)
     RM = 1;
                                                            precompute R<sup>M-1</sup> (mod Q)
     for (int i = 1; i \le M-1; i++)
        RM = (R * RM) \% Q;
     patHash = hash(pat, M);
  private long hash(String key, int M)
  { /* as before */ }
  public int search(String txt)
   { /* see next slide */ }
}
```

Rabin-Karp: Java implementation (continued)

Monte Carlo version. Return match if hash match.

```
public int search(String txt)
{
    int N = txt.length();
    int txtHash = hash(txt, M);
    if (patHash == txtHash) return 0;
    for (int i = M; i < N; i++)
    {
        txtHash = (txtHash + Q - RM*txt.charAt(i-M) % Q) % Q;
        txtHash = (txtHash*R + txt.charAt(i)) % Q;
        if (patHash == txtHash) return i - M + 1;
    }
    return N;
}</pre>
```

Las Vegas version. Check for substring match if hash match; continue search if false collision.

Rabin-Karp analysis

Theory. If Q is a sufficiently large random prime (about MN^2), then the probability of a false collision is about 1/N.

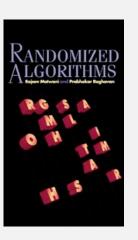
Practice. Choose Q to be a large prime (but not so large to cause overflow). Under reasonable assumptions, probability of a collision is about 1/Q.

Monte Carlo version.

- Always runs in linear time.
- Extremely likely to return correct answer (but not always!).

Las Vegas version.

- Always returns correct answer.
- Extremely likely to run in linear time (but worst case is MN).



Rabin-Karp fingerprint search

Advantages.

- Extends to 2d patterns.
- Extends to finding multiple patterns.

Disadvantages.

- Arithmetic ops slower than char compares.
- Las Vegas version requires backup.
- Poor worst-case guarantee.

Q. How would you extend Rabin-Karp to efficiently search for any one of P possible patterns in a text of length N?

Substring search cost summary

Cost of searching for an M-character pattern in an N-character text.

algorithm	version	operatio	n count	backup	correct?	extra space	
aigontiiii	VEISIOII	guarantee	typical	in input?	conect:		
brute force	_	MN	1.1 N	yes	yes	1	
Variab Manie Doug	full DFA (Algorithm 5.6)	2 N	1.1 N	по	yes	MR	
Knuth-Morris-Pratt	mismatch transitions only	3N	1.1 N	no	yes	M	
	full algorithm	3 N	N/M	yes	yes	R	
Boyer-Moore	mismatched char heuristic only (Algorithm 5.7)	MN	N/M	yes	yes	R	
Rabin-Karp [†]	Monte Carlo (Algorithm 5.8)	7 N	7 N	no	yes†	1	
	Las Vegas	7 N [†]	7 N	yes	yes	1	

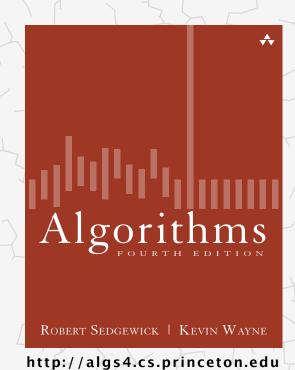
[†] probabilisitic guarantee, with uniform hash function

- introduction
- brute force
- Knuth-Morris-Pratt
- Boyer-Moore
- Rabin-Karp

Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE

Algorithms



5.3 SUBSTRING SEARCH

- introduction
- brute force
- Knuth-Morris-Pratt
- Boyer-Moore
- ▶ Rabin-Karp