



# Character Animation

COS 426, Spring 2016  
Princeton University

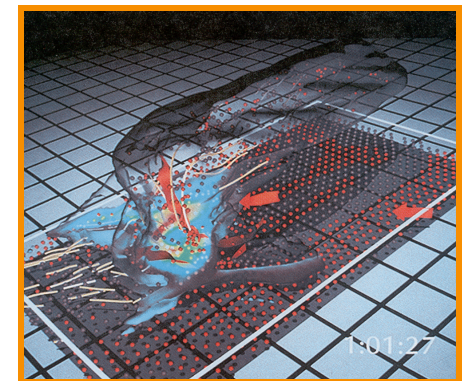
# Computer Animation



- Animation ←
  - Make objects change over time according to scripted actions
- Simulation / dynamics
  - Predict how objects change over time according to physical laws



Pixar



University of Illinois

# Computer Animation



- Describing how 3D objects (& cameras) move over time



# Computer Animation



- Challenge is balancing between ...
  - Animator control
  - Physical realism

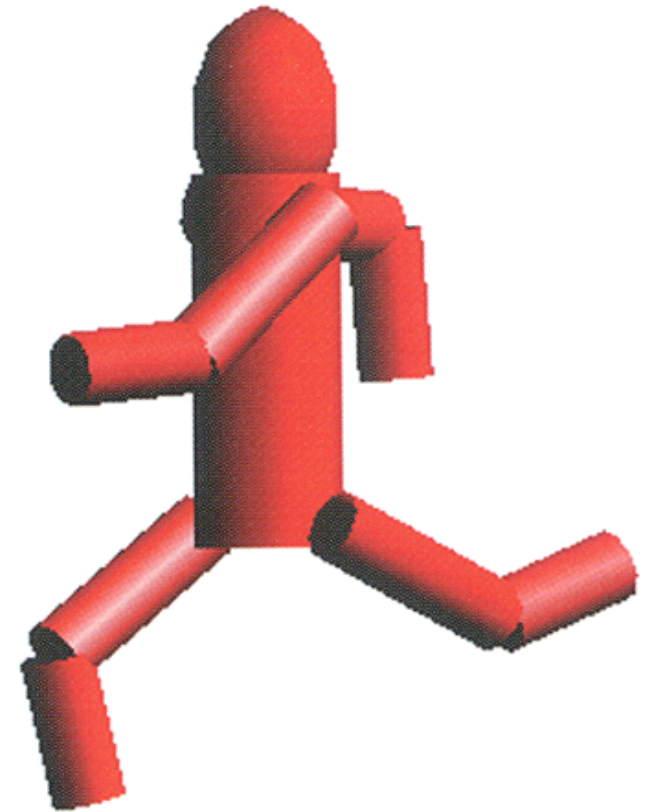




# Character Animation Methods

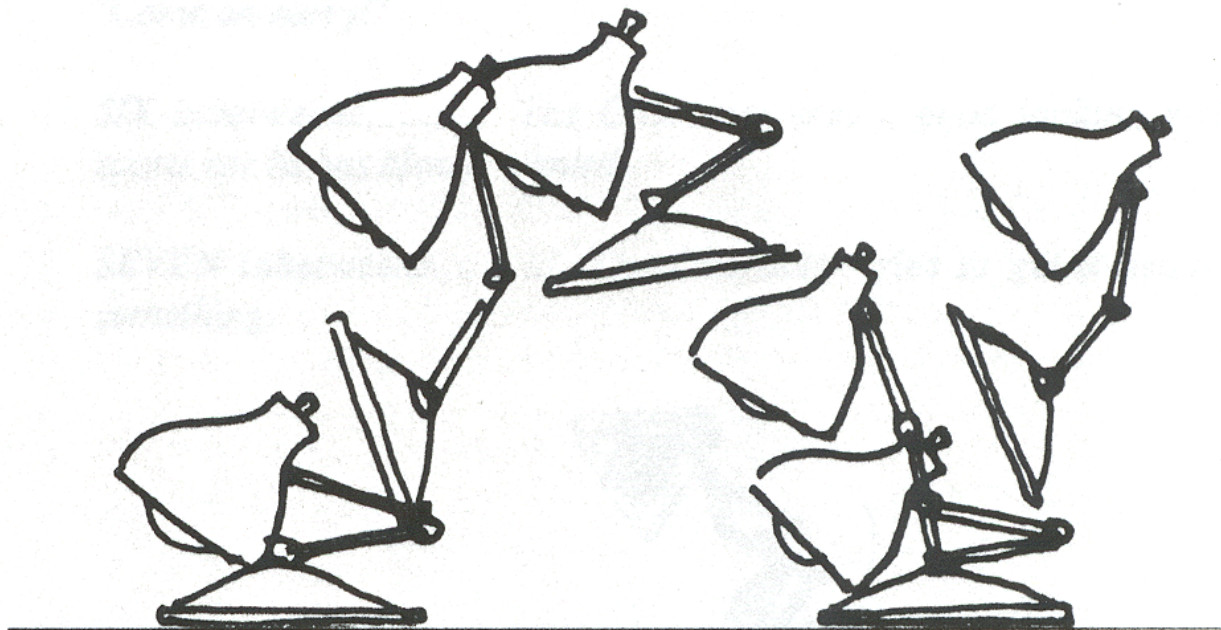


- Keyframing / Forward Kinematics
- Inverse Kinematics
- Dynamics
- Motion capture



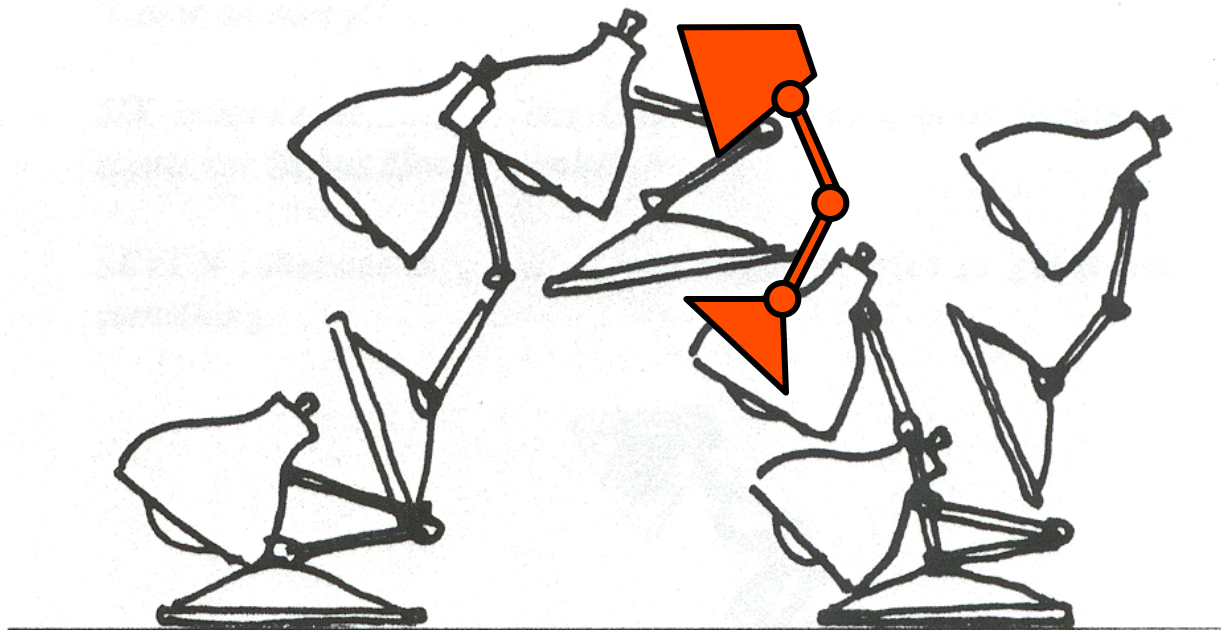
# Keyframe Animation

- Define character poses at specific time steps called “keyframes”



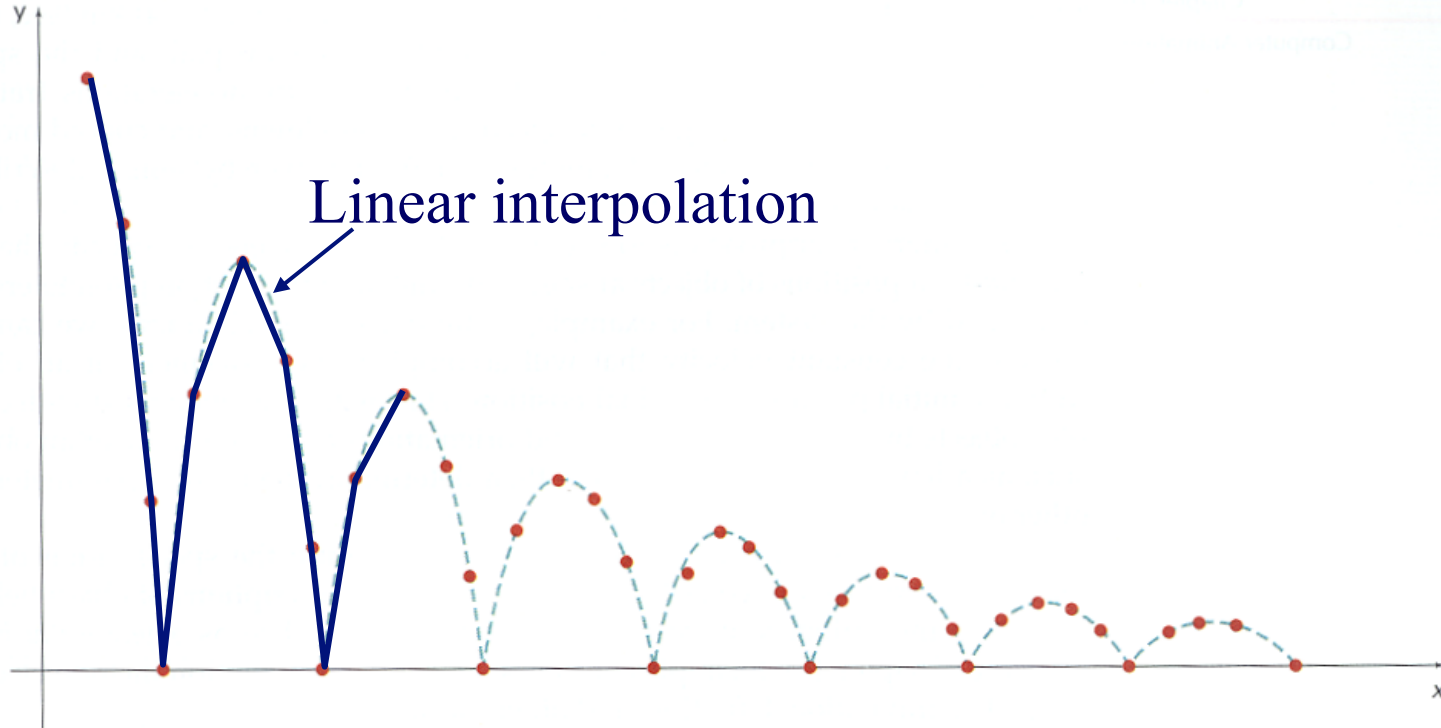
# Keyframe Animation

- Interpolate variables describing keyframes to determine poses for character in between



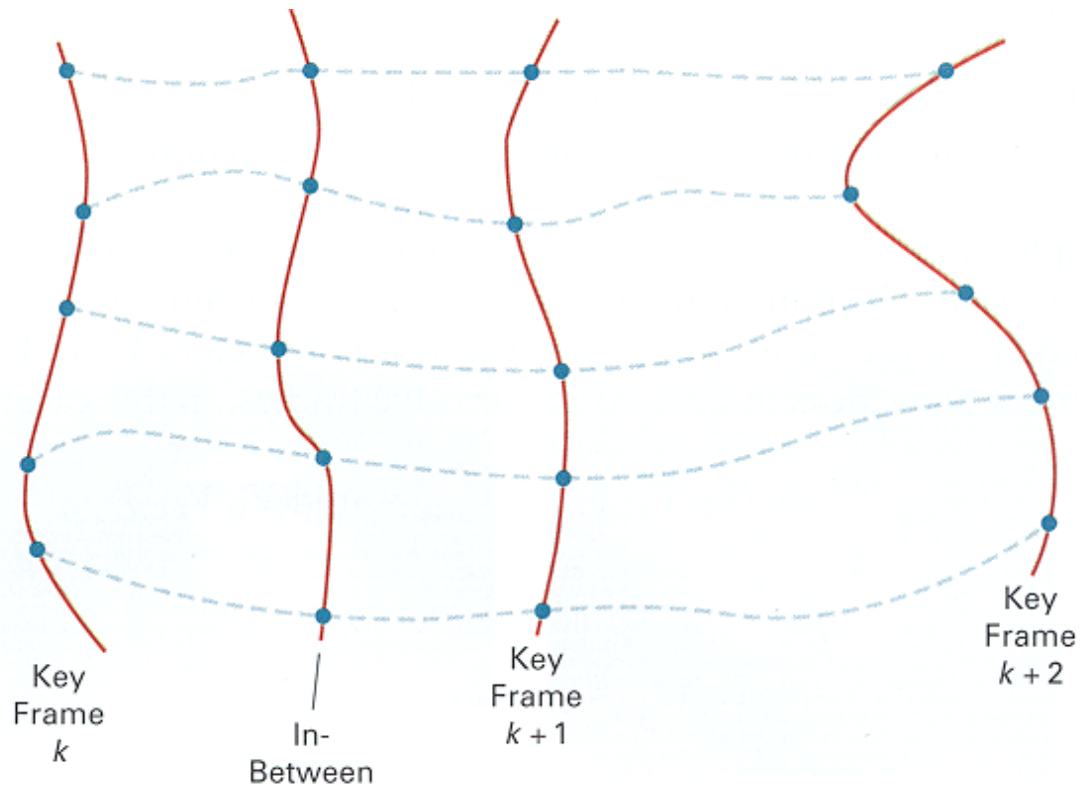
# Keyframe Animation

- Inbetweening:
  - Linear interpolation - usually not enough continuity



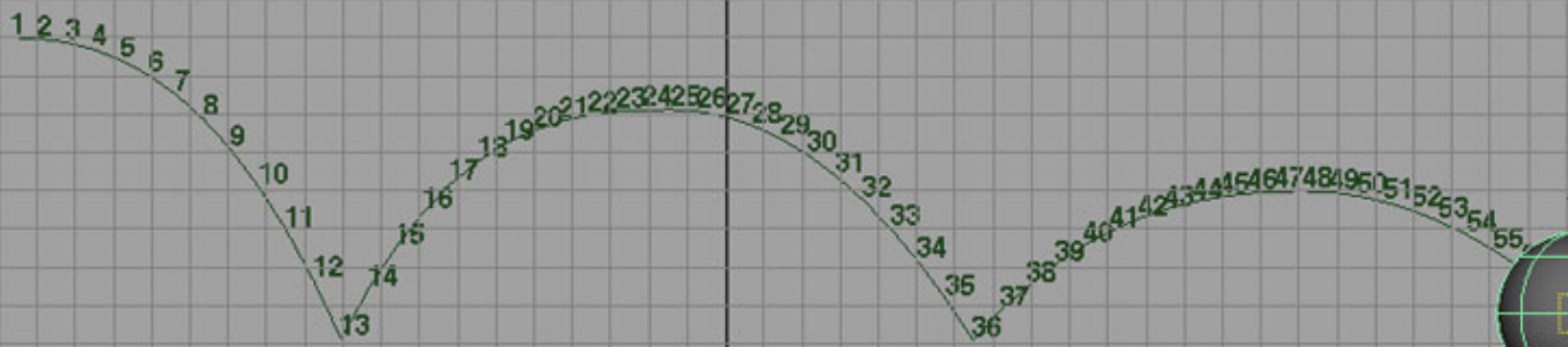
# Keyframe Animation

- Inbetweening:
  - Spline interpolation - maybe good enough





FRONT



front

View Select Curves Keys Tangents List Show Panels

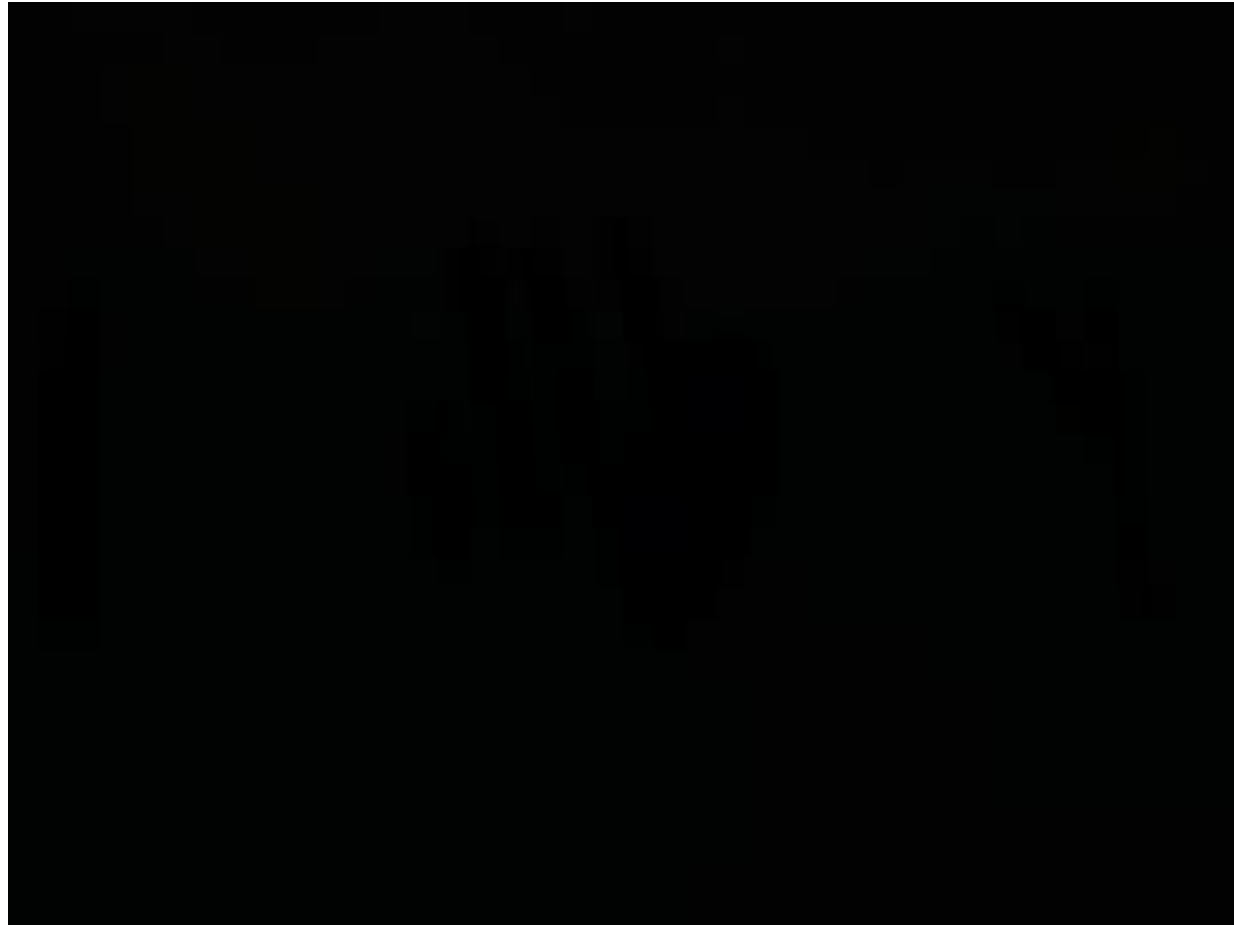
Stats 59 2.137

nurbsSphere1

- Translate X
- Translate Y



# Example: Ball Boy

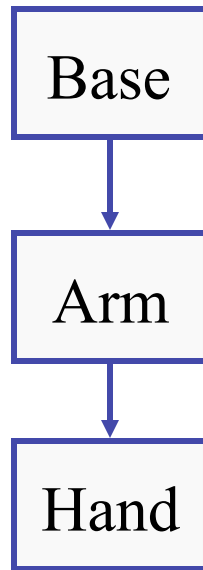


“Ballboy”

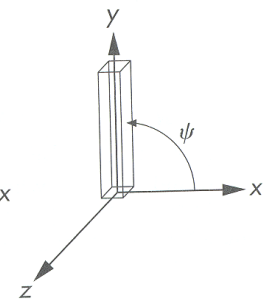
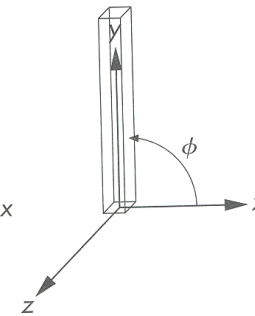
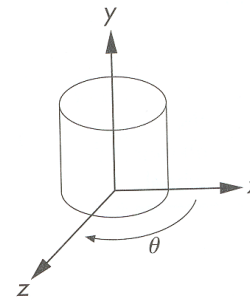
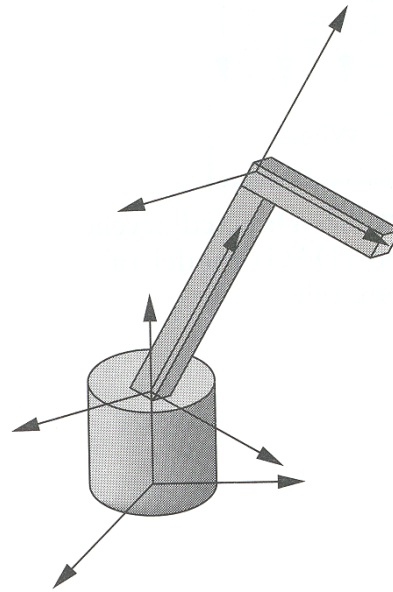
Fujito, Milliron, Ngan, & Sanocki  
Princeton University

# Articulated Figures

- Character poses described by set of rigid bodies connected by “joints”



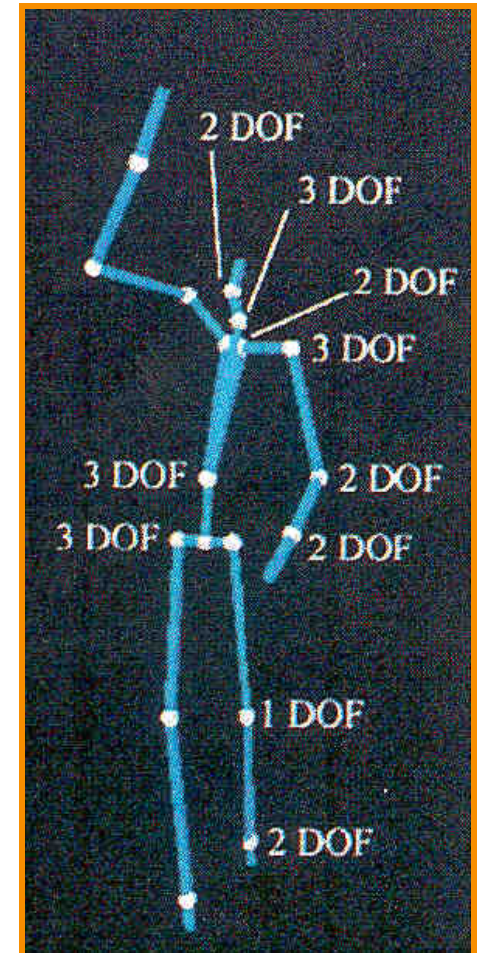
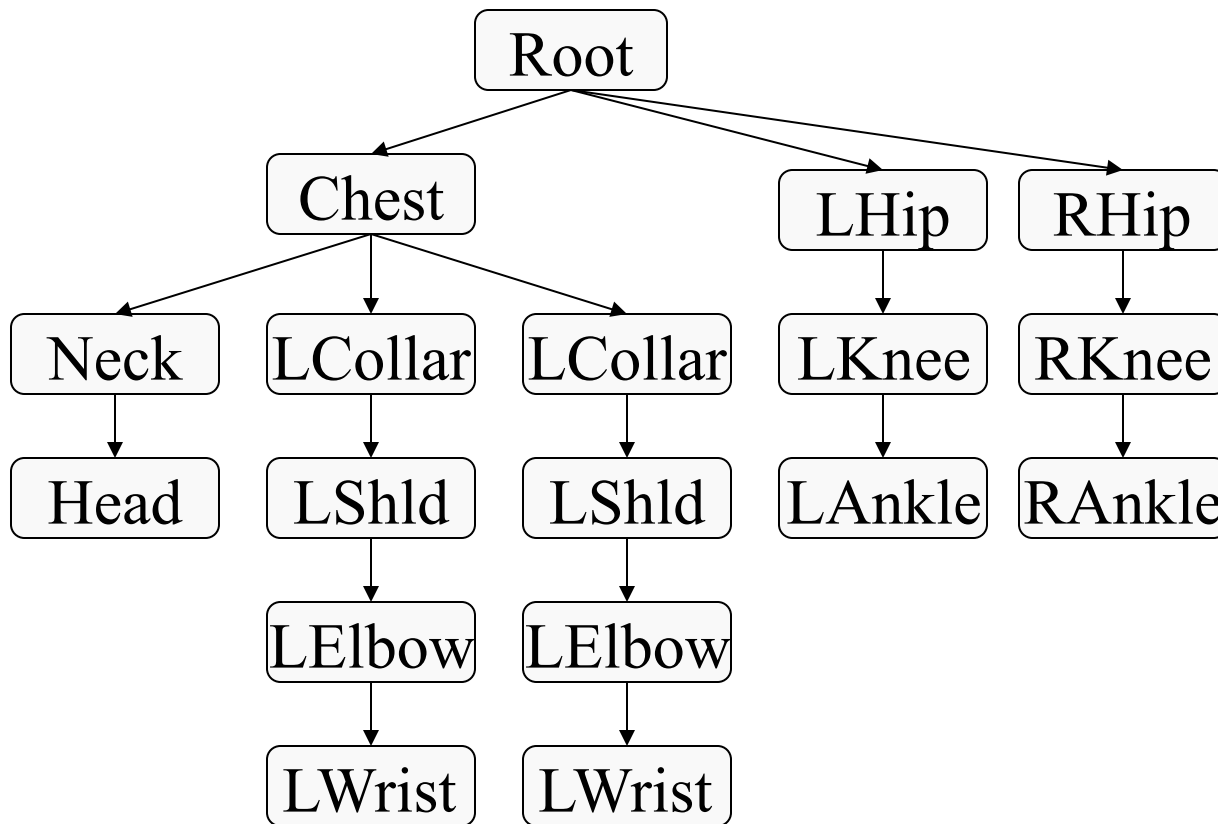
Scene Graph



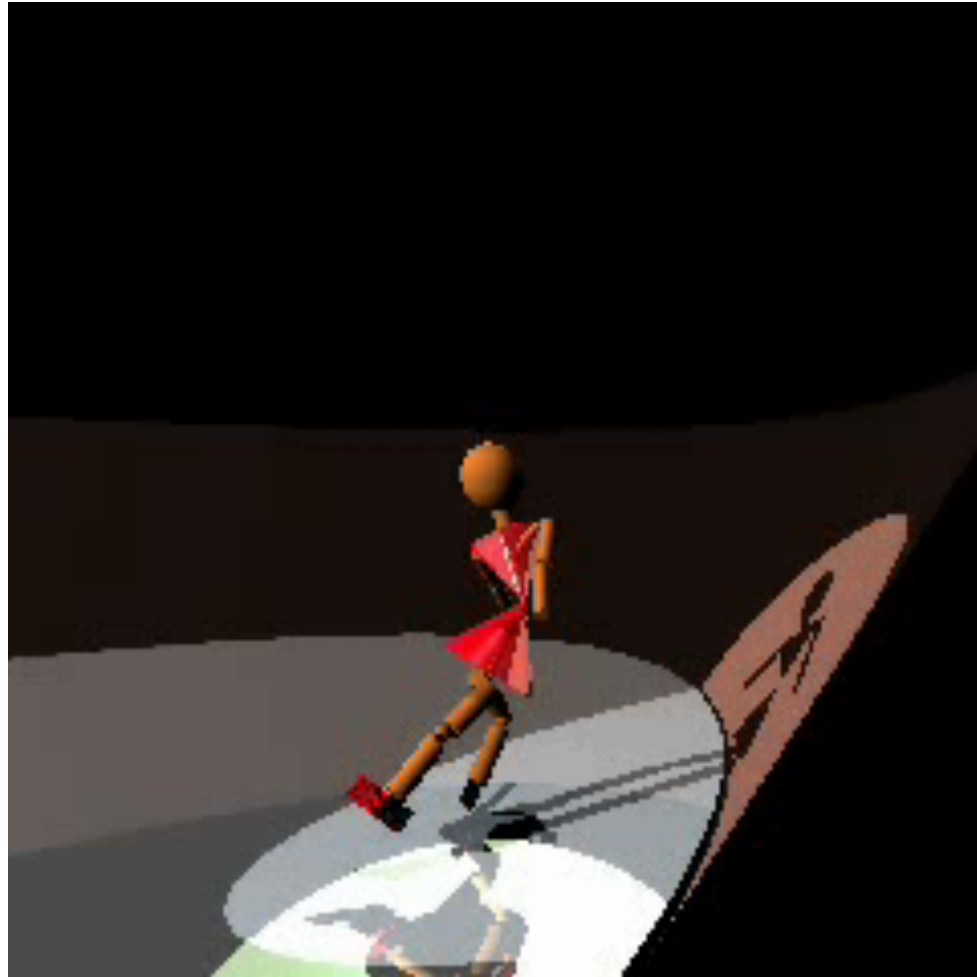
Angel Figures 8.8 & 8.9

# Articulated Figures

- Well-suited for humanoid characters



# Example: Ice Skating



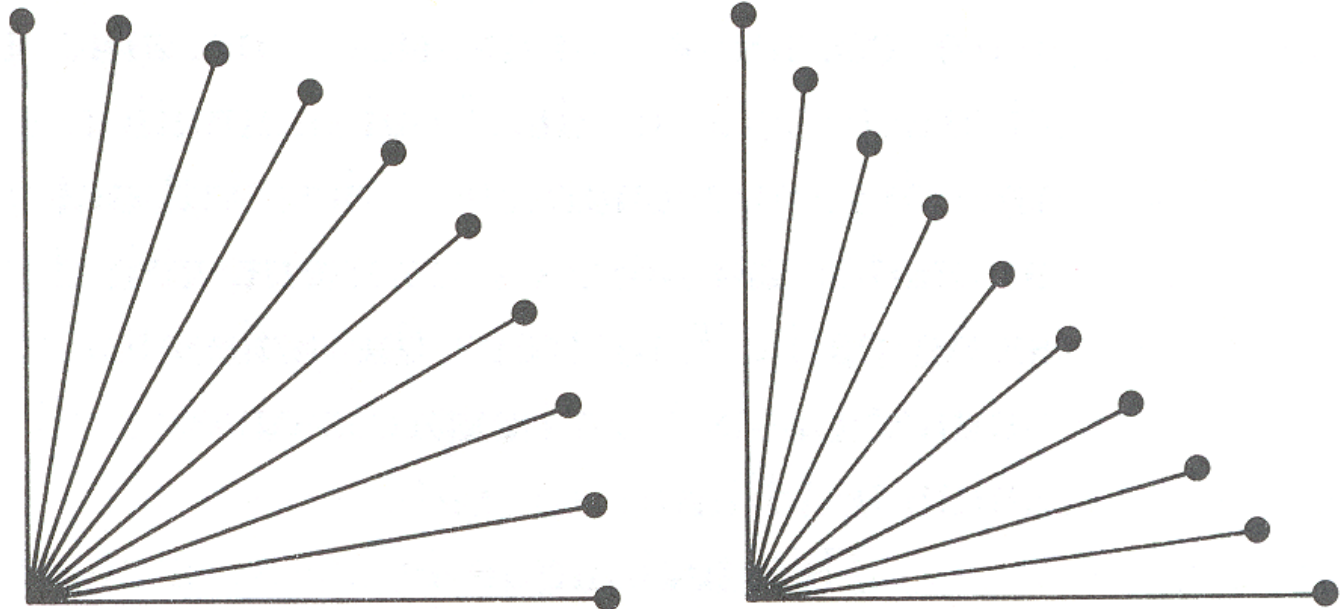
(Mao Chen, Zaijin Guan, Zhiyan Liu, Xiaohu Qie,  
CS426, Fall98, Princeton University)



# Articulated Figures



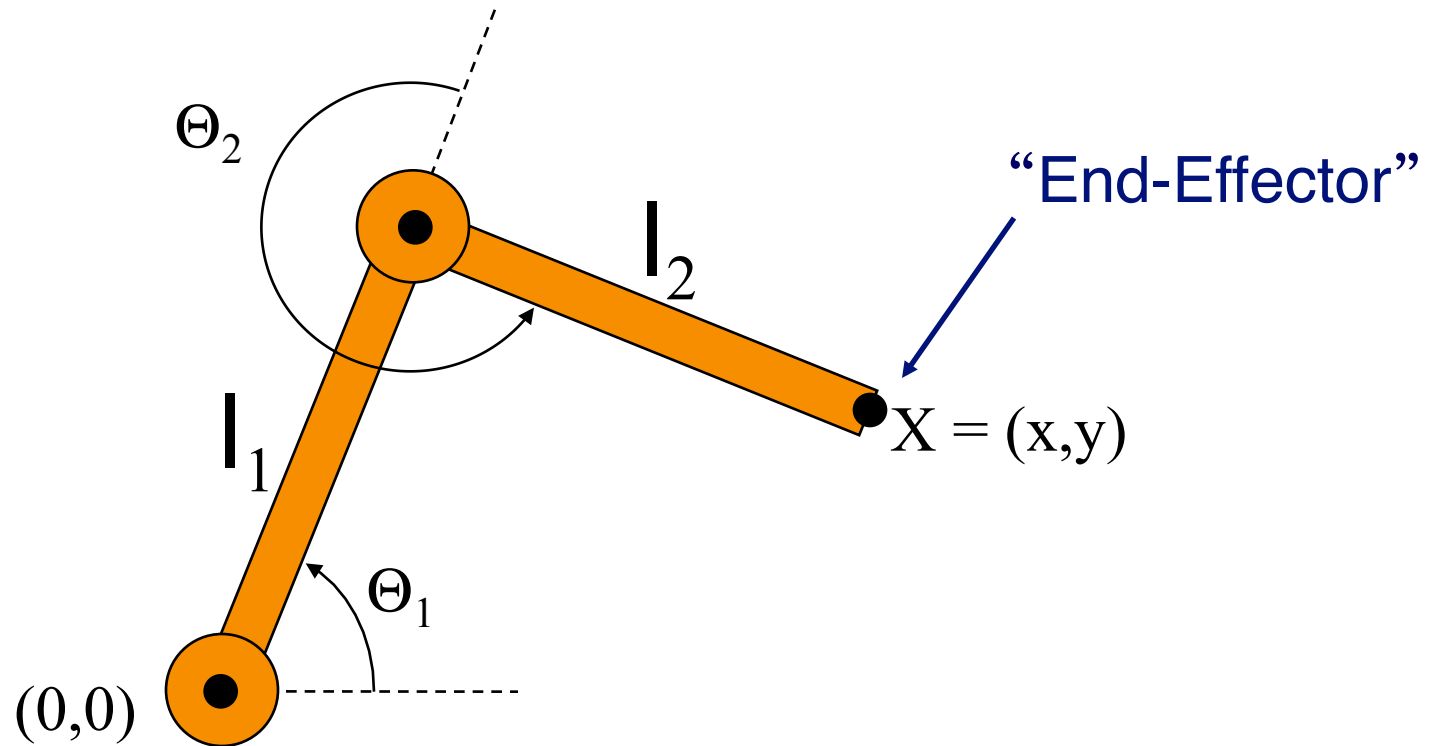
- Animation focuses on **joint angles**



# Forward Kinematics

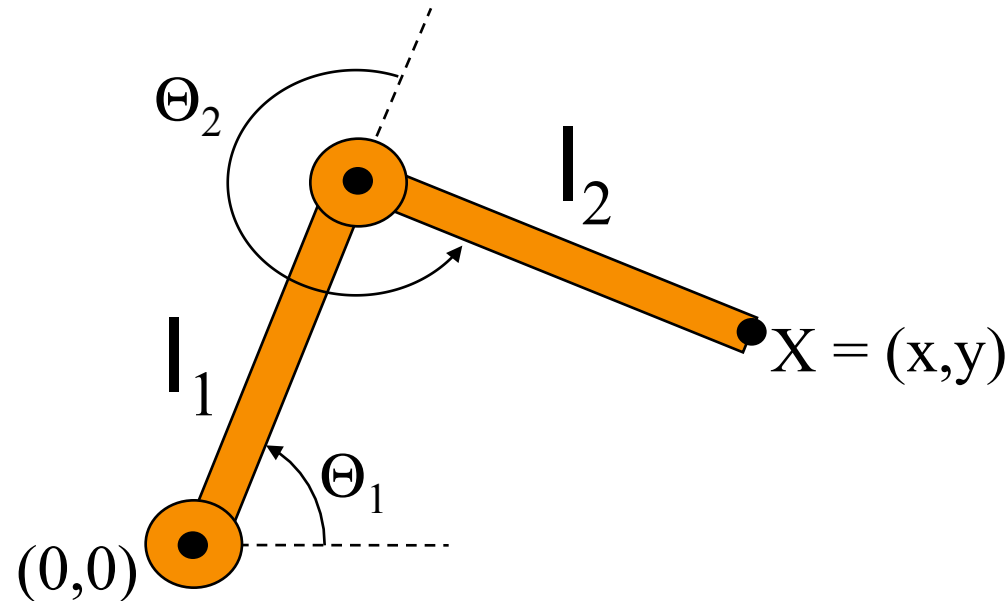


- Describe motion of articulated character



# Forward Kinematics

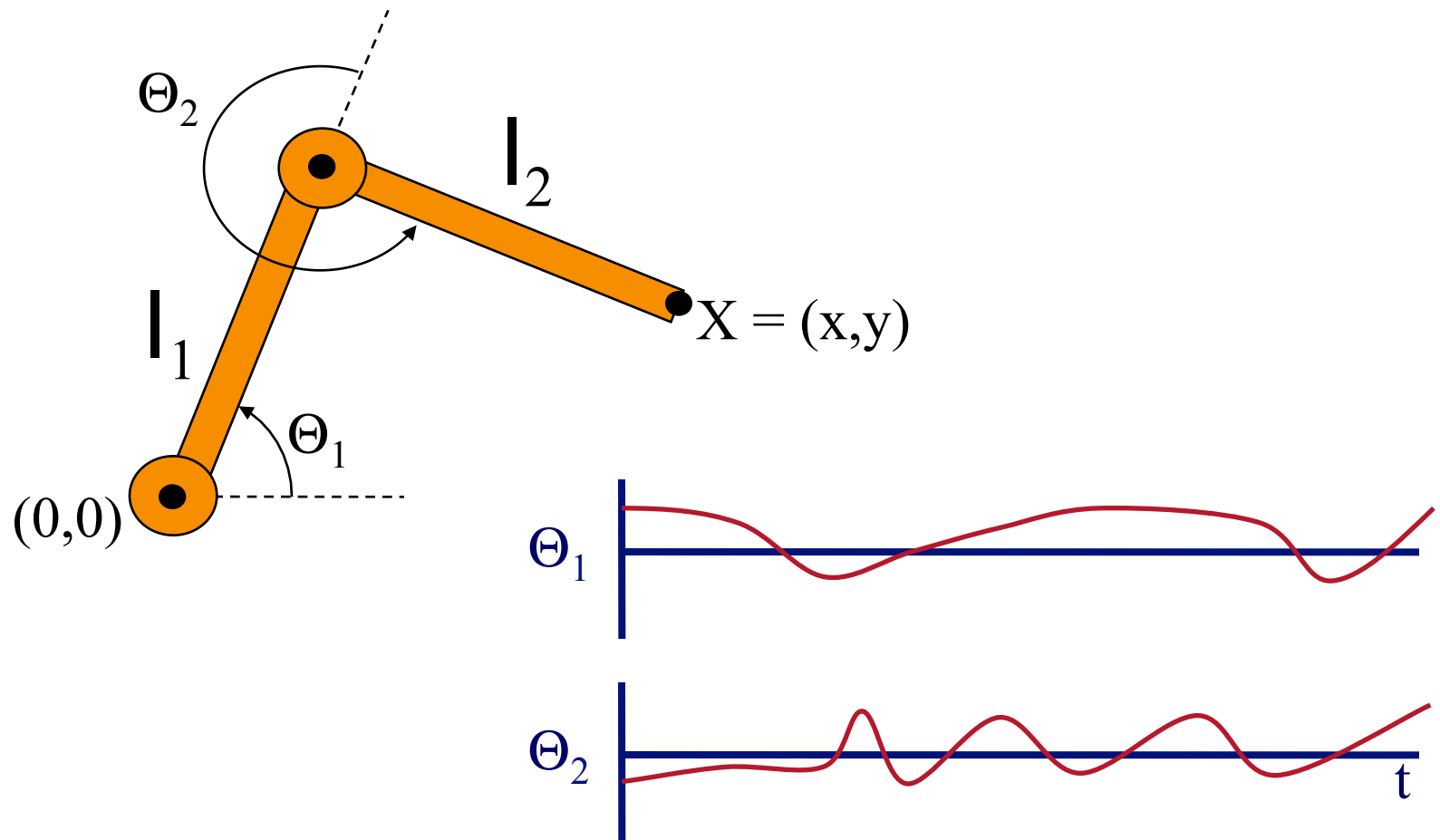
- Animator specifies joint angles:  $\Theta_1$  and  $\Theta_2$
- Computer finds positions of end-effector:  $X$



$$X = (l_1 \cos \Theta_1 + l_2 \cos(\Theta_1 + \Theta_2), l_1 \sin \Theta_1 + l_2 \sin(\Theta_1 + \Theta_2))$$

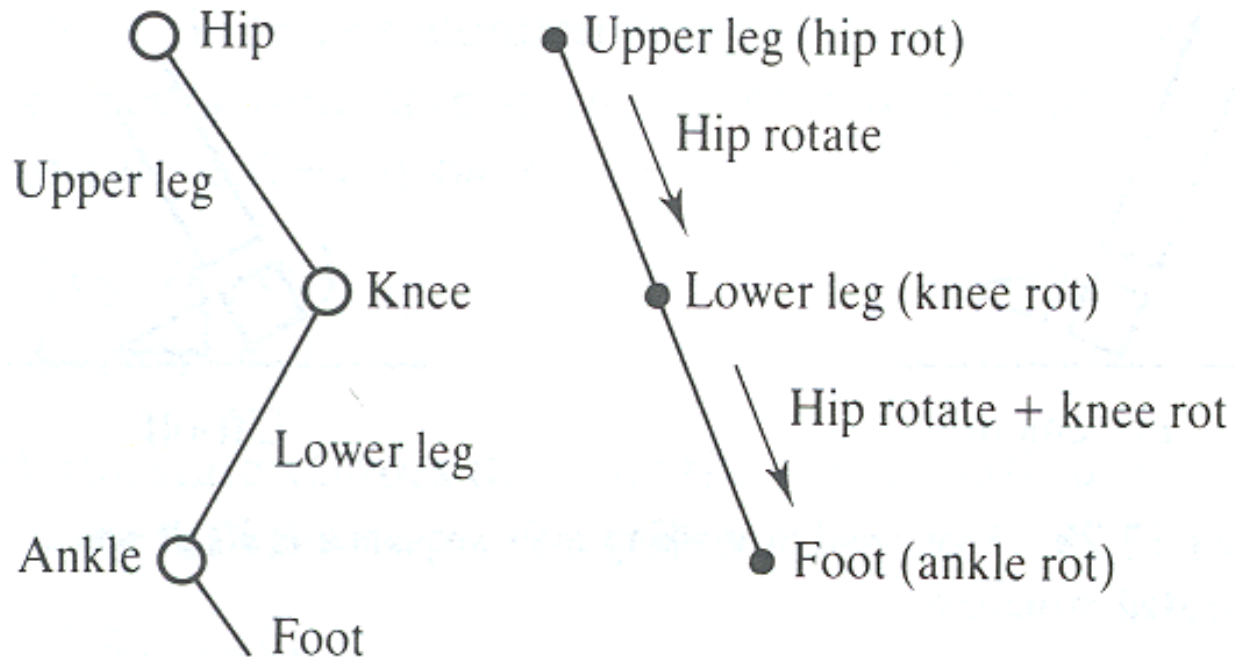
# Forward Kinematics

- Joint motions specified e.g. by spline curves



# Example: Walk Cycle

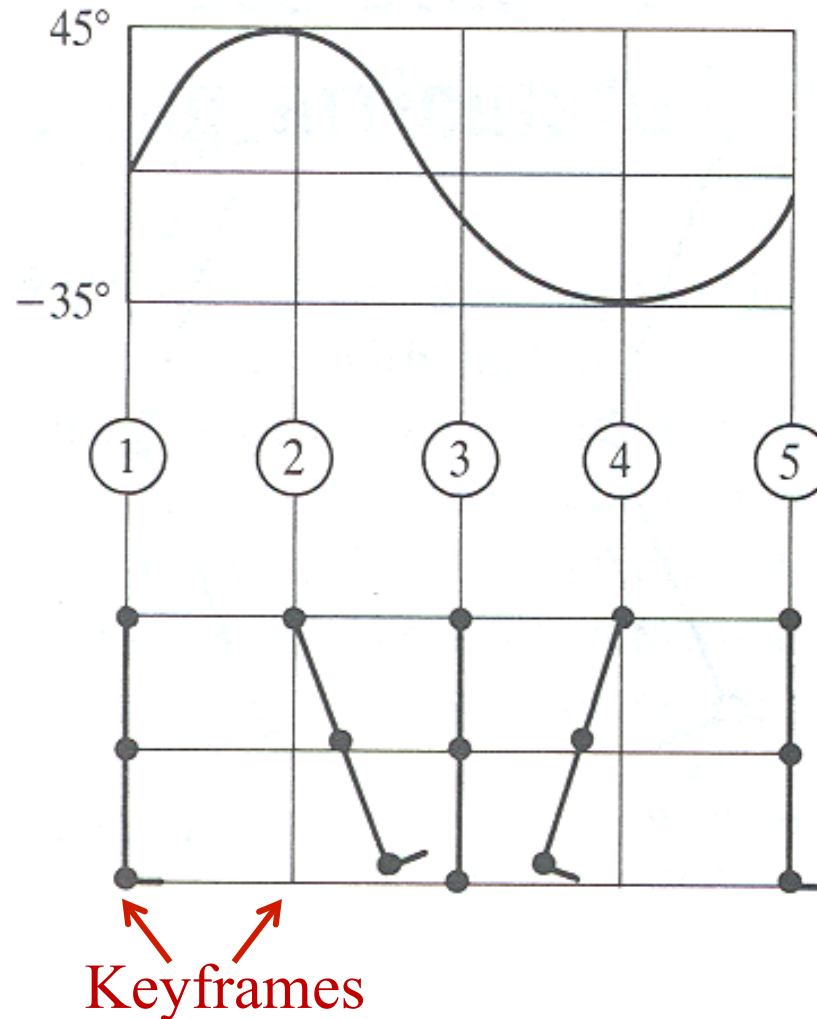
- Articulated figure:





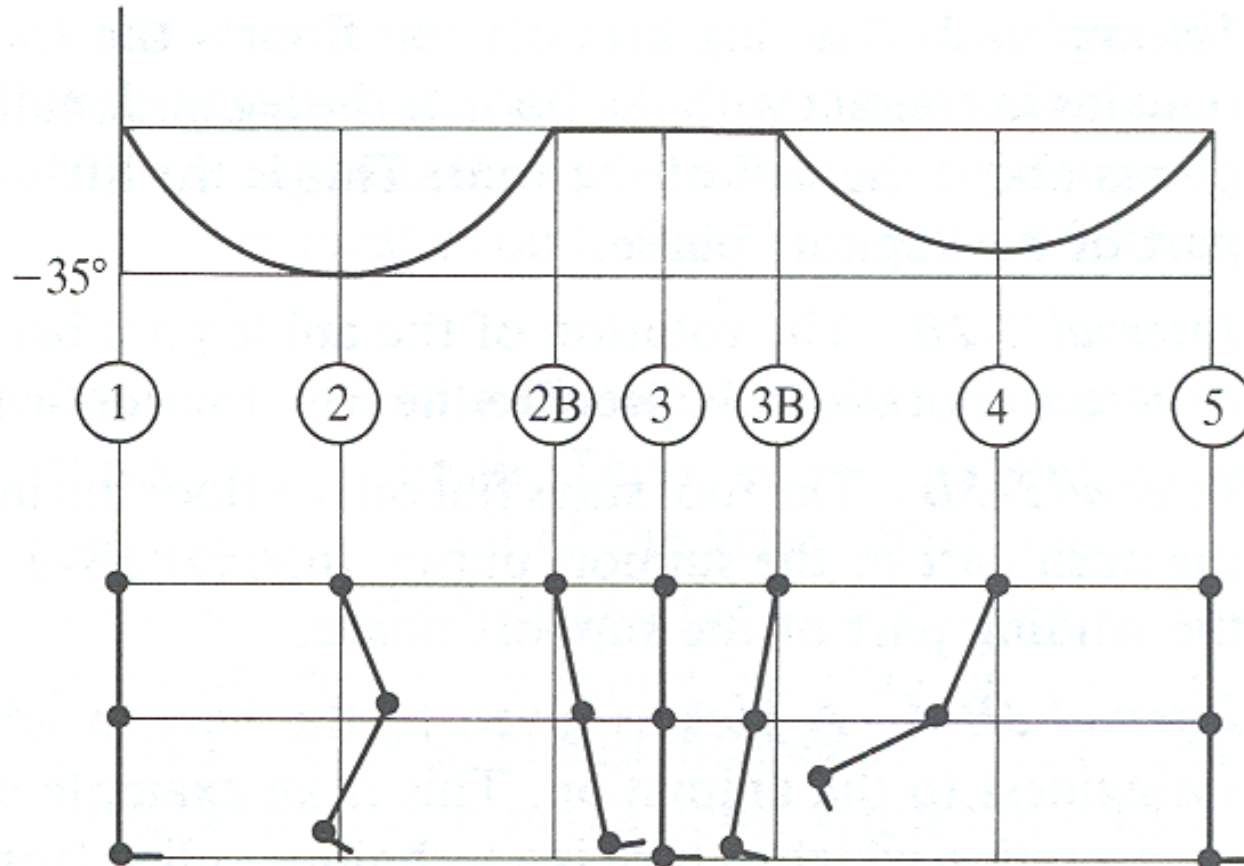
# Example: Walk Cycle

- Hip joint orientation:



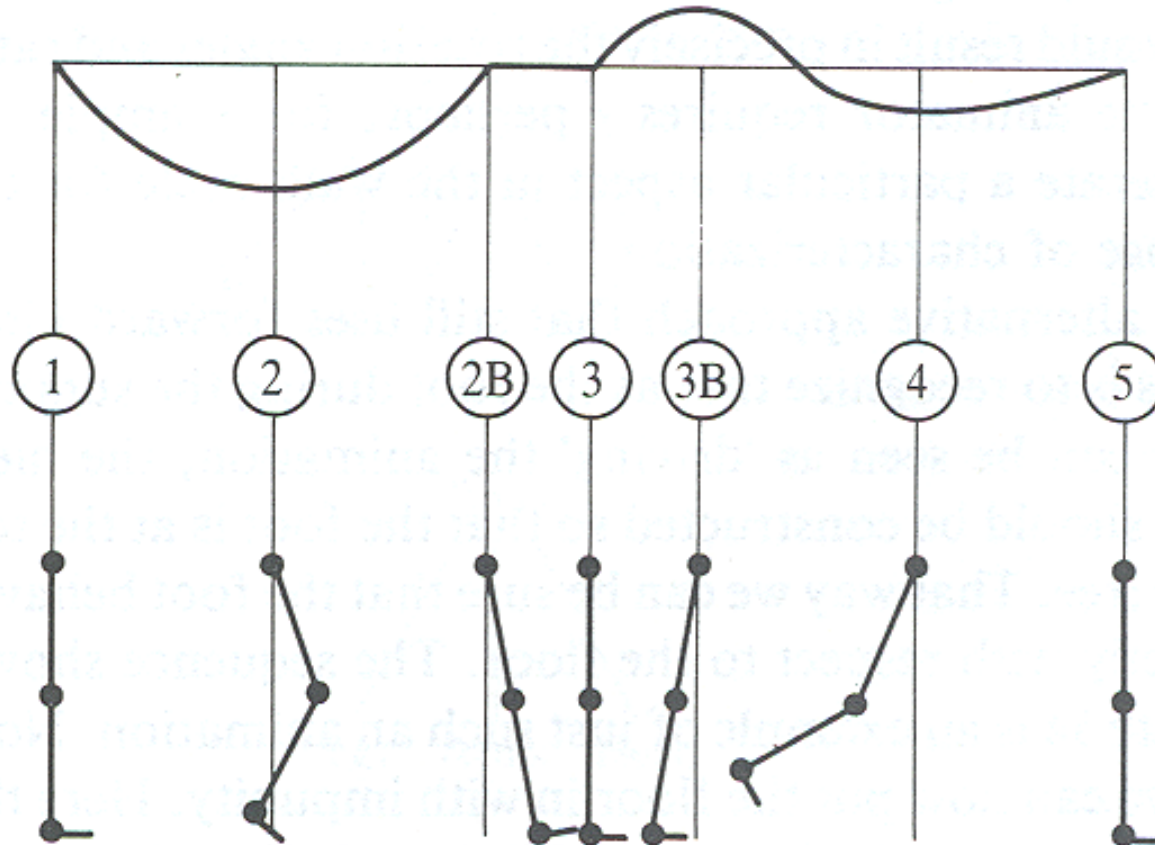
# Example: Walk Cycle

- Knee joint orientation:

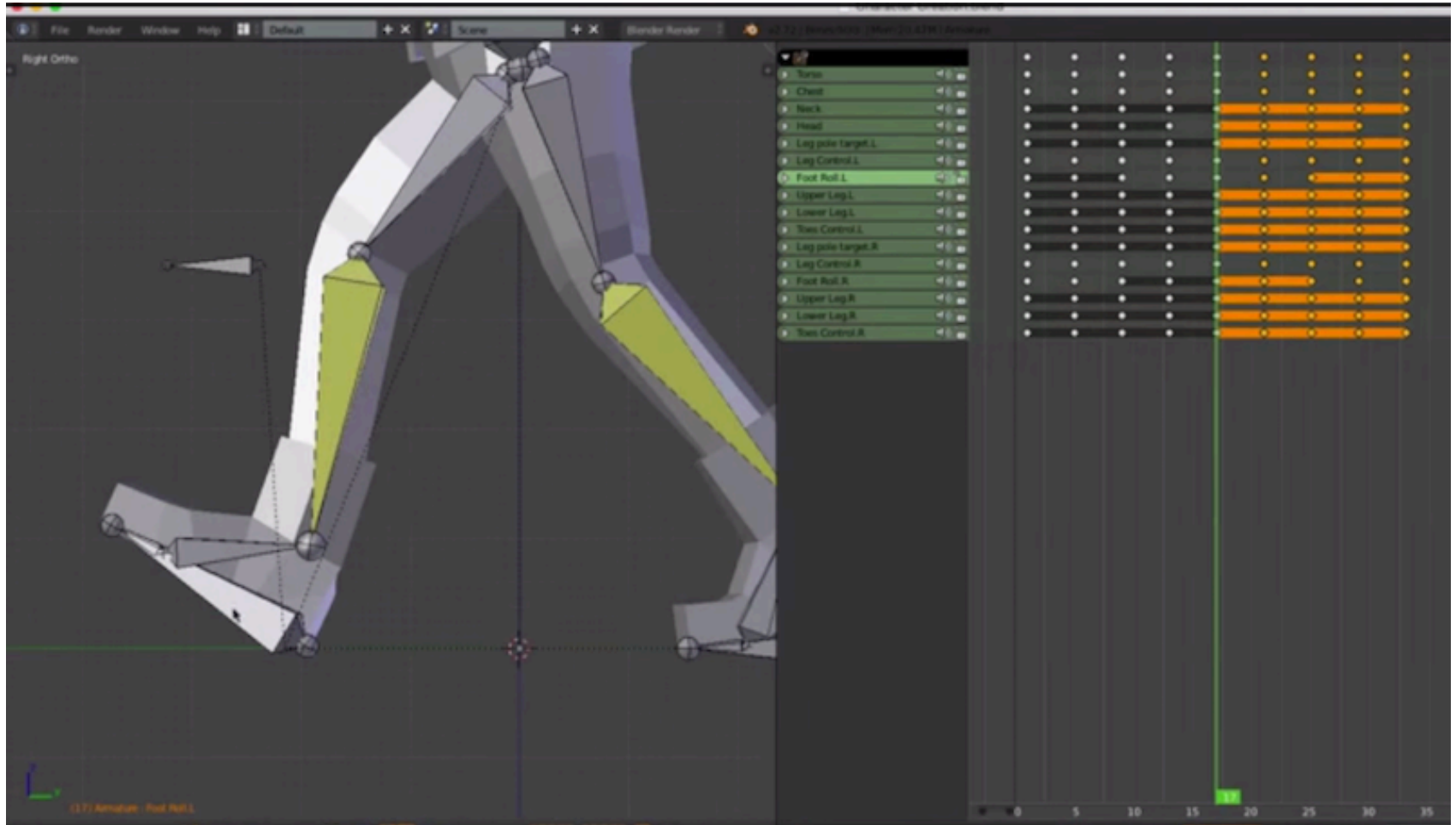


# Example: Walk Cycle

- Ankle joint orientation:



# Example: walk cycle

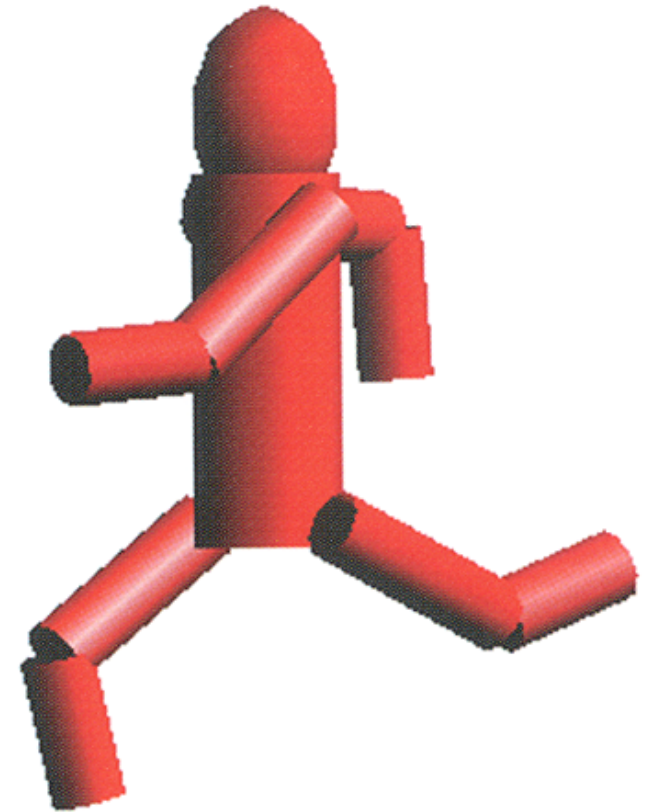


Lague: [www.youtube.com/watch?v=DuUWxUitJos](http://www.youtube.com/watch?v=DuUWxUitJos)

# Character Animation Methods



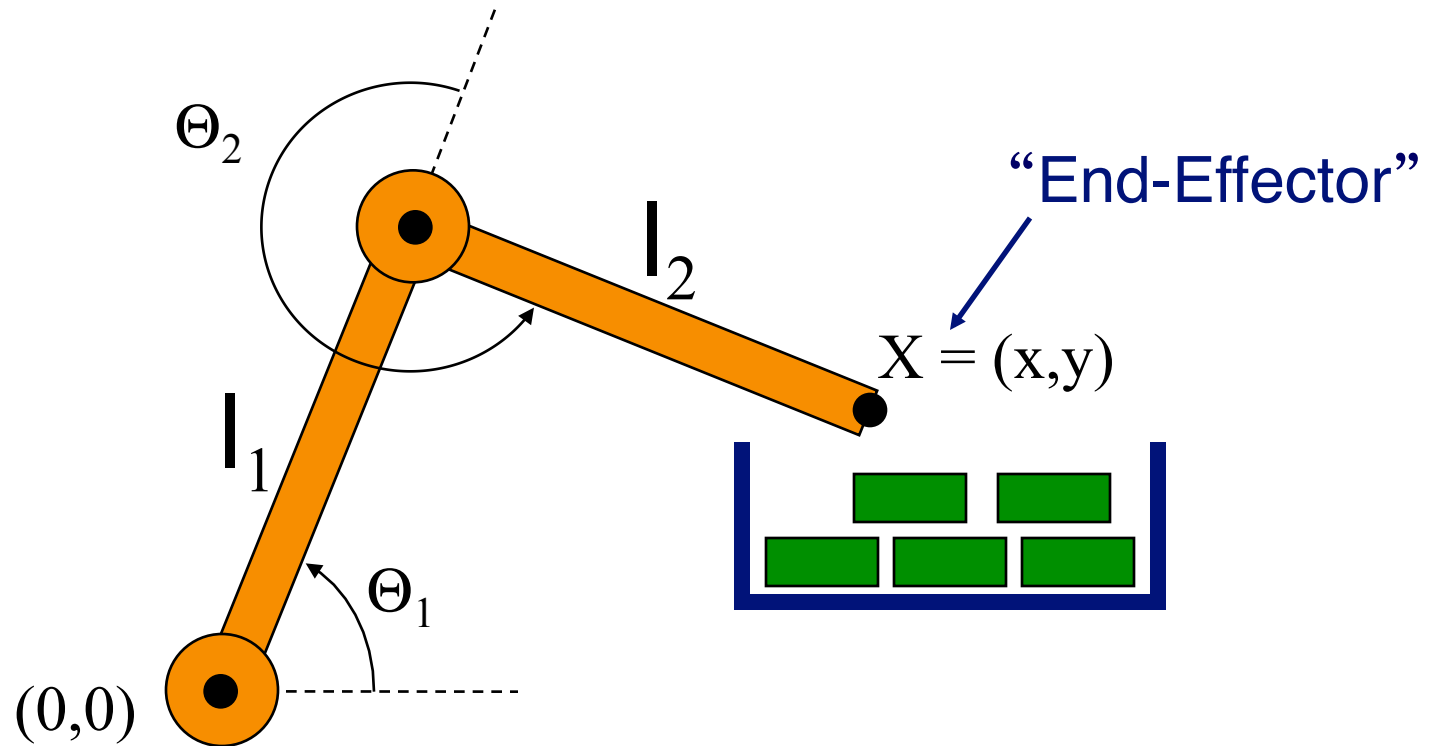
- Keyframing / Forward Kinematics
- **Inverse Kinematics**
- Dynamics
- Motion capture





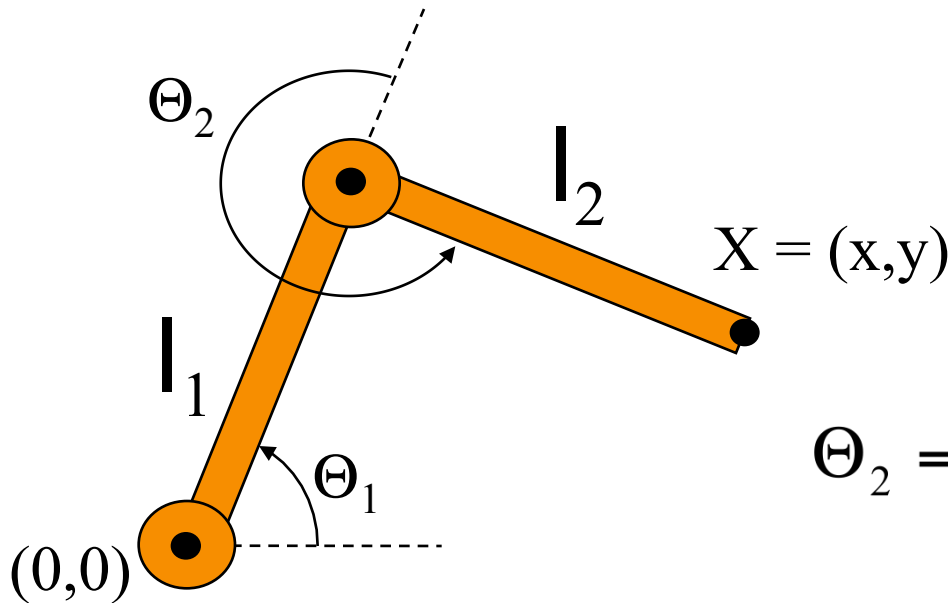
# Inverse Kinematics

- What if animator knows position of “end-effector”?



# Inverse Kinematics

- Animator specifies end-effector positions:  $X$
- Computer finds joint angles:  $\Theta_1$  and  $\Theta_2$ :

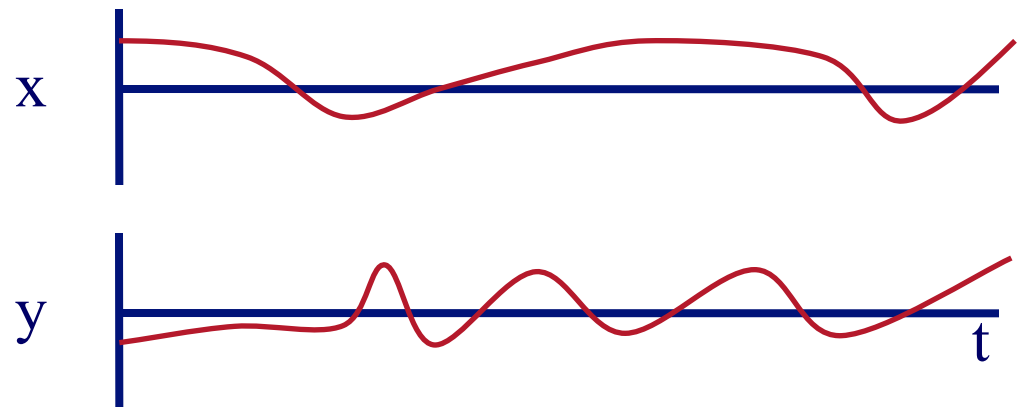
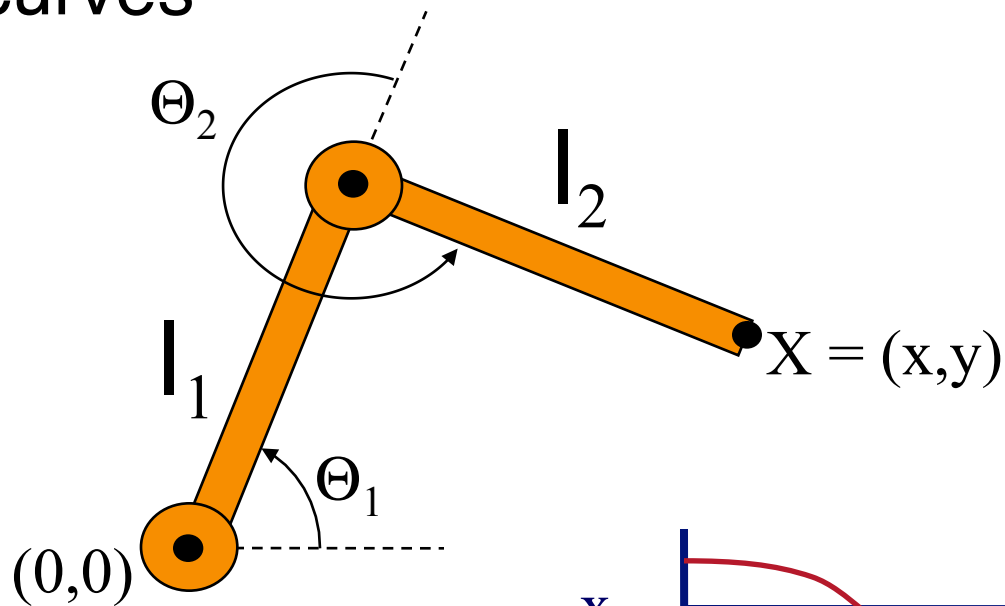


$$\Theta_2 = \cos^{-1} \left( \frac{x^2 + y^2 - l_1^2 - l_2^2}{2l_1l_2} \right)$$

$$\Theta_1 = \frac{-(l_2 \sin(\Theta_2)x + (l_1 + l_2 \cos(\Theta_2))y)}{(l_2 \sin(\Theta_2))y + (l_1 + l_2 \cos(\Theta_2))x}$$

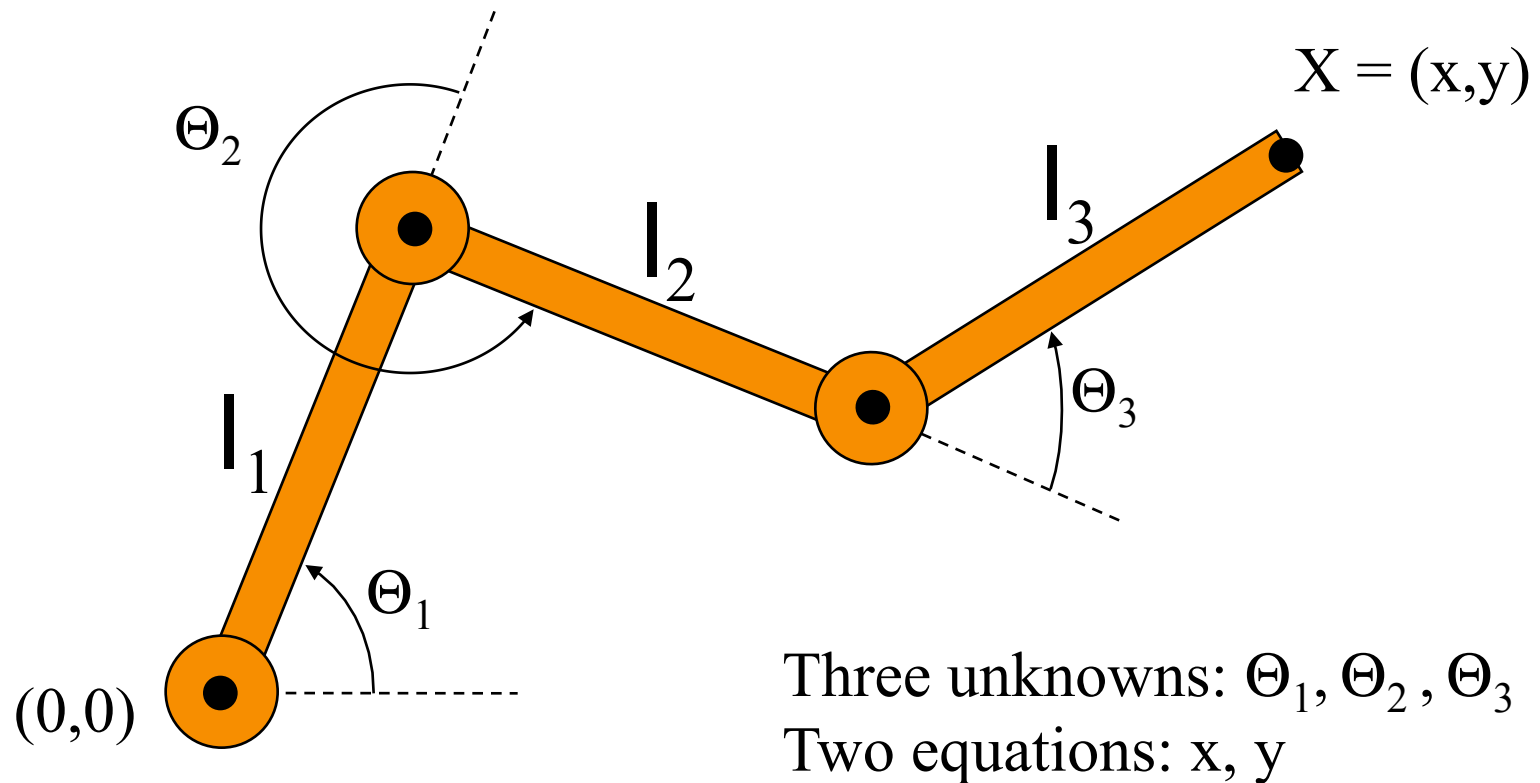
# Inverse Kinematics

- End-effector positions can be specified by spline curves



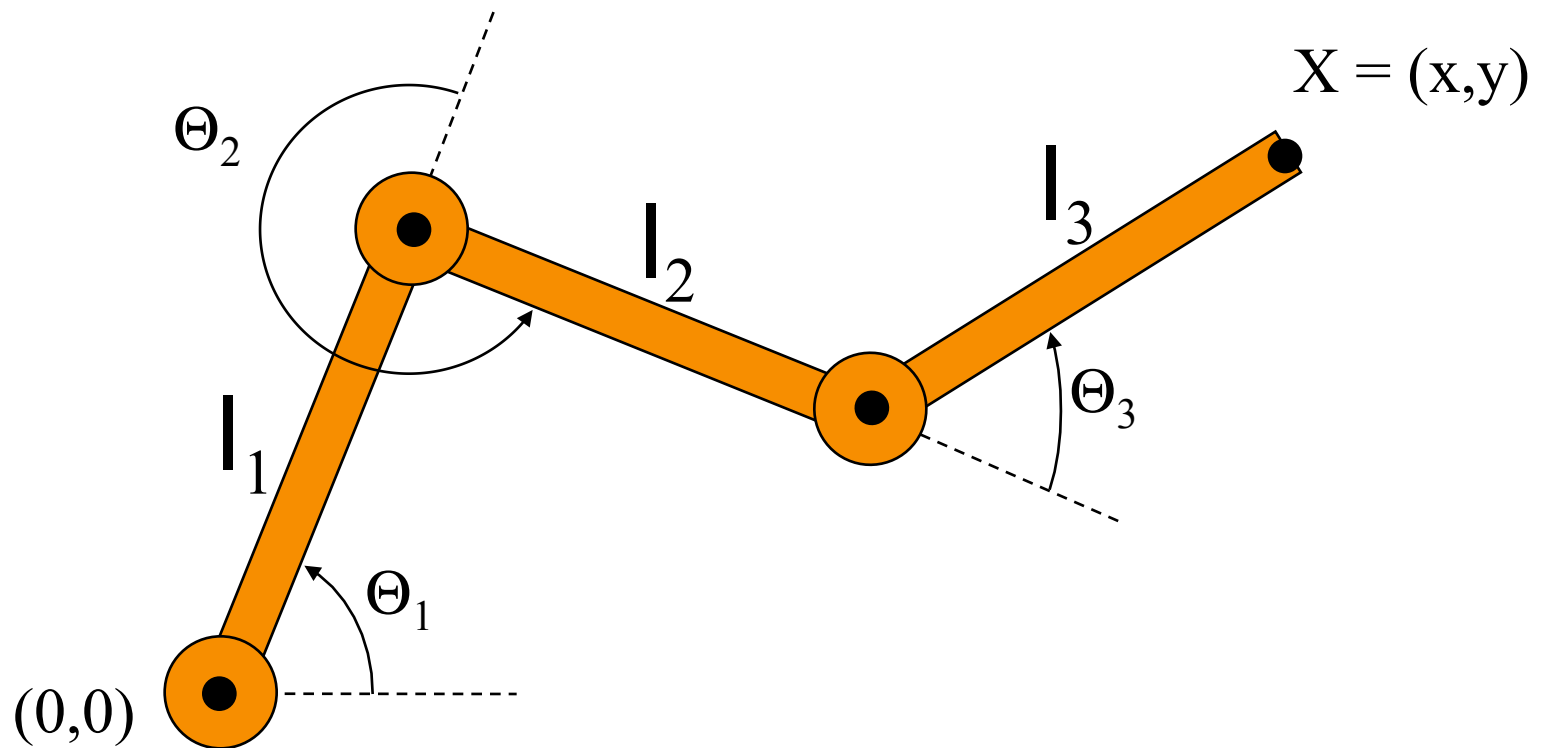
# Inverse Kinematics

- Problem for more complex structures
  - System of equations is usually under-constrained
  - Multiple solutions



# Inverse Kinematics

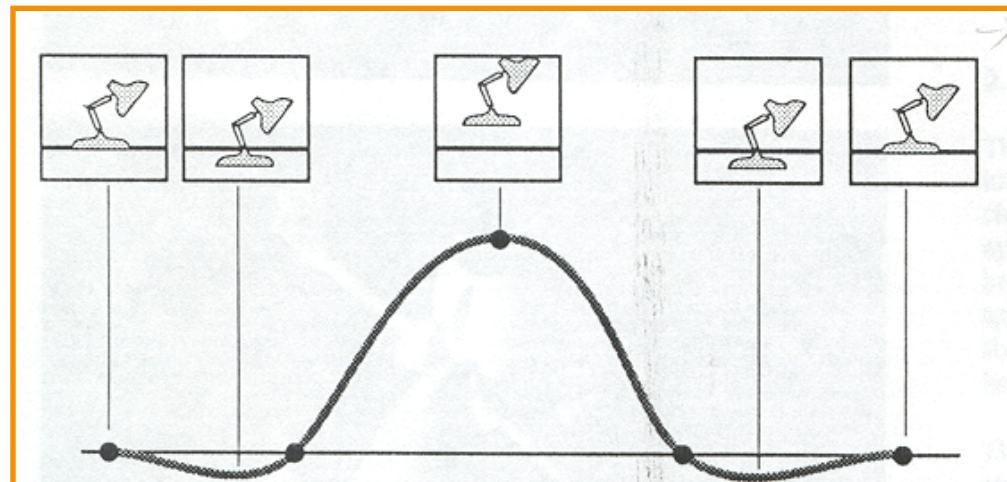
- Solution for more complex structures:
  - Find best solution (e.g., minimize energy in motion)
  - Non-linear optimization





# Kinematics

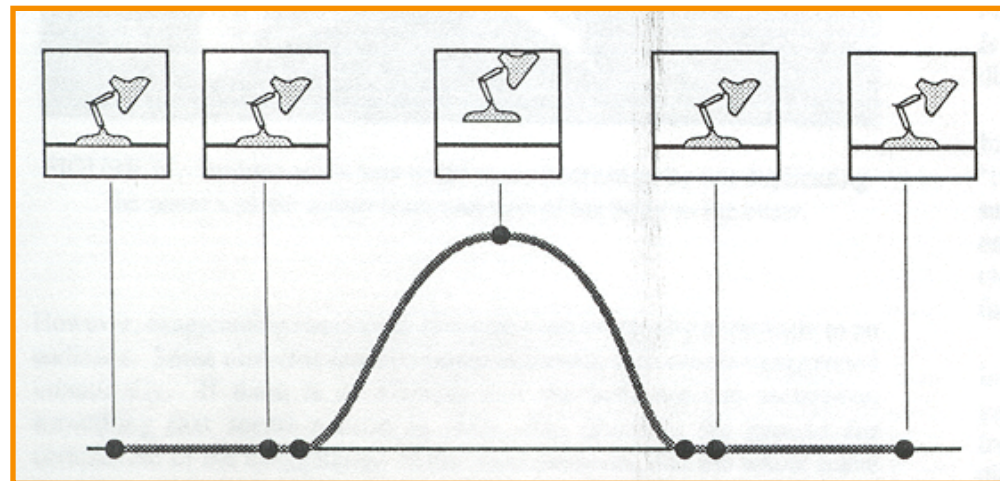
- Advantages
  - Simple to implement
  - Complete animator control
- Disadvantages
  - Motions may not follow physical laws
  - Tedious for animator



Lasseter '87

# Kinematics

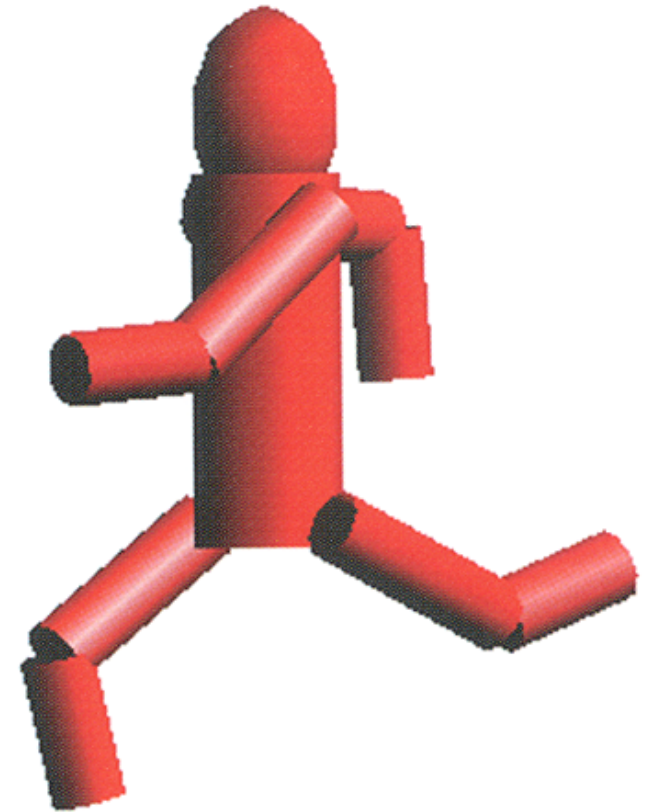
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# Character Animation Methods



- Keyframing / Forward Kinematics
- Inverse Kinematics
- **Dynamics**
- Motion capture

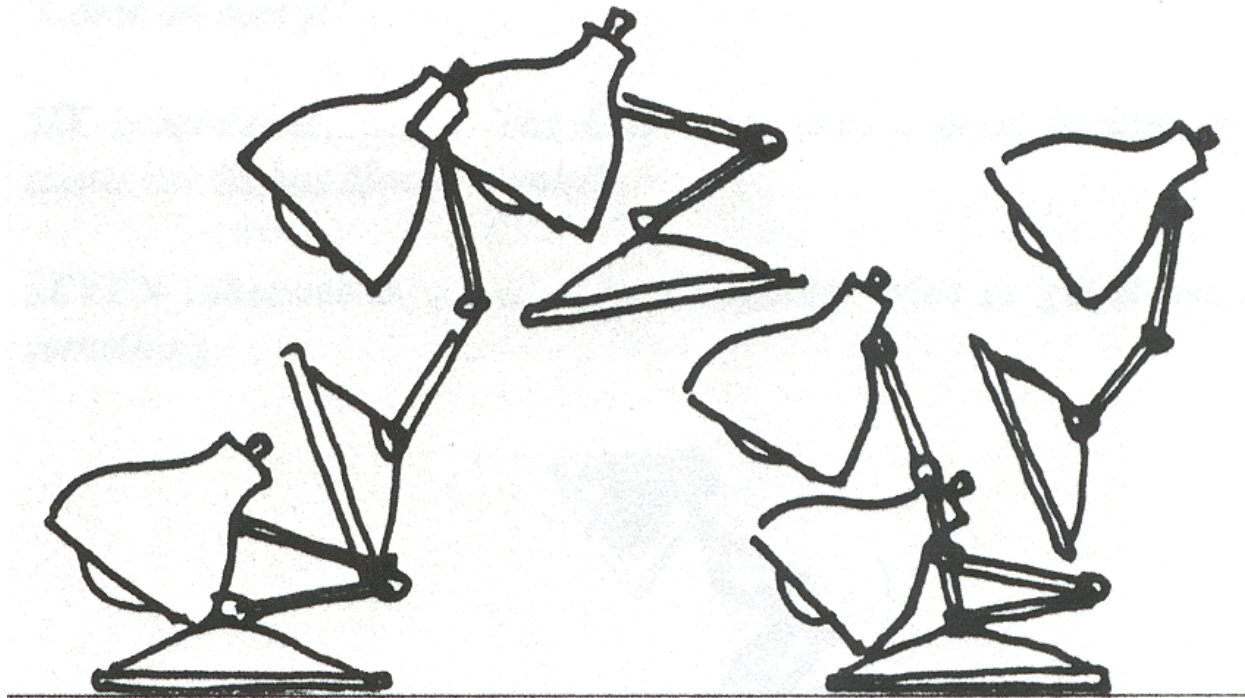




# Dynamics



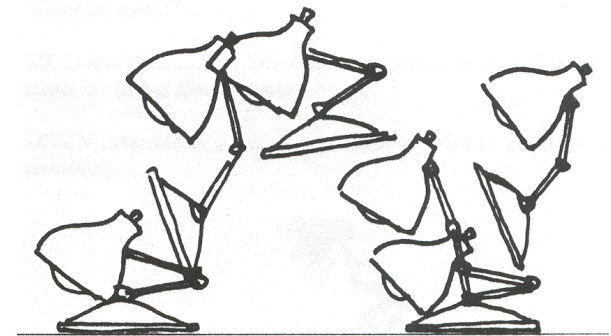
- Simulation of physics ensures realism of motion



# Spacetime Constraints



- Animator specifies constraints:
  - What the character's physical structure is
    - » e.g., articulated figure
  - What the character has to do (keyframes)
    - » e.g., jump from here to there within time  $t$
  - What other physical structures are present
    - » e.g., floor to push off and land
  - How the motion should be performed
    - » e.g., minimize energy



# Spacetime Constraints

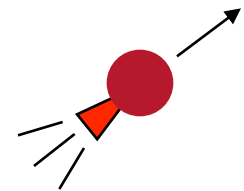


- Computer finds the “best” physical motion satisfying constraints
- Example: particle with jet propulsion
  - $\mathbf{x}(t)$  is position of particle at time  $t$
  - $\mathbf{f}(t)$  is force of jet propulsion at time  $t$
  - Particle’s equation of motion is:

$$m\mathbf{x}'' - \mathbf{f} - m\mathbf{g} = 0$$

- Suppose we want to move from  $a$  to  $b$  within  $t_0$  to  $t_1$  with minimum jet fuel:

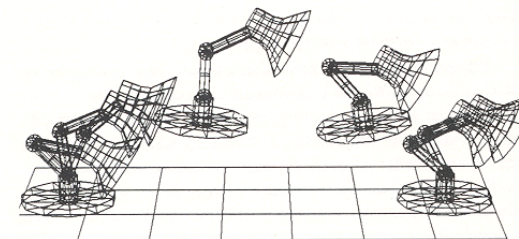
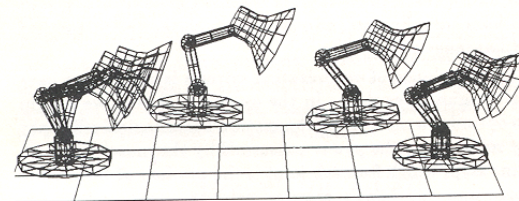
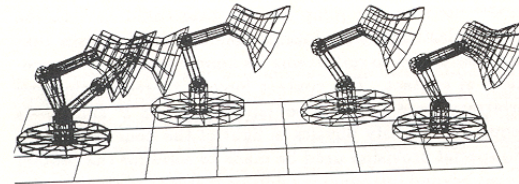
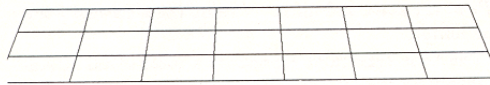
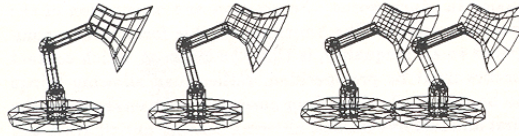
$$\text{Minimize } \int_{t_0}^{t_1} |f(t)|^2 dt \text{ subject to } x(t_0) = a \text{ and } x(t_1) = b$$



# Spacetime Constraints



- Solve with iterative optimization methods





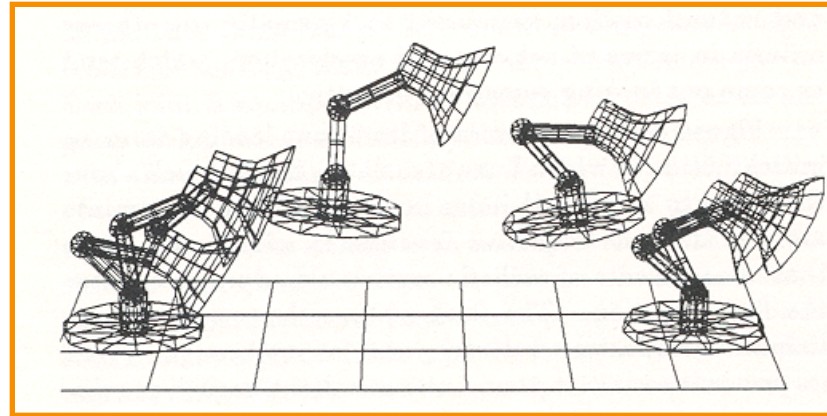
# Spacetime Constraints

- Advantages:
  - Free animator from having to specify details of physically realistic motion with spline curves
  - Easy to vary motions due to new parameters and/or new constraints
- Challenges:
  - Specifying constraints and objective functions
  - Avoiding local minima during optimization

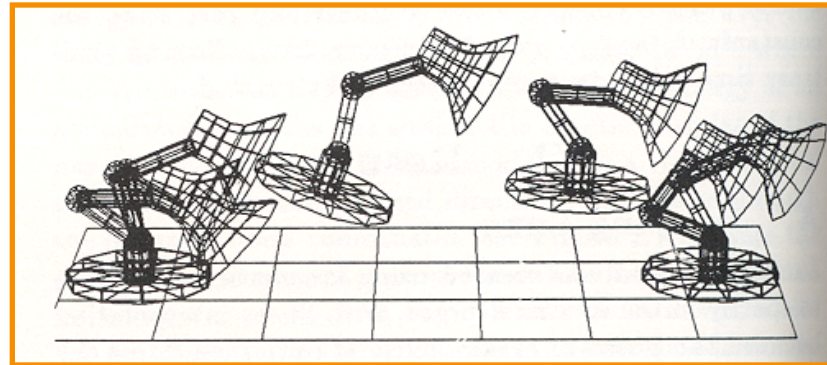
# Spacetime Constraints



- Adapting motion:



Original Jump



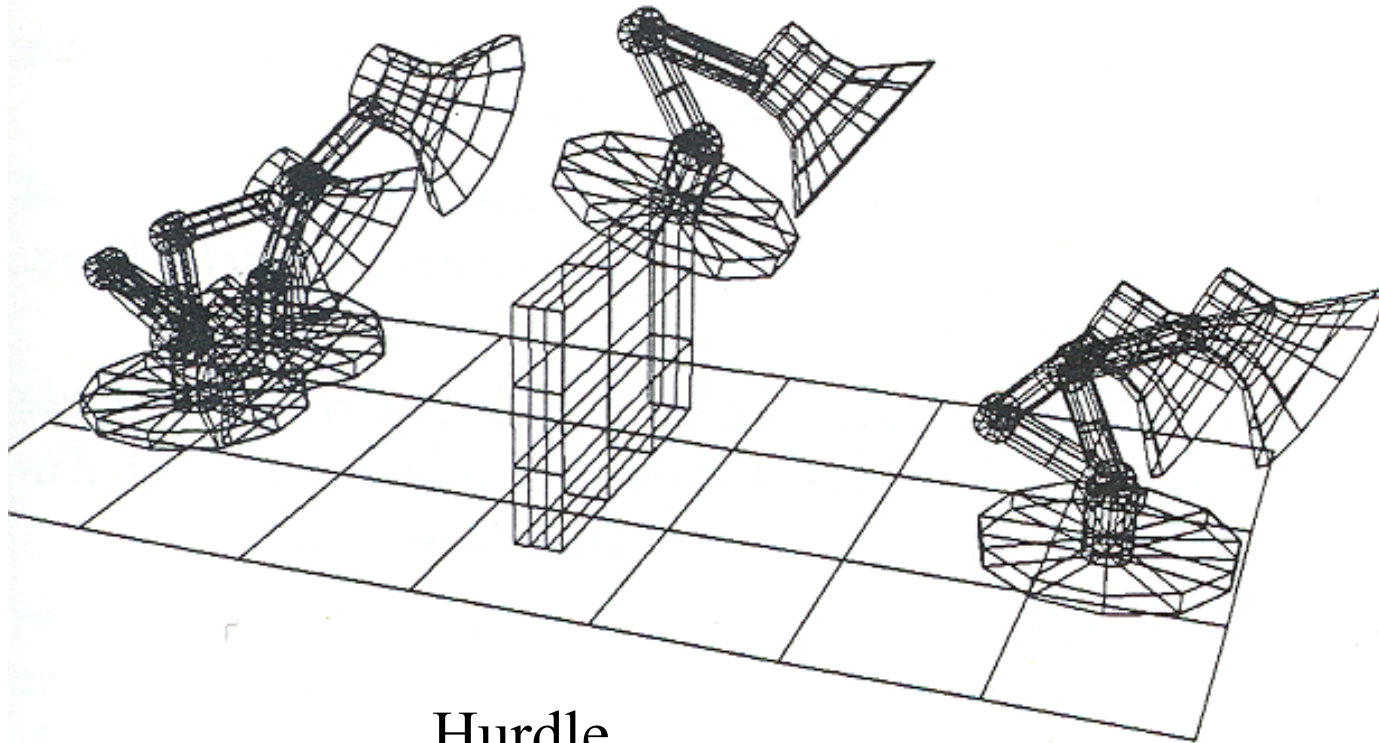
Heavier Base



# Spacetime Constraints



- Adapting motion:

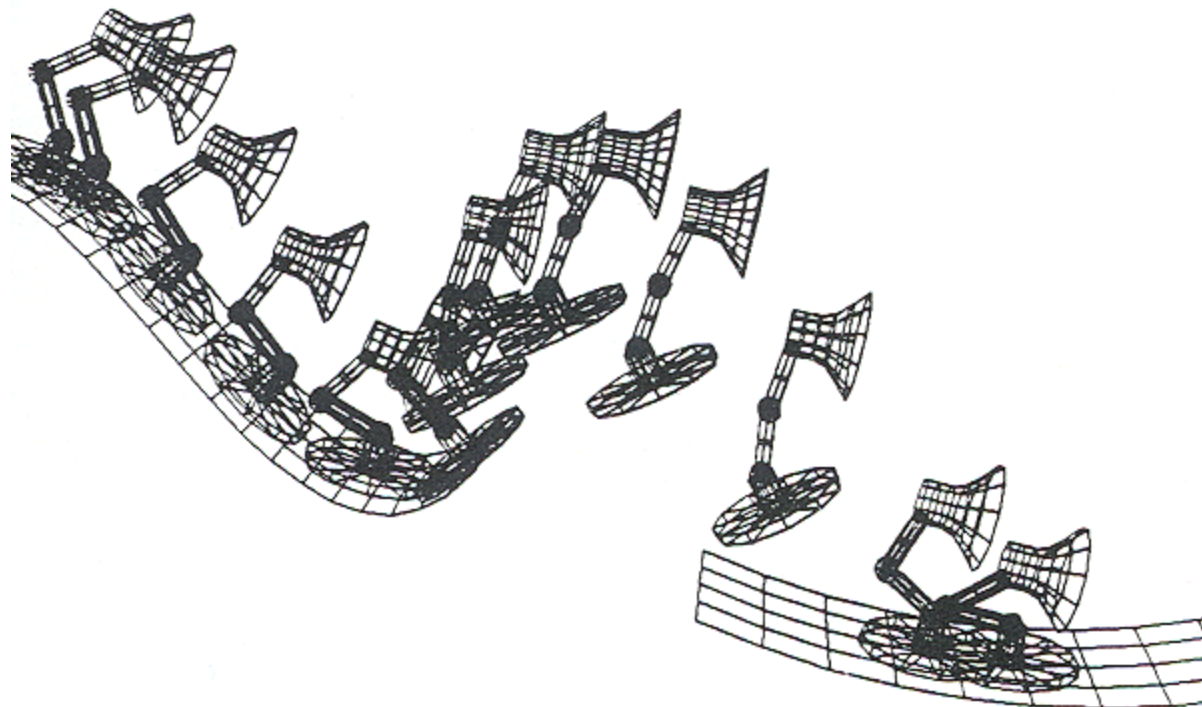


Hurdle

# Spacetime Constraints



- Adapting motion:



Ski Jump





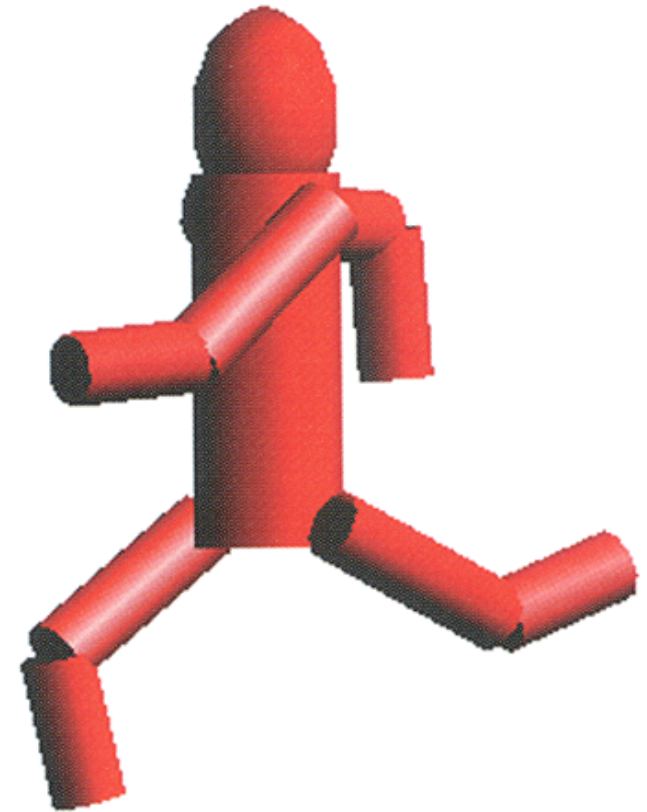
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# Character Animation Methods



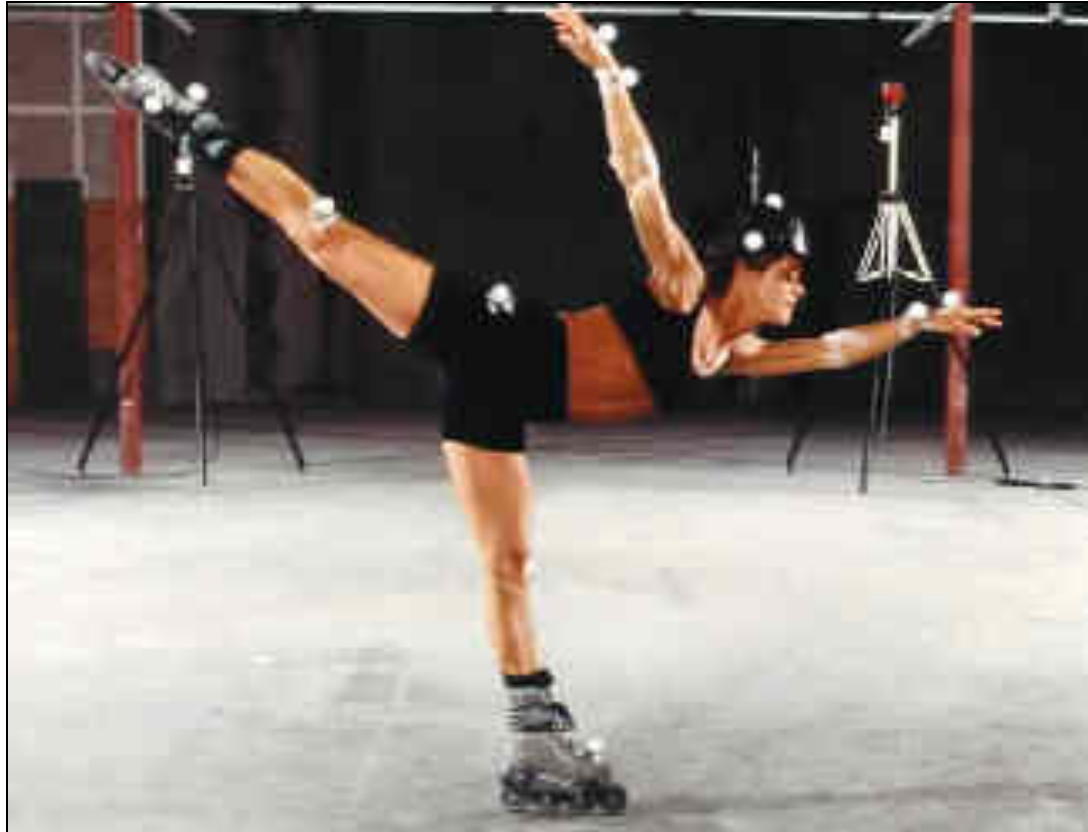
- Keyframing / Forward Kinematics
- Inverse Kinematics
- Dynamics
- Motion capture



# Motion Capture

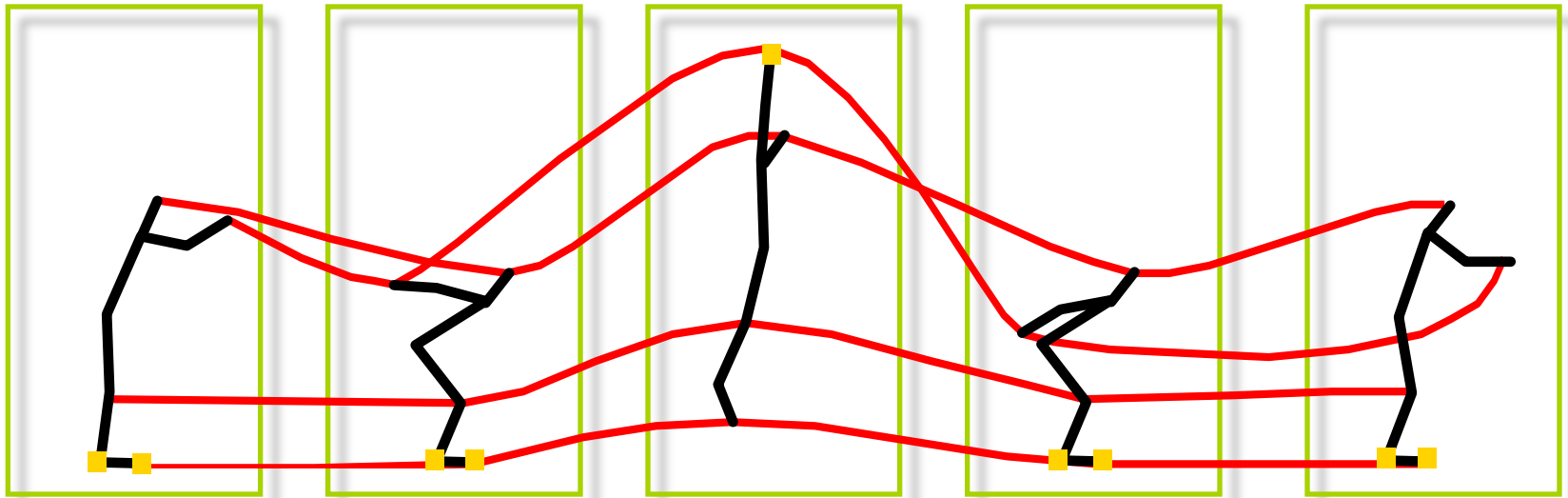


- Measure motion of real characters and then simply “play it back” with kinematics



# Motion Capture

- Measure motion of real characters and then simply “play it back” with kinematics



Captured Motion



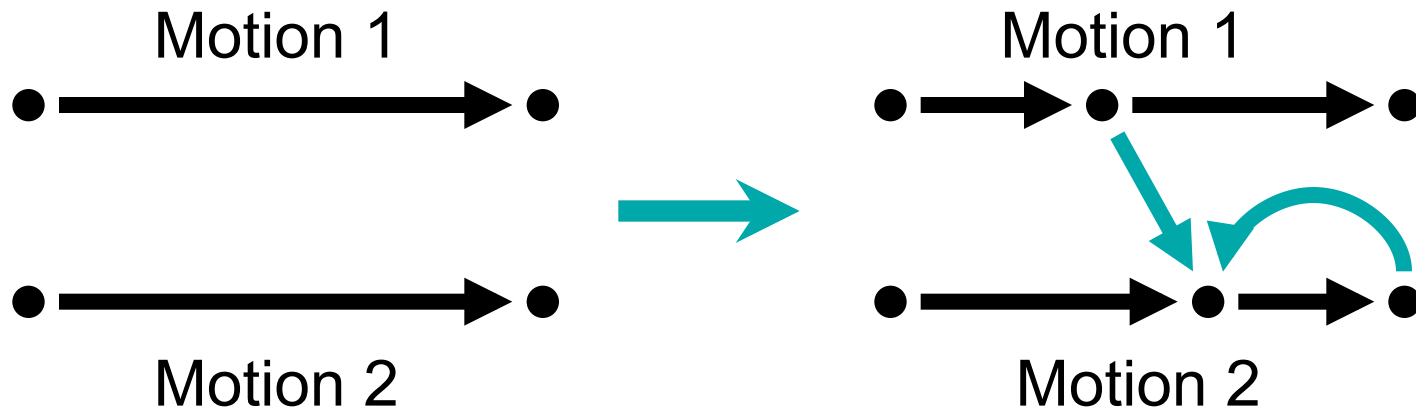
# Motion Capture

- Advantage:
  - Physical realism
- Challenge:
  - Animator control

# Motion Capture



- Motion graphs:

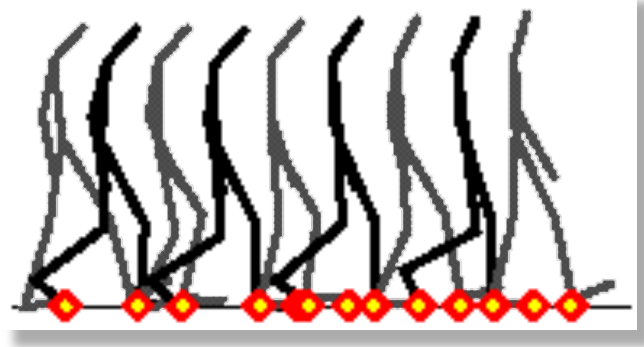


# Motion Capture



- Retargeting motion:

Original motion data + constraints:



New character:



New motion data:



# Beyond Skeletons...



- Motion blur
- Skinning



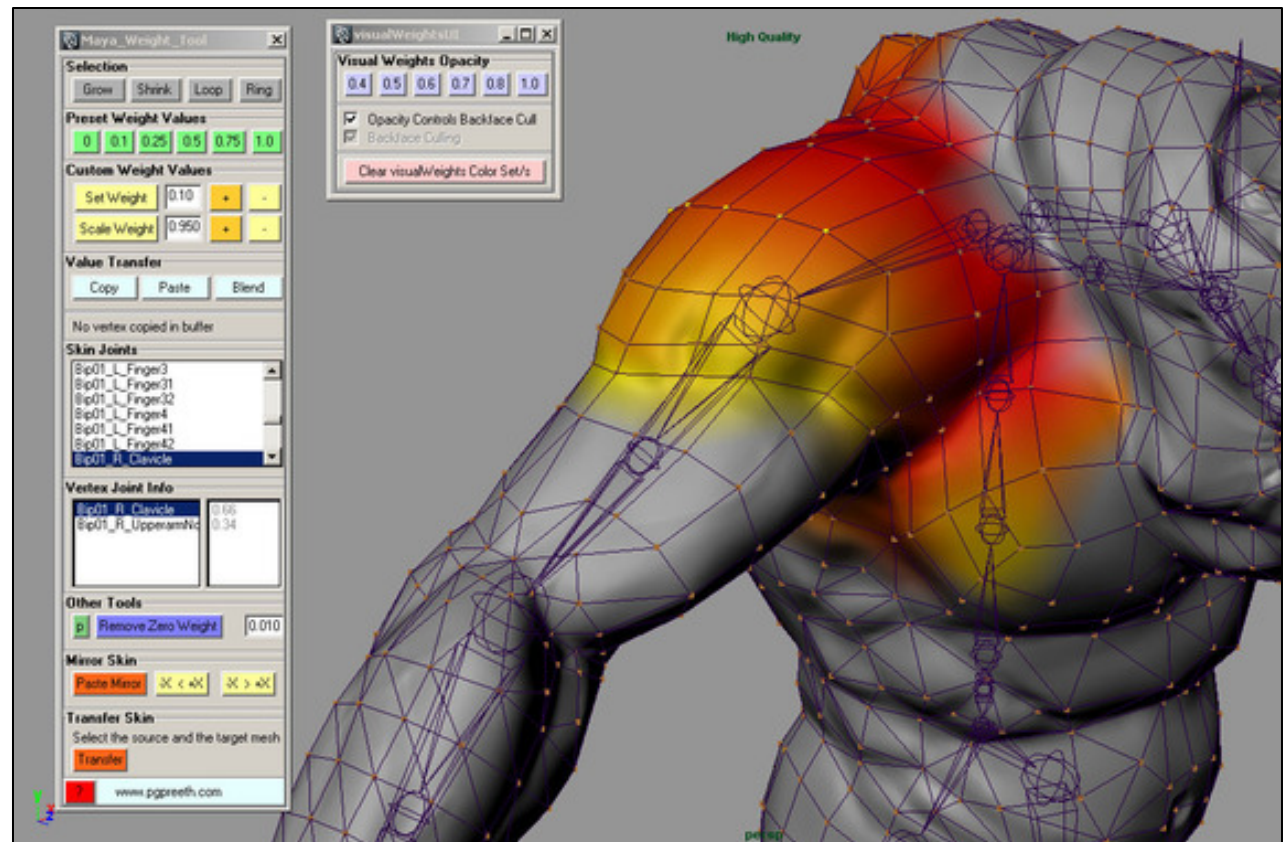
Simulate aperture open over interval.  
Average rendering during interval.



# Beyond Skeletons...

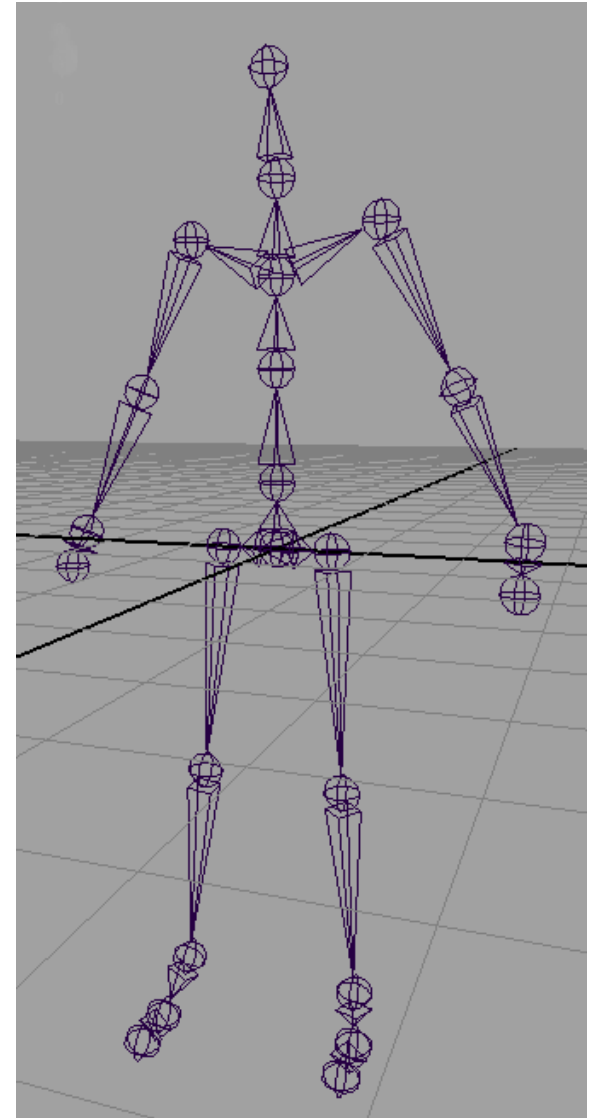


- Motion blur
- Skinning



# Kinematic Skeletons

- Hierarchy of transformations (“bones”)
  - Changes to parent affect all descendent bones
- So far: bones affect objects in scene or parts of a mesh
  - Equivalently, each point on a mesh acted upon by one bone
  - Leads to discontinuities when parts of mesh animated
- Extension: each point on a mesh acted upon by more than one bone





# Linear Blend Skinning

- Each vertex of skin potentially influenced by all bones
  - Normalized weight vector  $w^{(v)}$  gives influence of each bone transform
  - When bones move, influenced vertices also move
- Computing a transformation  $T_v$  for a skinned vertex
  - For each bone
    - » Compute global bone transformation  $T_b$  from transformation hierarchy
  - For each vertex
    - » Take a linear combination of bone transforms
    - » Apply transformation to vertex in original pose

$$T_v = \sum_{b \in B} w_b^{(v)} T_b$$

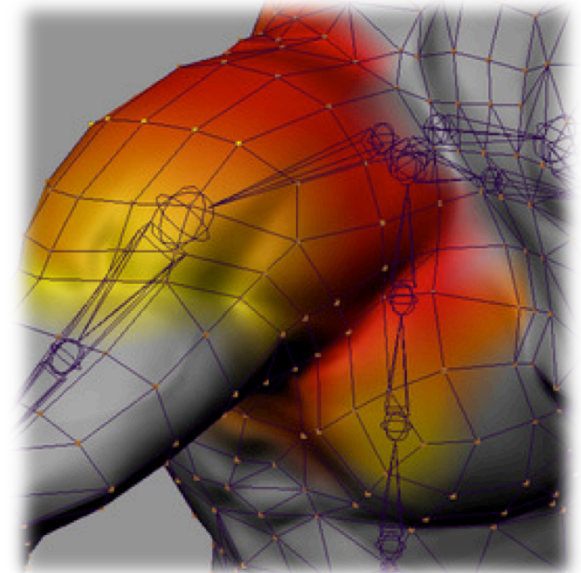
- Equivalently, transformed vertex position is weighted combination of positions transformed by bones

$$v_{transformed} = \sum_{b \in B} w_b^{(v)} (T_b v)$$

# Assigning Weights: “Rigging”



- Painted by hand
- Automatic: function of relative distances to nearest bones
  - Smoothness of skinned surface depends on smoothness of weights!



# Summary



- Kinematics
  - Animator specifies poses (joint angles or positions) at keyframes and computer determines motion by kinematics and interpolation
- Dynamics
  - Animator specifies physical attributes, constraints, and starting conditions and computer determines motion by physical simulation
- Motion capture
  - Computer captures motion of real character and provides tools for animator to edit it