

# Cryptography

COS 461: Computer Networks  
Princeton University

# Overview

- Network security and definitions
- Brief introduction to cryptography
  - Cryptographic hash functions
  - Symmetric-key crypto
  - Public-key crypto
  - Hybrid crypto

# Internet's Design: Insecure

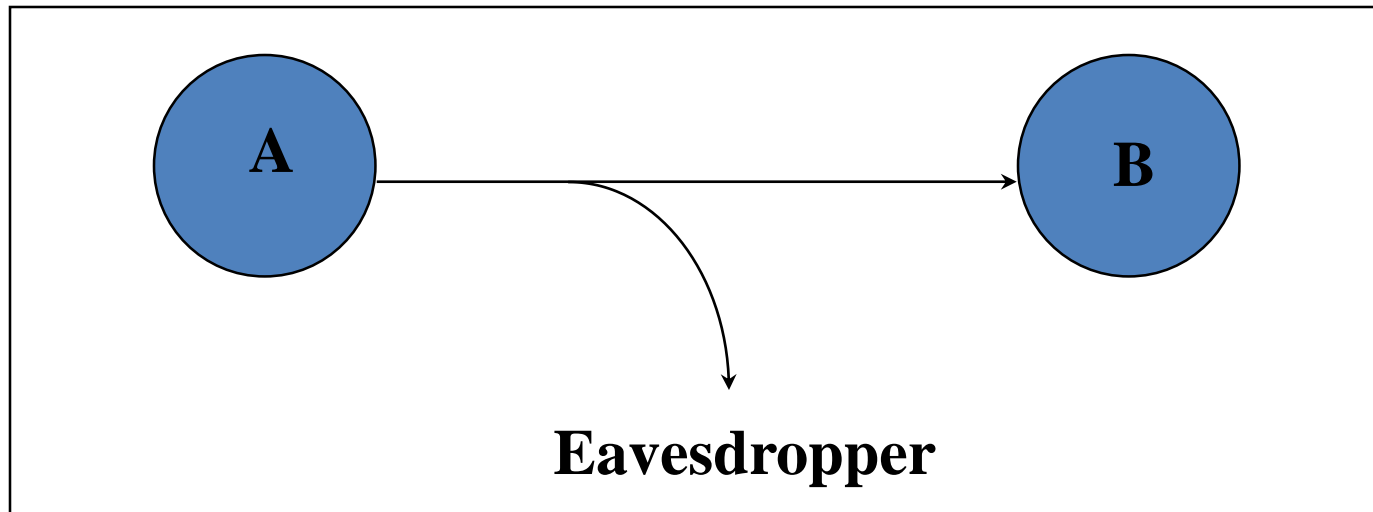
- Designed for simplicity
- “On by default” design
- Readily available zombie machines
- Attacks look like normal traffic
- Internet's federated operation obstructs cooperation for diagnosis/mitigation

# Basic Concepts

- **Confidentiality:** Concealment of information or resources
- **Authenticity:** Identification and assurance of origin of info
- **Integrity:** Trustworthiness of data or resources in terms of preventing improper and unauthorized changes
- **Availability:** Ability to use desired info or resource
- **Non-repudiation:** Offer of evidence that a party indeed is sender or a receiver of certain information
- **Access control:** Facilities to determine and enforce who is allowed access to what resources (host, software, network, ...)

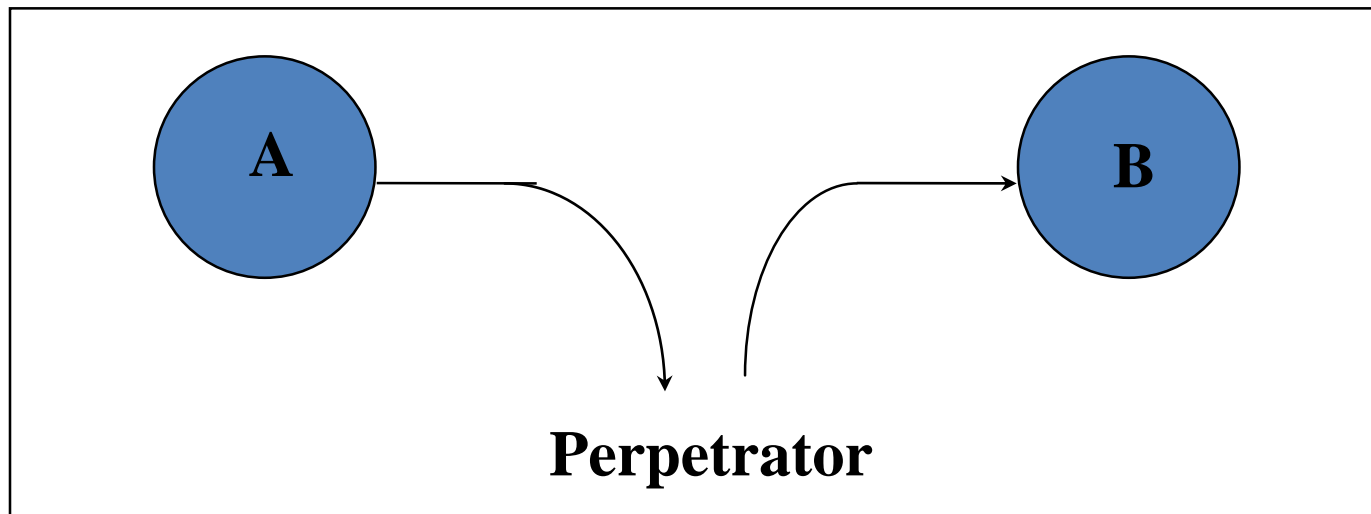
# Eavesdropping - Message Interception (Attack on Confidentiality)

- Unauthorized access to information
- Packet sniffers and wiretappers (e.g. tcpdump)
- Illicit copying of files and programs



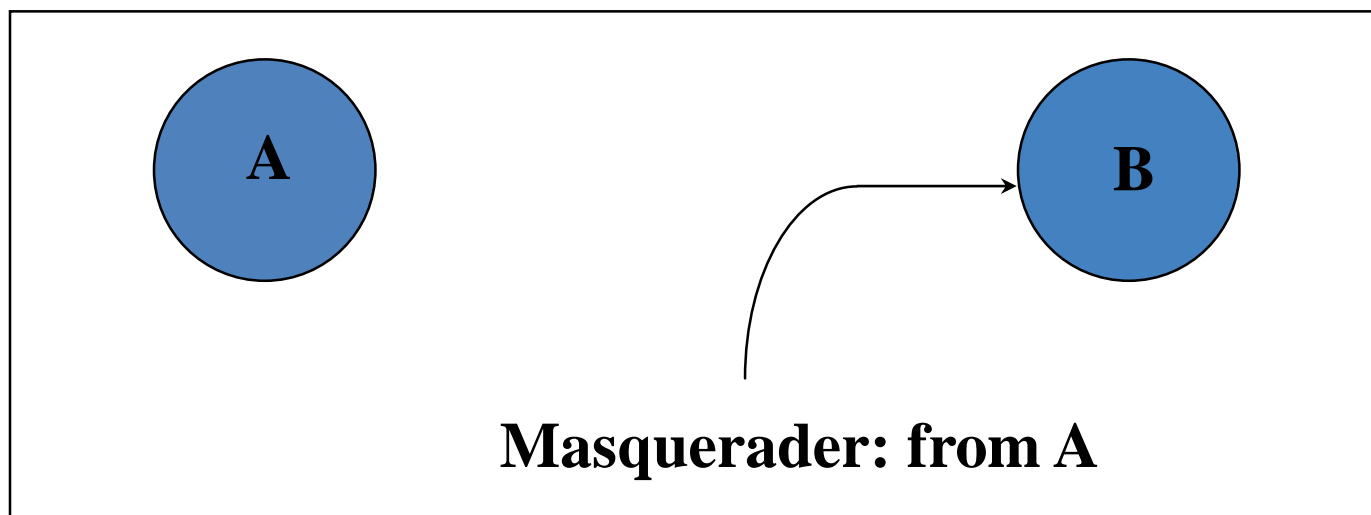
# Integrity Attack - Tampering

- Stop the flow of the message
- Delay and optionally modify the message
- Release the message again



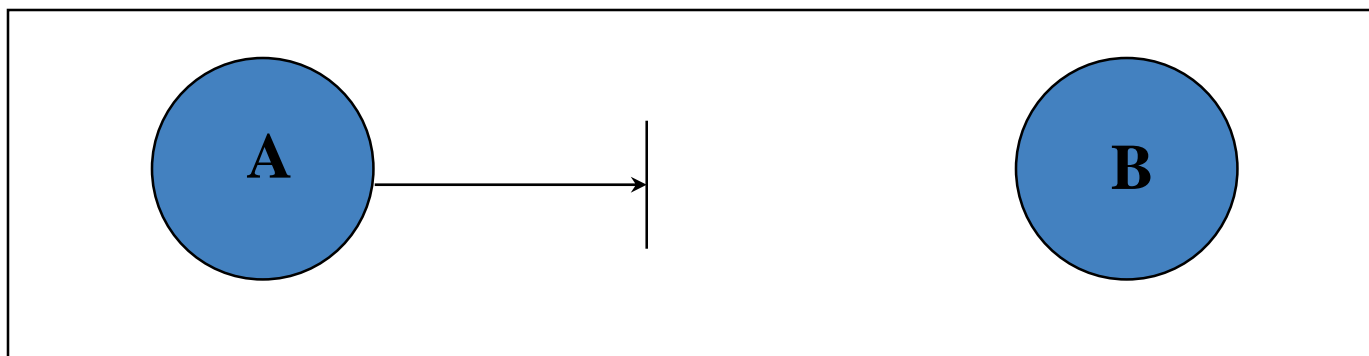
# Authenticity Attack - Fabrication

- Unauthorized assumption of other's identity
- Generate and distribute objects under identity



# Attack on Availability

- Destroy hardware (cutting fiber) or software
- Modify software in a subtle way
- Corrupt packets in transit



- **Blatant *denial of service* (DoS):**
  - Crashing the server
  - Overwhelm the server (use up its resource)



# Introduction to Cryptography

# What is Cryptography?

- Comes from Greek meaning “secret writing”
  - Primitives also can provide integrity, authentication
- Cryptographers invent secret codes to attempt to hide messages from unauthorized observers



- Modern encryption:
  - *Algorithm* public, *key* secret and provides security
  - May be symmetric (secret) or asymmetric (public)

# Cryptographic Algorithms: Goal

- **One-way functions: cryptographic hash**
  - Easy to compute hash
  - Hard to invert
- **“Trapdoor” functions: encryption/signatures**
  - Given ciphertext alone, hard to compute plaintext (invert)
  - Given ciphertext and key (the “trapdoor”), relatively easy to compute plaintext
  - “Level” of security often based on “length” of key

# Cryptographic hash functions

# Cryptography Hash Functions

- Take message,  $m$ , of arbitrary length and produces a smaller (short) number,  $h(m)$
- One-way function
  - Easy to compute  $h(m)$
  - Hard to find an  $m$ , given  $h(m)$
  - Often assumed: output of hash fn's “looks” random
- Collision resistance:
  - Strong: Find any  $m \neq m'$  such that  $h(m) == h(m')$
  - Weak: Given  $m$ , find  $m'$  such that  $h(m) == h(m')$
  - For 160-bit hash (SHA-1)
    - Strong collision are birthday paradox:  $2^{\{160/2\}} = 2^{80}$
    - Weak collision requires  $2^{160}$

# Example use #1: Passwords

- Can't store passwords in a file that could be read
  - Concerned with insider attacks!
- Must compare typed passwords to stored passwords
  - Does `hash (typed) == hash (password)` ?
- Actually, a “salt” is often used: `hash (input || salt)`

# Example use #2: Self-certifying naming

- File-sharing software (LimeWire, BitTorrent)
  - File named by  $F_{\text{name}} = \text{hash}(\text{data})$
  - Participants verify that  $\text{hash}(\text{downloaded}) == F_{\text{name}}$ 
    - If check fails, reject data
    - To successfully “forge” data’, must find weak collision
- Recursively applied...
  - BitTorrent file has many chunks
  - Control file downloaded from tracker includes:
    - forall chunks,  $F_{\text{chunk name}} = \text{hash}(\text{chunk})$
  - BitTorrent client verifies each individual chunk

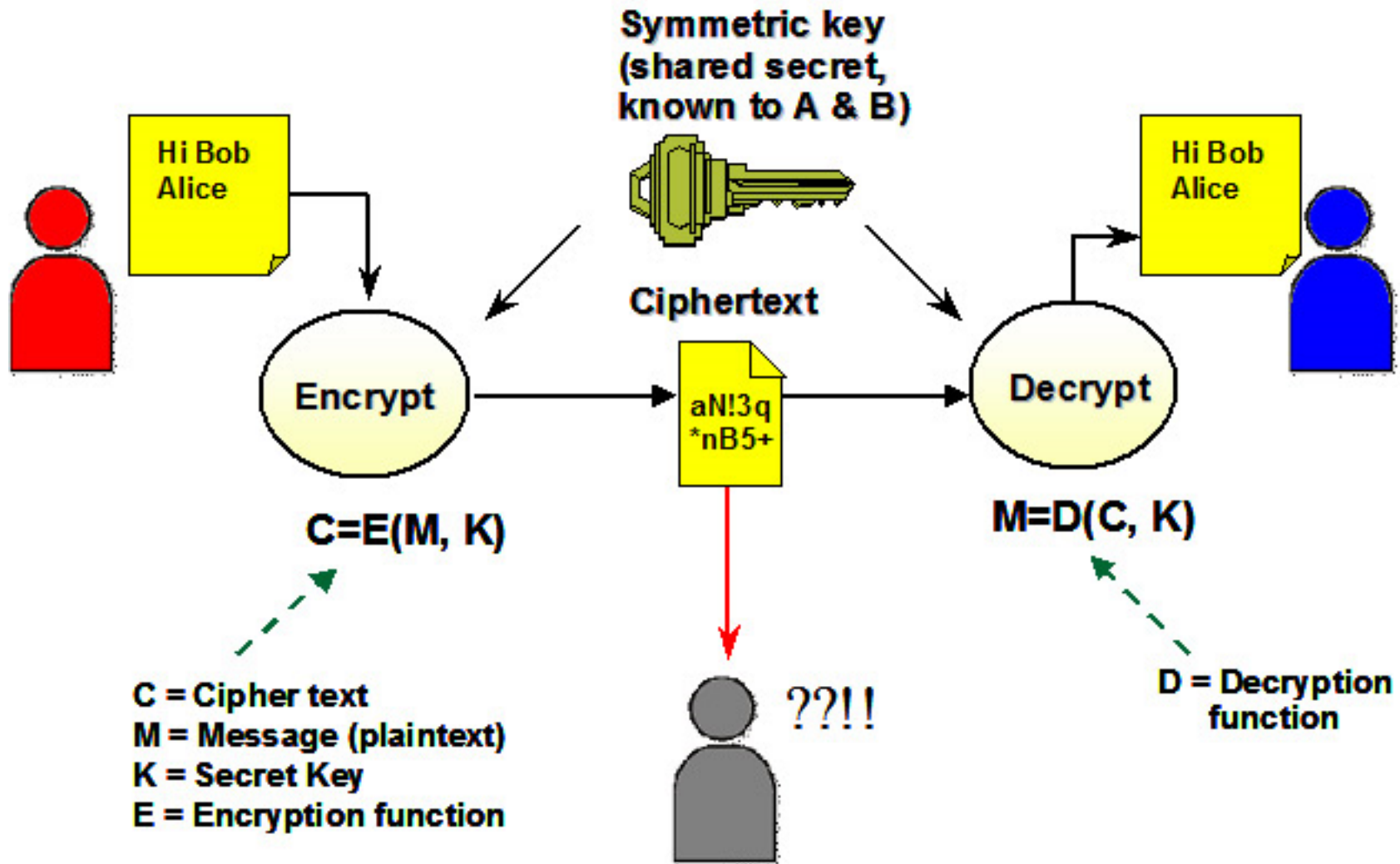
# Symmetric (Secret) Key Cryptography



# Symmetric Encryption

- Also: “conventional / private-key / single-key”
  - Sender and recipient share a common key
  - All classical encryption algorithms are private-key
  - Dual use: confidentiality or authentication/integrity
    - Encryption vs. msg authentication code (MAC)
- Was only type of encryption prior to invention of public-key in 1970' s
  - Most widely used
  - (Much) more computationally efficient than “public key”

# Symmetric Cipher Model



# Distribution of Symmetric Keys

- Manual delivery is challenging...
- The number of keys grows quadratically with the number of endpoints  $(n*(n-1)/2)$ 
  - Further complexity for application/user level encryption
- Key distribution center (KDC) a good alternative
  - Only  $n$  master keys required
  - KDC generate session key for Alice and Bob

# Public-Key Cryptography

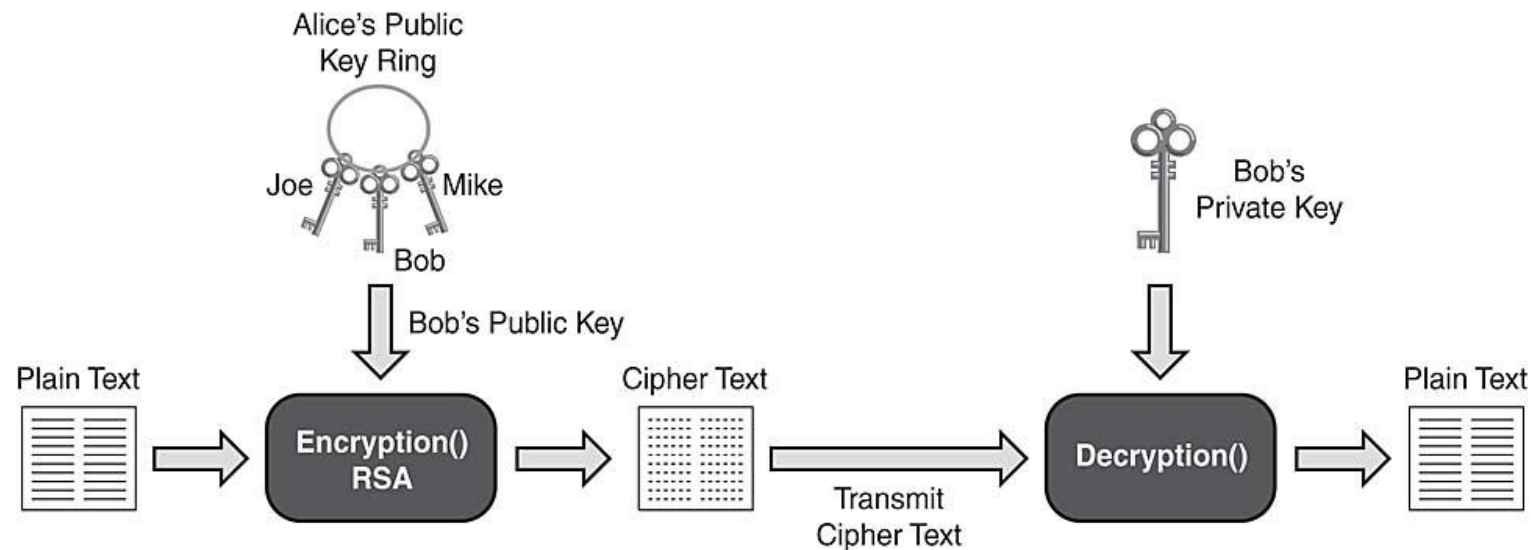
# Why Public-Key Cryptography?

- Developed to address two key issues:
  - Key distribution: Secure communication w/o having to trust a key distribution center with your key
  - Digital signatures: Verify msg comes intact from claimed sender (w/o prior establishment)
- Public invention due to Whitfield Diffie & Martin Hellman in 1976
  - Known earlier in classified community

# Public-Key Cryptography

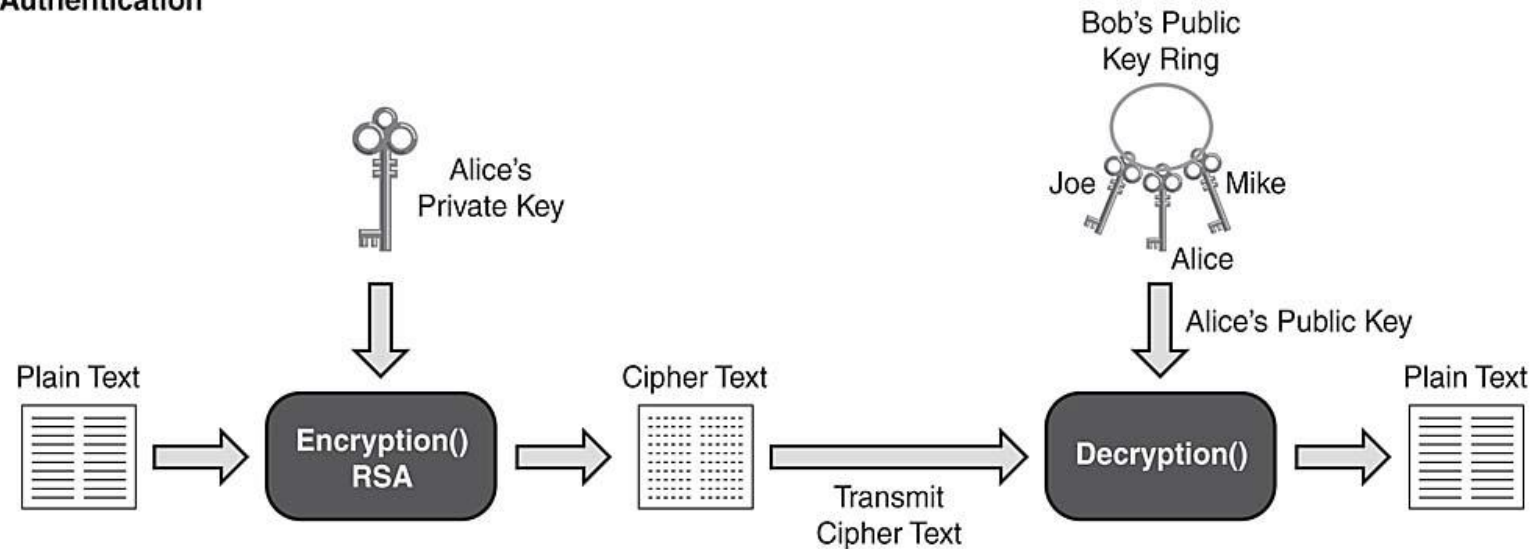
- **Public-key:** Known by anybody, and can be used to encrypt messages and verify signatures
- **Private-key:** Known only to recipient, used to decrypt messages and sign (create) signatures
- Can encrypt messages or verify signatures w/o ability to decrypt messages or create signatures

# Public-Key Cryptography



**Encryption**

**Authentication**



# Security of Public Key Schemes

- Public-key encryption is a “trap-door” function:
  - Easy to compute  $c \leftarrow F(m, k_p)$
  - Hard to compute  $m \leftarrow F^{-1}(c)$  without knowing  $k_s$
  - Easy to compute  $m \leftarrow F^{-1}(c, k_s)$  by knowing  $k_s$
- Like private key schemes, brute force search possible
  - But keys used are too large (e.g.,  $\geq 2048$  bits)
  - Hence is slow compared to private key schemes



# (Simple) RSA Algorithm

- **Security** due to cost of factoring large numbers
  - Factorization takes  $O(e^{\log n \log \log n})$  operations (hard)
  - Exponentiation takes  $O((\log n)^3)$  operations (easy)
- **To encrypt a message  $M$  the sender:**
  - Obtain public key  $\{e, n\}$ ; compute  $C = M^e \bmod n$
- **To decrypt the ciphertext  $C$  the owner:**
  - Use private key  $\{d, n\}$ ; computes  $M = C^d \bmod n$
- **Note that msg  $M$  must be smaller than the modulus  $n$** 
  - Otherwise, hybrid encryption:
    - Generate random symmetric key  $r$
    - Use public key encryption to encrypt  $r$
    - Use symmetric key encryption under  $r$  to encrypt  $M$

# Symmetric vs. Asymmetric

- **Symmetric Pros and Cons**
  - Simple and really very fast (order of 1000 to 10000 faster than asymmetric mechanisms)
  - **Must agree/distribute the key beforehand**
  - AES/CBC (256-bit) → 80 MB / s
  - *(for 2048 bits, that's .003 ms)*
- **Public Key Pros and Cons**
  - Easier predistribution for public keys
    - Public Key Infrastructure (in textbook)
  - **Much slower**
  - 2048-RSA → 6.1ms Decrypt, 0.16ms Encrypt