

Lighting and Reflectance

COS 426

Ray Casting



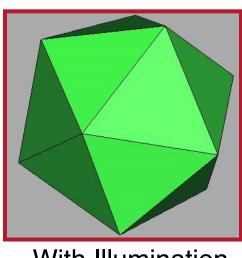
```
R2Image *RayCast(R3Scene *scene, int width, int height)
    R2Image *image = new R2Image(width, height);
    for (int i = 0; i < width; i++) {
        for (int j = 0; j < \text{height}; j++) {
             R3Ray ray = ConstructRayThroughPixel(scene->camera, i, j);
             R3Rgb radiance = ComputeRadiance(scene, &ray);
             image->SetPixel(i, j, radiance);
    return image;
```



Ray Casting



```
R3Rgb ComputeRadiance(R3Scene *scene, R3Ray *ray)
    R3Intersection intersection = ComputeIntersection(scene, ray);
    return ComputeRadiance(scene, ray, intersection);
```



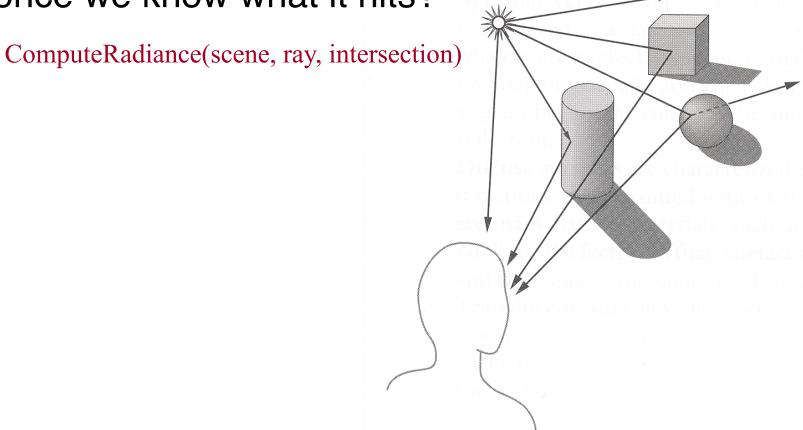
With Illumination

Illumination



How do we compute radiance for a sample ray

once we know what it hits?

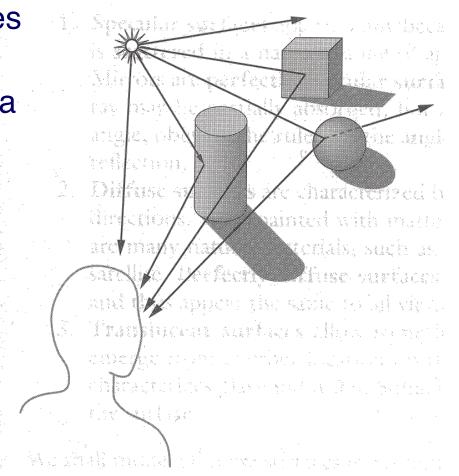


Goal



- Must derive computer models for ...
 - Emission at light sources
 - Scattering at surfaces
 - Reception at the camera

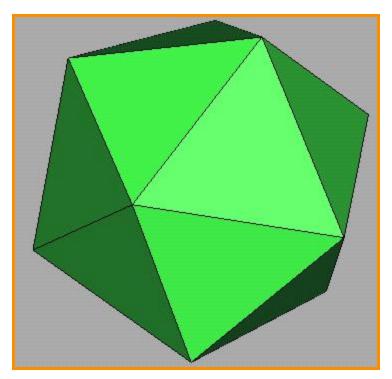
- Desirable features ...
 - Concise
 - Efficient to compute
 - "Accurate"



Overview



- Direct Illumination
 - Emission at light sources
 - Scattering at surfaces
- Global illumination
 - Shadows
 - Refractions
 - Inter-object reflections

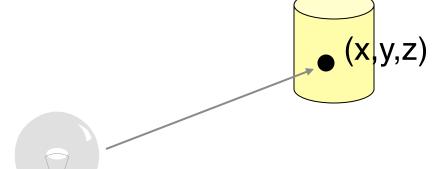


Direct Illumination

Emission at Light Sources



- $I_{L}(x,y,z,\theta,\phi,\lambda)$...
 - describes the intensity of energy,
 - leaving a light source, ...
 - arriving at location(x,y,z), ...
 - from direction (θ, ϕ) , ...
 - \circ with wavelength λ

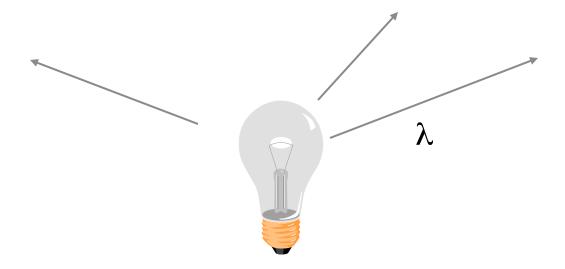


Light

Empirical Models



- Ideally measure irradiant energy for "all" situations
 - Too much storage
 - Difficult in practice



OpenGL Light Source Models



- Simple mathematical models:
 - Point light
 - Spot light
 - Directional light





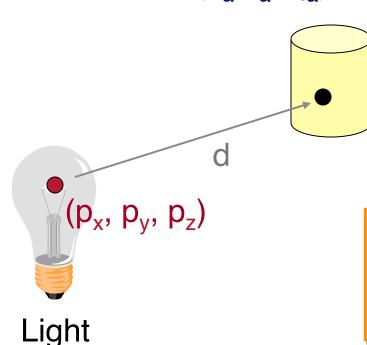


Point Light Source





- Models omni-directional point source
 - ∘ intensity (I₀),
 - position (p_x, p_y, p_z),
 - coefficients (c_a, I_a, q_a) for attenuation with distance (d)



$$I_L = \frac{I_0}{c_a + l_a d + q_a d^2}$$

Point Light Source





$$I_L = \frac{I_0}{c_a + l_a d + q_a d^2}$$

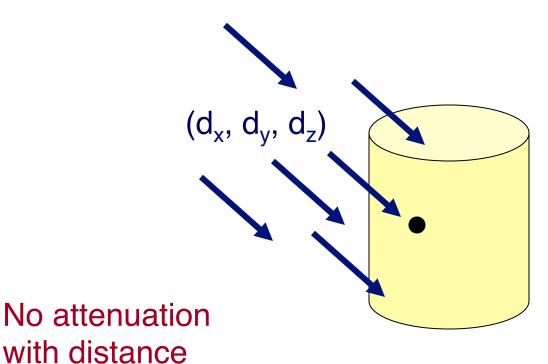
- Physically-based: "inverse square law"
 - $\circ c_a = l_a = 0$
- Use c_a and $l_a \neq 0$ for (non-physical) artistic effects

Directional Light Source





- Models point light source at infinity
 - ∘ intensity (I₀),
 - direction (d_x,d_y,d_z)



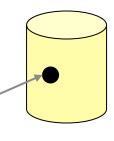
 $I_L = I_0$

Spot Light Source





- Models point light source with direction
 - ∘ intensity (I₀),
 - position (p_x, p_y, p_z),
 - direction (d_x, d_y, d_z)
 - attenuation with distance
 - falloff (sd), and cutoff (sc)



$$(p_x, p_y, p_z)$$

$$O = \cos^{-1}(L \cdot D)$$

$$I \cdot (\cos \theta)$$

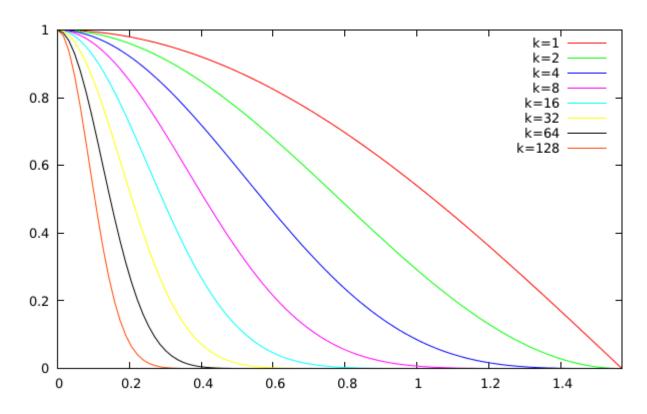
$$I_{L} = \begin{cases} \frac{I_{0}(\cos\Theta)^{sd}}{c_{a} + l_{a}d + q_{a}d^{2}} & \text{if } \Theta \leq sc, \\ 0 & \text{otherwise} \end{cases}$$

Cosine Lobes



 $(\cos\Theta)^k$

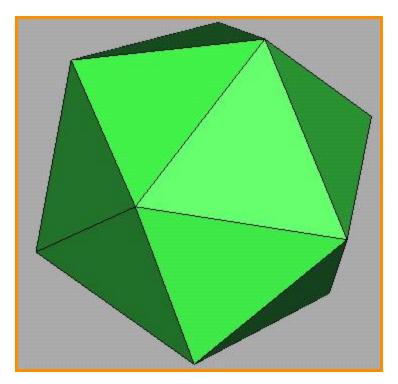
Common model for "blob" at origin



Overview



- Direct Illumination
 - Emission at light sources
 - Scattering at surfaces
- Global illumination
 - Shadows
 - Refractions
 - Inter-object reflections



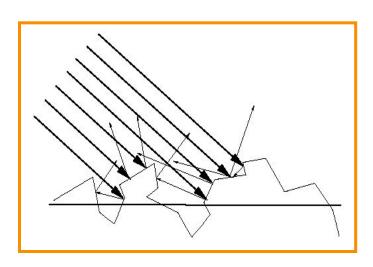
Direct Illumination

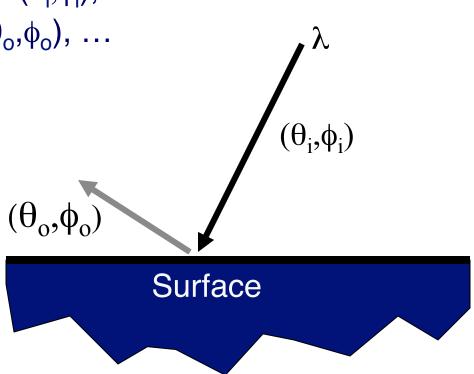
Scattering at Surfaces



Bidirectional Reflectance Distribution Function f (θ, φ, θ, φ, λ)

- $f_r(\theta_i, \phi_i, \theta_o, \phi_o, \lambda) \dots$
 - describes the aggregate fraction of incident energy,
 - arriving from direction (θ_i, ϕ_i) , ...
 - leaving in direction (θ_o,φ_o), ...
 with wavelength λ



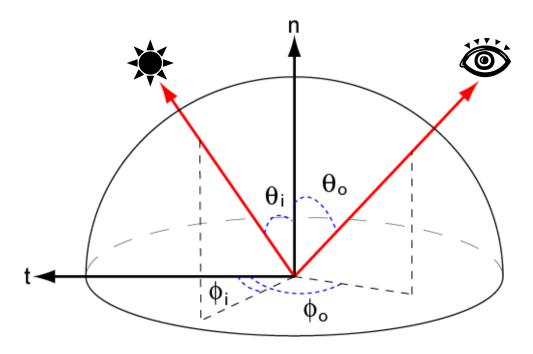


Empirical Models



Ideally measure BRDF for "all" combinations of angles: $\theta_i, \phi_i, \theta_o, \phi_o$

- Difficult in practice
- Too much storage

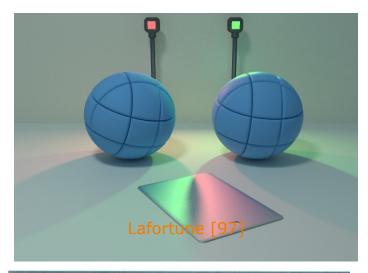


Parametric Models



Approximate BRDF with simple parametric function that is fast to compute.

- Phong [75]
- Blinn-Phong [77]
- Cook-Torrance [81]
- He et al. [91]
- Ward [92]
- Lafortune et al. [97]
- Ashikhmin et al. [00]
- etc.

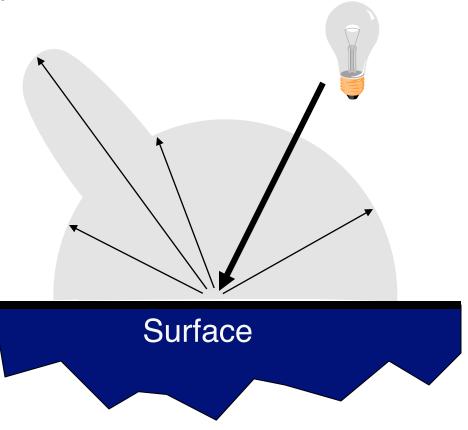






- Simple analytic model:
 - diffuse reflection +
 - specular reflection +
 - emission +
 - "ambient"

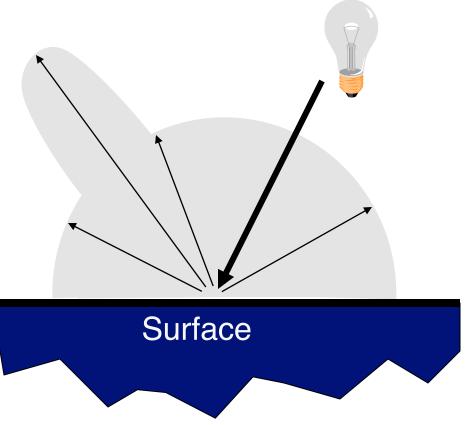
Based on model proposed by Phong





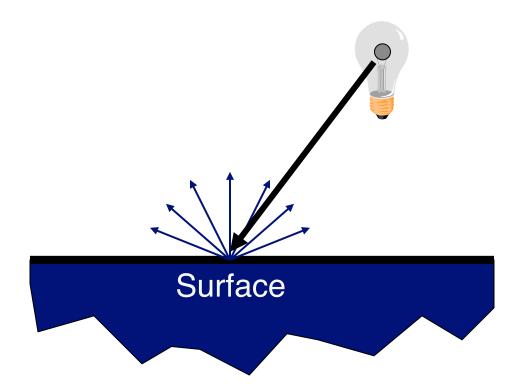
- Simple analytic model:
 - diffuse reflection +
 - specular reflection +
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Based on model proposed by Phong



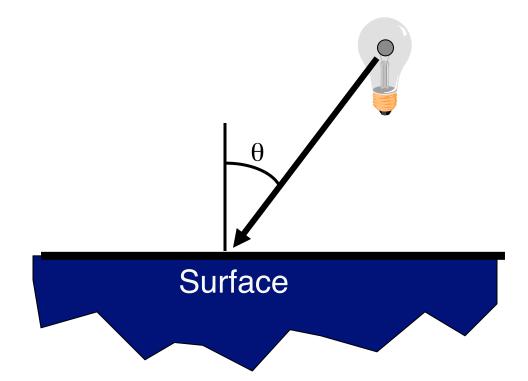


- Assume surface reflects equally in all directions
 - Examples: chalk, clay





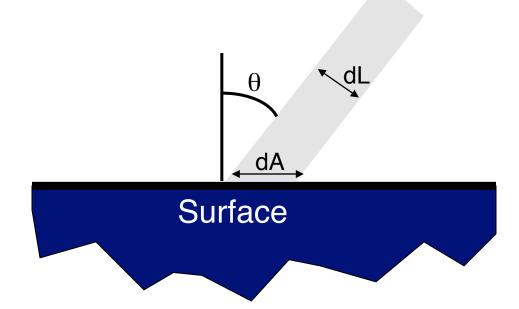
- What is brightness of surface?
 - Depends on angle of incident light





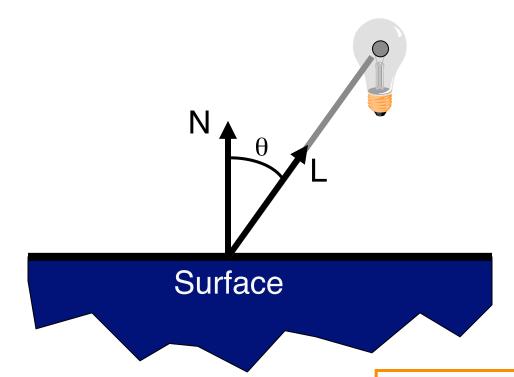
- What is brightness of surface?
 - Depends on angle of incident light

$$dL = dA \cos \Theta$$





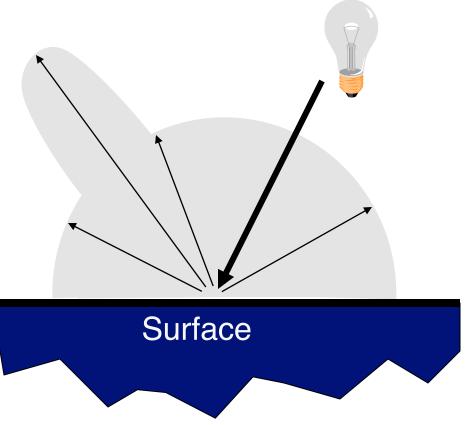
- Lambertian model
 - cosine law (dot product)



$$I_D = K_D(N \cdot L)I_L$$



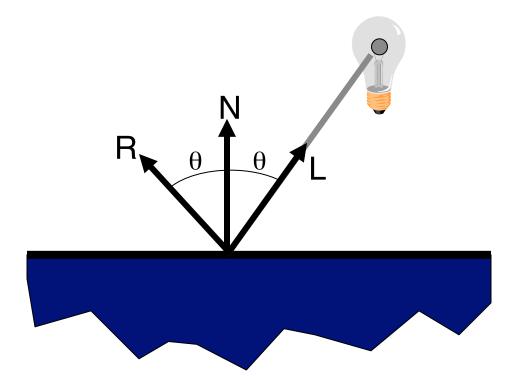
- Simple analytic model:
 - diffuse reflection +
 - specular reflection +
 - emission +
 - "ambient"



Specular Reflection



- Reflection is strongest near mirror angle
 - Examples: mirrors, metals

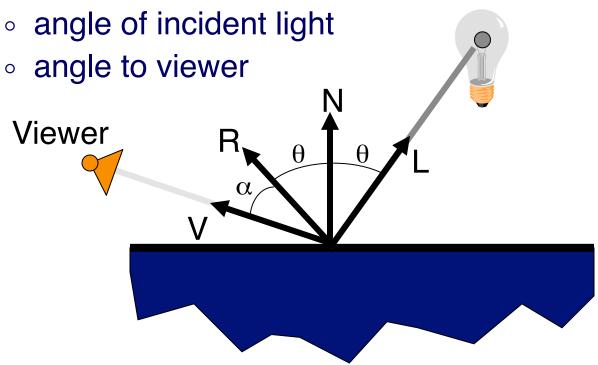


Specular Reflection



How much light is seen?

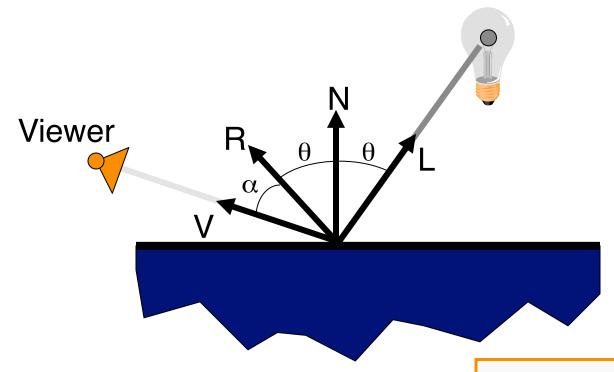
Depends on:



Specular Reflection



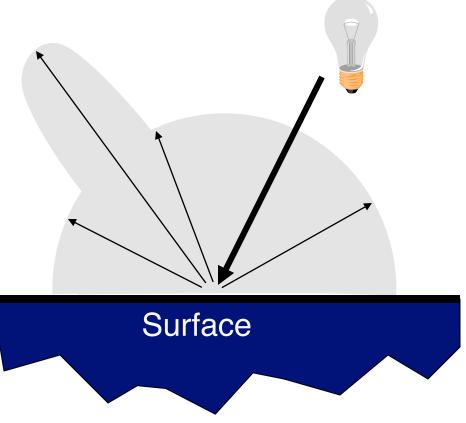
- Phong Model
 - $(\cos \alpha)^n$ This is a (vaguely physically-motivated) hack!



$$I_S = K_S(V \cdot R)^n I_L$$



- Simple analytic model:
 - diffuse reflection +
 - specular reflection +
 - emission +
 - "ambient"

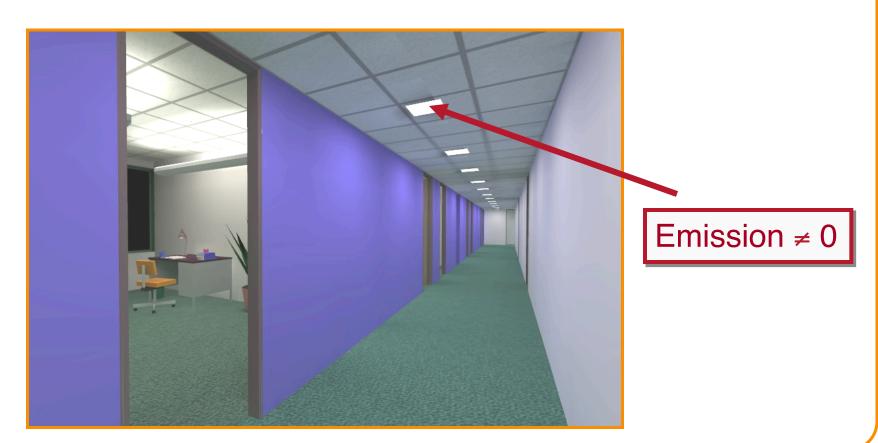


Emission



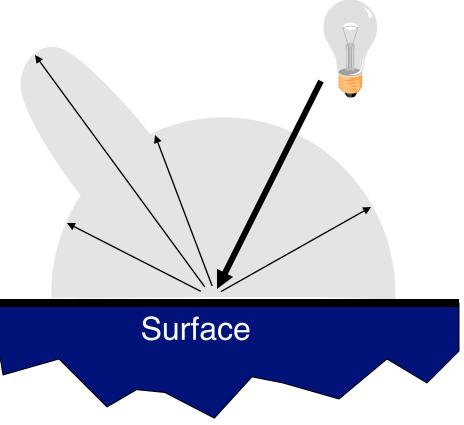
Represents light emanating directly from surface

Note: does not automatically act as light source!
 Does not affect other surfaces in scene!





- Simple analytic model:
 - diffuse reflection +
 - specular reflection +
 - emission +
 - "ambient"



Ambient Term



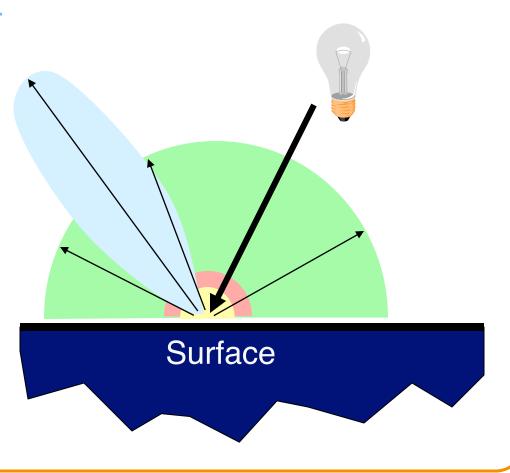
Represents reflection of all indirect illumination



This is a hack (avoids complexity of global illumination)!

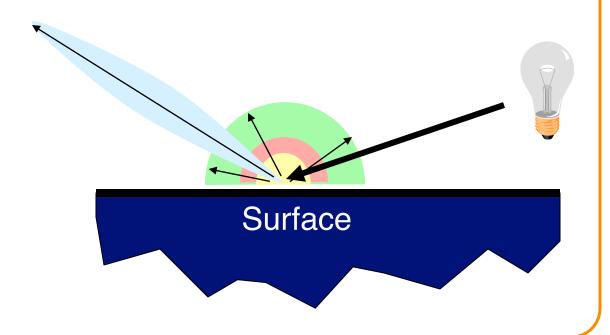


- Simple analytic model:
 - diffuse reflection +
 - specular reflection +
 - emission +
 - "ambient"





- Simple analytic model:
 - diffuse reflection +
 - specular reflection +
 - emission +
 - "ambient"



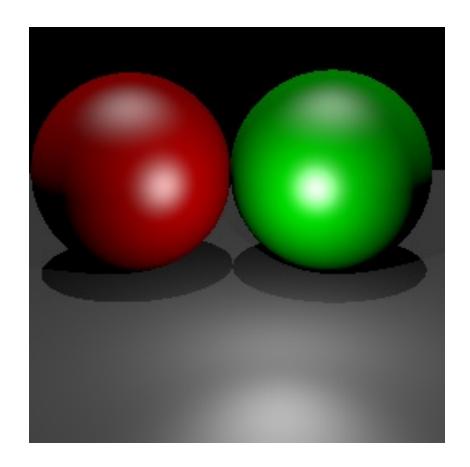


Sum diffuse, specular, emission, and ambient

Phong	$\rho_{ambient}$	$\rho_{diffuse}$	Pspecular	$\rho_{ m total}$
$\phi_i = 60^{\circ}$		*		- F
$\phi_i = 25^{\circ}$	•			
$\phi_i = 0^{\circ}$	•			



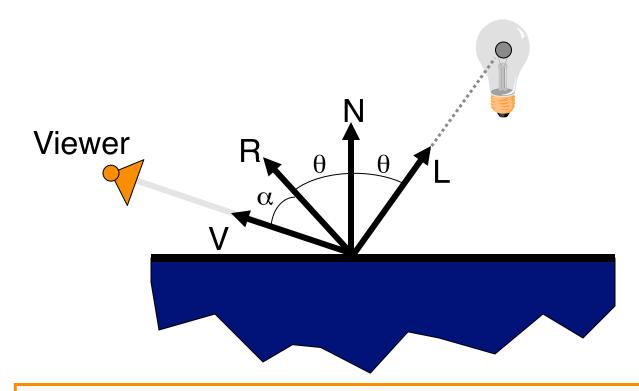
Good model for plastic surfaces, ...



Direct Illumination Calculation



Single light source:

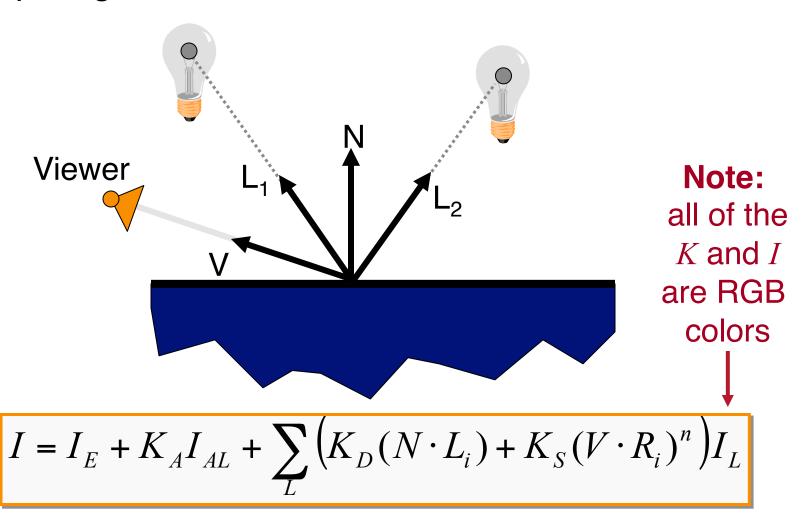


$$I = I_E + K_A I_{AL} + K_D (N \cdot L) I_L + K_S (V \cdot R)^n I_L$$

Direct Illumination Calculation



Multiple light sources:



Overview



- Direct Illumination
 - Emission at light sources
 - Scattering at surfaces
- Global illumination
 - Shadows
 - Transmissions
 - Inter-object reflections



Global Illumination

Global Illumination





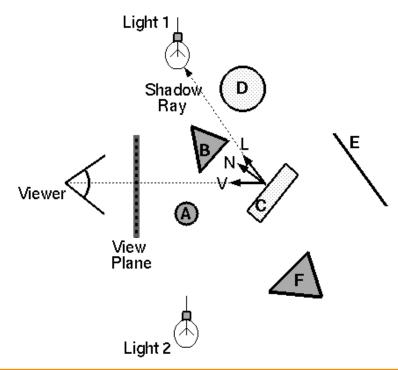
Greg Ward

Ray Casting (last lecture)



Trace primary rays from camera

Direct illumination from unblocked lights only



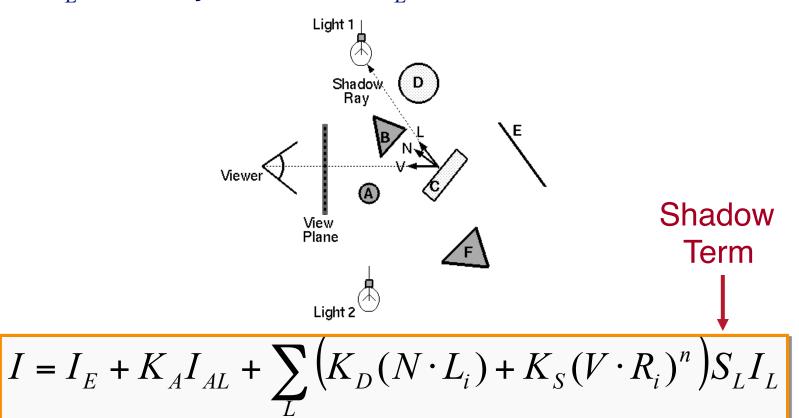
$$I = I_E + K_A I_{AL} + \sum_{L} \left(K_D (N \cdot L_i) + K_S (V \cdot R_i)^n \right) I_L$$

Shadows



Shadow term tells if light sources are blocked

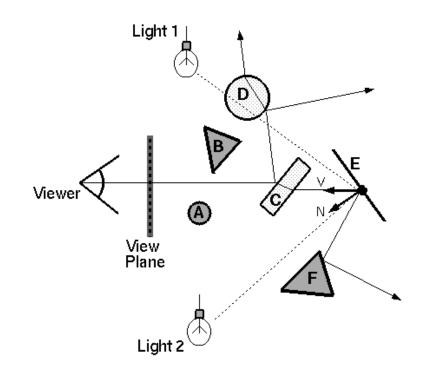
- Cast ray towards each light source
- \circ $S_L = 0$ if ray is blocked, $S_L = 1$ otherwise





Also trace secondary rays from hit surfaces

Mirror reflection and transparency



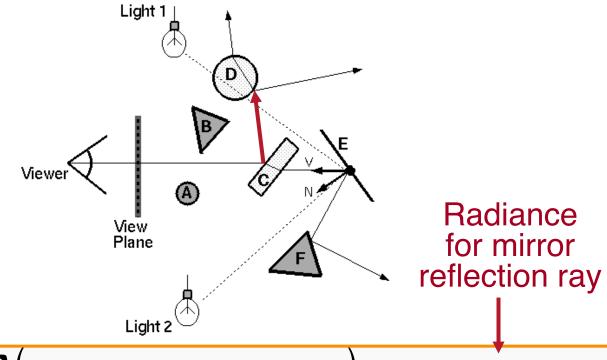
$$I = I_E + K_A I_{AL} + \sum_{L} \left(K_D (N \cdot L_i) + K_S (V \cdot R_i)^n \right) S_L I_L + \left(K_S I_R + K_T I_T \right)^n$$

Mirror reflections



Trace secondary ray in mirror direction

 Evaluate radiance along secondary ray and include it into illumination model



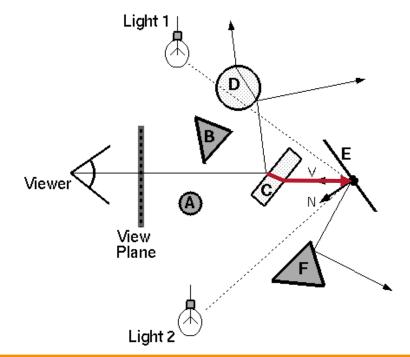
$$I = I_E + K_A I_{AL} + \sum_{T} (K_D (N \cdot L_i) + K_S (V \cdot R_i)^n) S_L I_L + K_S I_R + K_T I_T$$

Transparency



Trace secondary ray in direction of refraction

 Evaluate radiance along secondary ray and include it into illumination model



Radiance for refraction ray

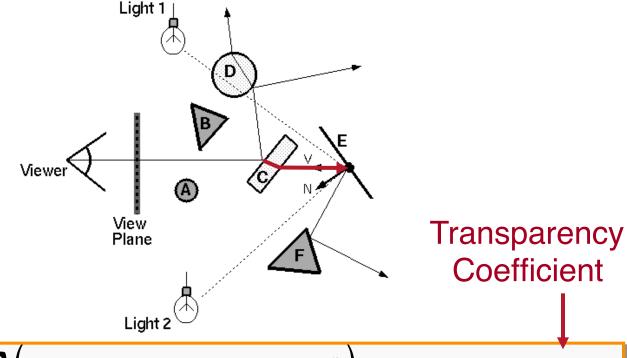
$$I = I_E + K_A I_{AL} + \sum_{T} (K_D (N \cdot L_i) + K_S (V \cdot R_i)^n) S_L I_L + K_S I_R + K_T I_T$$

Transparency



Transparency coefficient is fraction transmitted

- \circ K_T = 1 for translucent object, K_T = 0 for opaque
- \circ 0 < K_T < 1 for object that is semi-translucent



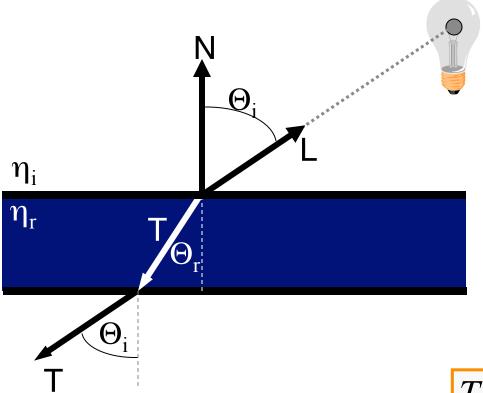
$$I = I_E + K_A I_{AL} + \sum_{T} (K_D (N \cdot L_i) + K_S (V \cdot R_i)^n) S_L I_L + K_S I_R + K_T I_T$$

Refractive Transparency



For thin surfaces, can ignore change in direction

Assume light travels straight through surface



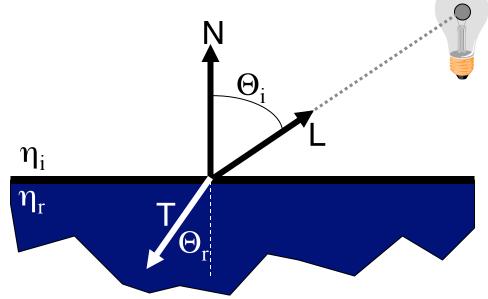
 $T \cong -L$

Refractive Tranparency



For solid objects, apply Snell's law:

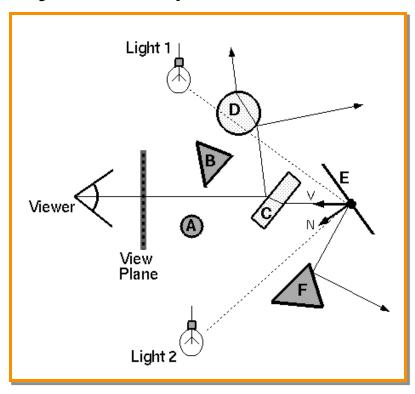
$$\eta_r \sin \Theta_r = \eta_i \sin \Theta_i$$

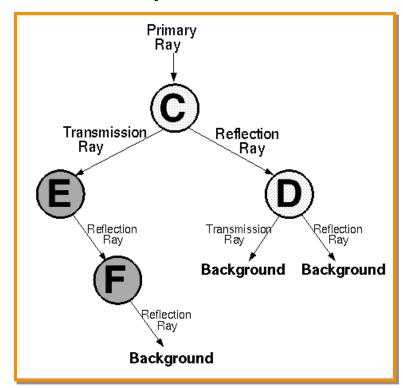


$$T = \left(\frac{\eta_i}{\eta_r} \cos \Theta_i - \cos \Theta_r\right) N - \frac{\eta_i}{\eta_r} L$$



Ray tree represents illumination computation





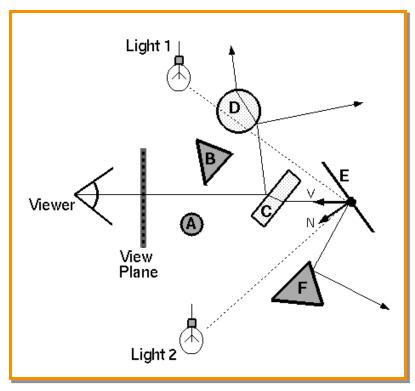
Ray traced through scene

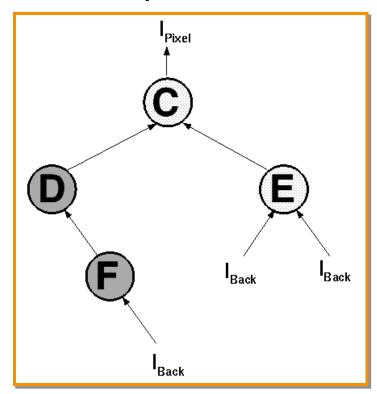
Ray tree

$$I = I_E + K_A I_{AL} + \sum_{L} \left(K_D (N \cdot L_i) + K_S (V \cdot R_i)^n \right) S_L I_L + K_S I_R + K_T I_T$$



Ray tree represents illumination computation





Ray traced through scene

Ray tree

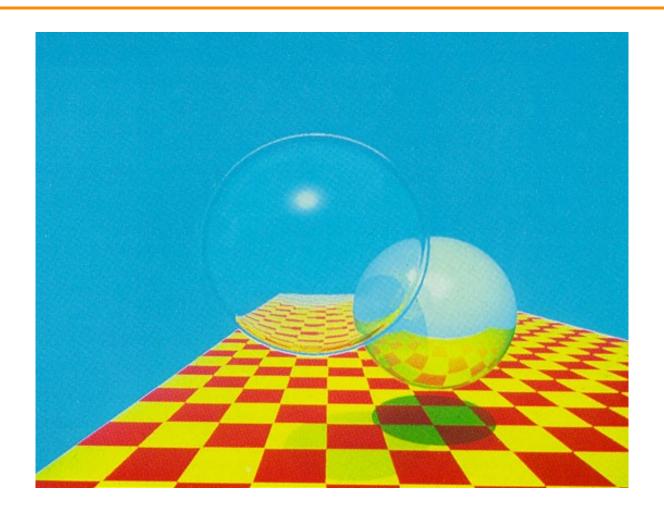
$$I = I_E + K_A I_{AL} + \sum_{L} (K_D (N \cdot L_i) + K_S (V \cdot R_i)^n) S_L I_L + K_S I_R + K_T I_T$$



ComputeRadiance is called recursively

Example





Turner Whitted, 1980

Summary



- Ray casting (direct Illumination)
 - Usually use simple analytic approximations for light source emission and surface reflectance
- Recursive ray tracing (global illumination)
 - Incorporate shadows, mirror reflections, and pure refractions

All of this is an approximation so that it is practical to compute

More on global illumination next time!

Illumination Terminology



- Radiant power [flux] (Φ)
 - Rate at which light energy is transmitted (in Watts).
- Radiant Intensity (I)
 - Power radiated onto a unit solid angle in direction (in Watts/sr)
 - » e.g.: energy distribution of a light source (inverse square law)
- Radiance (L)
 - Radiant intensity per unit projected surface area (in Watts/m²sr)
 - » e.g.: light carried by a single ray (no inverse square law)
- Irradiance (E)
 - Incident flux density on a locally planar area (in Watts/m²)
 - » e.g.: light hitting a surface at a point
- Radiosity (B)
 - Exitant flux density from a locally planar area (in Watts/m²)