



# Image Processing

COS 426, Spring 2014  
Tom Funkhouser

# Image Processing



Goal: read an image, process it, write the result



input.jpg



output.jpg

```
imgproc input.jpg output.jpg -histogram_equalization
```

# Image Processing Operations



- Luminance
  - Brightness
  - Contrast.
  - Gamma
  - Histogram equalization
- Color
  - Black & white
  - Saturation
  - White balance
- Linear filtering
  - Blur & sharpen
  - Edge detect
  - Convolution
- Non-linear filtering
  - Median
  - Bilateral filter
- Dithering
  - Quantization
  - Ordered dither
  - Floyd-Steinberg



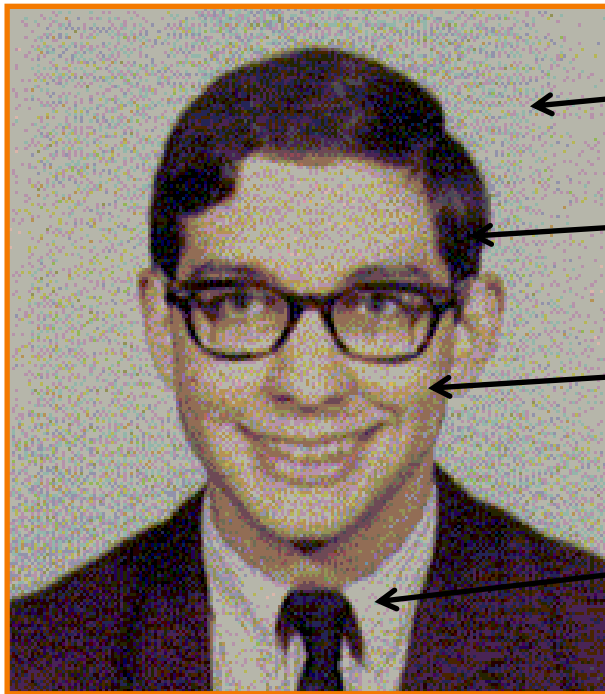
# Image Processing Operations

- **Luminance**
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# What is Luminance?

Measures perceived “gray-level” of pixel

$$L = 0.30 * \text{red} + 0.59 * \text{green} + 0.11 * \text{blue}$$



← 0.5

← 0.0

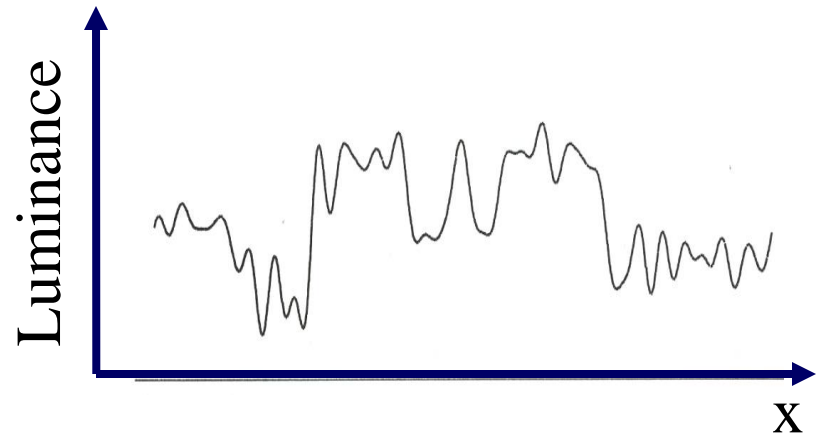
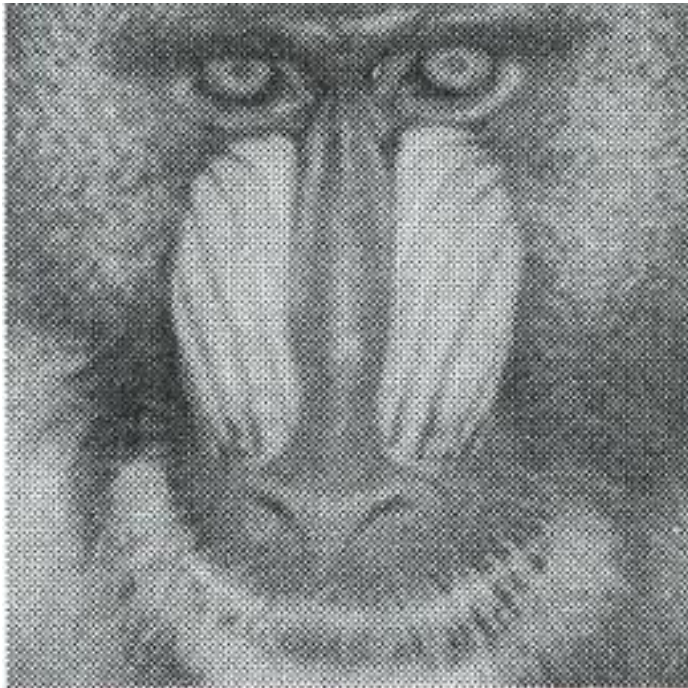
← 0.7

← 0.9

# Luminance



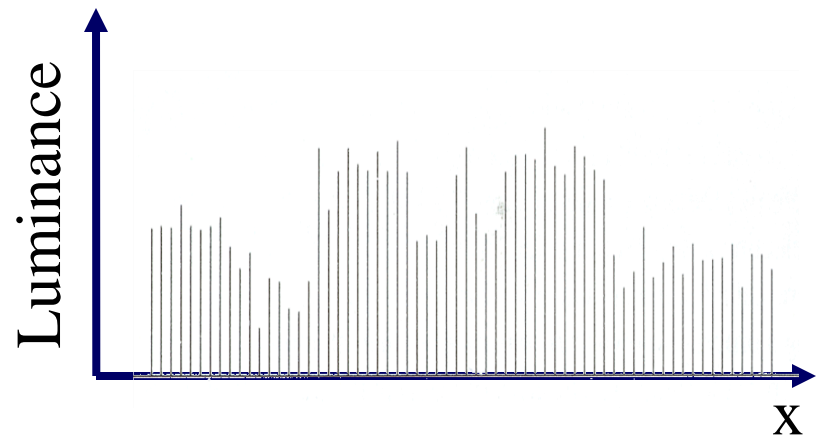
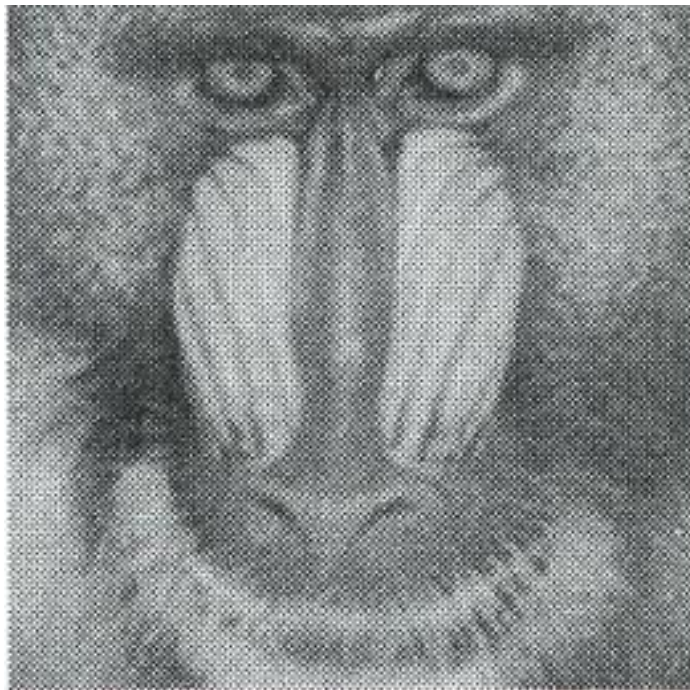
Measures perceived “gray-level” of pixel



Values of luminance for positions  
on one horizontal scanline

# Luminance

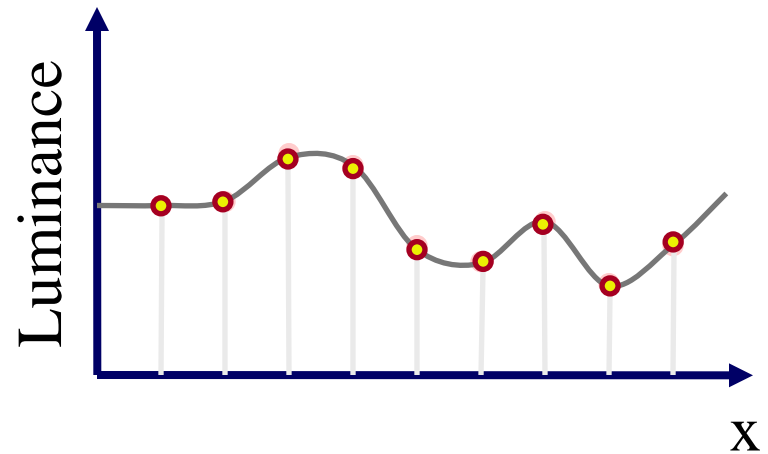
Measures perceived “gray-level” of pixel



Samples of luminance for pixels  
on one horizontal scanline

# Adjusting Brightness

- What must be done to the RGB values to make this image brighter?





# Adjusting Brightness

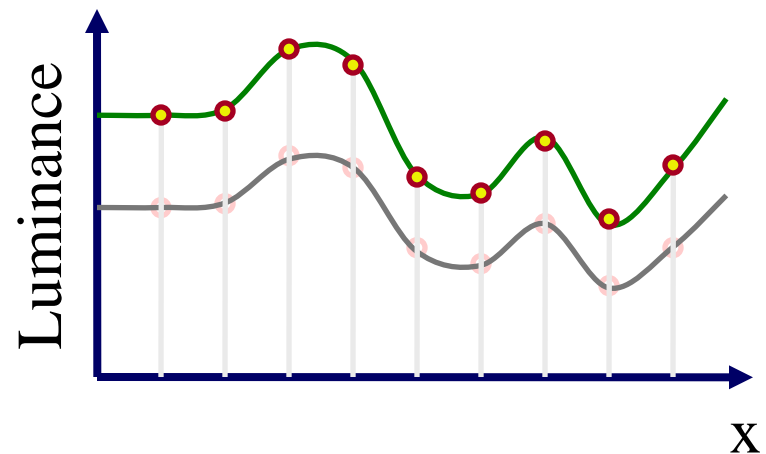
- Method 1: Convert to HSV, scale V, convert back
- Method 2: Scale R, G, and B directly
  - Multiply each of red, green, and blue by a factor
  - Must clamp to  $[0..1]$  ... always



Original



Brighter



# Adjusting Contrast

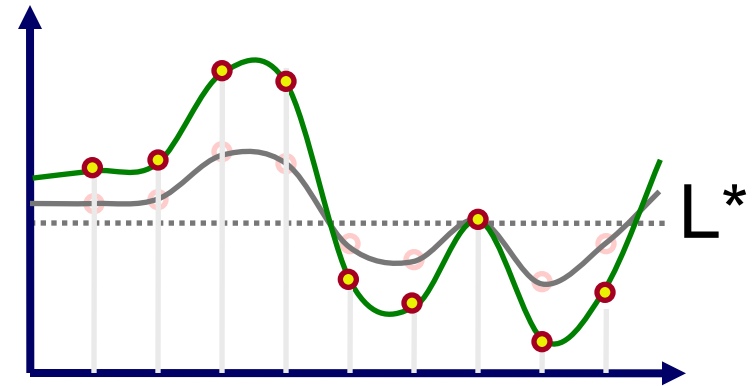
- Compute one mean luminance  $L^*$  for whole image  
Scale deviation from  $L^*$  for each pixel component



Original



More Contrast

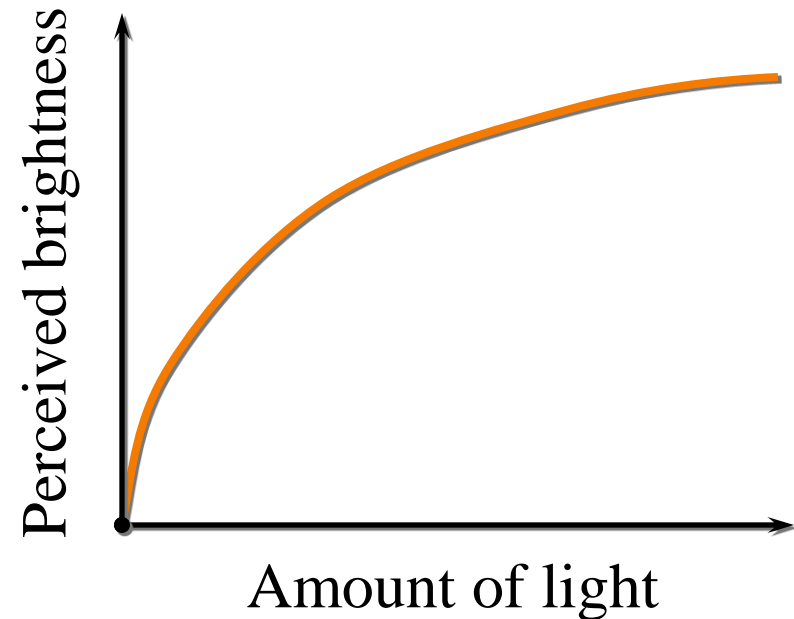


# Adjusting Gamma



Apply non-linear function to account for difference between brightness and perceived brightness of display

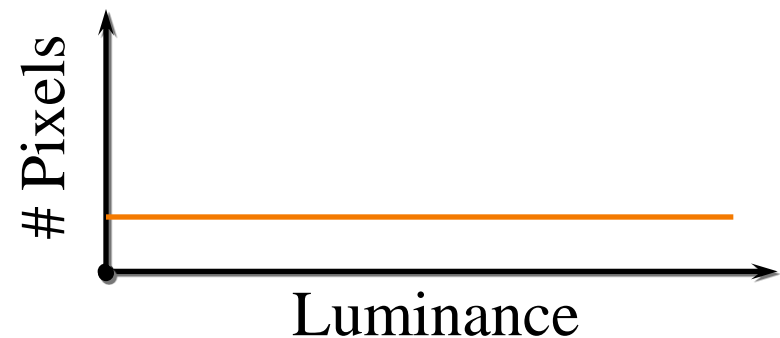
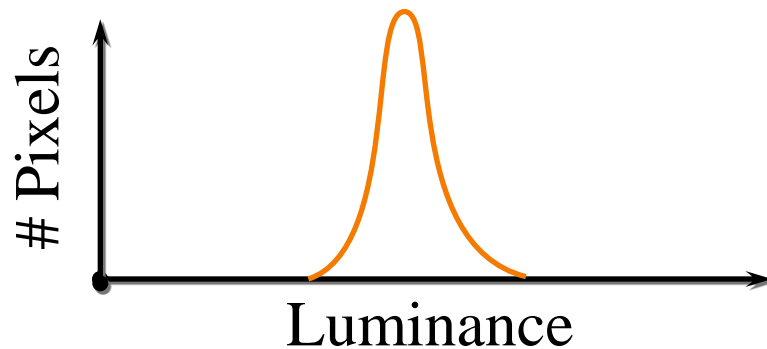
$$I_{\text{out}} = I_{\text{in}}^{\gamma}$$



$\gamma$  depends on camera and monitor

# Histogram Equalization

Change distribution of luminance values to cover full range [0-1]



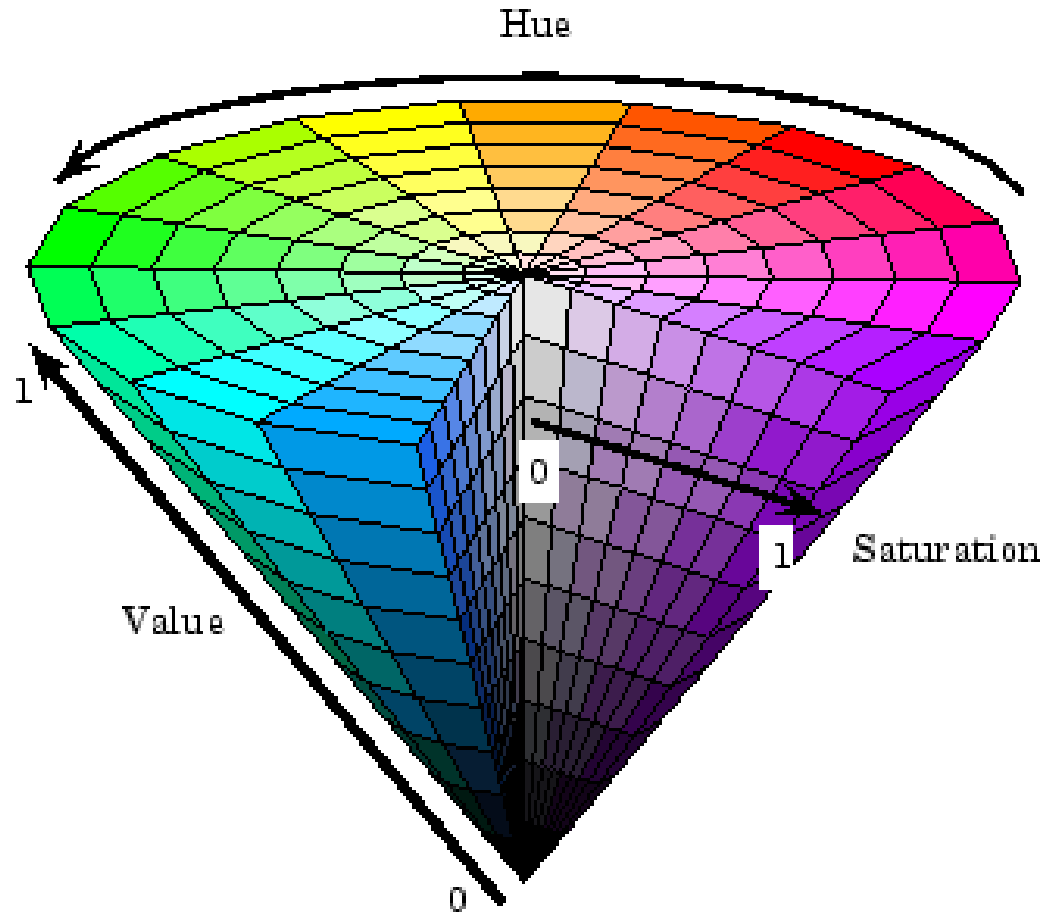


# Image Processing Operations

- Luminance
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  - Gamma
  - Histogram equalization
- Color
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  - Floyd-Steinberg

# Color processing

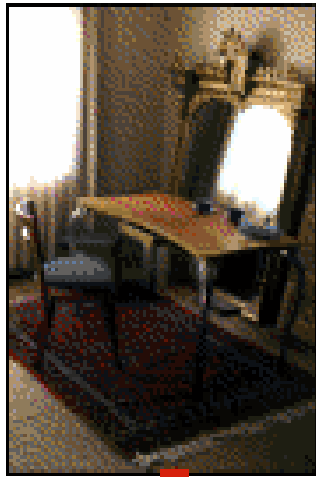
- Color models
  - RGB
  - CMY
  - HSV
  - XYZ
  - $La^*b^*$
  - Etc.



HSV Color Model

# Black & White

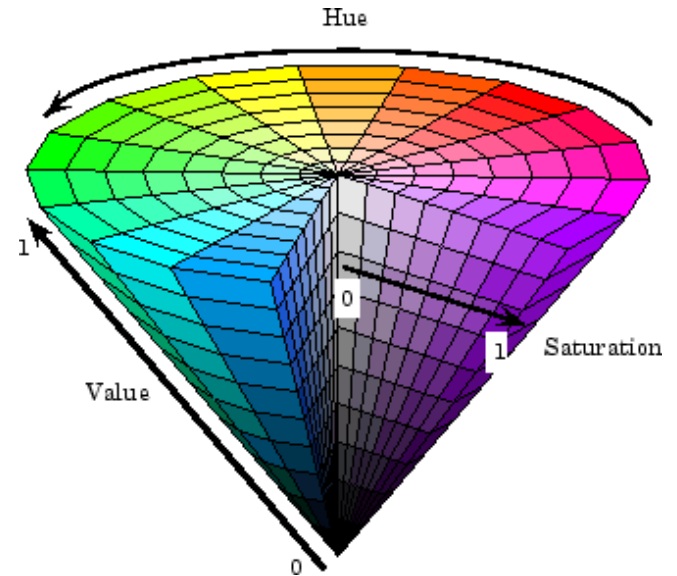
Convert from color to gray-levels



Original

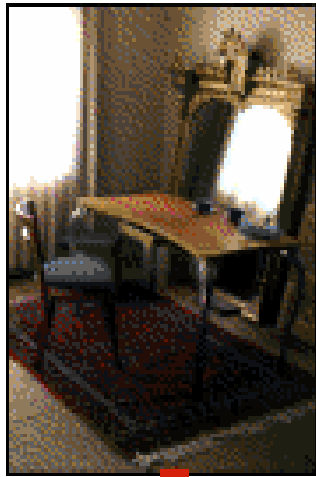


Black & White  
(actually gray levels)



# Black & White

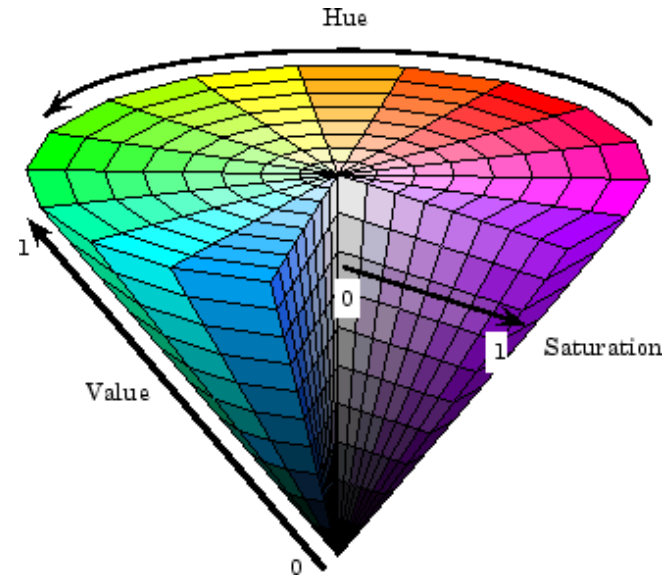
Convert from color to gray-levels



Original



Black & White  
(actually gray levels)



Method 1: Convert to HSV, set  $S=0$ , convert back to RGB

Method 2: Set RGB of every pixel to  $(L,L,L)$



# Adjusting Saturation



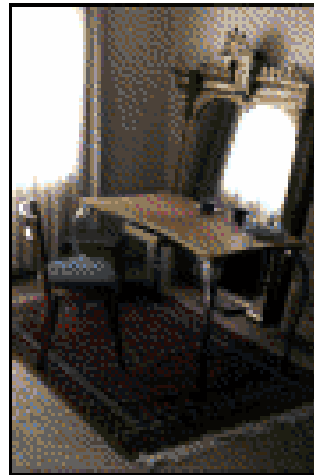
Increase/decrease color saturation of every pixel



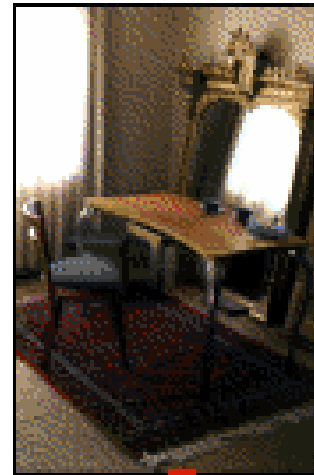
-1.0



0.0



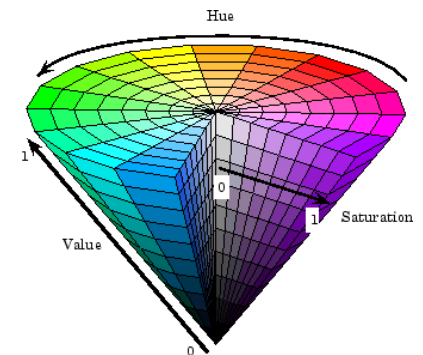
0.5



1.0



2.5



# Adjusting Saturation



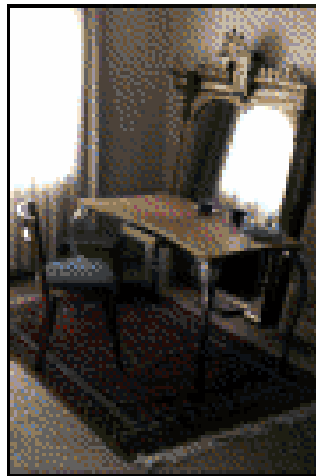
Increase/decrease color saturation of every pixel



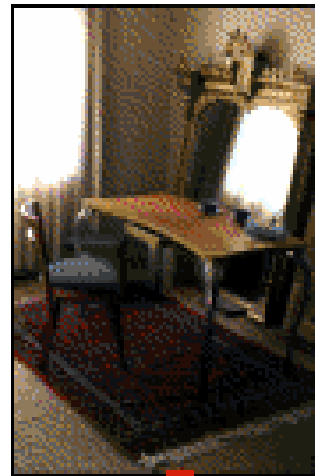
-1.0



0.0



0.5



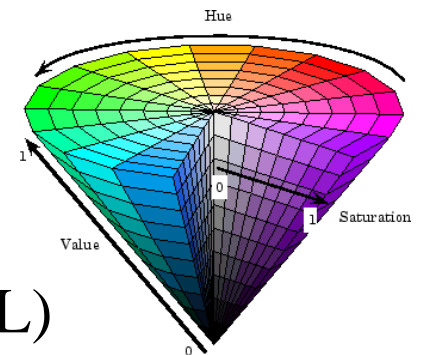
1.0



2.5

Method 1: Convert to HSV, scale S, convert back

Method 2: Set each pixel to factor \* (R-L, G-L, B-L)



# White Balance



Adjust colors so that a given RGB value is mapped to a neutral color

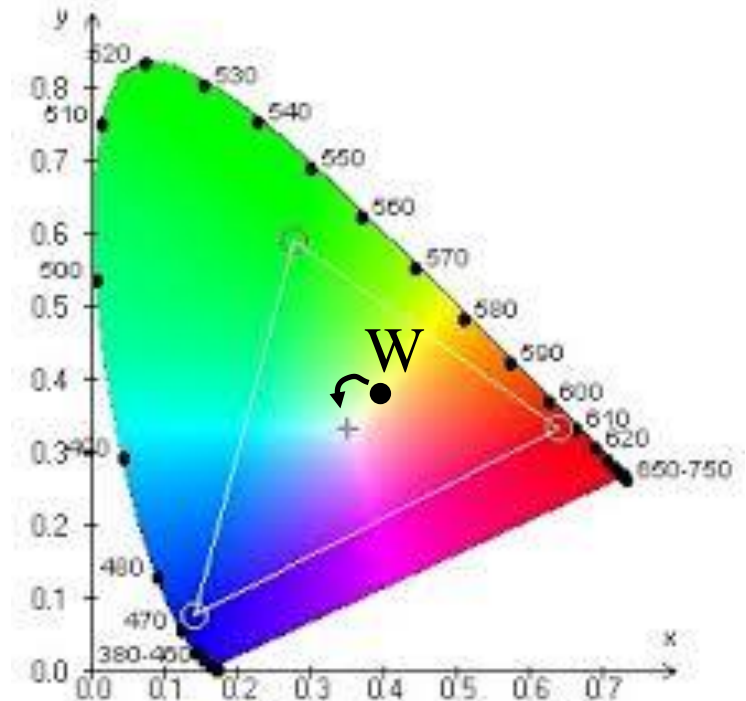


# White Balance



Conceptually:

Provide an RGB value  $W$  that should be mapped to white  
Perform transformation of color space

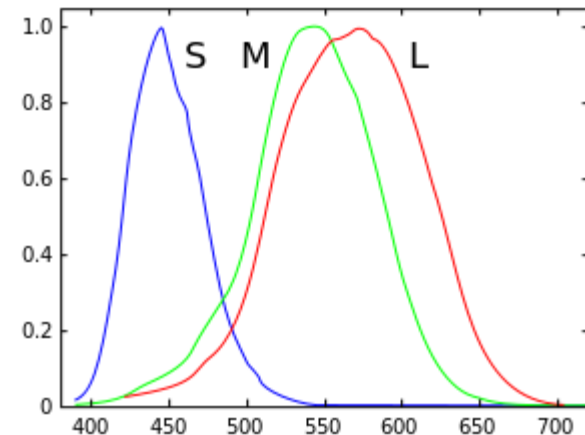
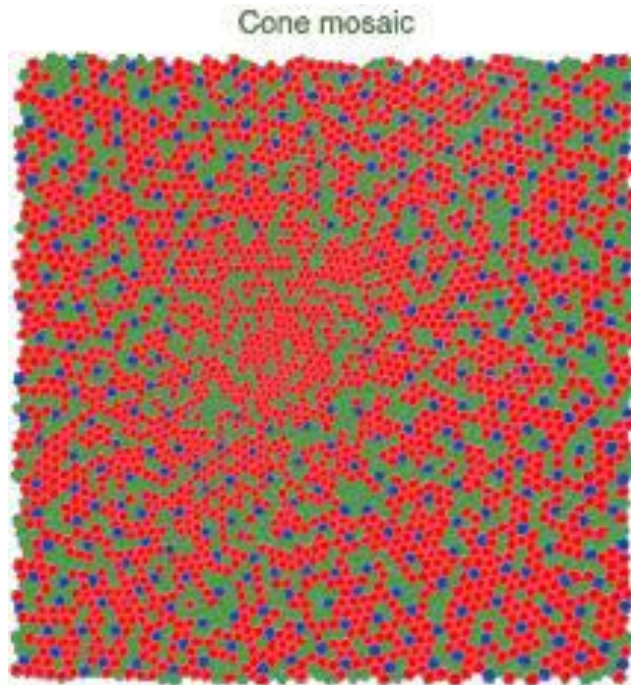


# White Balance



Von Kries method: adjust colors in LMS color space

- LMS primaries represent the responses of the three different types of cones in our eyes





# White Balance

For each pixel RGB:

1) Convert to XYZ color space

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 0.4124 & 0.3576 & 0.1805 \\ 0.2126 & 0.7152 & 0.0722 \\ 0.0193 & 0.1192 & 0.9502 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

2) Convert to LMS color space

$$\begin{bmatrix} L \\ M \\ S \end{bmatrix} = \begin{bmatrix} 0.40024 & 0.7076 & -0.08081 \\ -0.2263 & 1.16532 & 0.0457 \\ 0 & 0 & 0.91822 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$

3) Divide by  $L_w M_w S_w$

4) Convert back to RGB

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# Blur



What is the basic operation for each pixel when blurring an image?



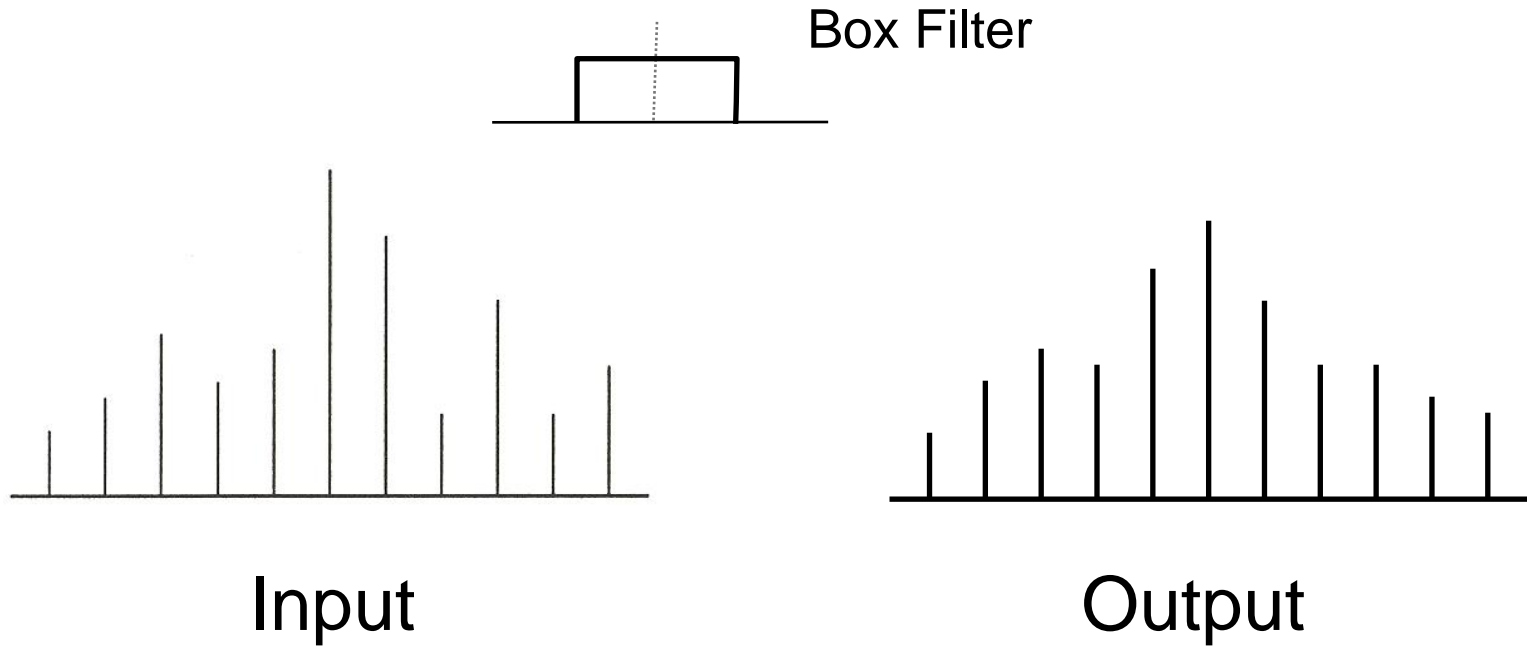




# Basic Operation: Convolution

Output value is weighted sum of values in neighborhood of input image

- Pattern of weights is the “filter” or “kernel”

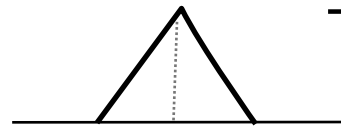




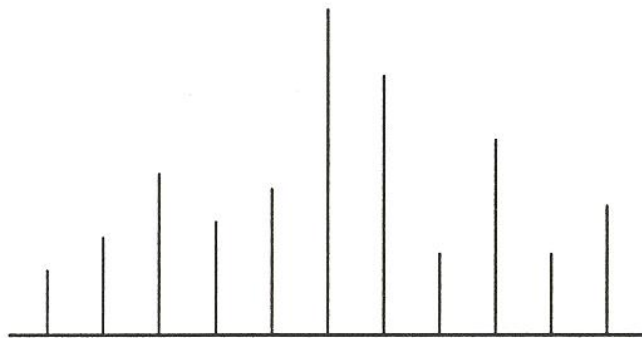
# Basic Operation: Convolution

Output value is weighted sum of values in neighborhood of input image

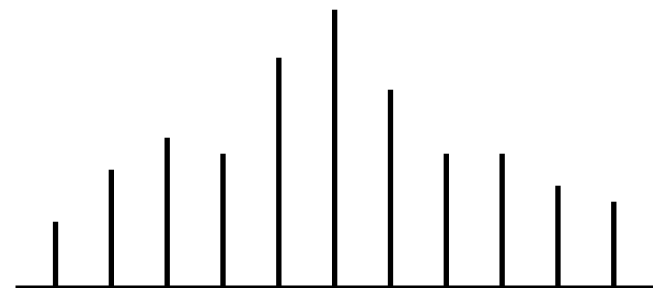
- Pattern of weights is the “filter” or “kernel”



Triangle Filter



Input



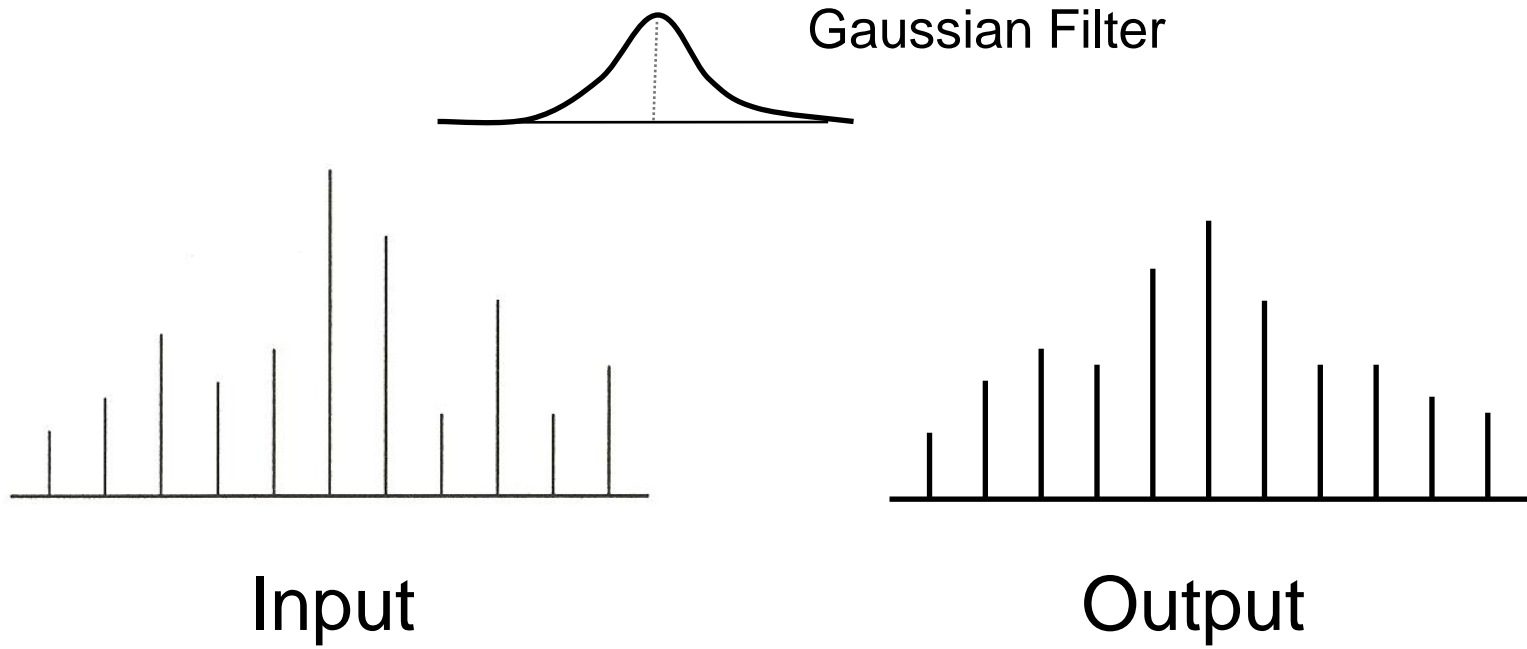
Output



# Basic Operation: Convolution

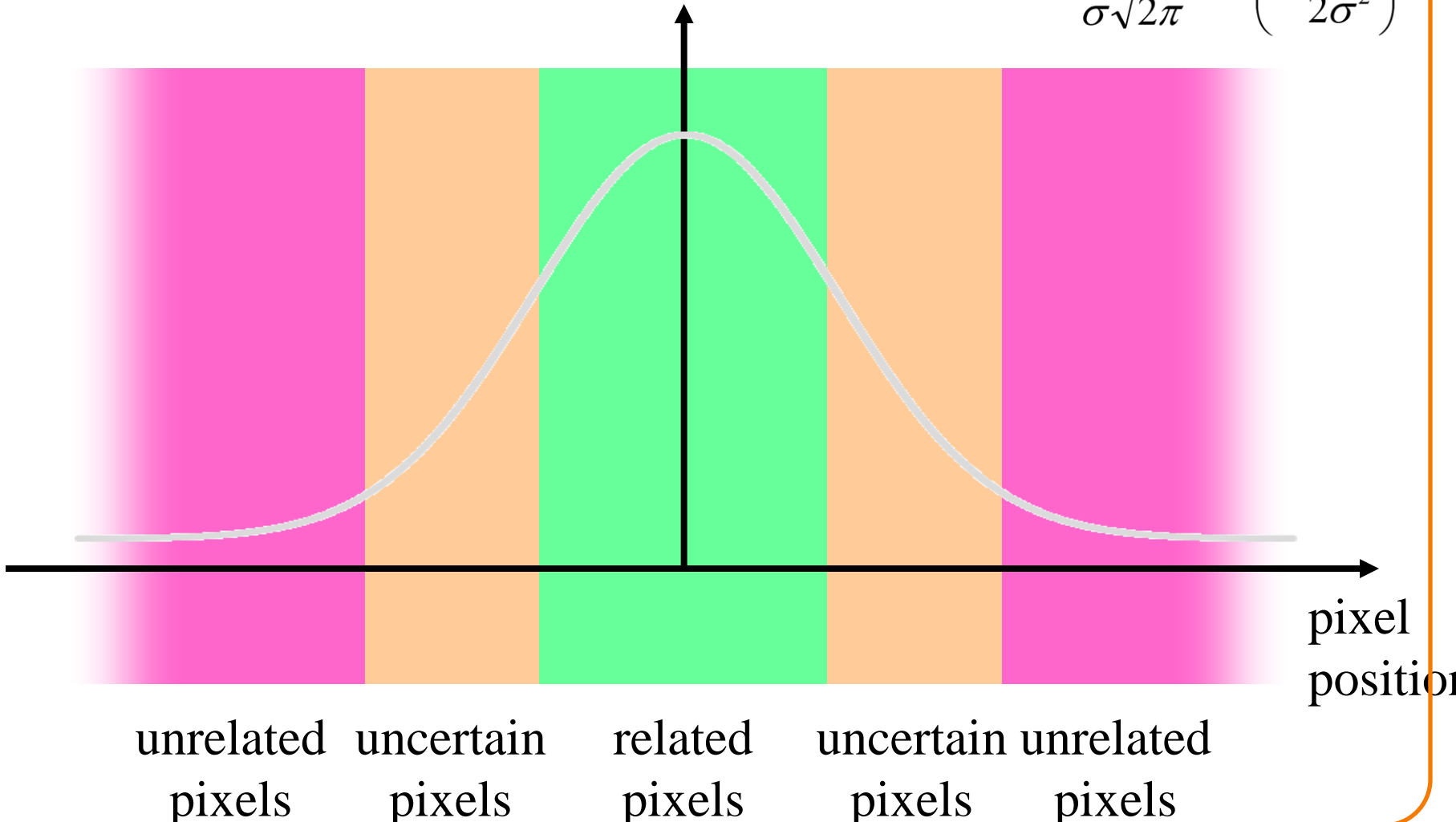
Output value is weighted sum of values in neighborhood of input image

- Pattern of weights is the “filter” or “kernel”



# Convolution with a Gaussian Filter

$$G(x, \sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{x^2}{2\sigma^2}\right)$$

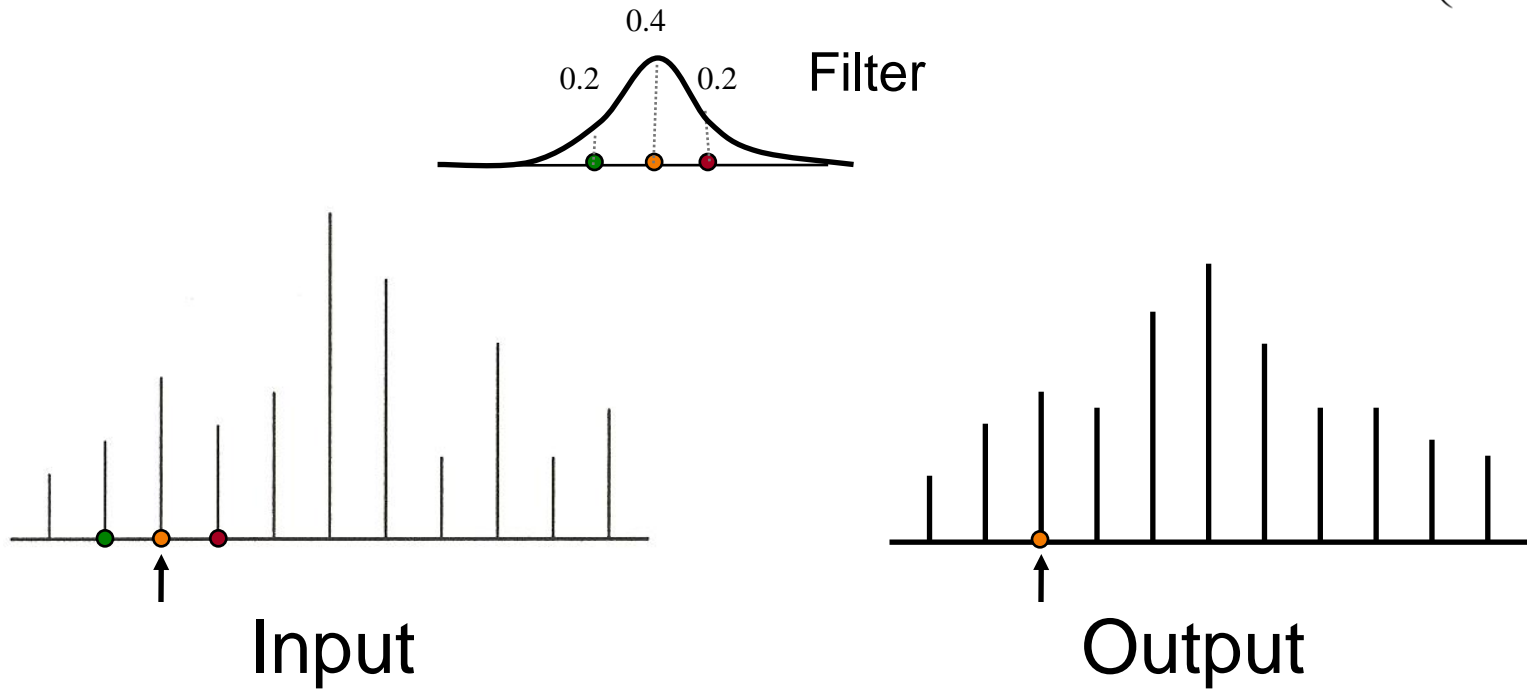


# Convolution with a Gaussian Filter



Output value is weighted sum of values in neighborhood of input image

$$G(x, \sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{x^2}{2\sigma^2}\right)$$

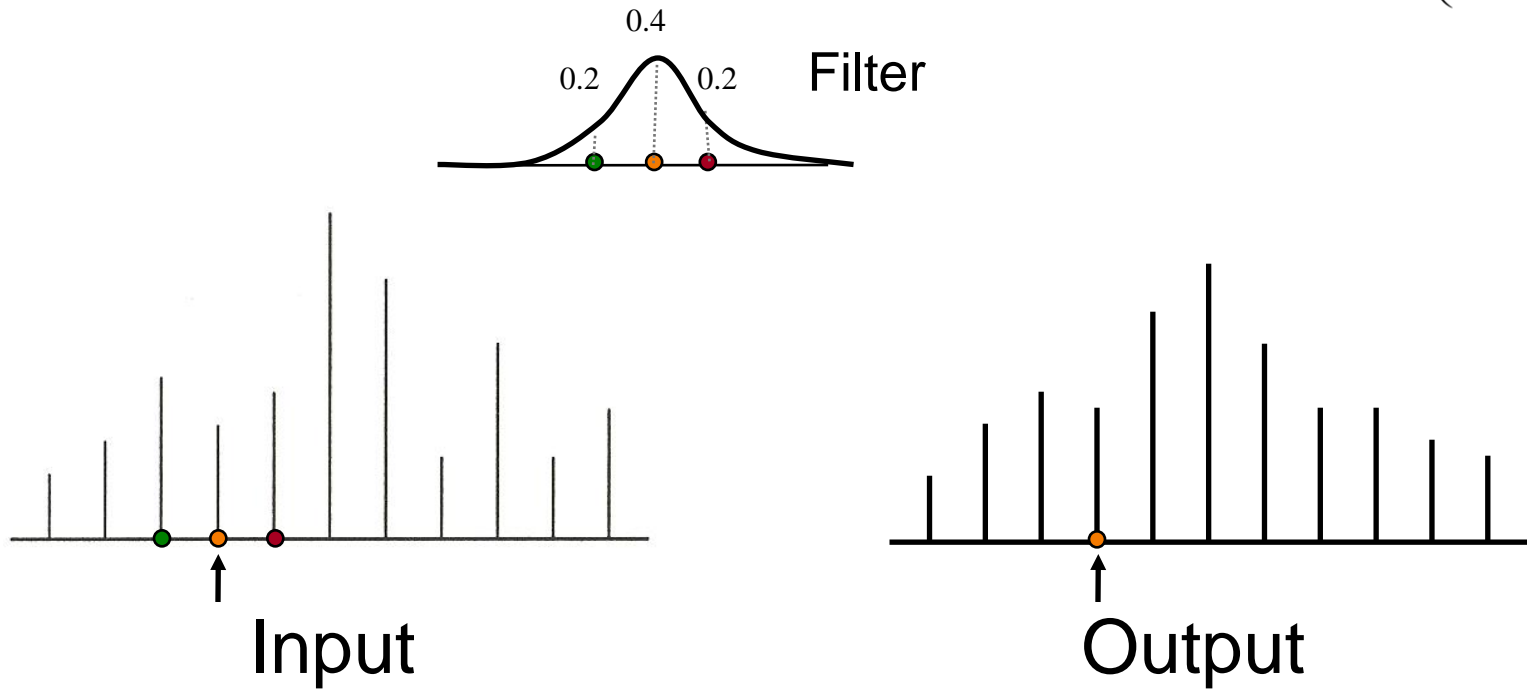


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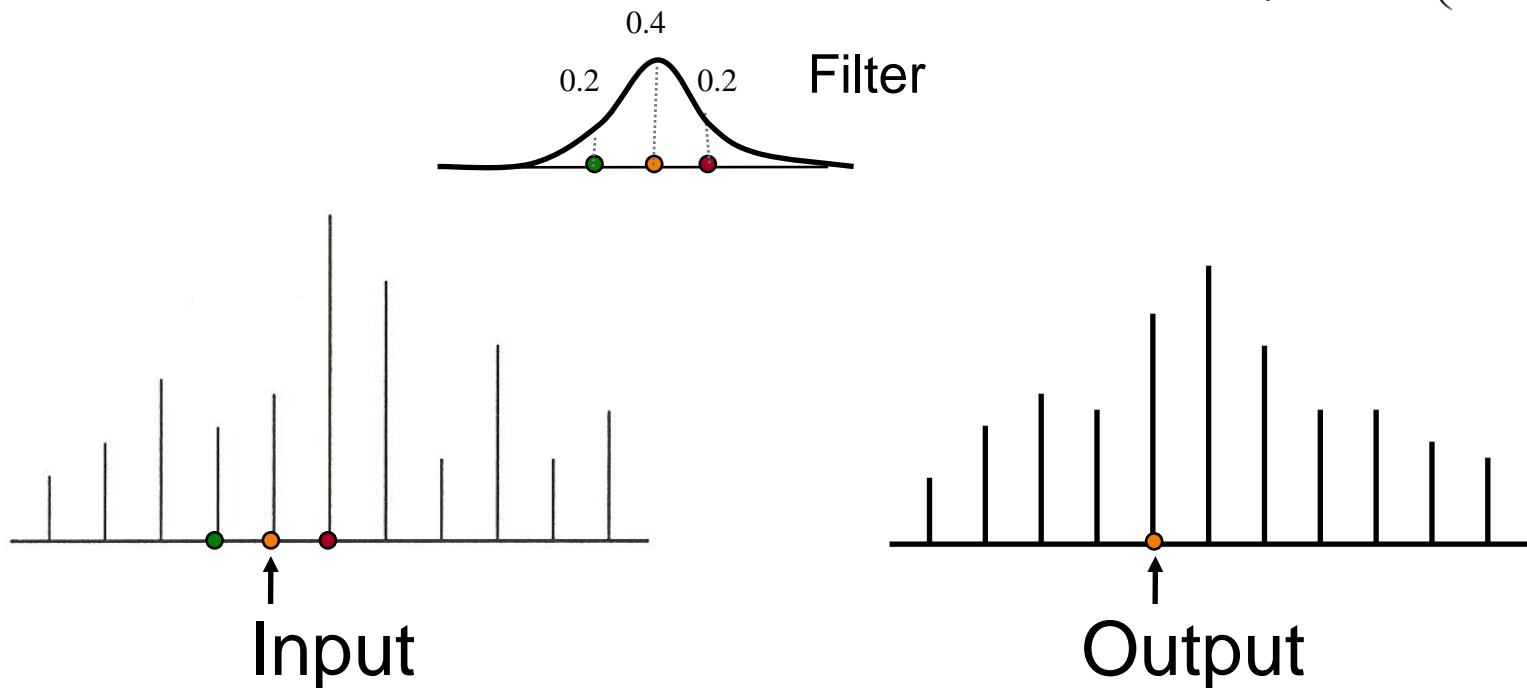


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Output value is weighted sum of values in neighborhood of input image

$$G(x, \sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{x^2}{2\sigma^2}\right)$$

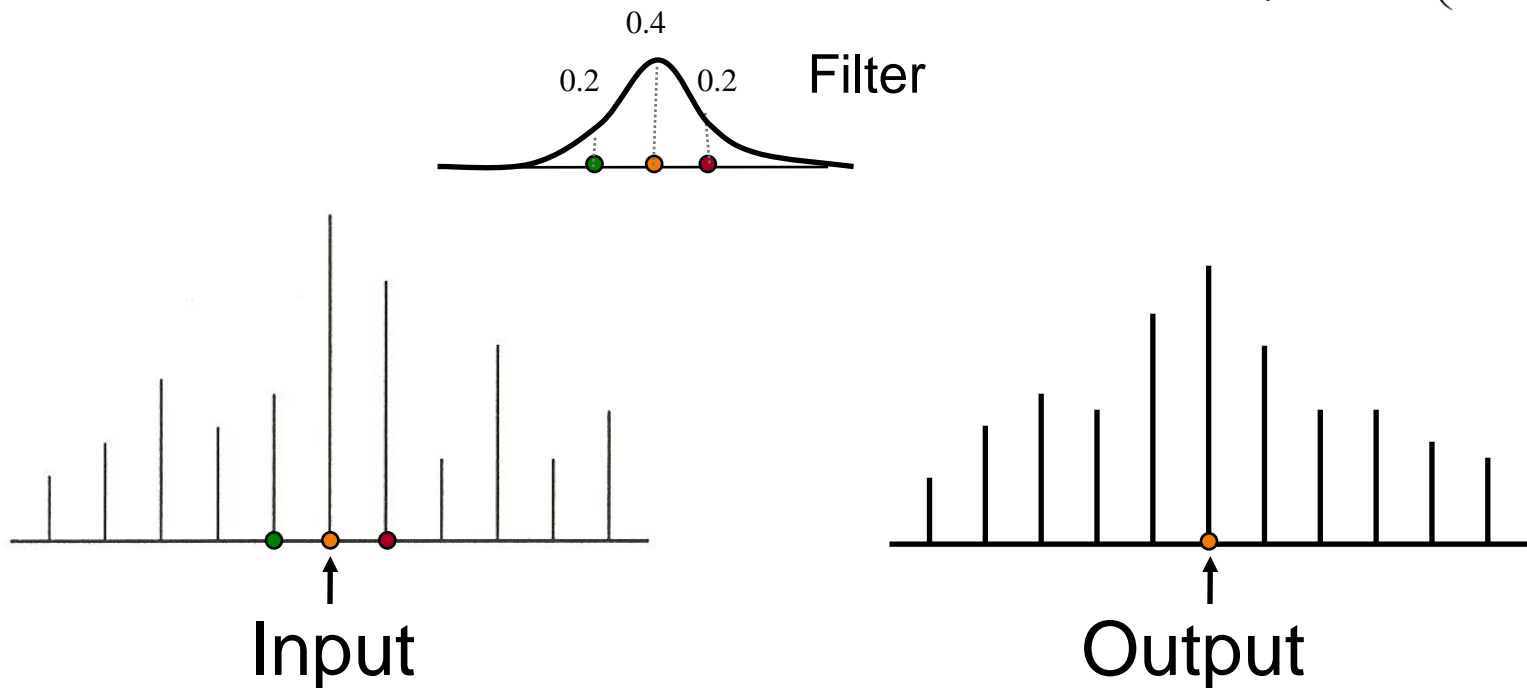


# Convolution with a Gaussian Filter



Output value is weighted sum of values in neighborhood of input image

$$G(x, \sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{x^2}{2\sigma^2}\right)$$



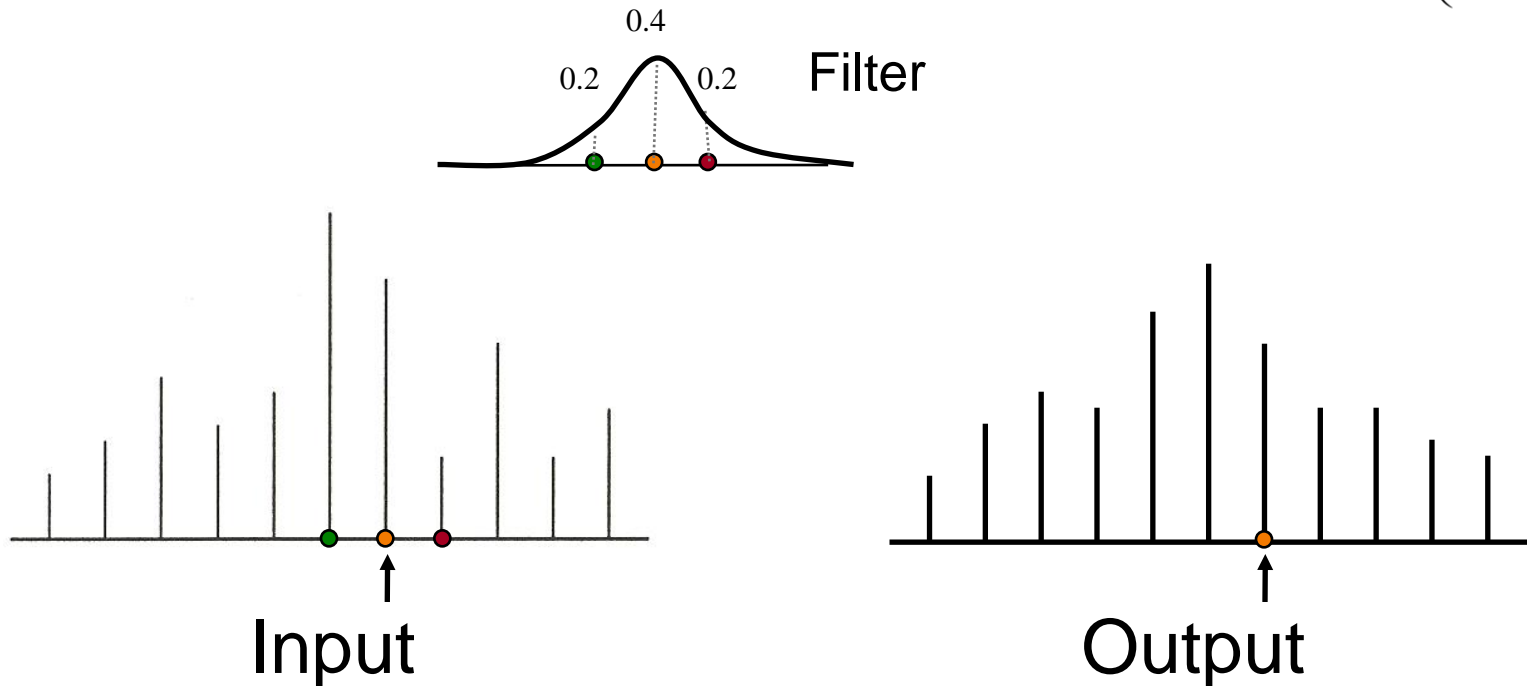


# Convolution with a Gaussian Filter



Output value is weighted sum of values in neighborhood of input image

$$G(x, \sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{x^2}{2\sigma^2}\right)$$

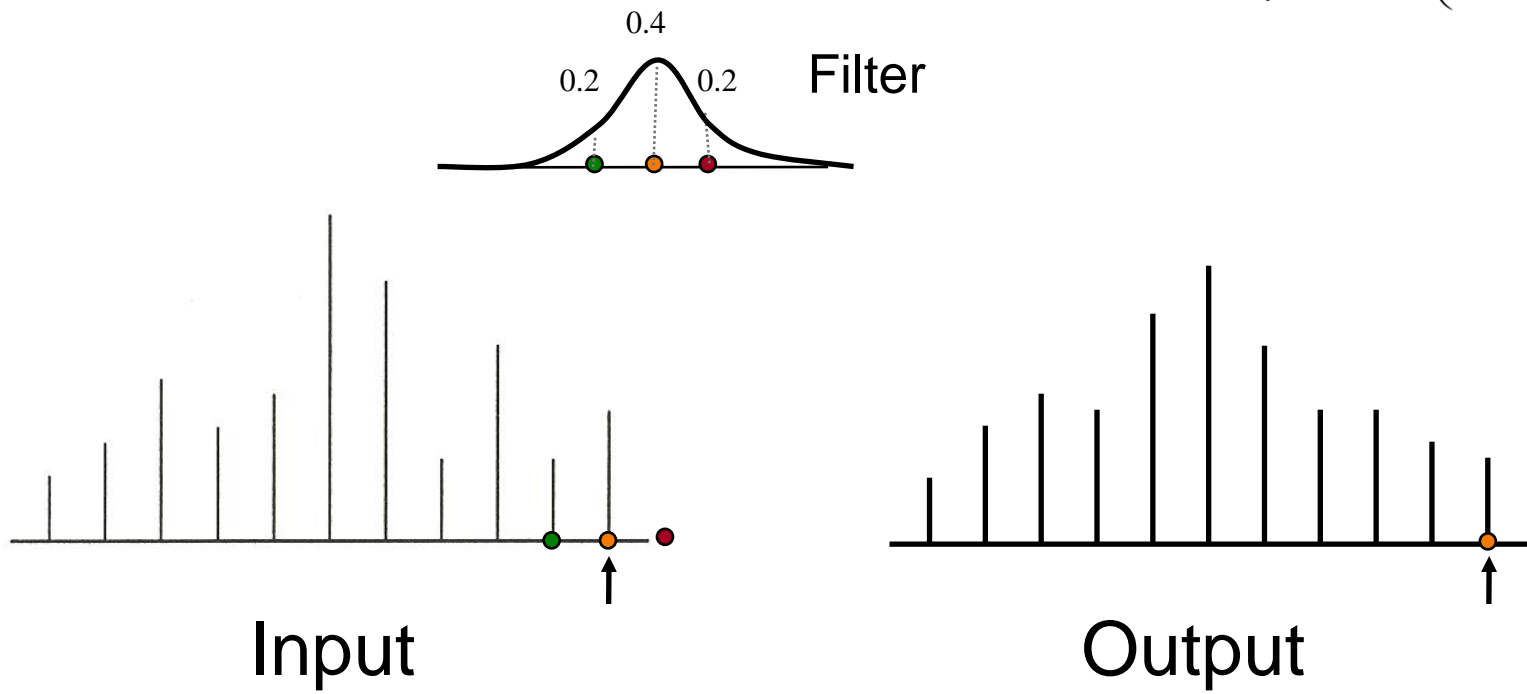


# Convolution with a Gaussian Filter



What if filter extends beyond boundary?

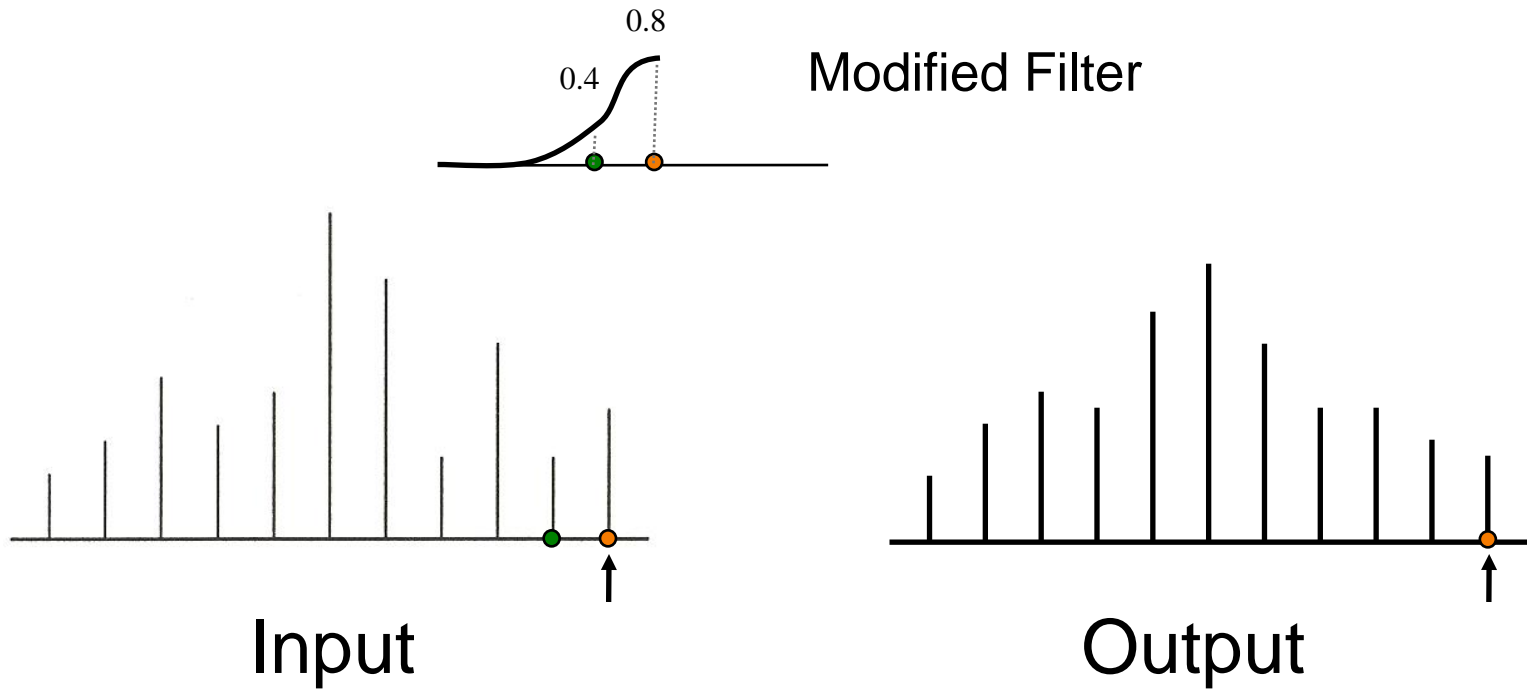
$$G(x, \sigma) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{x^2}{2\sigma^2}\right)$$



# Convolution with a Gaussian Filter



What if filter extends beyond boundary?



# Convolution with a Gaussian Filter



Output contains samples from smoothed input

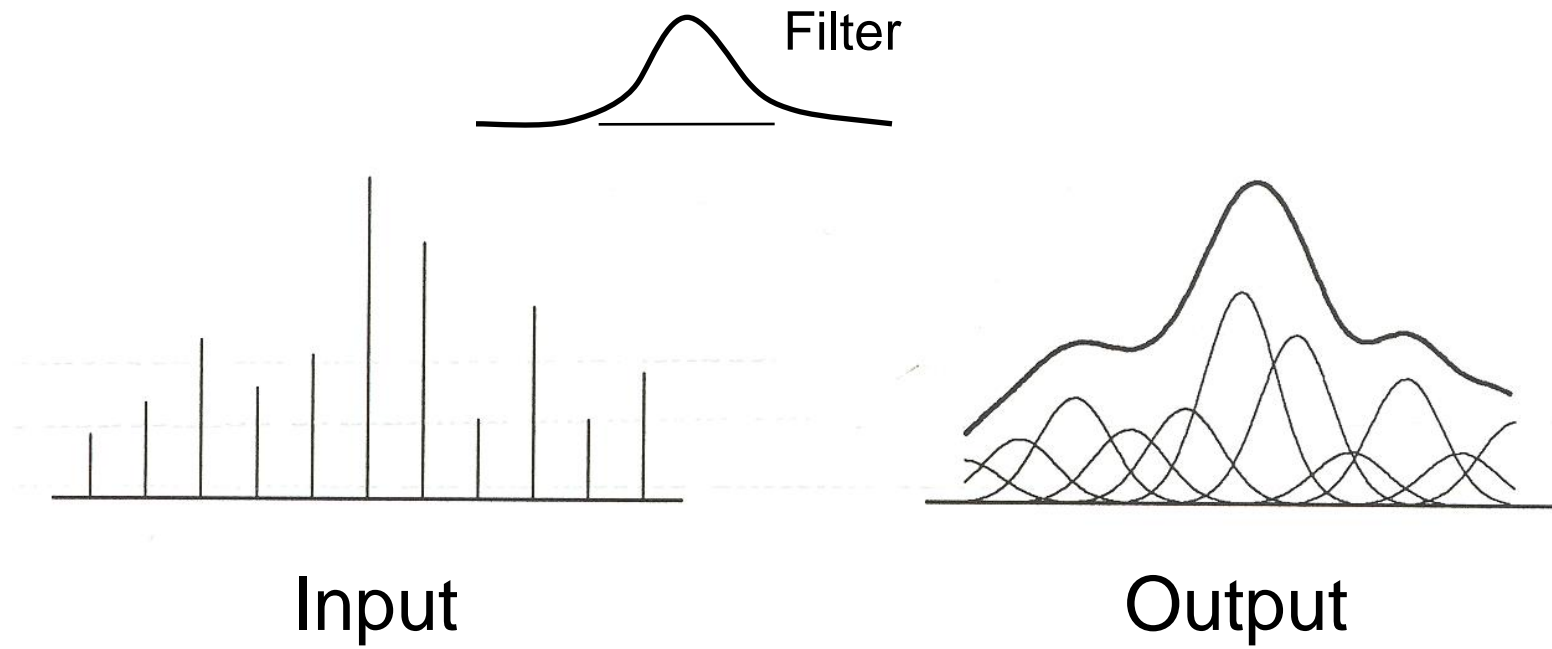
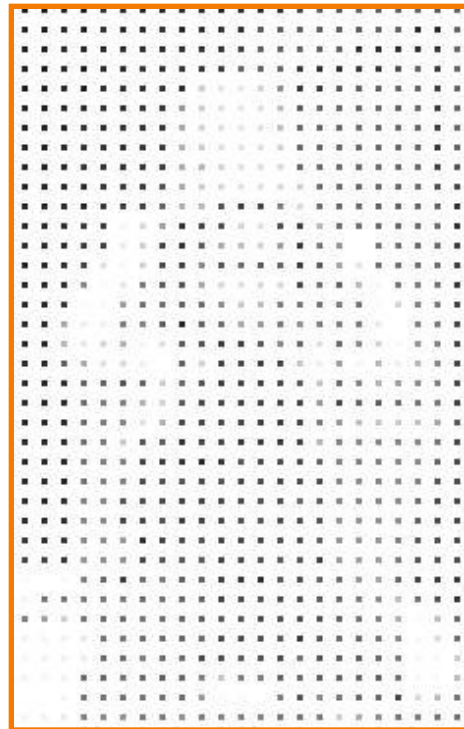


Figure 2.4 Wolberg

# Linear Filtering

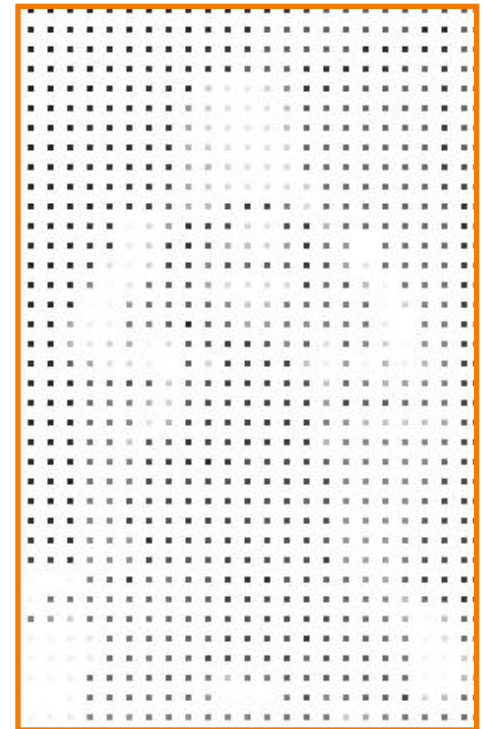
## 2D Convolution

- o Each output pixel is a linear combination of input pixels in 2D neighborhood with weights prescribed by a filter



Input Image

$$\otimes \begin{matrix} \boxed{\text{Grid}} \\ \text{Filter} \end{matrix} =$$

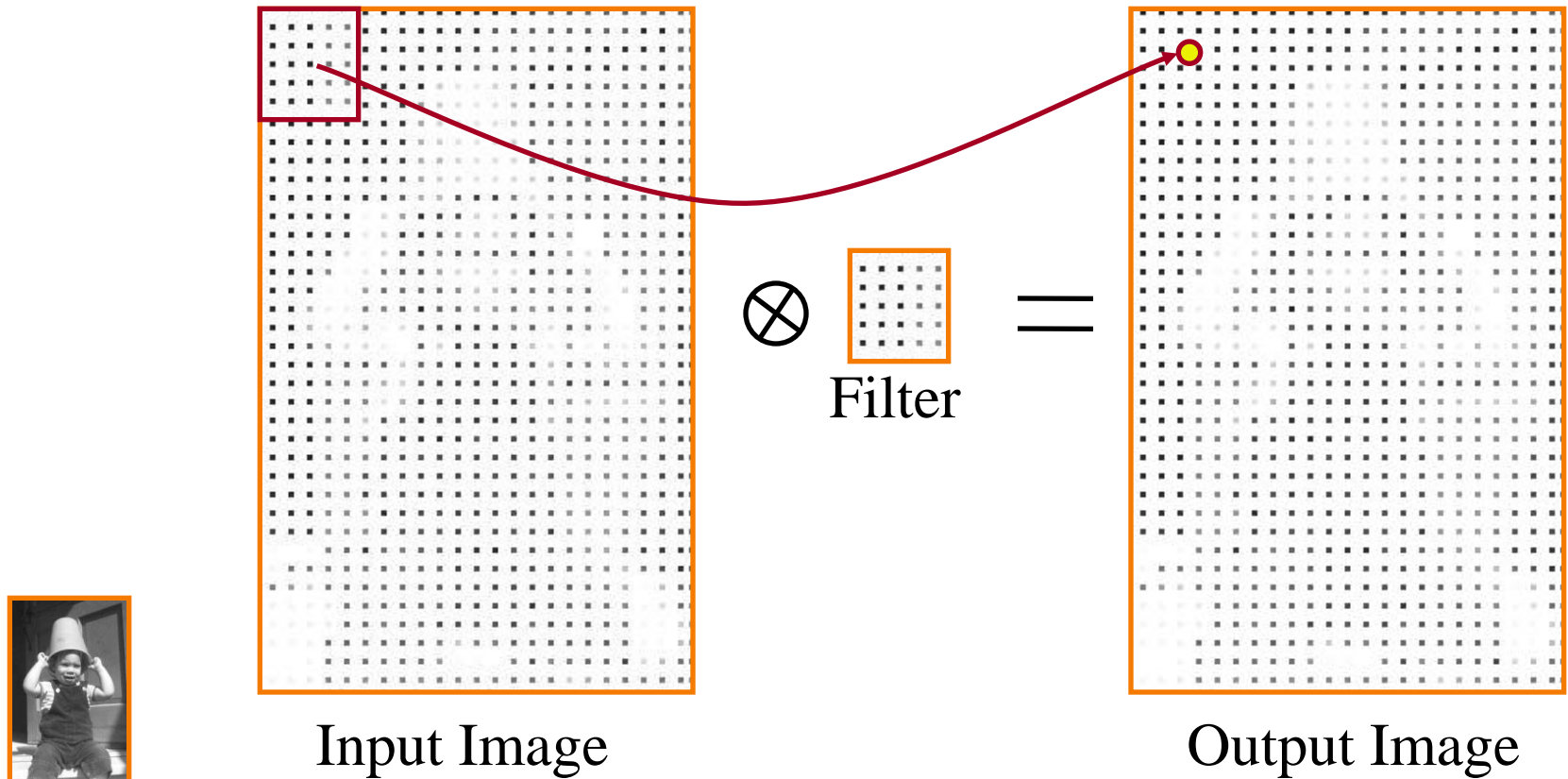


Output Image

# Linear Filtering

## 2D Convolution

- o Each output pixel is a linear combination of input pixels in 2D neighborhood with weights prescribed by a filter



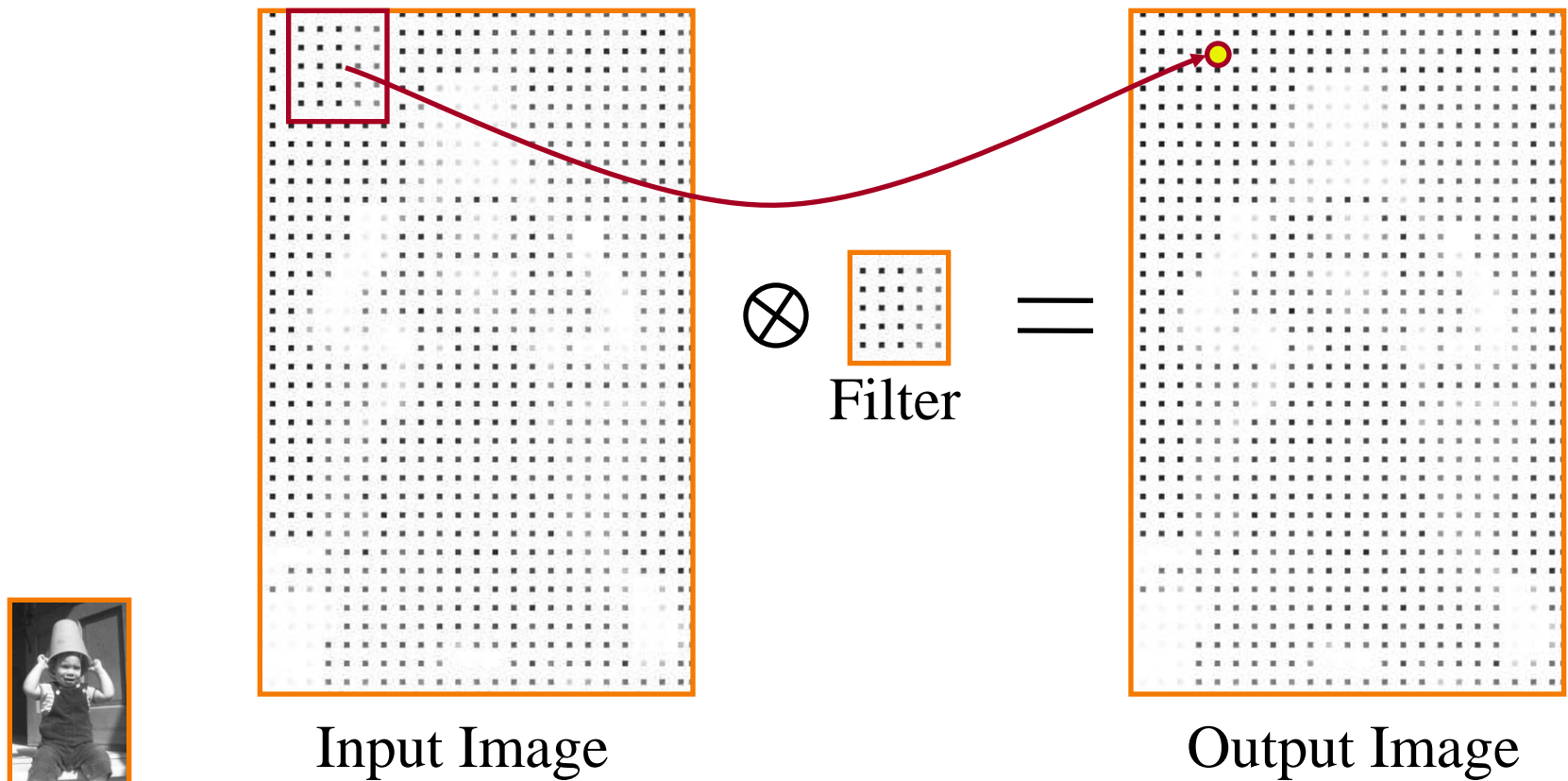
Input Image

Output Image

# Linear Filtering

## 2D Convolution

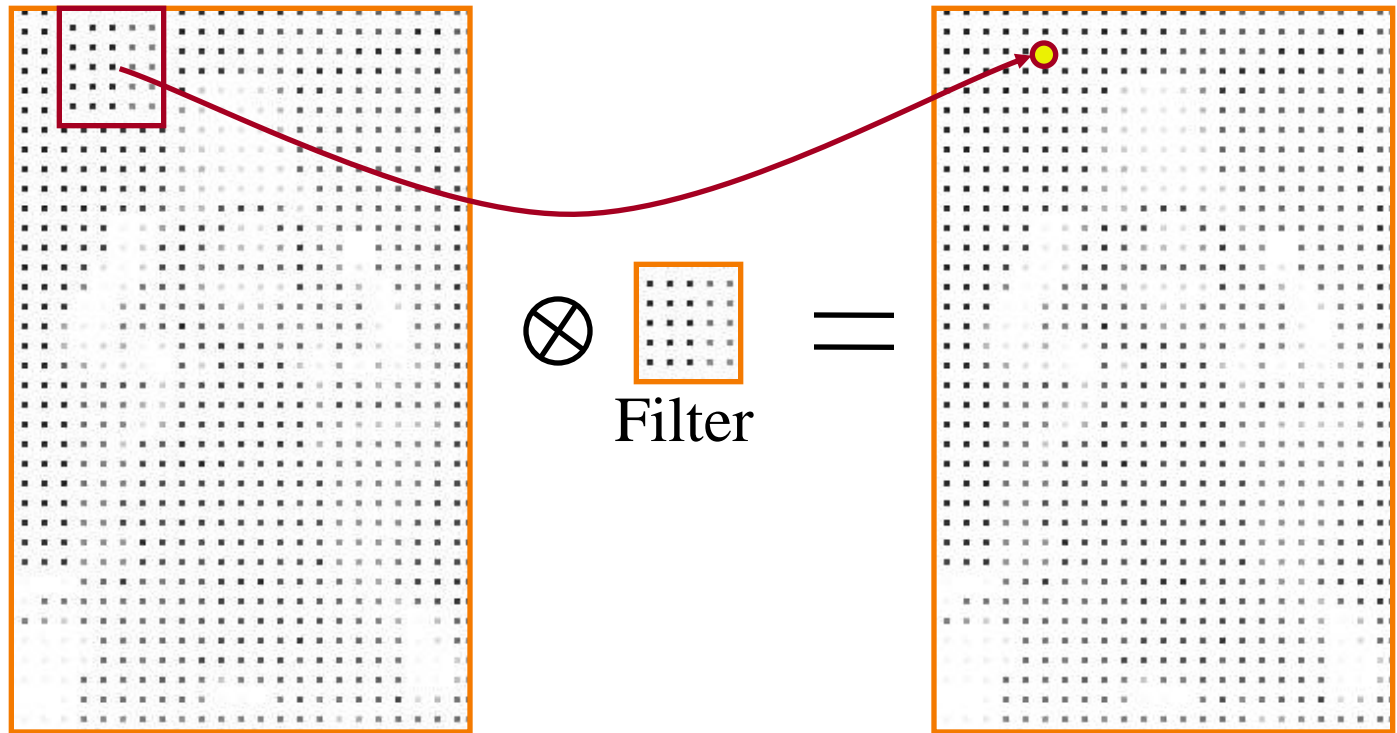
- o Each output pixel is a linear combination of input pixels in 2D neighborhood with weights prescribed by a filter



# Linear Filtering

## 2D Convolution

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Input Image

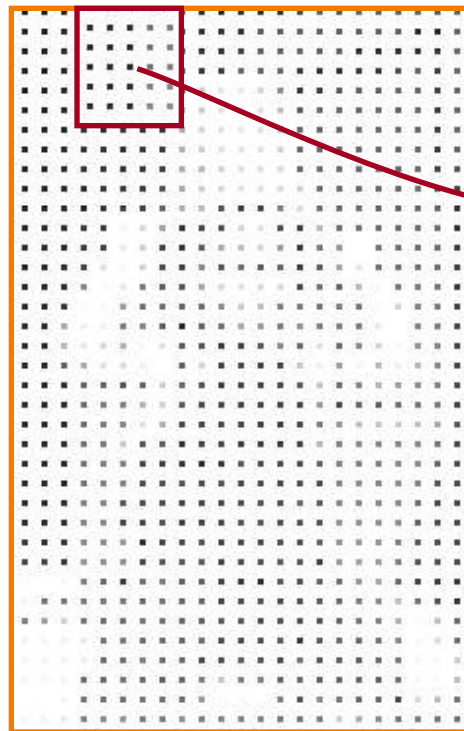
Output Image



# Linear Filtering

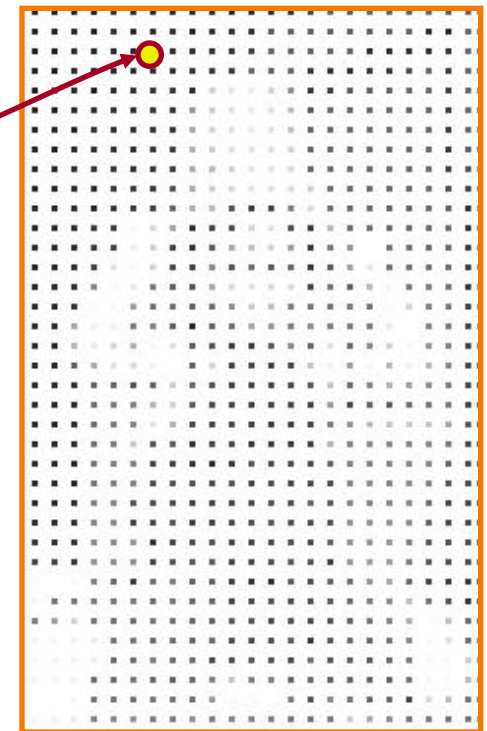
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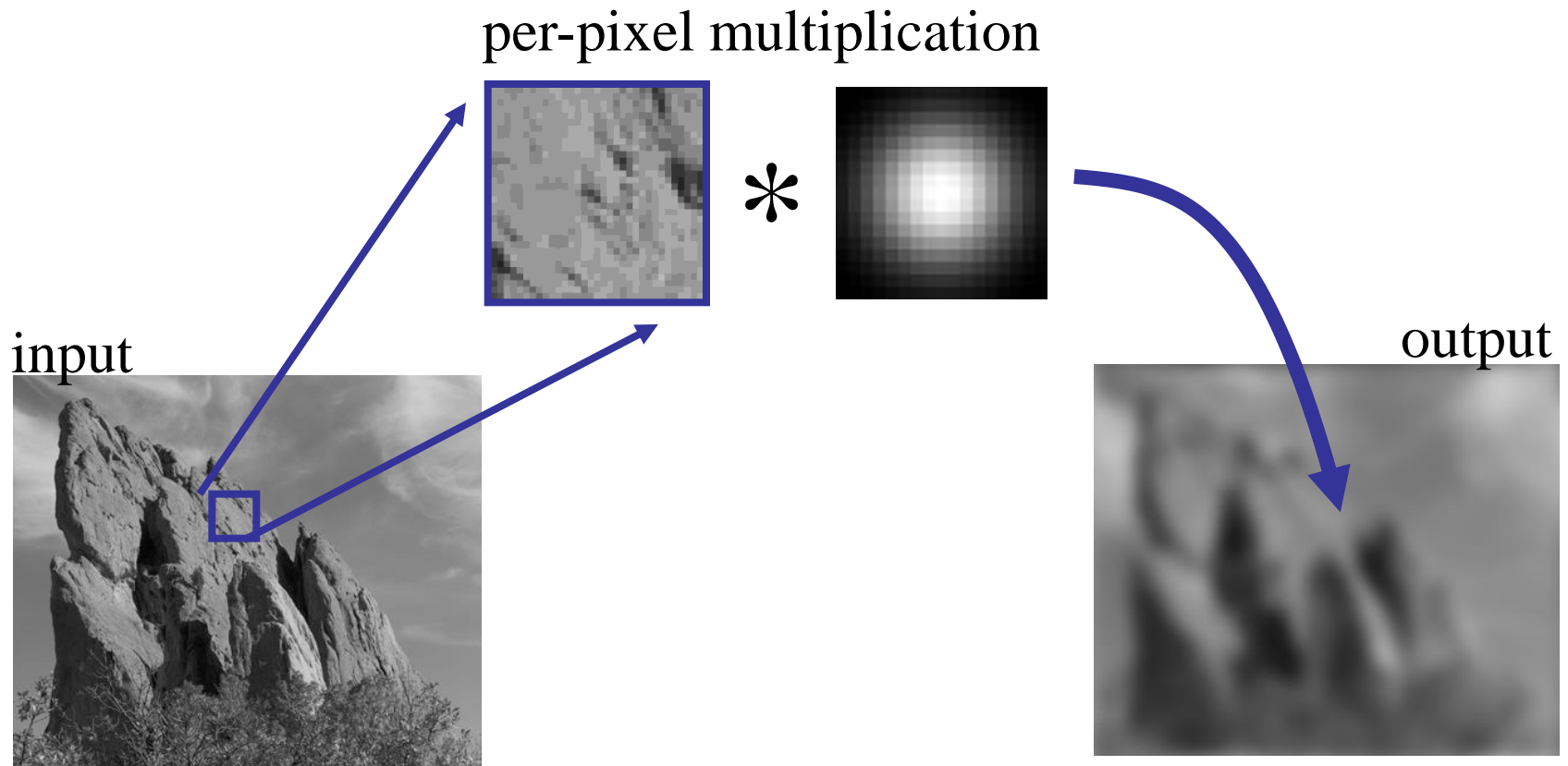
Input Image

$$\otimes \begin{matrix} \square \\ \text{Filter} \end{matrix} =$$



Output Image

# Gaussian Blur



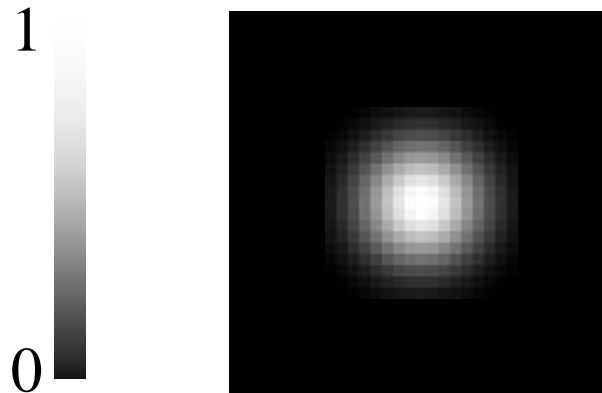
# Gaussian Blur

Output value is weighted sum of values in neighborhood of input image

$$\textit{Blur}(I_p, \sigma) = \sum_{\mathbf{q} \in S} G(\|\mathbf{p} - \mathbf{q}\|, \sigma) I_{\mathbf{q}}$$



normalized  
Gaussian function



**input**



**Gaussian blur**



# Linear Filtering

- Many interesting linear filters
  - Blur
  - Edge detect
  - Sharpen
  - Emboss
  - etc.

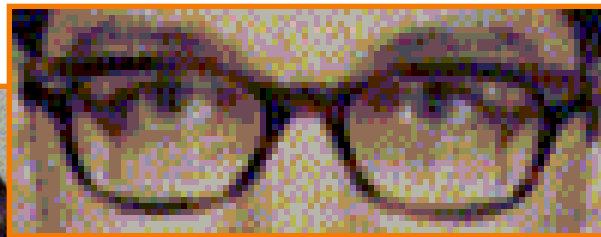
Filter = ?

# Blur

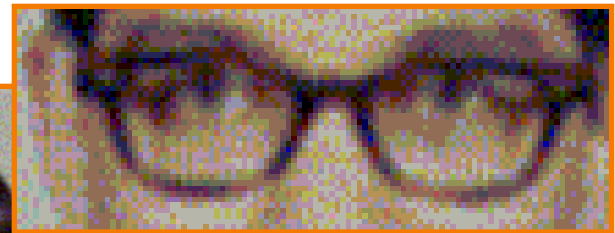
Convolve with a 2D Gaussian filter



Original



Blur



$$G(x, y, \sigma) = \frac{1}{2\pi\sigma^2} \exp\left(-\frac{x^2 + y^2}{2\sigma^2}\right)$$

$$\text{Filter} = \begin{bmatrix} 1/16 & 2/16 & 1/16 \\ 2/16 & 4/16 & 2/16 \\ 1/16 & 2/16 & 1/16 \end{bmatrix}$$

# Edge Detection



Convolve with a 2D Laplacian filter that finds differences between neighbor pixels



Original



Detect edges

$$\text{Filter} = \begin{bmatrix} -1 & -1 & -1 \\ -1 & +8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$



# Sharpen



Sum detected edges with original image



Original



Sharpened

$$\text{Filter} = \begin{bmatrix} -1 & -1 & -1 \\ -1 & +9 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$

# Emboss

Convolve with a filter that highlights gradients in particular directions



Original



Embossed

$$\text{Filter} = \begin{bmatrix} -1 & -1 & 0 \\ -1 & 0 & 1 \\ 0 & 1 & 1 \end{bmatrix}$$



# Side Note: Separable Filters

Some filters are separable (e.g., Gaussian)

- First, apply 1-D convolution across every row
- Then, apply 1-D convolution across every column
- Big impact on performance

# Image Processing Operations



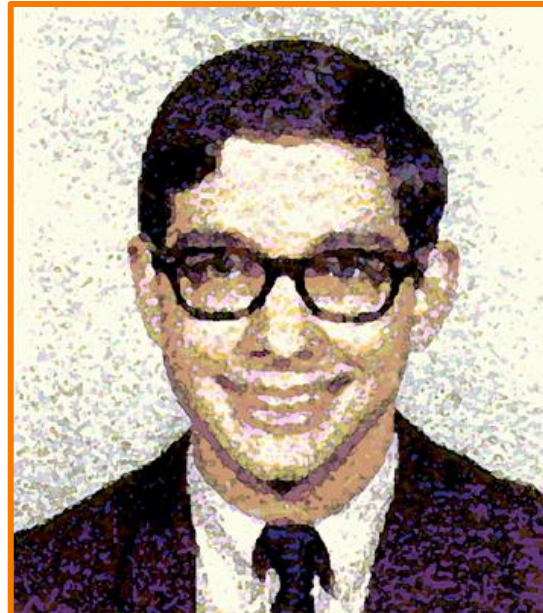
- Luminance
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# Non-Linear Filtering

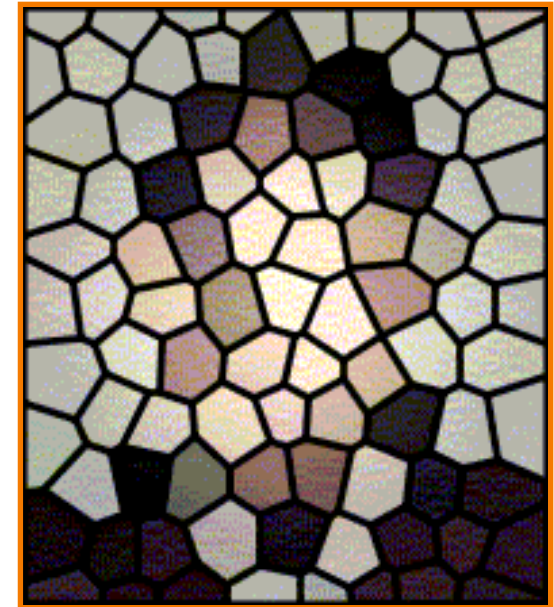
Each output pixel is a non-linear function of input pixels in neighborhood (filter depends on input)



Original



Paint



Stained Glass



# Median Filter

Each output pixel is median of input pixels in neighborhood



original image



1px median filter



3px median filter



10px median filter

# Bilateral Filter

Gaussian blur uses same filter for all pixels

Blurs across edges as much as other areas



Original



Gaussian Blur

# Bilateral Filter

Gaussian blur uses same filter for all pixels

Prefer a filter that preserves edges (adapts to content)



Original



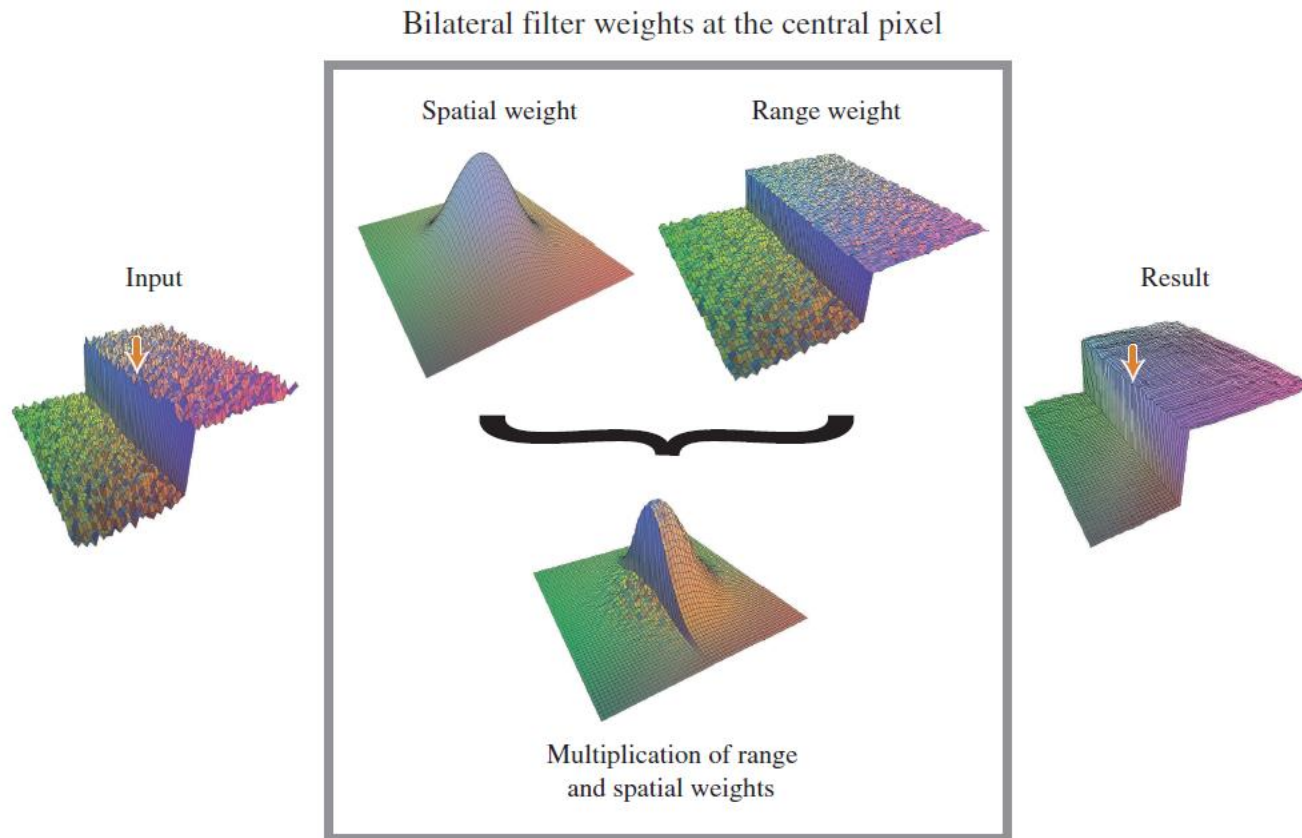
Bilateral Filter





# Bilateral Filtering

Combine Gaussian filtering in both spatial domain and color domain





input

$\sigma_r = 0.1$



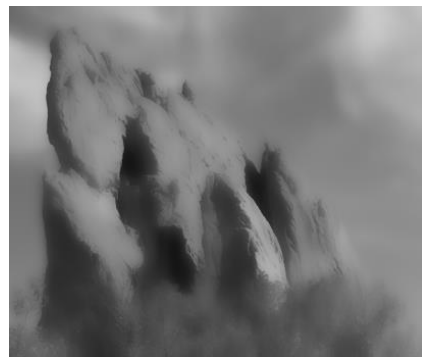
$\sigma_r = 0.25$



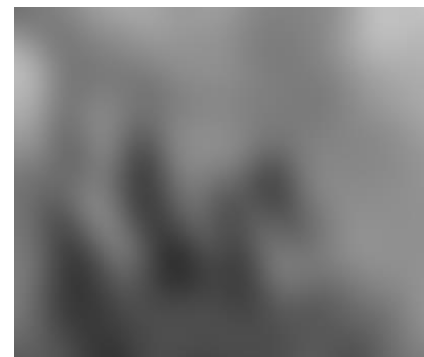
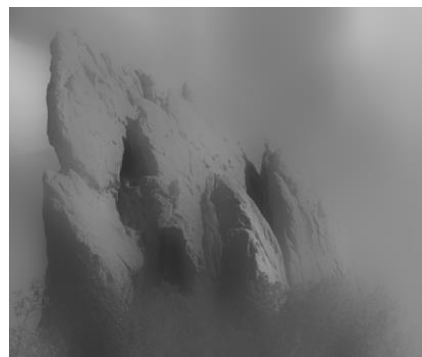
$\sigma_r = \infty$   
(Gaussian blur)



$\sigma_s = 2$



$\sigma_s = 6$



$\sigma_s = 18$





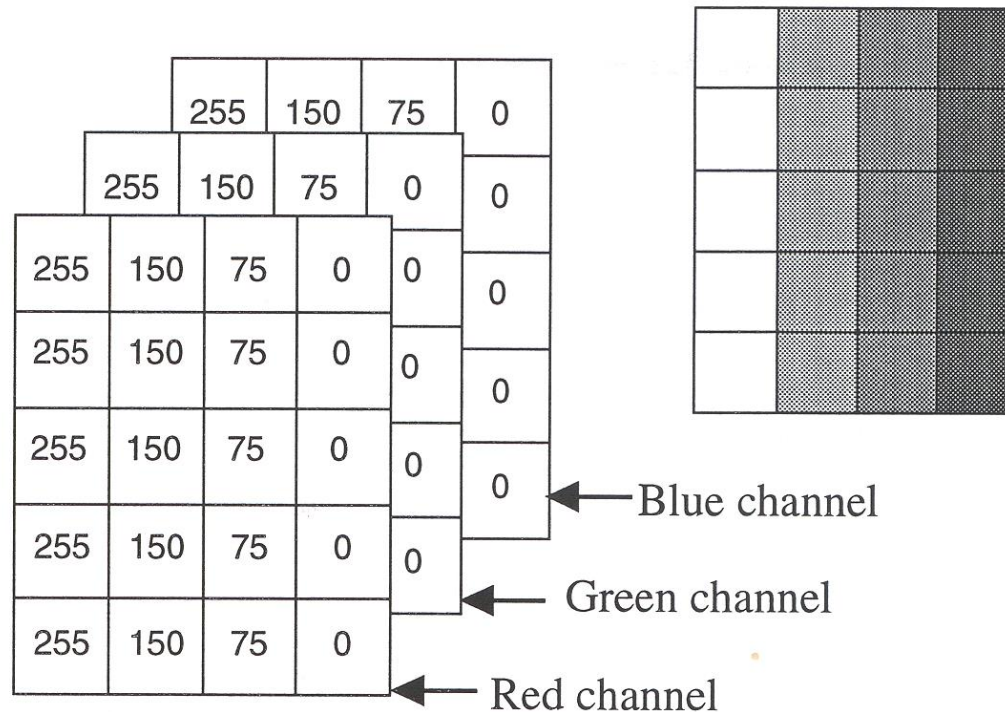
# Image Processing Operations

- Luminance
  - Brightness
  - Contrast.
  - Gamma
  - Histogram equalization
- Color
  - Black & white
  - Saturation
  - White balance
- Linear filtering
  - Blur & sharpen
  - Edge detect
  - Convolution
- Non-linear filtering
  - Median
  - Bilateral filter
- Dithering
  - Quantization
  - Ordered dither
  - Floyd-Steinberg

# Quantization

## Reduce intensity resolution

- o Frame buffers have limited number of bits per pixel
- o Physical devices have limited dynamic range



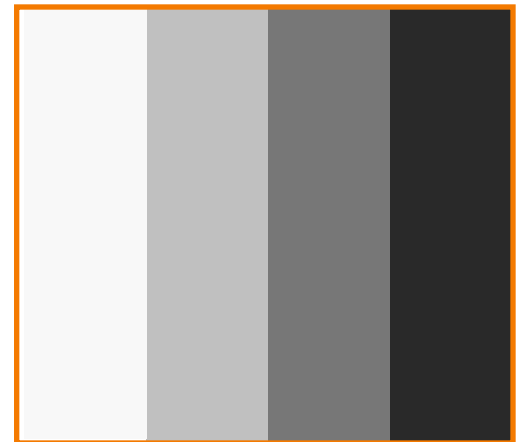
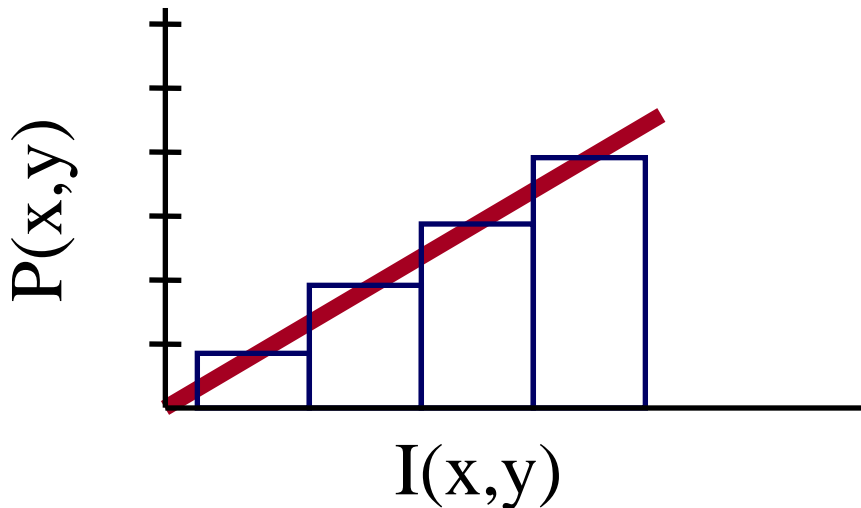


# Uniform Quantization

$P(x, y) = \text{round}( I(x, y) )$   
where  $\text{round}()$  chooses nearest value that can be represented.



$I(x,y)$



$P(x,y)$   
(2 bits per pixel)

# Uniform Quantization



Images with decreasing bits per pixel:



8 bits



4 bits



2 bits



1 bit

Notice contouring.

# Reducing Effects of Quantization



- Intensity resolution / spatial resolution tradeoff
- Dithering
  - Random dither
  - Ordered dither
  - Error diffusion dither
- Halftoning
  - Classical halftoning



# Dithering



Distribute errors among pixels

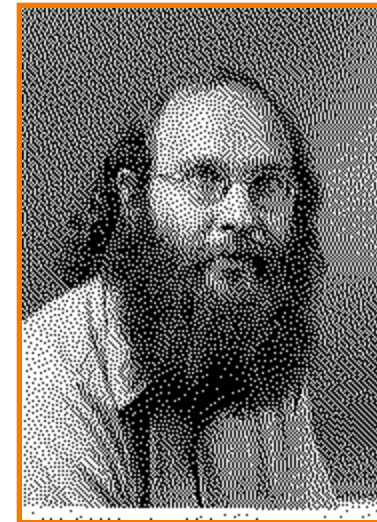
- o Exploit spatial integration in our eye
- o Display greater range of perceptible intensities



Original  
(8 bits)



Uniform  
Quantization  
(1 bit)



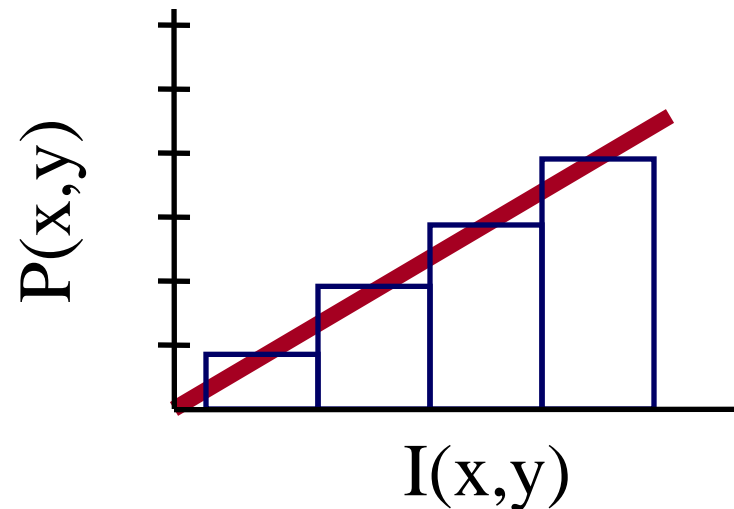
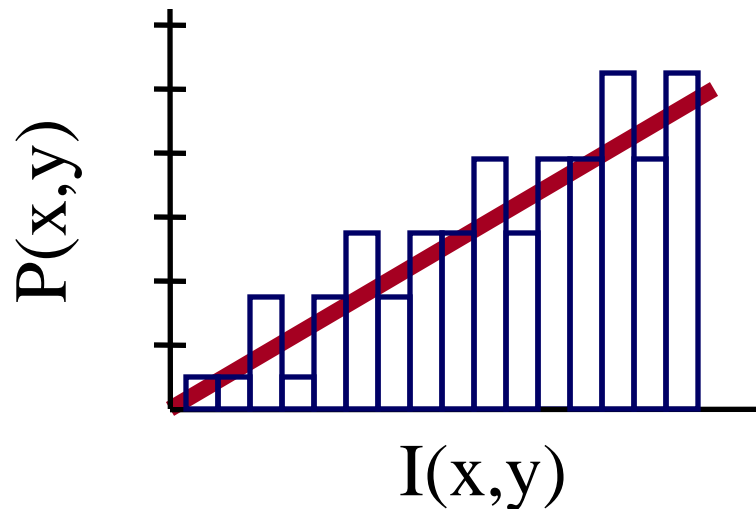
Floyd-Steinberg  
Dither  
(1 bit)



# Random Dither

Randomize quantization errors

- o Errors appear as noise



$$P(x, y) = \text{round}(I(x, y) + \text{noise}(x,y))$$

# Random Dither



Original  
(8 bits)



Uniform  
Quantization  
(1 bit)



Random  
Dither  
(1 bit)



# Ordered Dither

Pseudo-random quantization errors

o Matrix stores pattern of thresholds

$$i = x \bmod n$$

$$j = y \bmod n$$

$$e = I(x,y) - \text{trunc}(I(x,y))$$

$$\text{threshold} = (D(i,j)+1)/(n^2+1)$$

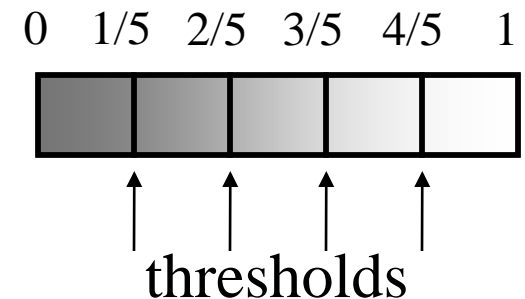
if ( $e > \text{threshold}$ )

$$P(x,y) = \text{ceil}(I(x,y))$$

else

$$P(x,y) = \text{floor}(I(x,y))$$

$$D_2 = \begin{bmatrix} 3 & 1 \\ 0 & 2 \end{bmatrix}$$





# Ordered Dither

Bayer's ordered dither matrices

$$D_n = \begin{bmatrix} 4D_{n/2} + D_2(1,1)U_{n/2} & 4D_{n/2} + D_2(1,2)U_{n/2} \\ 4D_{n/2} + D_2(2,1)U_{n/2} & 4D_{n/2} + D_2(2,2)U_{n/2} \end{bmatrix}$$

$$D_2 = \begin{bmatrix} 3 & 1 \\ 0 & 2 \end{bmatrix}$$

$$D_4 = \begin{array}{cc|cc} 15 & 7 & 13 & 5 \\ 3 & 11 & 1 & 9 \\ \hline 12 & 4 & 14 & 6 \\ 0 & 8 & 2 & 10 \end{array}$$

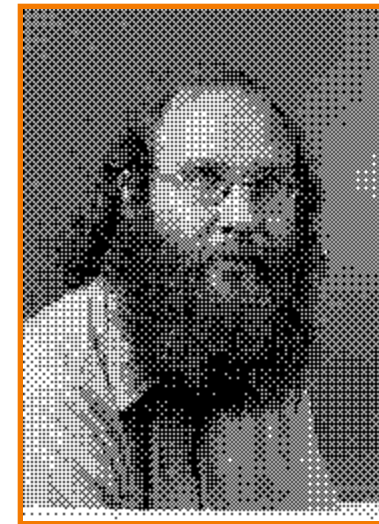
# Ordered Dither



Original  
(8 bits)



Random  
Dither  
(1 bit)



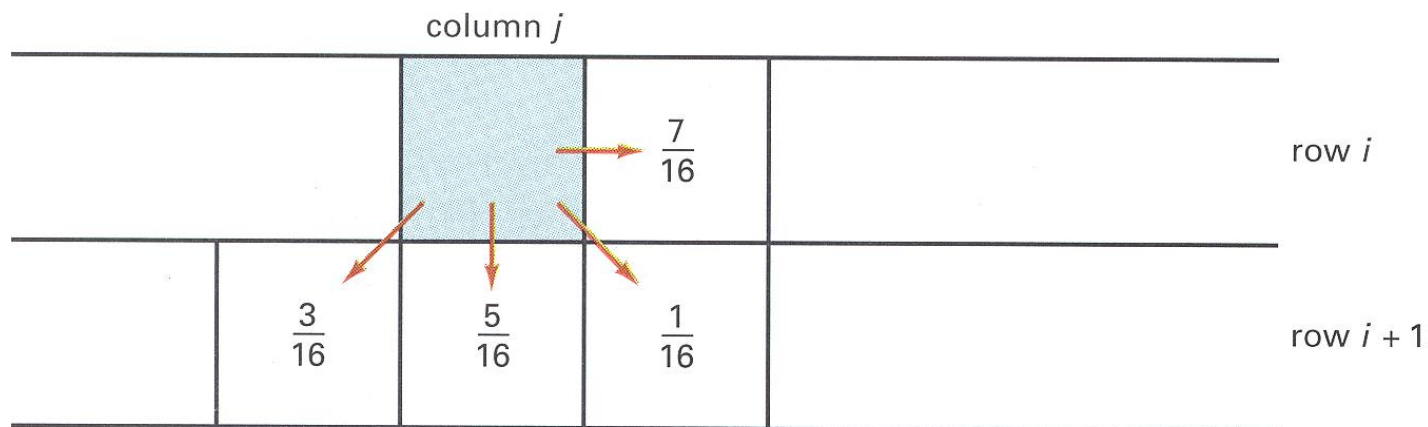
Ordered  
Dither  
(1 bit)



# Error Diffusion Dither

Spread quantization error over neighbor pixels

- o Error dispersed to pixels right and below
- o Floyd-Steinberg weights:



$$\frac{3}{16} + \frac{5}{16} + \frac{1}{16} + \frac{7}{16} = 1.0$$

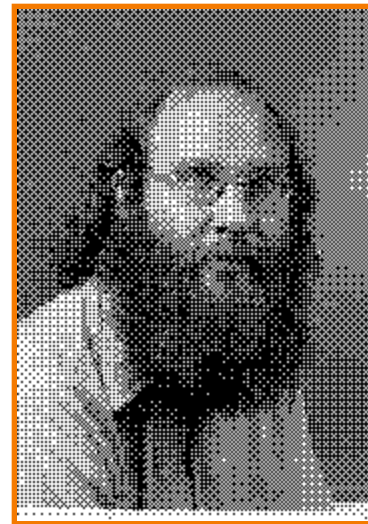
# Error Diffusion Dither



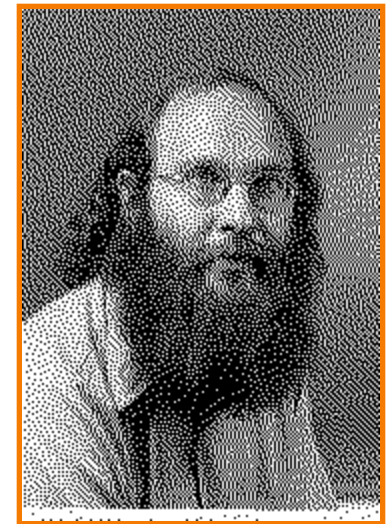
Original  
(8 bits)



Random  
Dither  
(1 bit)



Ordered  
Dither  
(1 bit)



Floyd-Steinberg  
Dither  
(1 bit)



# Summary



- Color transformations
  - Different color spaces useful for different operations
- Filtering
  - Compute new values for image pixels based on function of old values in neighborhood
- Dithering
  - Reduce visual artifacts due to quantization
  - Distribute errors among pixels
    - Exploit spatial integration in our eye