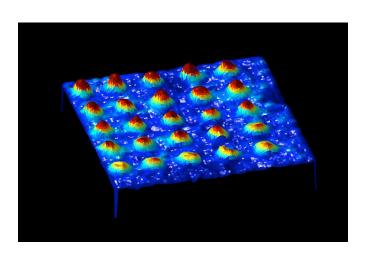
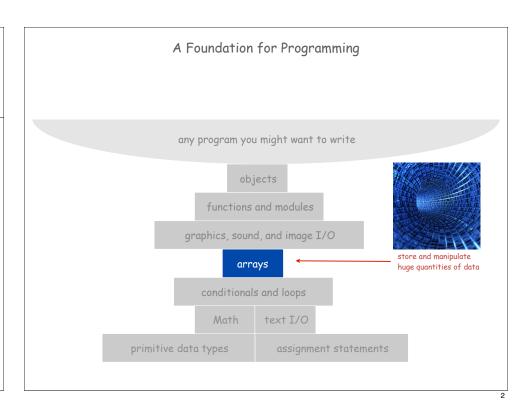
1.4 Arrays





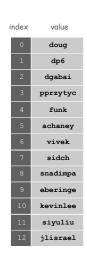
Arrays

This lecture. Store and manipulate huge quantities of data.

Array. Indexed sequence of values of the same type.

Examples.

- 52 playing cards in a deck.
- 5 thousand undergrads at Princeton.
- 1 million characters in a book.
- 10 million audio samples in an MP3 file.
- 4 billion nucleotides in a DNA strand.
- 73 billion Google queries per year.
- 50 trillion cells in the human body.
- 6.02×10^{23} particles in a mole.



Many Variables of the Same Type

Goal. 10 variables of the same type.

```
// Tedious and error-prone code.
double a0, a1, a2, a3, a4, a5, a6, a7, a8, a9;
a0 = 0.0;
a1 = 0.0;
a2 = 0.0;
a3 = 0.0;
a4 = 0.0;
a5 = 0.0;
a6 = 0.0;
a7 = 0.0;
a8 = 0.0;
a9 = 0.0;
...
a4 = 3.0;
...
double x = a4 + a8;
```

Many Variables of the Same Type

Goal. 10 variables of the same type.

```
// Easy alternative.
double[] a = new double[10];
...
a[4] = 3.0;
...
a[8] = 8.0;
...
double x = a[4] + a[8];
```

Many Variables of the Same Type

Goal. 1 million variables of the same type.

```
// Scales to handle large arrays.
double[] a = new double[1000000];
...
a[234567] = 3.0;
...
a[876543] = 8.0;
...
double x = a[234567] + a[876543];
```

Arrays in Java

Java has special language support for arrays.

- To make an array: declare, create, and initialize it.
- To access element i of array named a, use a[i].
- Array indices start at 0.

Arrays in Java

Java has special language support for arrays.

- To make an array: declare, create, and initialize it.
- To access element i of array named a, use a[i].
- Array indices start at 0.

Compact alternatives: Declare, create, and initialize in one statement.

• Default: all entries automatically set to 0.

,

Sample Array Code: Vector Dot Product

Dot product. Given two vectors x[] and y[] of length n, their dot product is the sum of the products of their corresponding components.

```
double[] x = { 0.3, 0.6, 0.1 };
double[] y = { 0.5, 0.1, 0.4 };

double sum = 0.0;
for (int i = 0; i < N; i++)
    sum += x[i]*y[i];</pre>
```

i	x[i]	y[i]	x[i]*y[i]	sum	
				0	_
0	.30	.50	.15	.15	
1	. 60	.10	.06	.21	
2	.10	.40	.04	.25	
				.25	

Array Processing Examples

```
double[] a = new double[N];
for (int i = 0; i < N; i++)
    a[i] = Math.random();</pre>
```

create an array with N random values

```
for (int i = 0; i < N; i++)
    System.out.println(a[i]);</pre>
```

print the array values, one per line

```
double max = Double.NEGATIVE_INFINITY;
for (int i = 0; i < N; i++)
  if (a[i] > max) max = a[i];
```

find the maximum of the array values

```
double[] b = new double[N];
for (int i = 0; i < N; i++)
   b[i] = a[i];</pre>
```

copy to another array

```
double sum = 0.0;
for (int i = 0; i < N; i++)
    sum += a[i];
double average = sum / N;</pre>
```

compute the average of the array values

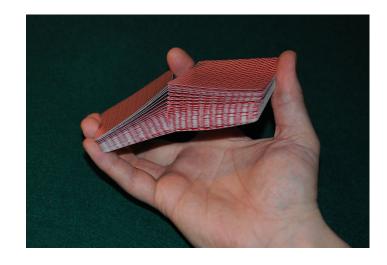
```
for (int i = 0; i < N/2; i++)
{
   double temp = b[i];
   b[i] = b[N-1-i];
   b[N-i-1] = temp;
}</pre>
```

reverse the elements within the array

Mumbo-Jumbo Demystification, Part 1

```
public class Gambler {
   public static void main(String[] args) {
      int stake = Integer.parseInt(args[0]);
      int goal = Integer.parseInt(args[1]);
      int trials = Integer.parseInt(args[2]);
      . . .
      . . .
   }
}
```

Shuffling a Deck



Setting Array Values at Compile Time

Ex. Print a random card.

```
String[] rank =
{
    "2", "3", "4", "5", "6", "7", "8", "9",
    "10", "Jack", "Queen", "King", "Ace"
};

String[] suit =
{
    "Clubs", "Diamonds", "Hearts", "Spades"
};

int i = (int) (Math.random() * 13); // between 0 and 12
int j = (int) (Math.random() * 4); // between 0 and 3

System.out.println(rank[i] + " of " + suit[j]);
```

Array Challenge 2

Swap the for statements: rank index in inner loop, suit index in outer loop. Now, in which order are they printed?

```
String[] rank = { "2", "3" ..., "King", "Ace" };
String[] suit =
    { "clubs", "diamonds", "hearts", "spades" };

String[] deck = new String[52];
for (int j = 0; j < 4; j++)
    for (int i = 0; i < 13; i++)
        deck[4*i + j] = rank[i] + " of " + suit[j];

for (int i = 0; i < 52; i++)
    System.out.println(deck[i]);</pre>
```

```
A. 2 of clubs
2 of diamonds
2 of hearts
2 of spades
3 of clubs
...
```

B. 2 of clubs 3 of clubs 4 of clubs 5 of clubs 6 of clubs

Array Challenge 1

The following code sets array values to the 52 card values and prints them. In which order are they printed?

```
String[] rank = { "2", "3" ..., "King", "Ace" };
       String[] suit =
        { "clubs", "diamonds", "hearts", "spades" };
       String[] deck = new String[52];
       for (int i = 0; i < 13; i++)
                                                                  typical array
                                                                 processing code
          for (int j = 0; j < 4; j++)
                                                                  changes values
             deck[4*i + j] = rank[i] + " of " + suit[j];
                                                                   at runtime
       for (int i = 0; i < 52; i++)
          System.out.println(deck[i]);
                                    B. 2 of clubs
A. 2 of clubs
                                        3 of clubs
   2 of diamonds
   2 of hearts
                                        4 of clubs
   2 of spades
                                        5 of clubs
   3 of clubs
                                        6 of clubs
```

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these lines swapped from previous slide

Array Challenge 3

The following code sets array values to the 52 card values and prints them. What change to the code will produce the "B" order?

```
String[] rank = { "2", "3" ..., "King", "Ace" };
String[] suit =
    { "clubs", "diamonds", "hearts", "spades" };

String[] deck = new String[52];
for (int i = 0; i < 13; i++)
    for (int j = 0; j < 4; j++)
        deck[4*i + j] = rank[i] + " of " + suit[j];

for (int i = 0; i < 52; i++)
    System.out.println(deck[i]);</pre>
```

```
      A. 2 of clubs
      B. 2 of clubs

      2 of diamonds
      3 of clubs

      2 of hearts
      4 of clubs

      2 of spades
      5 of clubs

      3 of clubs
      6 of clubs

      ...
      ...
```

Shuffling

Goal. Given an array, rearrange its elements in random order.

Shuffling algorithm.

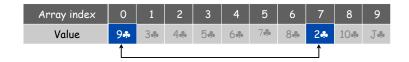
- In iteration i, pick random card from deck[i] through deck[N-1], with each card equally likely.
- Exchange it with deck[i].

```
int N = deck.length;
for (int i = 0; i < N; i++)
{
   int r = i + (int) (Math.random() * (N-i));
   String t = deck[r];
   deck[r] = deck[i];
   deck[i] = t;
}
</pre>
```

Shuffle an Array

Shuffle a deck of cards.

- In ith iteration, put a random element from remainder of deck at index i.
- choose random integer r between i and N-1
- -swap values in positions r and i



random integer = 7

Shuffling a Deck of Cards

```
public class Deck
   public static void main(String[] args)
      String[] suit = { "Clubs", "Diamonds", "Hearts", "Spades" };
      String[] rank = { "2", "3", "4", "5", "6", "7", "8", "9",
                         "10", "Jack", "Queen", "King", "Ace"
      int SUITS = suit.length;
      int RANKS = rank.length;

    avoid "hardwired" constants like 52, 4, and 13.

     int N = SUITS * RANKS;
      String[] deck = new String[N];
                                                                     build the deck
      for (int i = 0; i < RANKS; i++)
         for (int j = 0; j < SUITS; j++)
            deck[SUITS*i + j] = rank[i] + " of " + suit[j];
      for (int i = 0; i < N; i++)
                                                                          shuffle
         int r = i + (int) (Math.random() * (N-i));
         String t = deck[r];
         deck[r] = deck[i];
         deck[i] = t;
      for (int i = 0; i < N; i++)
                                                                  print shuffled deck
         System.out.println(deck[i]);
```

Shuffling a Deck of Cards

% java Deck 5 of Clubs Jack of Hearts 9 of Spades 10 of Spades 9 of Clubs 7 of Spades 6 of Diamonds 7 of Hearts 7 of Clubs 4 of Spades Queen of Diamonds 10 of Hearts 5 of Diamonds Jack of Clubs Ace of Hearts 5 of Spades

% java Deck 10 of Diamonds King of Spades 2 of Spades 3 of Clubs 4 of Spades Queen of Clubs 2 of Hearts 7 of Diamonds 6 of Spades Queen of Spades 3 of Spades Jack of Diamonds 6 of Diamonds 8 of Spades 9 of Diamonds 10 of Spades

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Coupon Collector



Coupon Collector Problem

Coupon collector problem. Given ${\tt N}$ different card types, how many do you have to collect before you have (at least) one of each type?



assuming each possibility is equally likely for each card that you collect

Simulation algorithm. Repeatedly choose an integer \mathtt{i} between 0 and N-1. Stop when we have at least one card of every type.

- Q. How to check if we've seen a card of type i?
- A. Maintain a boolean array so that found[i] is true if we've already collected a card of type i.

Coupon Collector: Java Implementation

```
public class CouponCollector
  public static void main(String[] args)
      int N = Integer.parseInt(args[0]);
      int cardcnt = 0; // number of cards collected
      int valcnt = 0;
                       // number of distinct cards
      // Do simulation.
      boolean[] found = new boolean[N];
      while (valcnt < N)
         int val = (int) (Math.random() * N);
         cardcnt++;
                                                type of next card
         if (!found[val])
                                                (between 0 and N-1)
            valcnt++;
            found[val] = true;
      // all N distinct cards found
      System.out.println(cardcnt);
```

Coupon Collector: Debugging

Debugging. Add code to print contents of all variables.

*** 1	found				ì		valent	cardent
val	0	1	2	3	4	5	Valent	Cardent
	F	F	F	F	F	F	0	0
2	F	F	T	F	F	F	1	1
0	T	F	T	F	F	F	2	2
4	T	F	T	F	T	F	3	3
0	T	F	T	F	T	F	3	4
1	T	T	T	F	T	F	4	5
2	T	T	T	F	T	F	4	6
5	T	T	T	F	T	T	5	7
0	T	T	T	F	T	T	5	8
1	T	T	T	F	T	T	5	9
3	Т	T	T	T	T	T	6	10

Challenge. Debugging with arrays requires tracing many variables.

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Coupon Collector: Mathematical Context

Coupon collector problem. Given N different possible cards, how many do you have to collect before you have (at least) one of each type?

Ex. N = 30 baseball teams. Expect to wait \approx 120 years before all teams win a World Series.

Coupon Collector: Scientific Context

- ${\sf Q}.$ Given a sequence from nature, does it have same characteristics as a random sequence?
- A. No easy answer many tests have been developed.

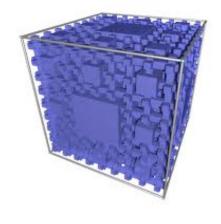
Coupon collector test. Compare number of elements that need to be examined before all values are found against the corresponding answer for a random sequence.



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Two Dimensional Arrays

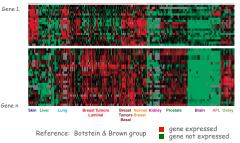
Multidimensional Arrays



Two dimensional arrays.

- Table of data for each experiment and outcome.
- Table of grades for each student and assignments.
- \bullet Table of grayscale values for each pixel in a 2D image.

Mathematical abstraction. Matrix. Java abstraction. 2D array.



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cpi esseu

Two Dimensional Arrays in Java

Declare, create, initialize. Like 1D, but add another pair of brackets.

```
int M = 10;
int N = 3;
double[][] a = new double[M][N];
```

a[][]

Array access.

Use a[i][j] to access entry in row i and column j. Indices start at 0.

Initialize.

This code is implicit (sets all entries to 0).

```
for (int i = 0; i < M; i++)
  for (int j = 0; j < N; j++)
    a[i][j] = 0.0;</pre>
```

	a[2][0]	a[2][1]	a[2][2]
۱j.	a[3][0]	a[3][1]	a[3][2]
	a[4][0]	a[4][1]	a[4][2]
	a[5][0]	a[5][1]	a[5][2]
a[6]	a[6][0]	a[6][1]	a[6][2]
	a[7][0]	a[7][1]	a[7][2]
	a[8][0]	a[8][1]	a[8][2]
	a[9][0]	a[9][1]	a[9][2]

A 10-by-3 array

a[0][0] a[0][1] a[0][2]

a[1][0] a[1][1] a[1][2]

121 [2] [1] [2] [1] [2] [2]

Warning. This implicit code might slow down your program for big arrays.

Setting 2D Array Values at Compile Time

Initialize 2D array by listing values.

```
double[][] p =
{
     { .02, .92, .02, .02, .02 },
     { .02, .02, .32, .32 },
     { .02, .02, .02, .92, .02 },
     { .92, .02, .02, .02, .02 },
     { .47, .02, .47, .02, .02 },
};
```

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Matrix Addition

Matrix addition. Given two N-by-N matrices a and b, define c to be the N-by-N matrix where c[i][j] is the sum a[i][j] + b[i][j].

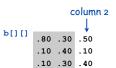
```
double[][] c = new double[N][N];
for (int i = 0; i < N; i++)
  for (int j = 0; j < N; j++)
    c[i][j] = a[i][j] + b[i][j];</pre>
```

Matrix Multiplication

Matrix multiplication. Given two N-by-N matrices a and b, define c to be the N-by-N matrix where c[i][j] is the dot product of the i^{th} row of a and the j^{th} row of b.

```
double[][] c = new double[N][N];
for (int i = 0; i < N; i++)
  for (int j = 0; j < N; j++)
  for (int k = 0; k < N; k++)
    c[i][j] += a[i][k] * b[k][j];</pre>
```

```
a[][] .70 .20 .10 
 .30 .60 .10 ← row 1 
 .50 .10 .40
```



```
c[][[] = .3 *.5

c[][] .59 .32 .41 +.6 *.1

.31 .36 .25 +.1 *.4

.45 .31 .42 = .25
```

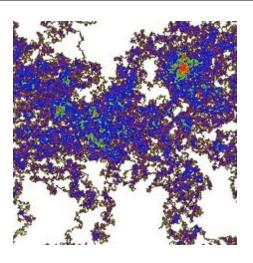
Array Challenge 4

How many multiplications to multiply two N-by-N matrices?

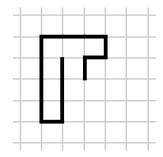
```
double[][] c = new double[N][N];
for (int i = 0; i < N; i++)
  for (int j = 0; j < N; j++)
     for (int k = 0; k < N; k++)
         c[i][j] += a[i][k] * b[k][j];
```

- A. N
- $B. N^2$
- C. N³
- D. N⁴

Application: 2D Random Walks



Application: Self-Avoiding Walks





Self-Avoiding Walk

Model.

- N-by-N lattice.
- Start in the middle.
- Randomly move to a neighboring intersection, avoiding all previously visited intersections.
- Two possible outcomes: escape and dead end





Applications. Polymers, statistical mechanics, etc.

- Q. What fraction of time will you escape in an 5-by-5 lattice?
- Q. In an N-by-N lattice?
- Q. In an N-by-N-by-N lattice?

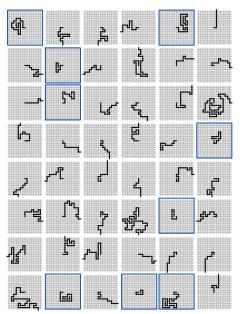
Self-Avoiding Walk: Implementation

```
public class SelfAvoidingWalk
   public static void main(String[] args)
      int N = Integer.parseInt(args[0]);
                                             // lattice size
                                             // number of trials
      int T = Integer.parseInt(args[1]);
      int deadEnds = 0;
                                             // trials ending at dead end
      for ( each trial )
         boolean[][] a = new boolean[N][N]; // intersections visited
         int x = N/2, y = N/2;
                                              // current position
         while ( you're still inside the lattice )
            if ( you're at a dead end )
                                                                              dead end
            { deadEnds++; break; }
            a[x][y] = true;
                                             // mark as visited
            double r = Math.random();
                    (r < 0.25) { if (!a[x+1][y]) x++; }
                                                                              take a random
            else if (r < 0.50) { if (!a[x-1][y]) x--; }
                                                                              step to a new
            else if (r < 0.75) { if (!a[x][y+1]) y++; }
                                                                              intersection
            else if (r < 1.00) { if (!a[x][y-1]) y--; }
      System.out.println(100*deadEnds/T + "% dead ends");
```

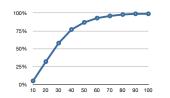
Self-Avoiding Walk: Implementation

```
public class SelfAvoidingWalk
   public static void main(String[] args)
                                             // lattice size
      int N = Integer.parseInt(args[0]);
                                             // number of trials
      int T = Integer.parseInt(args[1]);
      int deadEnds = 0;
                                             // trials ending at dead end
      for (int t = 0; t < T; t++)
         boolean[][] a = new boolean[N][N]; // intersections visited
         int x = N/2, y = N/2;
                                              // current position
         while (x > 0 && x < N-1 && y > 0 && y < N-1)
            if (a[x-1][y] \&\& a[x+1][y] \&\& a[x][y-1] \&\& a[x][y+1])
                                                                              dead end
            { deadEnds++; break; }
            a[x][y] = true;
                                             // mark as visited
            double r = Math.random();
                    (r < 0.25) { if (!a[x+1][y]) x++; }
                                                                              take a random
            else if (r < 0.50) { if (!a[x-1][y]) x--; }
                                                                              step to a new
            else if (r < 0.75) { if (!a[x][y+1]) y++; }
                                                                              intersection
            else if (r < 1.00) { if (!a[x][y-1]) y--; }
      System.out.println(100*deadEnds/T + "% dead ends");
```

Self-Avoiding Walks



```
% java SelfAvoidingWalk 10 100000
5% dead ends
% java SelfAvoidingWalk 20 100000
% java SelfAvoidingWalk 30 100000
58% dead ends
% java SelfAvoidingWalk 40 100000
77% dead ends
% java SelfAvoidingWalk 50 100000
87% dead ends
% java SelfAvoidingWalk 60 100000
93% dead ends
% java SelfAvoidingWalk 70 100000
96% dead ends
% java SelfAvoidingWalk 80 100000
98% dead ends
% java SelfAvoidingWalk 90 100000
99% dead ends
% java SelfAvoidingWalk 100 100000
99% dead ends
```



Summary

Arrays.

- Organized way to store huge quantities of data.
- Almost as easy to use as primitive types.
- Can directly access an element given its index.

Caveats:

- Need to fix size of array ahead of time.
- Don't forget to allocate memory with new.
- Indices start at 0 not 1.
- Out-of-bounds to access a[-1] or a[N] of N element array.
- -in Java: ArrayIndexOutOfBoundsException
- -in C: "ghastly error"

Ahead. Reading in large quantities of data from a file into an array.

Off by One

"You're always off by 1 in this business." - J. Morris

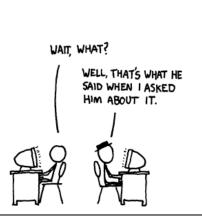
MAN, YOU'RE BEING INCONSISTENT WITH YOUR ARRAY INDICES. SOME ARE FROM ONE, SOME FROM ZERO.

DIFFERENT TASKS CALL FOR DIFFERENT CONVENTIONS. TO GUOTE STANFORD ALGORITHMS EXPERT DONALD KNUTH,

"WHO ARE YOU? HOW DID YOU GET IN MY HOUSE?"







http://imgs.xkcd.com/comics/donald_knuth.png