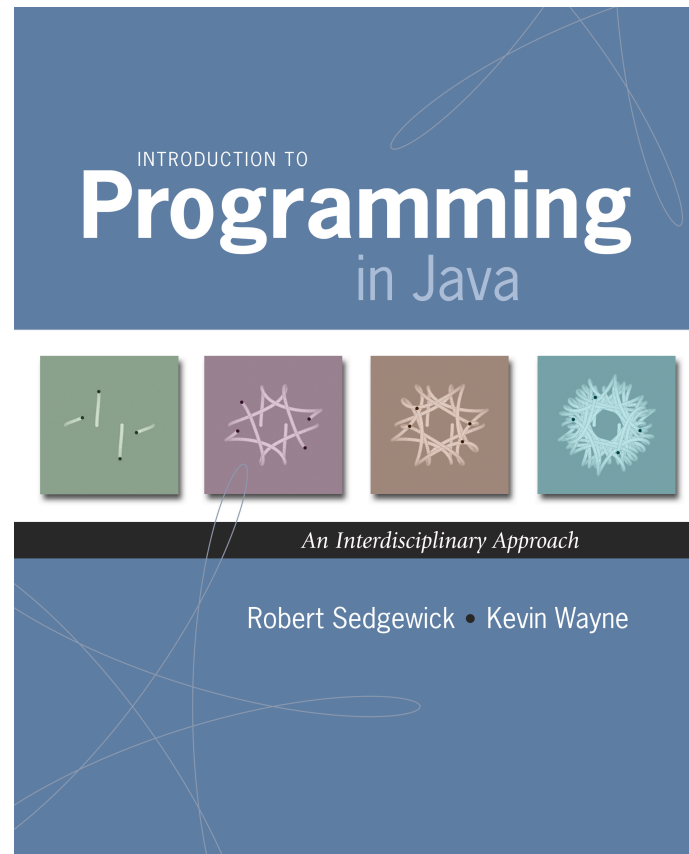


## 4.3 Stacks and Queues

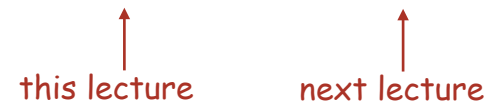
---



# Data Types and Data Structures

**Data types.** Set of values and operations on those values.

- Some are built into the Java language: `int`, `double[]`, `String`, ...
- Most are not: `Complex`, `Picture`, `Stack`, `Queue`, `ST`, `Graph`, ...



**Data structures.**

- Represent data or relationships among data.
- Some are built into Java language: arrays.
- Most are not: linked list, circular list, tree, sparse array, graph, ...



# Collections

## Fundamental data types.

- Set of operations (**add**, **remove**, **test if empty**) on generic data.
- Intent is clear when we insert.
- Which item do we remove?

## Stack. [LIFO = last in first out]

← this lecture

- Remove the item most recently added.
- Ex: cafeteria trays, Web surfing.

## Queue. [FIFO = first in, first out]

- Remove the item least recently added.
- Ex: Hoagie Haven line.

## Symbol table.

← next lecture

- Remove the item with a given key.
- Ex: Phone book.

# Stacks

---

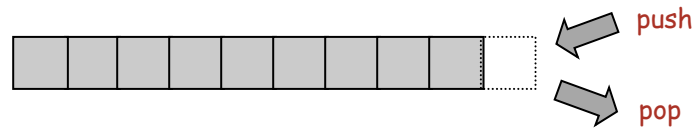


# Stack API

```
public class *StackOfStrings
```

---

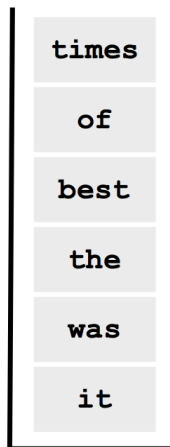
```
    *StackOfStrings() create an empty stack  
    boolean isEmpty() is the stack empty?  
    void push(String item) push a string onto the stack  
    String pop() pop the stack
```



# Stack Client Example 1: Reverse

```
public class Reverse {  
    public static void main(String[] args) {  
        StackOfStrings stack = new StackOfStrings();  
        while (!StdIn.isEmpty()) {  
            String s = StdIn.readString();  
            stack.push(s);  
        }  
        while (!stack.isEmpty()) {  
            String s = stack.pop();  
            StdOut.println(s);  
        }  
    }  
}
```

```
% more tiny.txt  
it was the best of times  
  
% java Reverse < tiny.txt  
times of best the was it
```



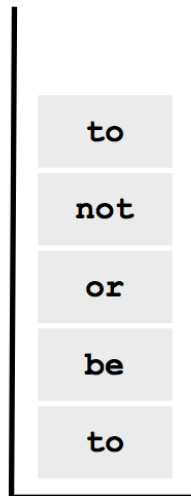
← stack contents when standard input is empty

## Stack Client Example 2: Test Client

```
public static void main(String[] args) {
    StackOfStrings stack = new StackOfStrings();
    while (!StdIn.isEmpty()) {
        String s = StdIn.readString();
        if (s.equals("-"))
            StdOut.println(stack.pop());
        else
            stack.push(s);
    }
}
```

```
% more test.txt
to be or not to - be - - that - - - is

% java StackOfStrings < test.txt
to be not that or be
```



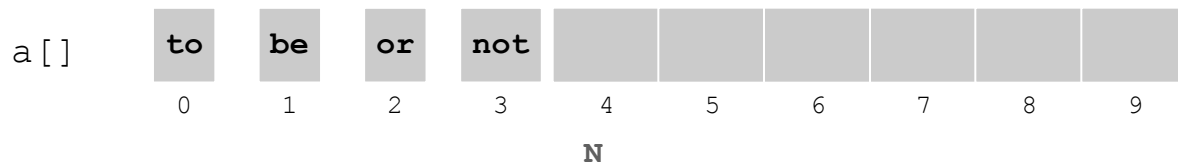
← stack contents just before first pop operation

# Stack: Array Implementation

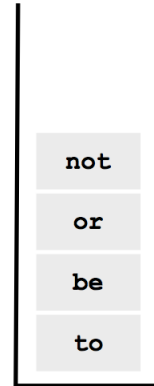
## Array implementation of a stack.

- Use array `a[]` to store `N` items on stack.
- `push()` add new item at `a[N]`.
- `pop()` remove item from `a[N-1]`.

how big to make array? [stay tuned]



stack and array contents after 4<sup>th</sup> push operation



```
public class ArrayStackOfStrings {  
    private String[] a;  
    private int N = 0;  
  
    public ArrayStackOfStrings(int max) { a = new String[max]; }  
    public boolean isEmpty() { return (N == 0); }  
    public void push(String item) { a[N++] = item; }  
    public String pop() { return a[--N]; }  
}
```

temporary solution: make client provide capacity



# Array Stack: Test Client Trace

		StdIn	StdOut	N	a[]				
					0	1	2	3	4
				0					
push		to		1	to				
		be		2	to	be			
		or		3	to	be	or		
		not		4	to	be	or	not	
		to		5	to	be	or	not	to
pop		-	to	4	to	be	or	not	to
		be		5	to	be	or	not	be
		-	be	4	to	be	or	not	be
		-	not	3	to	be	or	not	be
		that		4	to	be	or	that	be
		-	that	3	to	be	or	that	be
		-	or	2	to	be	or	that	be
		-	be	1	to	be	or	that	be
		is		2	to	is	or	not	to

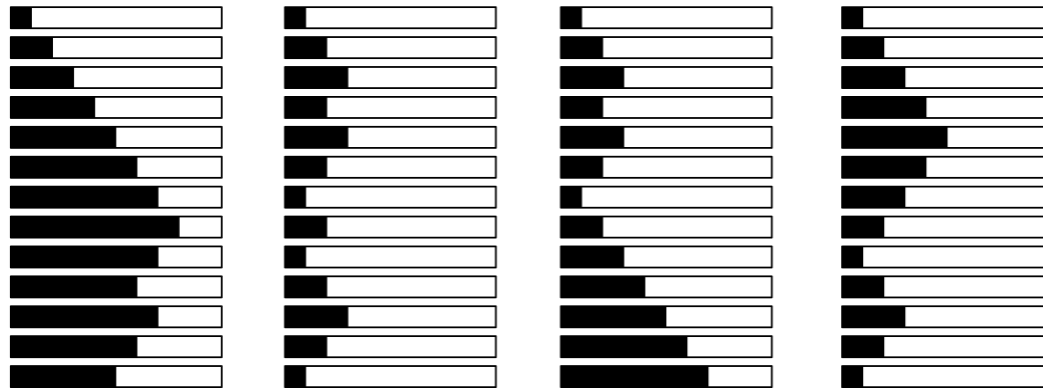
## Array Stack: Performance

**Running time.** Push and pop take constant time.

**Memory.** Proportional to client-supplied capacity, **not** number of items.

**Problem.**

- API does not take capacity as argument (bad to change API).
- Client might not know what capacity to use.
- Client might use multiple stacks.



**Challenge.** Stack where capacity is not known ahead of time.

# Linked Lists

---

# Sequential vs. Linked Allocation

**Sequential allocation.** Put items one after another.

- TOY: consecutive memory cells.
- Java: array of objects.

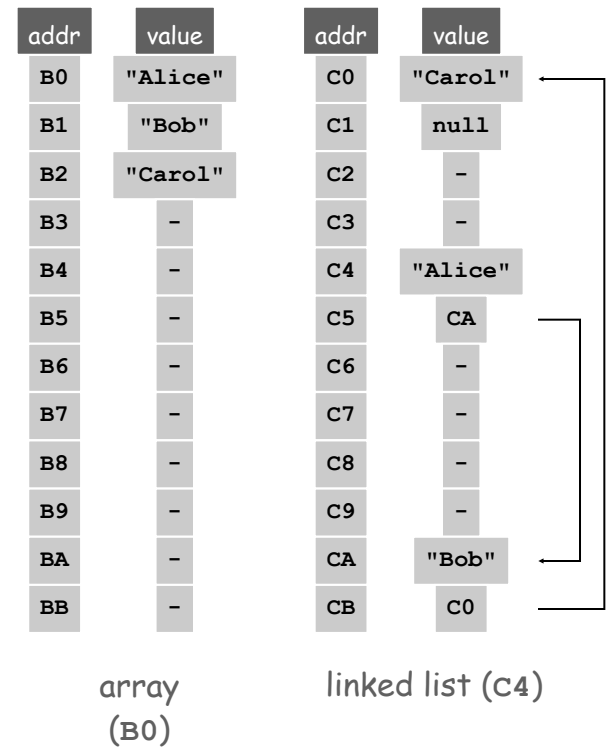
**Linked allocation.** Include in each object a **link** to the next one.

- TOY: link is memory address of next item.
- Java: link is reference to next item.

**Key distinctions.** *get i<sup>th</sup> item*

- Array: random access, fixed size.
- Linked list: sequential access, variable size.

*get next item*



# Linked Lists

## Linked list.

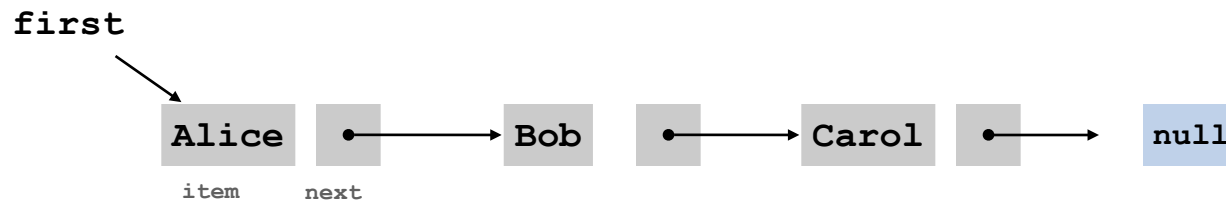
- A recursive data structure.
- An item plus a pointer to another linked list (or empty list).
- Unwind recursion: linked list is a sequence of items.

why private?  
stay tuned

## Node data type.

- A reference to a String.
- A reference to another Node.

```
private class Node {  
    private String item;  
    private Node next;  
}
```



special pointer value null  
terminates list

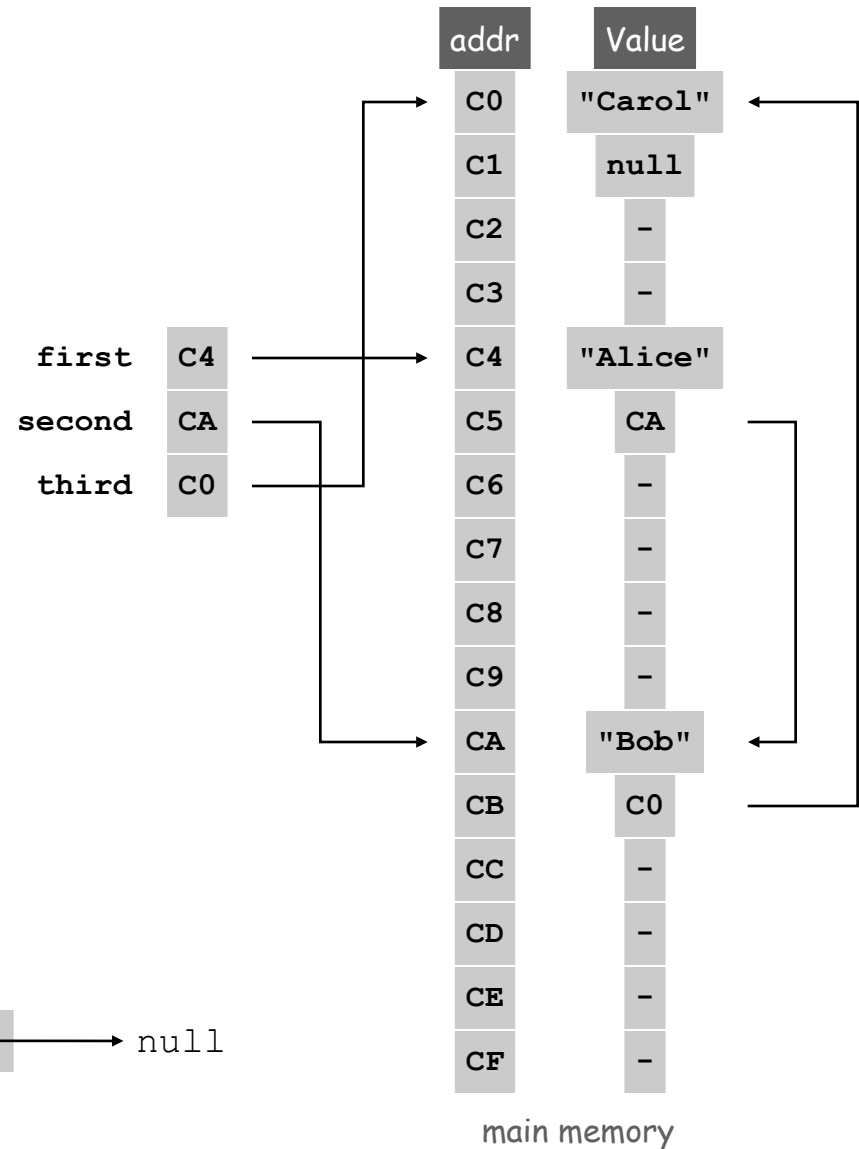
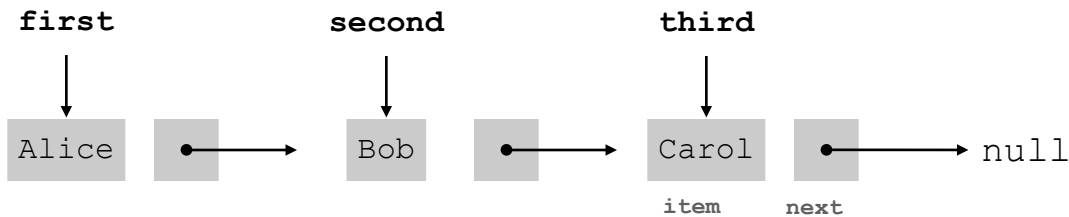
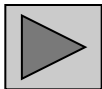
# Building a Linked List

```

Node third = new Node();
third.item = "Carol";
third.next = null;

Node second = new Node();
second.item = "Bob";
second.next = third;

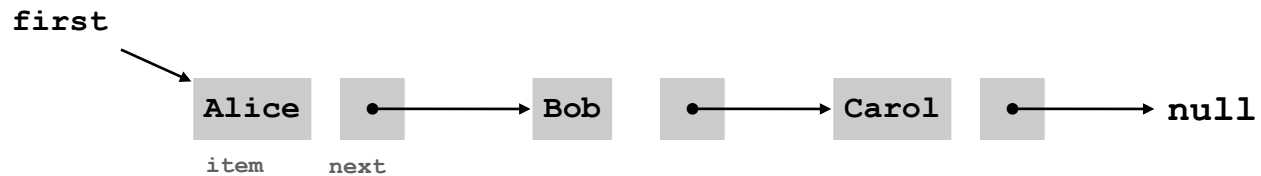
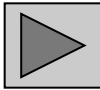
Node first = new Node();
first.item = "Alice";
first.next = second;
    
```



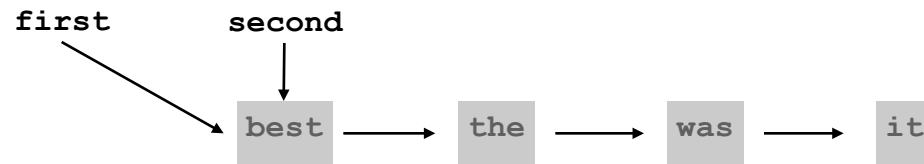
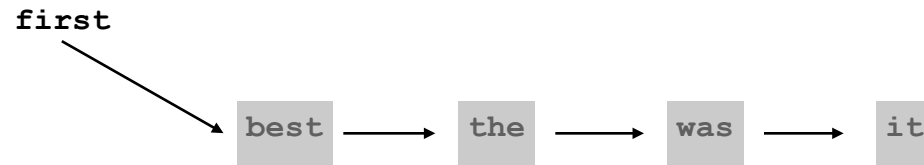
# List Processing Challenge 1

Q. What does the following code fragment do?

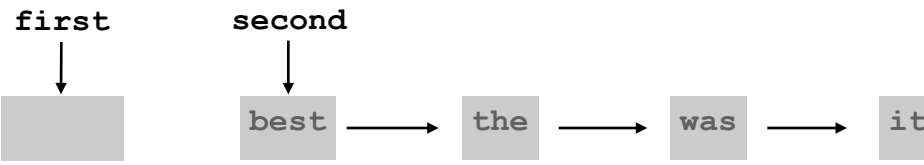
```
for (Node x = first; x != null; x = x.next) {  
    StdOut.println(x.item);  
}
```



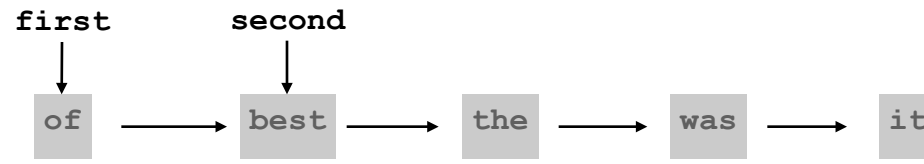
# Stack Push: Linked List Implementation



```
Node second = first;
```



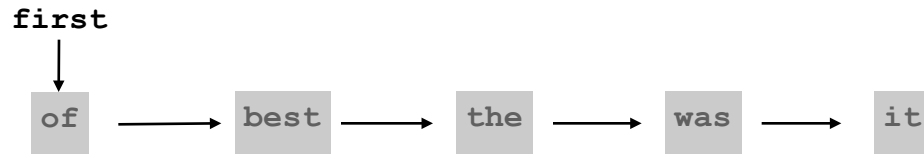
```
first = new Node();
```



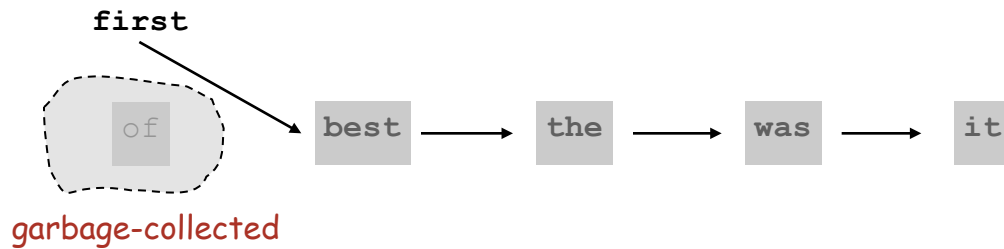
```
first.item = "of";  
first.next = second;
```



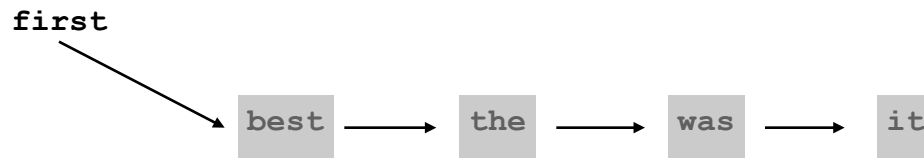
# Stack Pop: Linked List Implementation



```
String item = first.item;
```



```
first = first.next;
```



```
return item;
```

# Stack: Linked List Implementation

```
public class LinkedStackOfStrings {  
    private Node first = null;
```

```
    private class Node {  
        private String item;  
        private Node next;  
    }
```

"inner class"

```
    public boolean isEmpty() { return first == null; }
```

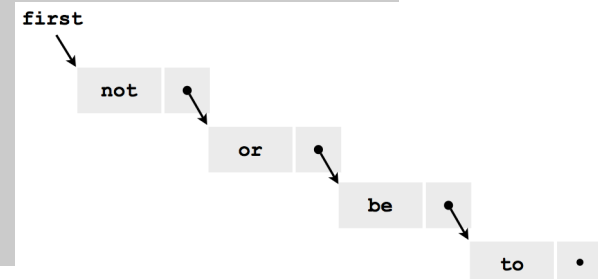
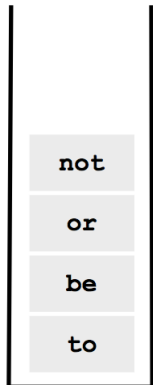
```
    public void push(String item) {  
        Node second = first;  
        first = new Node();  
        first.item = item;  
        first.next = second;  
    }
```

```
    public String pop() {  
        String item = first.item;  
        first = first.next;  
        return item;  
    }
```

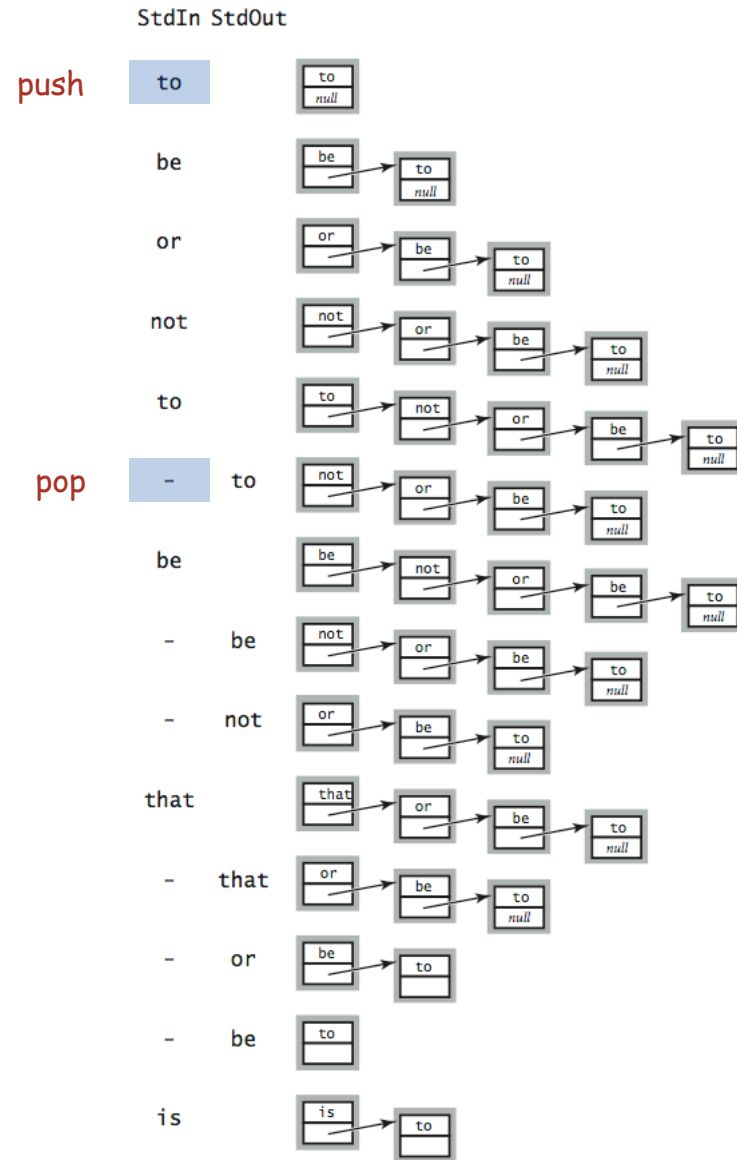
```
}
```

special reserved name

stack and linked list contents  
after 4<sup>th</sup> push operation



# Linked List Stack: Test Client Trace



# Stack Data Structures: Tradeoffs

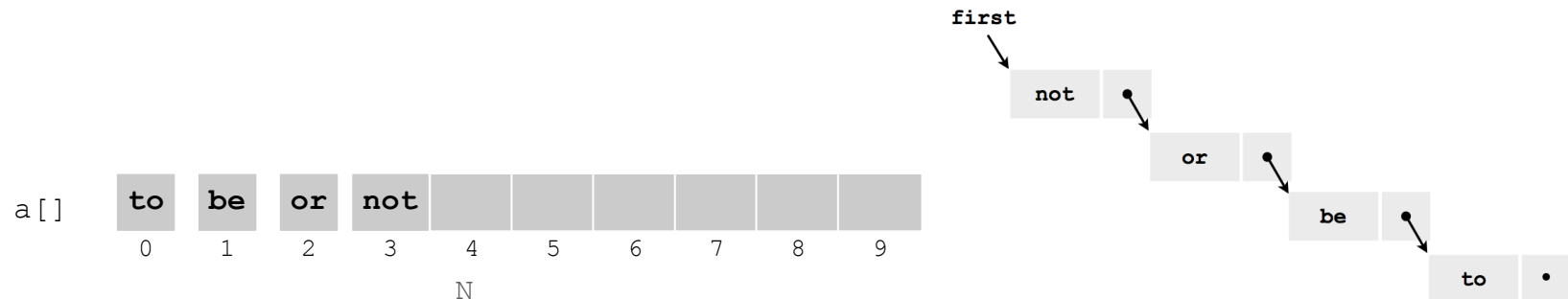
Two data structures to implement stack data type.

## Array.

- Every push/pop operation take constant time.
- **But...** must fix maximum capacity of stack ahead of time.

## Linked list.

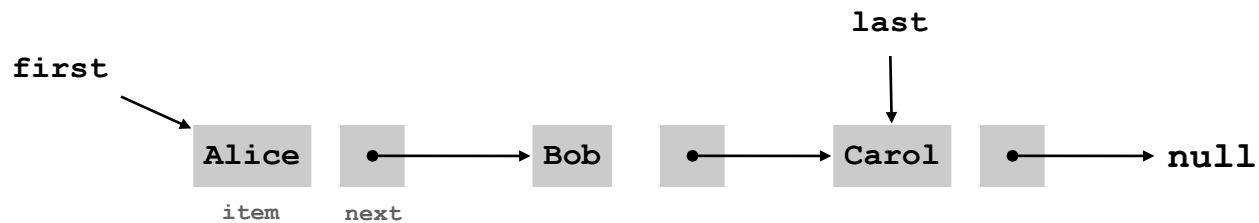
- Every push/pop operation takes constant time.
- Memory is proportional to number of items on stack.
- **But...** uses extra space and time to deal with references.



## List Processing Challenge 2

Q. What does the following code fragment do?

```
Node last = new Node();
last.item = StdIn.readString();
last.next = null;
Node first = last;
while (!StdIn.isEmpty()) {
    last.next = new Node();
    last = last.next;
    last.item = StdIn.readString();
    last.next = null;
}
```



# Parameterized Data Types

---

## Stack: Linked List Implementation

```
public class LinkedStackOfStrings {  
    private Node first = null;  
  
    private class Node {  
        private String item;  
        private Node next;  
    }  
        "inner class"  
  
    public boolean isEmpty() { return first == null; }  
  
    public void push(String item) {  
        Node second = first;  
        first = new Node();  
        first.item = item;  
        first.next = second;  
    }  
  
    public String pop() {  
        String item = first.item;  
        first = first.next;  
        return item;  
    }  
}
```

## Parameterized Data Types

We just implemented: `StackOfStrings`.

We also want: `StackOfInts`, `StackOfURLs`, `StackOfVans`, ...

**Strawman.** Implement a separate stack class for each type.

- Rewriting code is tedious and **error-prone**.
- Maintaining cut-and-pasted code is tedious and **error-prone**.





# Generics

Generics. Parameterize stack by a single type.

```
Stack<Apple> stack = new Stack<Apple>();  
Apple a = new Apple();  
Orange b = new Orange();  
stack.push(a);  
stack.push(b); // compile-time error  
a = stack.pop();
```

"stack of apples"

parameterized type

sample client

can't push an orange onto  
a stack of apples

## Generic Stack: Linked List Implementation

```
public class Stack<Item> {  
    private Node first = null;  
  
    private class Node {  
        private Item item;  
        private Node next;  
    }  
  
    public boolean isEmpty() { return first == null; }  
  
    public void push(Item item) {  
        Node second = first;  
        first = new Node();  
        first.item = item;  
        first.next = second;  
    }  
  
    public Item pop() {  
        Item item = first.item;  
        first = first.next;  
        return item;  
    }  
}
```

parameterized type name  
(chosen by programmer)

# Autoboxing

**Generic stack implementation.** Only permits reference types.

**Wrapper type.**

- Each primitive type has a **wrapper** reference type.
- Ex: `Integer` is wrapper type for `int`.

**Autoboxing.** Automatic cast from primitive type to wrapper type.

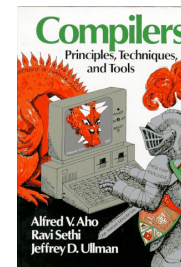
**Autounboxing.** Automatic cast from wrapper type to primitive type.

```
Stack<Integer> stack = new Stack<Integer>();  
stack.push(17);      // autobox   (int -> Integer)  
int a = stack.pop(); // auto-unbox (Integer -> int)
```

# Stack Applications

## Real world applications.

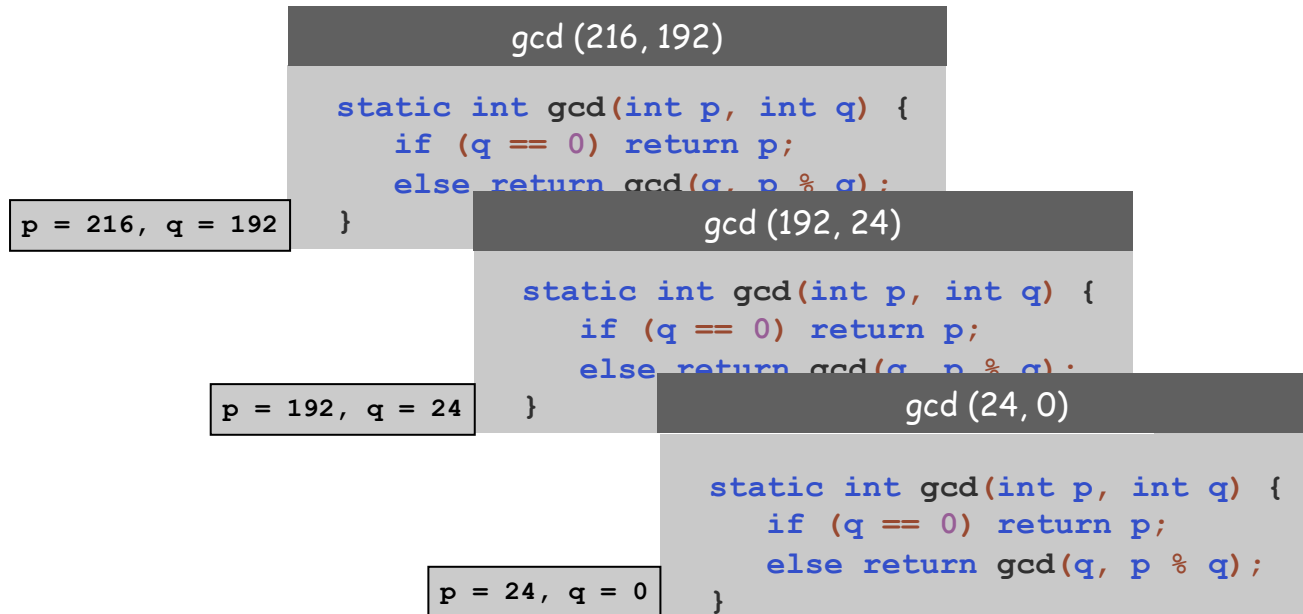
- Parsing in a compiler.
- Java virtual machine.
- Undo in a word processor.
- Back button in a Web browser.
- PostScript language for printers.
- Implementing function calls in a compiler.



# Function Calls

How a compiler implements functions.

- Function call: **push** local environment and return address.
- Return: **pop** return address and local environment.



**Recursive function.** Function that calls itself.

**Note.** Can always use an explicit stack to remove recursion.

# Arithmetic Expression Evaluation

**Goal.** Evaluate infix expressions.

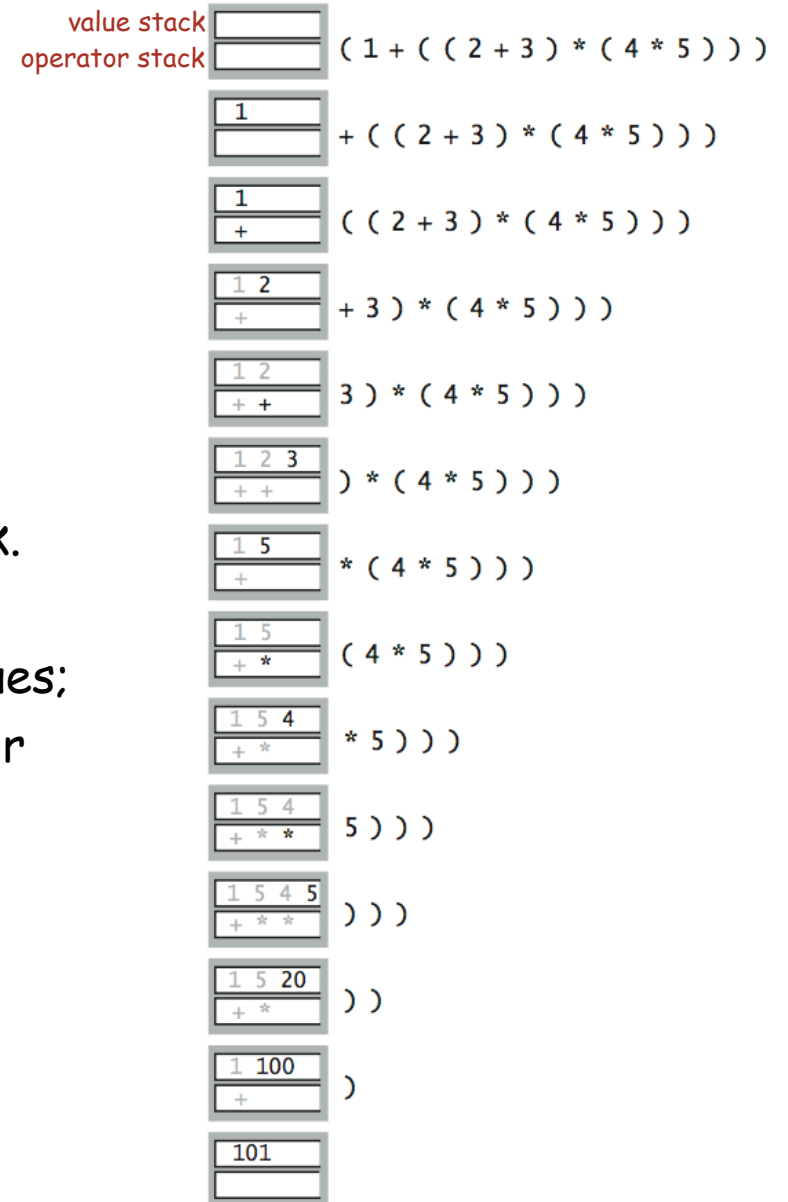
$$( 1 + ( ( 2 + 3 ) * ( 4 * 5 ) ) )$$

↖ operand      ↖ operator

**Two stack algorithm.** [E. W. Dijkstra]

- Value: push onto the value stack.
- Operator: push onto the operator stack.
- Left parens: ignore.
- Right parens: pop operator and two values; push the result of applying that operator to those values onto the operand stack.

**Context.** An interpreter!



# Arithmetic Expression Evaluation

```
public class Evaluate {
    public static void main(String[] args) {
        Stack<String> ops = new Stack<String>();
        Stack<Double> vals = new Stack<Double>();
        while (!StdIn.isEmpty()) {
            String s = StdIn.readString();
            if (s.equals("(")) ;
            else if (s.equals("+")) ops.push(s);
            else if (s.equals("*")) ops.push(s);
            else if (s.equals(")")) {
                String op = ops.pop();
                if (op.equals("+")) vals.push(vals.pop() + vals.pop());
                else if (op.equals("*")) vals.push(vals.pop() * vals.pop());
            }
            else vals.push(Double.parseDouble(s));
        }
        StdOut.println(vals.pop());
    }
}
```

```
% java Evaluate
( 1 + ( ( 2 + 3 ) * ( 4 * 5 ) ) )
101.0
```

## Correctness

**Why correct?** When algorithm encounters an operator surrounded by two values within parentheses, it leaves the result on the value stack.

```
( 1 + ( ( 2 + 3 ) * ( 4 * 5 ) ) )
```

So it's as if the original input were:

```
( 1 + ( 5 * ( 4 * 5 ) ) )
```

Repeating the argument:

```
( 1 + ( 5 * 20 ) )
```

```
( 1 + 100 )
```

```
101
```

**Extensions.** More ops, precedence order, associativity, whitespace.

```
1 + ( 2 - 3 - 4 ) * 5 * sqrt(6*6 + 7*7)
```



# Stack-Based Programming Languages

**Observation 1.** Remarkably, the 2-stack algorithm computes the same value if the operator occurs **after** the two values.

( 1 ( ( 2 3 + ) ( 4 5 \* ) \* ) + )

**Observation 2.** All of the parentheses are redundant!

1 2 3 + 4 5 \* \* +



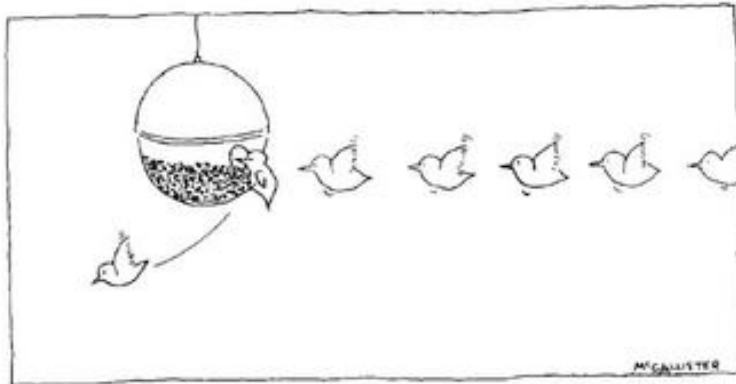
Jan Lukasiewicz

**Bottom line.** Postfix or "reverse Polish" notation.

**Applications.** Postscript, Forth, calculators, Java virtual machine, ...

# Queues

---



Drawing by McCallister; © 1977 The New Yorker Magazine, Inc.



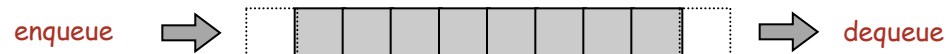
(ONN/NOOM GFRPHIO)

# Queue API

```
public class Queue<Item>
```

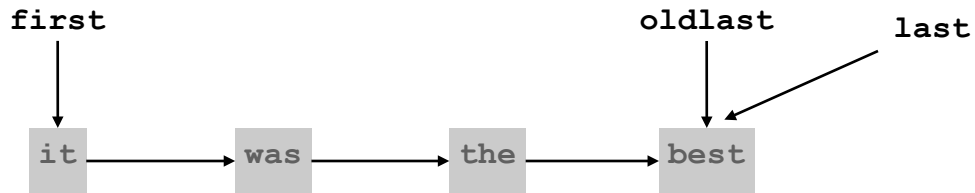
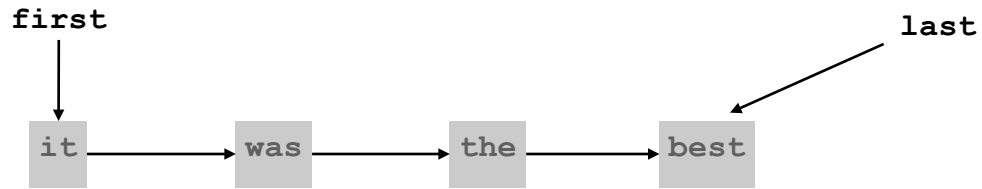
---

Queue<Item>()	<i>create an empty queue</i>
boolean isEmpty()	<i>is the queue empty?</i>
void enqueue(Item item)	<i>enqueue an item</i>
Item dequeue()	<i>dequeue an item</i>
int length()	<i>queue length</i>

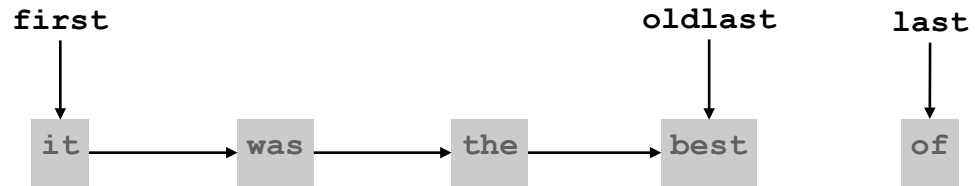


```
public static void main(String[] args) {  
    Queue<String> q = new Queue<String>();  
    q.enqueue("Vertigo");  
    q.enqueue("Just Lose It");  
    q.enqueue("Pieces of Me");  
    q.enqueue("Pieces of Me");  
    while(!q.isEmpty())  
        StdOut.println(q.dequeue());  
}
```

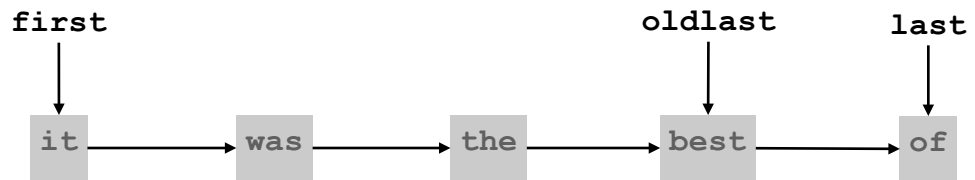
# Enqueue: Linked List Implementation



```
Node oldlast = last;
```

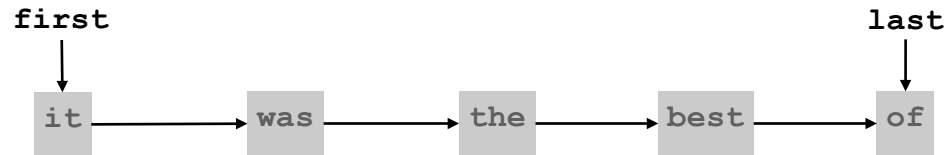


```
last = new Node();  
last.item = "of";  
last.next = null;
```

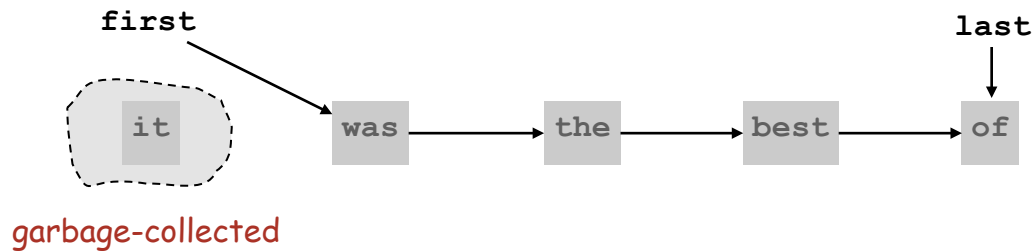


```
oldlast.next = last;
```

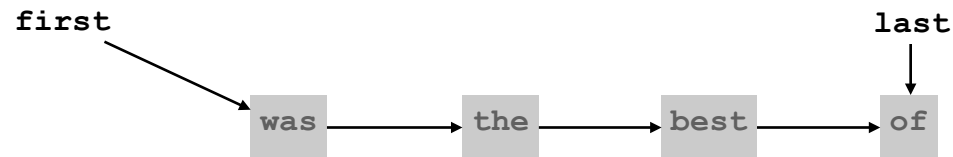
# Deque: Linked List Implementation



```
String item = first.item;
```



```
first = first.next;
```



```
return item;
```

## Queue: Linked List Implementation

```
public class Queue<Item> {  
    private Node first, last;  
  
    private class Node { Item item; Node next; }  
  
    public boolean isEmpty() { return first == null; }  
  
    public void enqueue(Item item) {  
        Node oldlast = last;  
        last = new Node();  
        last.item = item;  
        last.next = null;  
        if (isEmpty()) first = last;  
        else oldlast.next = last;  
    }  
  
    public Item dequeue() {  
        Item item = first.item;  
        first = first.next;  
        if (isEmpty()) last = null;  
        return item;  
    }  
}
```

# Queue Applications

## Some applications.

- iTunes playlist.
- Data buffers (iPod, TiVo).
- Asynchronous data transfer (file IO, pipes, sockets).
- Dispensing requests on a shared resource (printer, processor).

## Simulations of the real world.

- Guitar string.
- Traffic analysis.
- Waiting times of customers at call center.
- Determining number of cashiers to have at a supermarket.

## Conclusions

**Sequential allocation:** supports indexing, fixed size.

**Linked allocation:** variable size, supports sequential access.

**Linked structures are a central programming tool.**

- **Linked lists.**
- **Binary trees.**
- *Graphs.*
- *Sparse matrices.*