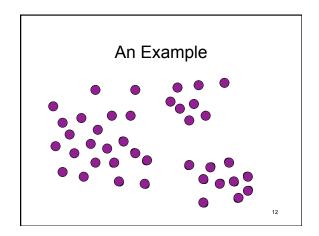
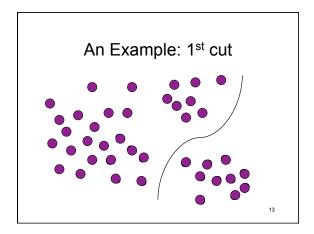
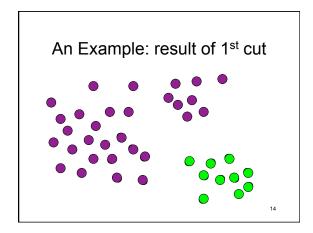


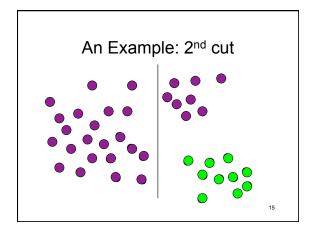


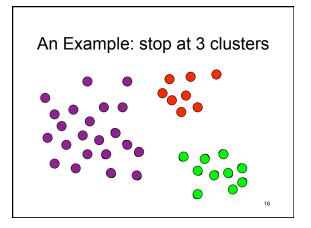
• not necessary to use a cut-based measure

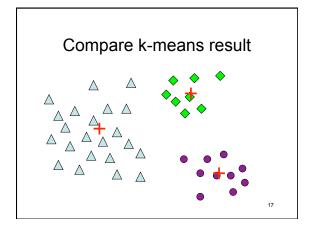


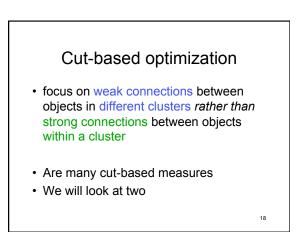


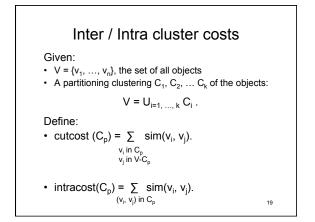


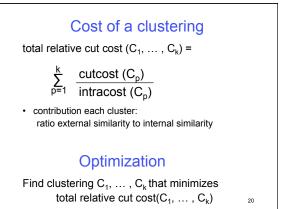


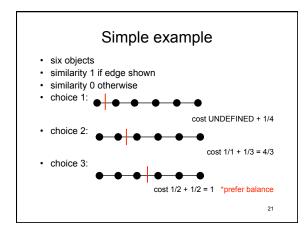


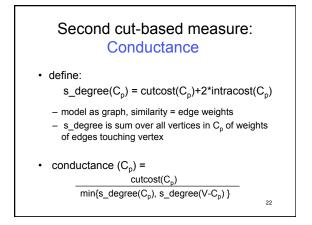


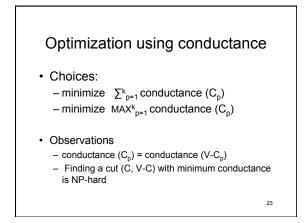


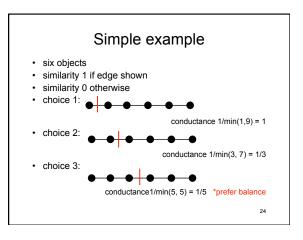








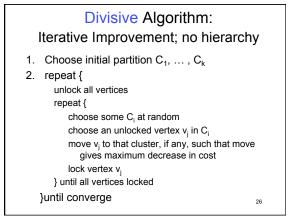




# Hierarchical divisive revisited

- can use one of cut-based algorithms to split a cluster
- · how choose cluster to split next?
  - if building entire tree, doesn't matter
  - if stopping a certain point, choose next cluster based on measure optimizing
    - e.g. for total relative cut cost, choose  $C_i$  with largest  $cutcost(C_i)$  /  $intracost(C_i)$

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### Observations on algorithm

- heuristic
- · uses randomness
- convergence usually improvement < some chosen threshold between outer loop iterations
- vertex "locking" insures that all vertices are examined before examining any vertex twice
- there are many variations of algorithm
- can use at each division of hierarchical divisive algorithm with k=2
  - more computation than an agglomerative merge

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### Compare to k-means

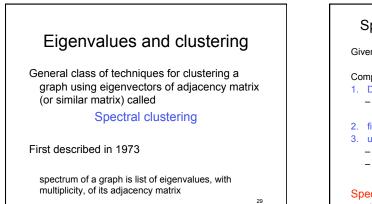
#### · Similarities:

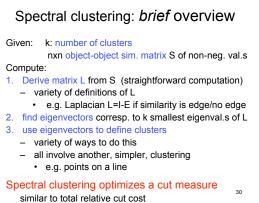
- number of clusters, k, is chosen in advance
- an initial clustering is chosen (possibly at random)
- iterative improvement is used to improve clustering

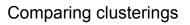
#### · Important difference:

- divisive algorithm can minimize a cut-based cost
  total relative cut cost, conductance use external
  - and internal measures
- k-means maximizes only similarity within a cluster
  ignores cost of cuts

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#### · Define external measure to

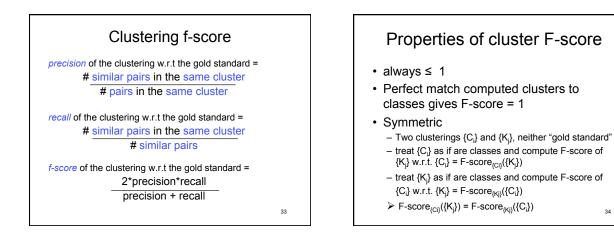
- comparing two clusterings as to similarity
- if one clustering "correct", one clustering by an algorithm, measures how well algorithm doing · refer to "correct" clusters as classes
  - "gold standard"
  - · refer to computed clusters as clusters
- · External measure independent of cost function optimized by algorithm

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### One measure: motivated by F-score in IR

#### Given:

- a set of classes  $S_1, \dots S_k$  of the objects use to define relevance
- a computed clustering  $C_1, \ldots C_k$  of the objects use to define retrieval
- · Consider pairs of objects
  - pair in same class, call *similar pair* ≡ relevant
  - pair in different classes ≡ irrelevant
  - pair in same clusters ≡ retrieved
  - pair in different clusters ≡ not retrieved
- · Use to define precision and recall



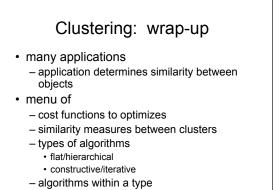
## another related external measure Rand index

( # similar pairs in the same cluster + # dissimilar pairs in the different clusters )

N (N-1)/2

percentage pairs that are correct

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