

COS 226 Data Structures and Algorithms
Computer Science Department
Princeton University
Spring 2016

Week 2 Activity

1. Sorting

(a) Sorting Analysis

- i. Write a recurrence relation that describes the complexity of selection sort.
(An example of a recurrence relation that describes binary search is $T(N) = T(N/2) + 1$)

- ii. Solve the recurrence relation of selection sort to show that selection sort is
 $\sim 1/2n^2$

(b) *Insertion Sort*

- i. Sort the word "ananda" using insertion sort.

- ii. Consider the assert statement (1) about the array segment $a[0..i]$ that is given at the end of the j loop in the sort below. Write another assert statement about the array before the beginning of the j loop.

```
public static void sort(Comparable[] a) {  
    int N = a.length;  
    for (int i = 1; i < N; i++) {  
  
        for (int j = i; j > 0 && less(a[j], a[j-1]); j--) {  
            exch(a, j, j-1);  
        }  
        assert isSorted(a, 0, i); ----- (1)  
    }  
    assert isSorted(a);  
}
```

- iii. Suppose that you have an array of length $2N$ consisting of N Bs followed by N As. Below is the array when $N = 10$.

B B B B B B B B A A A A A A A A A A

How many compares does it take to insertion sort (ascending order) the array as a function of N ? Use tilde notation to simplify your answer.

2. Iterators

- (a) Consider an example collection called Bag (different from Bag.java implementation of algs4). Refer to the code given in the appendix below. Complete ReverseIterator code so that a Bag Iterator will print elements backwards from the order they were added. (that is, from $a[n - 1] \dots a[0]$)

```
private class ReverseIterator implements Iterator<Item> {
    private _____; // next item to return

    public ReverseIterator() {
        _____
    }

    public boolean hasNext() { _____ }
    public void remove() { throw new UnsupportedOperationException(); }

    public _____ next() {
        if (!hasNext()) throw new NoSuchElementException();
        return _____;
    }
}
```

- (b) What is the output of the following code?

```
Bag<Integer> myBag = new Bag<Integer>();
myBag.add(3);
myBag.add(1);
myBag.add(2);
for (int i : myBag){
    for (int j : myBag) {
        StdOut.println(i + " " + j);
    }
    StdOut.println();
}
```

- (c) Rewrite the above code using explicit iterator methods hasNext and next.

3. Amortized Analysis (Bonus Question)

Suppose we have a resizing array implementation of a stack, that increases in size by 10 when the array is full, and decreases in size by 10 if the array has 20 or more empty spaces.

- (a) What is the best case cost of push and pop operations?
- (b) What is the worst case cost of push and pop operations?
- (c) What is the amortized cost of push and pop operations?
- (d) Give a sequence of push and pop operations that can result in worst case performance.
- (e) Is there any advantage to using increments by 10 instead of doubling.

1 Appendix

```
*****
 * Name: Andy Guna
 * NetID: guna
 * Precept: P99
 *
 * Partner Name: N/A
 * Partner NetID: N/A
 * Partner Precept: N/A
 *
 * Operating system:
 * Compiler:
 * Text editor / IDE:
 *
 * Hours to complete assignment (optional):
 *
 * A program that demonstrate the use of Iterators and generics. The Bag class (different from algs4)
 * implements Iterable. Also the Bag class is a generic class <Item>. The <Item> is
 * Initialized by the client Main (in this program as <int>. There are two
 * Iterator nested classes are provided, MyIterator and RandomIterator.
 * You can try to run the code with each one and see what happens.
 *
 * To run < java Bag N
 * (where N is the Bag size - you provide that)
 *
 ****
import java.util.Iterator;
import java.util.NoSuchElementException;

import edu.princeton.cs.algs4.StdOut;
import edu.princeton.cs.algs4.StdRandom;

// A different implementation of a Bag different from algs4 Bags implementation

public class Bag<Item> implements Iterable<Item> {

    private Item[] a;           // array of Items
    private int N;              // max number of elements in the bag
    private int size;           // actual number of elements in the bag

    public Bag(int N) {
        // need cast because Java does not support generic array creation
        a = (Item[]) new Object[N];
        this.N = N;
        this.size = 0;
    }

    public boolean isEmpty() { return size == 0; }
    public int size()          { return size; }
    public int capacity()      { return N; }

    // resize the underlying array holding the elements
    private void resize(int max) {
        Item[] temp = (Item[]) new Object[max];
        for (int i = 0; i < N; i++)
            temp[i] = a[i];
        a = temp;
        this.N = max;
    }
}
```

```

// insert an item
public void add(Item item) {
    if (item == null) throw new NullPointerException();
    if (size == a.length) resize(2*a.length); // double size of array if necessary
    a[size++] = item; // add element
}

// removes a random item
public Item remove() {
    if (isEmpty())
        throw new NoSuchElementException("bag is underflow");
    Item value = a[--size];
    return value;
}

public Iterator<Item> iterator() { return new ReverseIterator(); }

private class ReverseIterator implements Iterator<Item> {

    private ; // next item to return

    public ReverseIterator() {

    }

    public boolean hasNext() { }

    public void remove() { throw new UnsupportedOperationException(); }

    public Item next() {

    }
}

// a test client
public static void main(String[] args) {
    int N = Integer.parseInt(args[0]);
    Bag<Integer> MyBag = new Bag<Integer>(N);

    // add N integers
    for (int i = 0; i < N; i++) {
        MyBag.add(new Integer(i));
    }
    //iteration

    for (int i : MyBag){
        for (int j : MyBag) {
            StdOut.println(i + " " + j);
        }
        StdOut.println();
    }
}
}

```