

ALGORITHM 2.4 Top-down mergesort

```

public class Merge
{ // Top-down mergesort.
  private static Comparable[] aux; // auxiliary array for merges

  public static void sort(Comparable[] a)
  {
    aux = new Comparable[a.length]; // Allocate space just once.
    sort(a, 0, a.length - 1);
  }

  private static void sort(Comparable[] a, int lo, int hi)
  { // Sort a[lo..hi].
    if (hi <= lo) return;
    int mid = lo + (hi - lo)/2;
    sort(a, lo, mid); // Sort left half.
    sort(a, mid+1, hi); // Sort right half.
    merge(a, lo, mid, hi); // Merge results (code on page 178).
  }
}

```

To sort a subarray $a[lo..hi]$ we divide it into two parts $a[lo..mid]$ and $a[mid+1..hi]$, sort them independently (via recursive calls), and merge the resulting ordered subarrays to produce the result.

	lo	hi	a[]
			0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15
			M E R G E S O R T E X A M P L E
merge(a, 0, 0, 1)	↙	↘	E M R G E S O R T E X A M P L E
merge(a, 2, 2, 3)			E M G R E S O R T E X A M P L E
merge(a, 0, 1, 3)			E G M R E S O R T E X A M P L E
merge(a, 4, 4, 5)			E G M R E S O R T E X A M P L E
merge(a, 6, 6, 7)			E G M R E S O R T E X A M P L E
merge(a, 4, 5, 7)			E G M R E O R S T E X A M P L E
merge(a, 0, 3, 7)			E E G M O R R S T E X A M P L E
merge(a, 8, 8, 9)			E E G M O R R S E T X A M P L E
merge(a, 10, 10, 11)			E E G M O R R S E T A X M P L E
merge(a, 8, 9, 11)			E E G M O R R S A E T X M P L E
merge(a, 12, 12, 13)			E E G M O R R S A E T X M P L E
merge(a, 14, 14, 15)			E E G M O R R S A E T X M P L E
merge(a, 12, 13, 15)			E E G M O R R S A E T X E L M P
merge(a, 8, 11, 15)			E E G M O R R S A E E L M P T X
merge(a, 0, 7, 15)			A E E E E G L M M O P R R S T X

Trace of merge results for top-down mergesort