## ISC 233 Warmup: Finite Language Class

Develop a class Language for processing finite formal languages, supporting union, concatenation, and *n*-closure.

**Definitions.** A *language* is a set of strings. A *set* is a collection of elements where no two elements are equal; we provide a class SET. java that enforces this property. The *union* of two languages is the set of all strings that are in either or both of the two languages. The *concatenation* of two languages is the set of all strings that can be formed by appending a string from the second language to a string from the first language. The *n-closure* of a language is the set of all strings that can be formed by concatenating *n* strings from the language. Here are some examples, using RE notation:

```
union: a \mid abc = \{ a, abc \}

concatenation: (b \mid bc \mid bcd) (cd \mid d) = \{ bccd, bcd, bcdcd, bcdd, dd \}

2-closure: (e \mid ef) \{2\} = \{ ee, eef, efe, efef \}
```

Your task. Make sure that you have downloaded the files Language.java and SET.java as per the online instructions. Language.java is a client of the SET data type, which takes care of maintaining sets of distinct elements (adding a string to a set of strings that is already contains that string has no effect, as desired). Add code to Language.java as indicated within the file to implement the concatenate() method and the closure() method. We have provided implementations of the constructors and the union() and toString() method to help you get started.

**Example.** Note that Language.java has a main() client to test your methods by printing out the strings in the languages a | abc, (b|bc|bcd)(cd|d) and (e|ef){2}. Your program must behave as follows (the strings on each line can be in any order):

```
% java-introcs Language
a abc
bccd bcd bcdcd bcdd bd
ee eef efe efef
```

Note that the string bcd appears only once in the second language, even though it can be formed either by concatenating b and cd or by concatenating bc and d.

**Restrictions.** Also as indicated within the file, you must use only a single instance variable language which is final. In other words, your Language class has to be *immutable*—the invoking Language object cannot change during a union, concatenate, or closure operation.

**Hint 1.** To implement these methods, you will need to use Java's for-each loop. See the provided toString() and union() methods for examples of using a for-each loop with SET<String>.

**Hint 2.** There are many methods in SET.java but the only ones you will need to use for this exam are: the constructor, the add() method, and for-each loops (see Hint 1).

Food for thought. Why not just use an array as the underlying data structure?