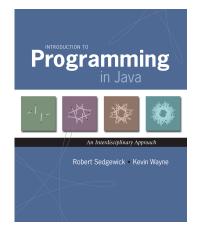
4.3 Stacks and Queues



Introduction to Programming in Java: An Interdisciplinary Approach · Robert Sedgewick and Kevin Wayne · Copyright © 2002–2010 · 4/2/11 10:56 AM

Data types. Set of values and operations on those values.

- Some are built into the Java language: int, double[], string, ...
- Most are not: Complex, Picture, Stack, Queue, ST, Graph, ...

| this lecture | next lecture |
|--------------|--------------|

2

Data structures.

- Represent data or relationships among data.
- Some are built into Java language: arrays.
- Most are not: linked list, circular list, tree, sparse array, graph, ...



Collections

Fundamental data types.

- Set of operations (add, remove, test if empty) on generic data.
- Intent is clear when we insert.
- Which item do we remove?

Stack. [LIFO = last in first out]

- Remove the item most recently added.
- Ex: cafeteria trays, Web surfing.

Queue. [FIFO = first in, first out]

- Remove the item least recently added.
- Ex: Hoagie Haven line.

Symbol table.

— next lecture

3

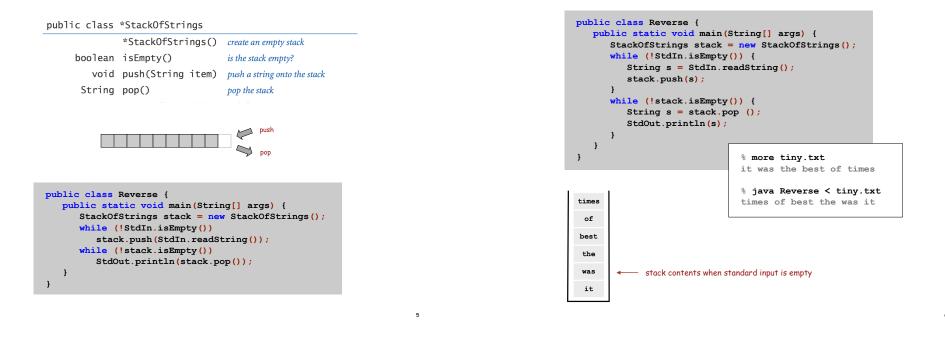
this lecture

- Remove the item with a given key.
- Ex: Phone book.

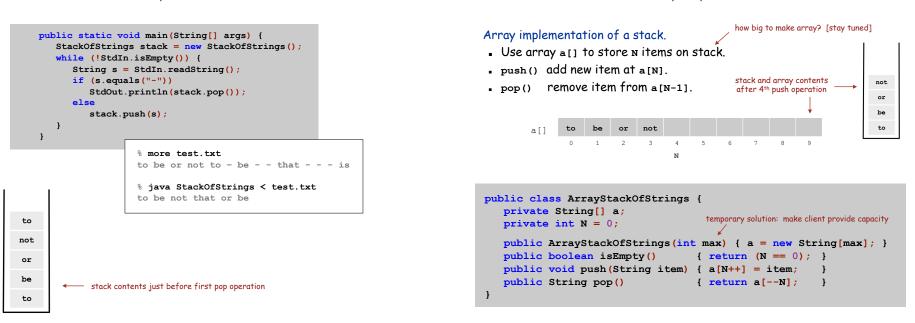
Stacks



Stack: Array Implementation



Stack Client Example 2: Test Client



| | C . 17 | StdOut | N - | | a[] | | | |
|------|--------|--------|-----|----|-----|----|------|----|
| | Stain | | | 0 | 1 | 2 | 3 | 4 |
| | | | 0 | | | | | |
| push | to | | 1 | to | | | | |
| | be | | 2 | to | be | | | |
| | or | | 3 | to | be | or | | |
| | not | | 4 | to | be | or | not | |
| | to | | 5 | to | be | or | not | to |
| рор | - | to | 4 | to | be | or | not | to |
| | be | | 5 | to | be | or | not | be |
| | - | be | 4 | to | be | or | not | be |
| | - | not | 3 | to | be | or | not | be |
| | that | | 4 | to | be | or | that | be |
| | - | that | 3 | to | be | or | that | be |
| | - | or | 2 | to | be | or | that | be |
| | - | be | 1 | to | be | or | that | be |
| | is | | 2 | to | is | or | not | to |

Array Stack: Performance

Running time. Push and pop take constant time.

Memory. Proportional to client-supplied capacity, not number of items.

Problem.

9

11

- API does not take capacity as argument (bad to change API).
- Client might use multiple stacks.
- Client might not know what capacity to use.

Challenge. Stack where capacity is not known ahead of time.

Sequential vs. Linked Allocation

Sequential allocation. Put items one after another.

- TOY: consecutive memory cells.
- Java: array of objects.

Linked allocation. Include in each object a link to the next one.

- TOY: link is memory address of next item.
- Java: link is reference to next item.

Key distinctions. _ get ith item

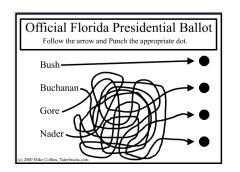
- Array: random access, fixed size.
- Linked list: sequential access, variable size.

get next item



array linked list

Linked Lists



addr

C0

C1

Value

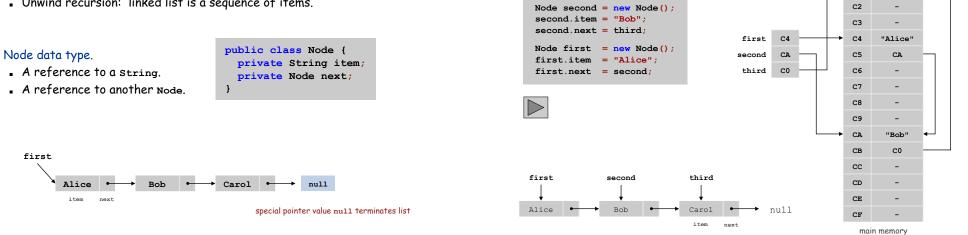
"Carol"

null

_

Linked list.

- A recursive data structure.
- An item plus a pointer to another linked list (or empty list).
- Unwind recursion: linked list is a sequence of items.



14

16

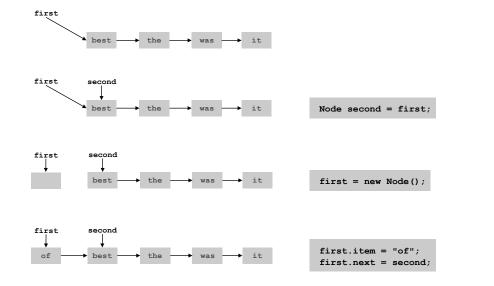
Node third = new Node();

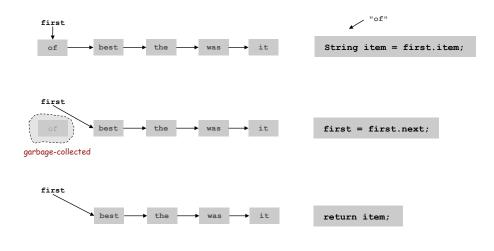
third.item = "Carol";

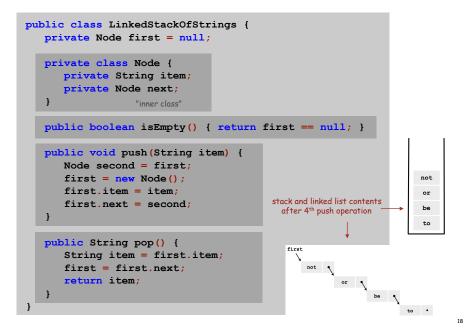
third.next = null;

Stack Push: Linked List Implementation









Stack Data Structures: Tradeoffs

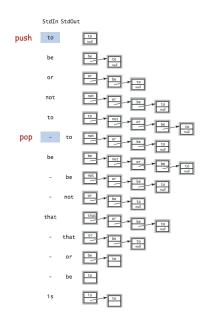
Two data structures to implement Stack data type.

Array.

- Every push/pop operation take constant time.
- But... must fix maximum capacity of stack ahead of time.

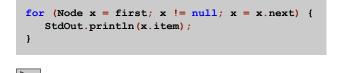
Linked list.

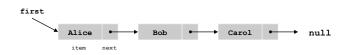
- Every push/pop operation takes constant time.
- Memory is proportional to number of items on stack.
- But... uses extra space and time to deal with references.



List Processing Challenge 1

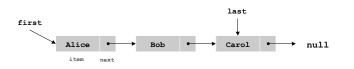
Q. What does the following code fragment do?





Q. What does the following code fragment do?

Node last = new Node(); last.item = StdIn.readString(); last.next = null; Node first = last; while (!StdIn.isEmpty()) { last.next = new Node(); last = last.next; last.item = StdIn.readString(); last.next = null; }



Parameterized Data Types

We implemented: StackOfStrings.

We also want: StackOfURLs, StackOfInts, ...

Strawman. Implement a separate stack class for each type.

- Rewriting code is tedious and error-prone.
- Maintaining cut-and-pasted code is tedious and error-prone.

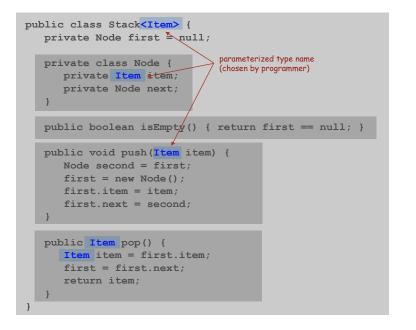
Parameterized Data Types

"stack of apples" parameterized type Stack<Apple> stack = new Stack<Apple>(); Apple a = new Apple(); Orange b = new Orange(); stack.push(a); stack.push(b); // compile-time error a = stack.pop(); sample client can't push an orange onto a stack of apples

Generics

Generics. Parameterize stack by a single type.

Generic Stack: Linked List Implementation



Autoboxing

Generic stack implementation. Only permits reference types.

Wrapper type.

- Each primitive type has a wrapper reference type.
- Ex: Integer is wrapper type for int.

Autoboxing. Automatic cast from primitive type to wrapper type. Autounboxing. Automatic cast from wrapper type to primitive type.

Stack<Integer> stack = new Stack<Integer>();
stack.push(17); // autobox (int -> Integer)
int a = stack.pop(); // autounbox (Integer -> int)

Stack Applications

Real world applications.

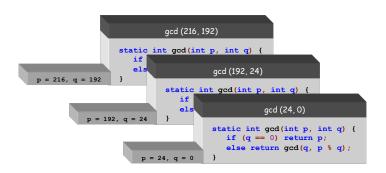
- Parsing in a compiler.
- Java virtual machine.
- Undo in a word processor.
- Back button in a Web browser.
- PostScript language for printers.
- Implementing function calls in a compiler.

Function Calls

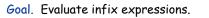
How a compiler implements functions.

- Function call: push local environment and return address.
- Return: pop return address and local environment.

Recursive function. Function that calls itself. Note. Can always use an explicit stack to remove recursion.



26

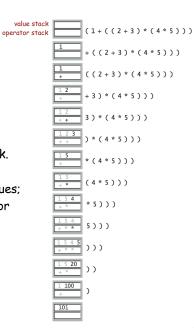


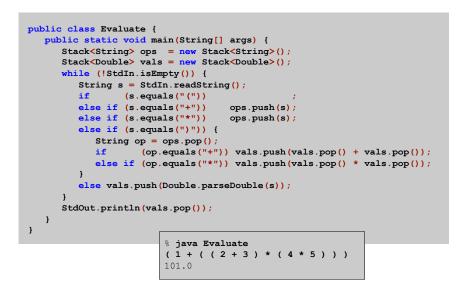
(1+((2+3)*(4*5))) operand operator

Two stack algorithm. [E. W. Dijkstra]

- Value: push onto the value stack.
- Operator: push onto the operator stack.
- Left parens: ignore.
- Right parens: pop operator and two values; push the result of applying that operator to those values onto the operand stack.

Context. An interpreter!





Correctness

Why correct? When algorithm encounters an operator surrounded by two values within parentheses, it leaves the result on the value stack.

(1+((2+3)*(4*5)))

So it's as if the original input were:

(1+(5*(4*5)))

Repeating the argument:

(1+(5*20)) (1+100) 101

Extensions. More ops, precedence order, associativity, whitespace.

1 + (2 - 3 - 4) * 5 * sqrt(6*6 + 7*7)

Stack-Based Programming Languages

Observation 1. Remarkably, the 2-stack algorithm computes the same value if the operator occurs after the two values.

(1((23+)(45*)*)+)

Observation 2. All of the parentheses are redundant!

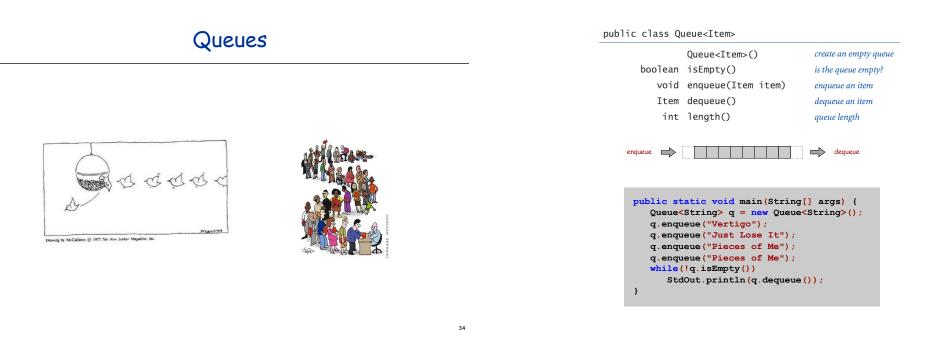
1 2 3 + 4 5 * * +



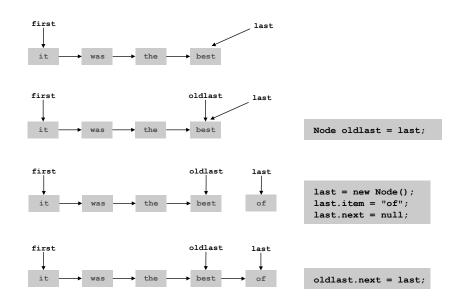
Bottom line. Postfix or "reverse Polish" notation.

Applications. Postscript, Forth, calculators, Java virtual machine, ...

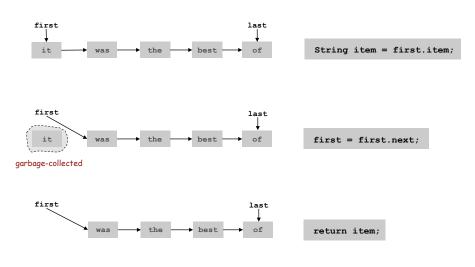
30



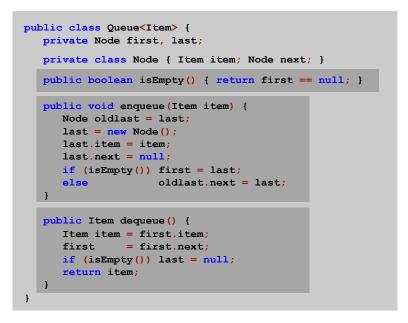
Enqueue: Linked List Implementation



Dequeue: Linked List Implementation







Some applications.

- iTunes playlist.
- Data buffers (iPod, TiVo).
- Asynchronous data transfer (file IO, pipes, sockets).
- Dispensing requests on a shared resource (printer, processor).

Simulations of the real world.

Guitar string.

38

40

- Traffic analysis.
- Waiting times of customers at call center.
- Determining number of cashiers to have at a supermarket.

M/D/1 Queuing Model

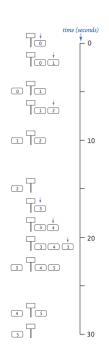
M/D/1 queue.

- Customers are serviced at fixed rate of $\boldsymbol{\mu}$ per minute.
- Customers arrive according to Poisson process at rate of λ per minute.



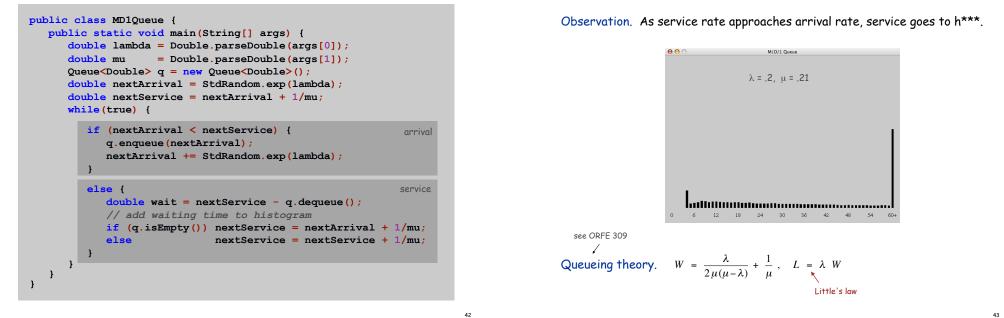
Q. What is average wait time W of a customer?

Q. What is average number of customers L in system?



| | arrival | departure | wait |
|---|---------|-----------|------|
| 0 | 0 | 5 | 5 |
| 1 | 2 | 10 | 8 |
| 2 | 7 | 15 | 8 |
| 3 | 17 | 23 | 6 |
| 4 | 19 | 28 | 9 |
| 5 | 21 | 30 | 9 |

Event-Based Simulation



44

Summary

Stacks and gueues are fundamental ADTs.

- Array implementation.
- Linked list implementation.
- Different performance characteristics.

Many applications.