1. Starting from an empty binary search tree, we inserted the letters P, R, I, N, C, E, T, O, N and got:

```
          P
         / \
        I   R
       / \  / \
      C   N E   O
     / \  / \  / \
    T   E O
```

a. What keys are examined when we search for E?
b. What keys are examined when we search for Q?

2. To insert an item into a binary tree, you (a) search for it, and (b) insert it where the search ended if it was not found. Build a new binary tree, starting from an empty tree and inserting I, N, S, E, R, T, U, S, P, L, Z.

3. Which of the following is not a valid binary search tree? What number cannot be found when we search for it? Of the valid ones, which one leads to the fastest searches?

```
      4
     / \
    2   6
   / \  / \
  1   35 7
```

```
      5
     / \
    3   6
   / \  / \
  1 47 2
```

```
      6
     / \
    3   7
   / \  / \
  2 4 5
```

4. (4.4.9) Suppose we have int values between 1 and 1000 in a BST and search for 363. Which of the following cannot be the sequence of keys examined?

(a) 2, 252, 401, 398, 330, 363
(b) 399, 387, 219, 266, 382, 381, 278, 363
(c) 3, 923, 220, 911, 244, 898, 258, 362, 363
(d) 4, 924, 278, 347, 621, 299, 392, 358, 363
(e) 5, 925, 202, 910, 245, 363