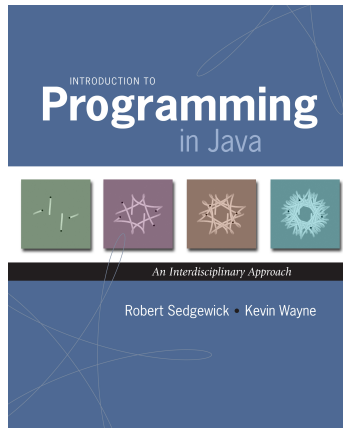


3.2 Creating Data Types



Introduction to Programming in Java: An Interdisciplinary Approach · Robert Sedgewick and Kevin Wayne · Copyright © 2002–2010 · 3/18/11 9:09 AM

Defining Data Types in Java

To define a data type, specify:

- Set of values.
- Operations defined on those values.

Java class. Defines a data type by specifying:

- **Instance variables.** (set of values)
- **Methods.** (operations defined on those values)
- **Constructors.** (create and initialize new objects)

Data type. Set of values and operations on those values.

Basic types.

Data Type	Set of Values	Some Operations
<code>boolean</code>	<code>true</code> , <code>false</code>	not, and, or, xor
<code>int</code>	-2^{31} to $2^{31} - 1$	add, subtract, multiply
<code>String</code>	sequence of Unicode characters	concatenate, compare

Last time. Write programs that **use** data types.

Today. Write programs to **create** our own data types.

Point Charge Data Type

Goal. Create a data type to manipulate point charges.

Set of values. Three real numbers. [position and electrical charge]

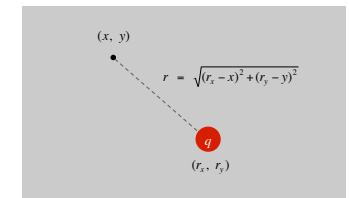
Operations.

- Create a new point charge at (r_x, r_y) with electric charge q .
- Determine electric potential V at (x, y) due to point charge.
- Convert to string.

$$V = k \frac{q}{r}$$

r = distance between (x, y) and (r_x, r_y)

k = electrostatic constant = $8.99 \times 10^9 \text{ N} \cdot \text{m}^2 / \text{C}^2$



Point Charge Data Type

Goal. Create a data type to manipulate point charges.

Set of values. Three real numbers. [position and electrical charge]

API.

```
public class Charge
{
    Charge(double x0, double y0, double q0)
    double potentialAt(double x, double y) electric potential at (x, y) due to charge
    String toString() string representation
}
```

Charge Data Type: A Simple Client

Client program. Uses data type operations to calculate something.

```
public static void main(String[] args) {
    double x = Double.parseDouble(args[0]);
    double y = Double.parseDouble(args[1]);
    Charge c1 = new Charge(.51, .63, 21.3);
    Charge c2 = new Charge(.13, .94, 81.9);
    double v1 = c1.potentialAt(x, y);
    double v2 = c2.potentialAt(x, y);
    StdOut.println(c1);
    StdOut.println(c2);
    StdOut.println(v1 + v2);
}
```

← automatically invokes the toString() method

```
% java Charge .50 .50
21.3 at (0.51, 0.63)
81.9 at (0.13, 0.94)
2.74936907085912e12
```

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Anatomy of Instance Variables

Instance variables. Specifies the set of values.

- Declare outside any method.
- Always use access modifier `private`.
- Use modifier `final` with instance variables that never change.

```
public class Charge
{
    private final double rx, ry;
    private final double q;
    .
    .
}
```

Annotations: *stay tuned*, *instance variable declarations*, *modifiers*

Anatomy of a Constructor

Constructor. Specifies what happens when you create a new object.

```
public Charge ( double x0 , double y0 , double q0 )
{
    rx = x0;
    ry = y0;
    q = q0;
}
```

Annotations: *access modifier*, *no return type*, *constructor name (same as class name)*, *argument variables*, *signature*, *body*, *instance variable names*

Anatomy of a constructor

Invoking a constructor. Use `new` operator to create a new object.

```
Charge c1 = new Charge(.51, .63, 21.3);
Charge c2 = new Charge(.13, .94, 81.9);
```

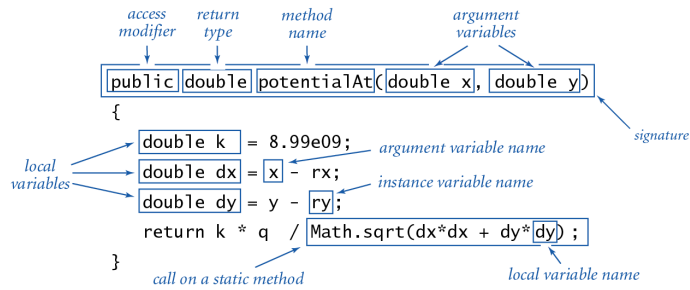
Annotations: *create and initialize object*, *invoke constructor*

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Anatomy of an Instance Method

Method. Define operations on instance variables.



Invoking a method. Use dot operator to invoke a method.

```

double v1 = c1.potentialAt(x, y);
double v2 = c2.potentialAt(x, y);
    
```

Annotations in the diagram:

- `c1`: object name
- `c2`: object name
- `.potentialAt`: invoke method

Potential Visualization

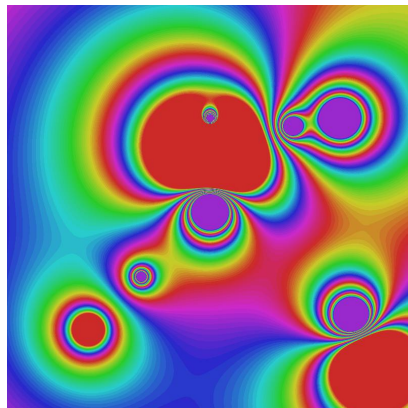
Potential visualization. Read in N point charges from standard input; compute total potential at each point in unit square.

```

% more charges.txt
9
.51 .63 -100
.50 .50 40
.50 .72 10
.33 .33 5
.20 .20 -10
.70 .70 10
.82 .72 20
.85 .23 30
.90 .12 -50
    
```

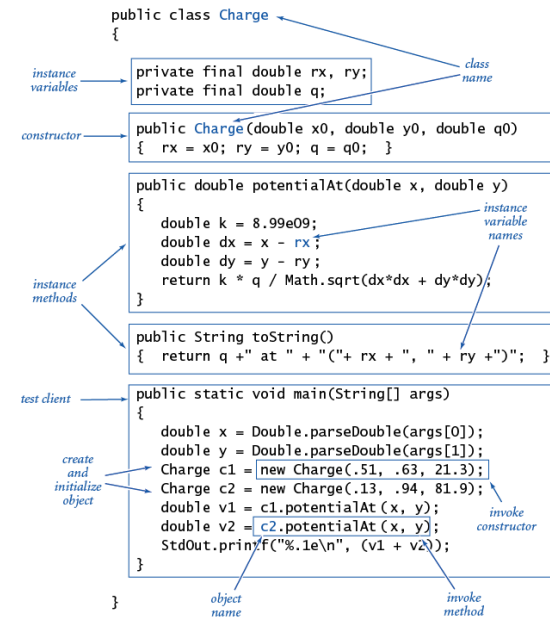
```

% java Potential < charges.txt
    
```



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Anatomy of a Class



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Potential Visualization

Arrays of objects. Allocate memory for the array with `new`; then allocate memory for each individual object with `new`.

```

// read in the data
int N = StdIn.readInt();
Charge[] a = new Charge[N];
for (int i = 0; i < N; i++) {
    double x0 = StdIn.readDouble();
    double y0 = StdIn.readDouble();
    double q0 = StdIn.readDouble();
    a[i] = new Charge(x0, y0, q0);
}
    
```

```
// plot the data
int SIZE = 512;
Picture pic = new Picture(SIZE, SIZE);
for (int i = 0; i < SIZE; i++) {
    for (int j = 0; j < SIZE; j++) {
        double V = 0.0;
        for (int k = 0; k < N; k++) {
            double x = 1.0 * i / SIZE;
            double y = 1.0 * j / SIZE;
            V += a[k].potentialAt(x, y);
        }
        Color color = getColor(V);
        pic.set(i, SIZE-1-j, color);
    }
}
pic.show();
```

$$V = \sum_k (k q_k / r_k)$$

compute color as a function of potential V

(0, 0) is upper left

Turtle Graphics

Turtle Graphics

Goal. Create a data type to manipulate a turtle moving in the plane.
Set of values. Location and orientation of turtle.

API. public class Turtle

Turtle(double x0, double y0, double a0) *create a new turtle at (x0, y0) facing a0 degrees counterclockwise from the x-axis*

void turnLeft(double delta) *rotate delta degrees counterclockwise*

void goForward(double step) *move distance step, drawing a line*

```
// draw a square
Turtle turtle = new Turtle(0.0, 0.0, 0.0);
turtle.goForward(1.0);
turtle.turnLeft(90.0);
turtle.goForward(1.0);
turtle.turnLeft(90.0);
turtle.goForward(1.0);
turtle.turnLeft(90.0);
turtle.goForward(1.0);
turtle.turnLeft(90.0);
```

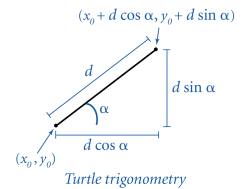
Turtle Graphics

```
public class Turtle {
    private double x, y; // turtle is at (x, y)
    private double angle; // facing this direction

    public Turtle(double x0, double y0, double a0) {
        x = x0;
        y = y0;
        angle = a0;
    }

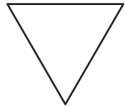
    public void turnLeft(double delta) {
        angle += delta;
    }

    public void goForward(double d) {
        double oldx = x;
        double oldy = y;
        x += d * Math.cos(Math.toRadians(angle));
        y += d * Math.sin(Math.toRadians(angle));
        StdDraw.line(oldx, oldy, x, y);
    }
}
```

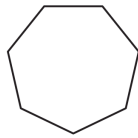


N-gon

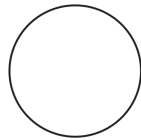
```
public class Ngon {
    public static void main(String[] args) {
        int N = Integer.parseInt(args[0]);
        double angle = 360.0 / N;
        double step = Math.sin(Math.toRadians(angle/2.0));
        Turtle turtle = new Turtle(0.5, 0, angle/2.0);
        for (int i = 0; i < N; i++) {
            turtle.goForward(step);
            turtle.turnLeft(angle);
        }
    }
}
```



3



7

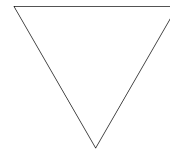


1440

17

Spira Mirabilis

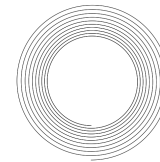
```
public class Spiral {
    public static void main(String[] args) {
        int N = Integer.parseInt(args[0]);
        double decay = Double.parseDouble(args[1]);
        double angle = 360.0 / N;
        double step = Math.sin(Math.toRadians(angle/2.0));
        Turtle turtle = new Turtle(0.5, 0, angle/2.0);
        for (int i = 0; i < 10 * N; i++) {
            step /= decay;
            turtle.goForward(step);
            turtle.turnLeft(angle);
        }
    }
}
```



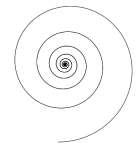
3 1.0



3 1.2



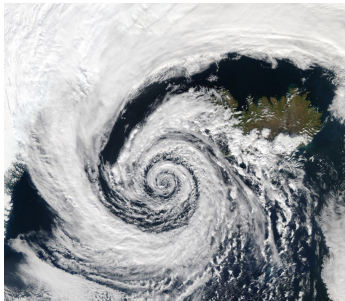
1440 1.00004



1440 1.0004

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Spira Mirabilis in Nature



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Complex Numbers

Goal. Create a data type to manipulate complex numbers.
Set of values. Two real numbers: real and imaginary parts.

API.

```
public class Complex
    Complex(double real, double imag)
Complex plus(Complex b)      sum of this number and b
Complex times(Complex b)    product of this number and b
double abs()                magnitude
String toString()           string representation
```

```
a = 3 + 4i, b = -2 + 3i
a + b = 1 + 7i
a × b = -18 + i
|a| = 5
```

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Relevance. A quintessential mathematical abstraction.

Applications.

- Fractals.
- Impedance in RLC circuits.
- Signal processing and Fourier analysis.
- Control theory and Laplace transforms.
- Quantum mechanics and Hilbert spaces.
- ...

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Complex Number Data Type: A Simple Client

Client program. Uses data type operations to calculate something.

```
public static void main(String[] args) {
    Complex a = new Complex( 3.0, 4.0);
    Complex b = new Complex(-2.0, 3.0);
    Complex c = a.times(b);
    StdOut.println("a = " + a);
    StdOut.println("b = " + b);
    StdOut.println("c = " + c);
}
```

result of c.toString()

```
% java TestClient
a = 3.0 + 4.0i
b = -2.0 + 3.0i
c = -18.0 + 1.0i
```

Remark. Can't write $c = a * b$ since no operator overloading in Java.

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Complex Number Data Type: Implementation

```
public class Complex {
    private final double re;
    private final double imag;           instance variables

    public Complex(double real, double imag) {
        re = real;
        imag = imag;
    }                                     constructor

    public String toString() { return re + " + " + imag + "i"; }
    public double abs() { return Math.sqrt(re*re + im*im); }

    public Complex plus(Complex b) {
        double real = re + b.re;
        double imag = imag + b.im;
        return new Complex(real, imag);
    }                                     creates a Complex object, and returns a reference to it

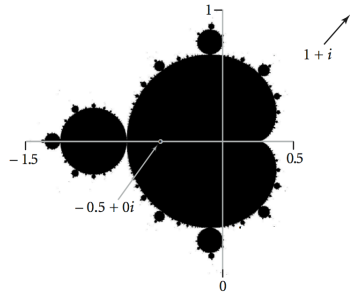
    public Complex times(Complex b) {
        double real = re * b.re - imag * b.im;
        double imag = re * b.im + imag * b.re;
        return new Complex(real, imag);
    }                                     refers to b's instance variable
}                                         methods
```

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Mandelbrot Set

Mandelbrot set. A set of complex numbers.

Plot. Plot (x, y) black if $z = x + y i$ is in the set, and white otherwise.



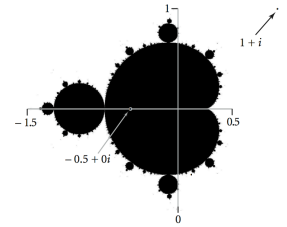
- No simple formula describes which complex numbers are in set.
- Instead, describe using an **algorithm**.

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Mandelbrot Set

Mandelbrot set. Is complex number z_0 in the set?

- Iterate $z_{t+1} = (z_t)^2 + z_0$.
- If $|z_t|$ diverges to infinity, then z_0 is not in set; otherwise z_0 is in set.



t	Z_t
0	$-1/2 + 0i$
1	$-1/4 + 0i$
2	$-7/16 + 0i$
3	$-79/256 + 0i$
4	$-26527/65536 + 0i$
5	$-1443801919/4294967296 + 0i$

$z = -1/2$ is in Mandelbrot set

t	Z_t
0	$1 + i$
1	$1 + 3i$
2	$-7 + 7i$
3	$1 - 97i$
4	$-9407 - 193i$
5	$88454401 + 3631103i$

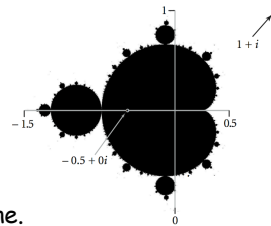
$z = 1 + i$ not in Mandelbrot set

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Plotting the Mandelbrot Set

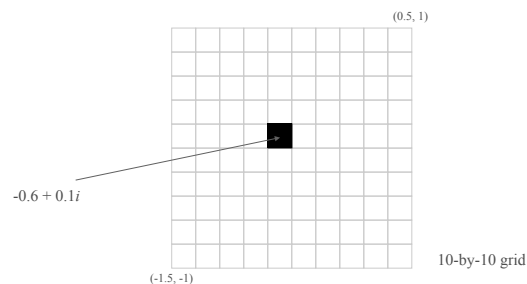
Practical issues.

- Cannot plot infinitely many points.
- Cannot iterate infinitely many times.



Approximate solution.

- Sample from an N -by- N grid of points in the plane.
- Fact: if $|z_t| > 2$ for any t , then z not in Mandelbrot set.
- Pseudo-fact: if $|z_{255}| \leq 2$ then z "likely" in Mandelbrot set.



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Complex Number Data Type: Another Client

Mandelbrot function with complex numbers.

- Is z_0 in the Mandelbrot set?
- Returns white (definitely no) or black (probably yes).

```
public static Color mand(Complex z0) {
    Complex z = z0;
    for (int t = 0; t < 255; t++) {
        if (z.abs() > 2.0) return StdDraw.WHITE;
        z = z.times(z);
        z = z.plus(z0);
    }
    return StdDraw.BLACK;
}
```

More dramatic picture: replace `stdDraw.WHITE` with grayscale or color.

`new Color(255-t, 255-t, 255-t)`

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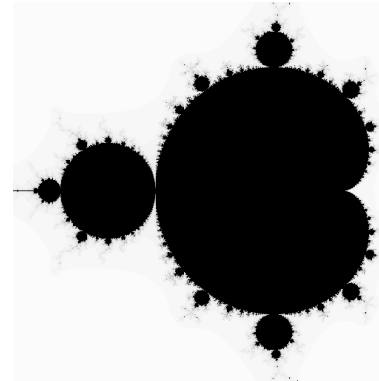
Plot the Mandelbrot set in gray scale.

```
public static void main(String[] args) {
    double xc = Double.parseDouble(args[0]);
    double yc = Double.parseDouble(args[1]);
    double size = Double.parseDouble(args[2]);
    int N = 512;
    Picture pic = new Picture(N, N);

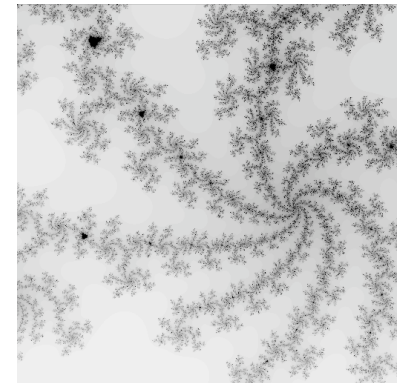
    for (int i = 0; i < N; i++) {
        for (int j = 0; j < N; j++) {
            double x0 = xc - size/2 + size*i/N;
            double y0 = yc - size/2 + size*j/N;
            Complex z0 = new Complex(x0, y0);
            Color color = mand(z0);
            pic.set(i, N-1-j, color);
        }
    }
    pic.show();
}
```

scale to screen coordinates
(0, 0) is upper left

% java Mandelbrot -.5 0 2

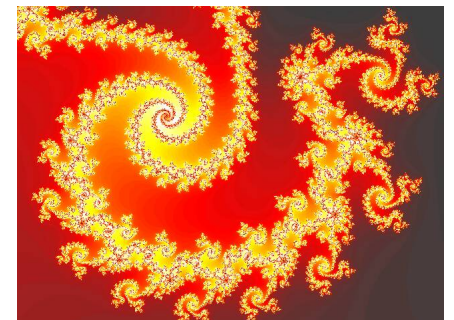
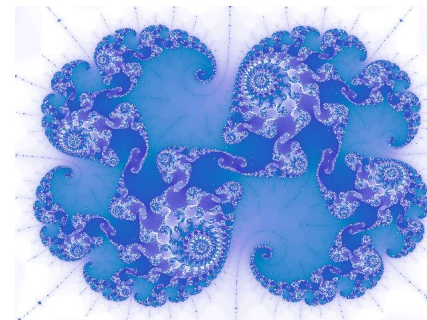
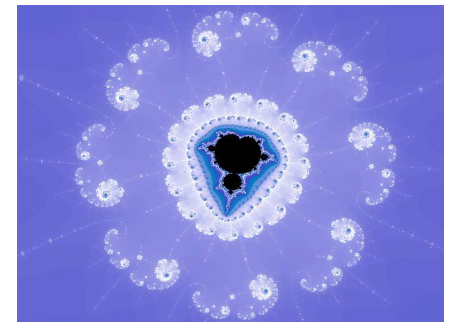
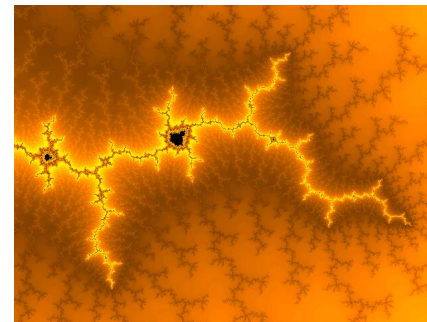
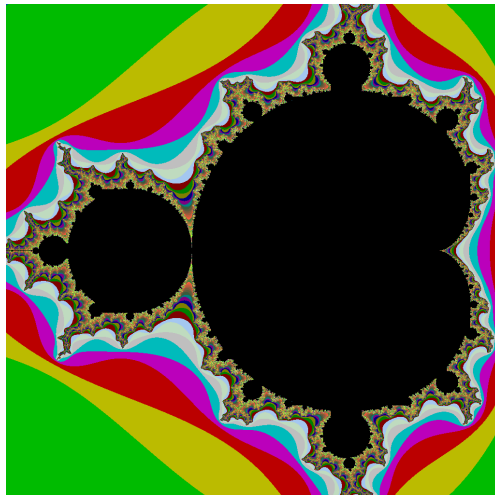


% java Mandelbrot .1045 -.637 .01



Mandelbrot Set

% java ColorMandelbrot -.5 0 2 < mandel.txt



Applications of Data Types

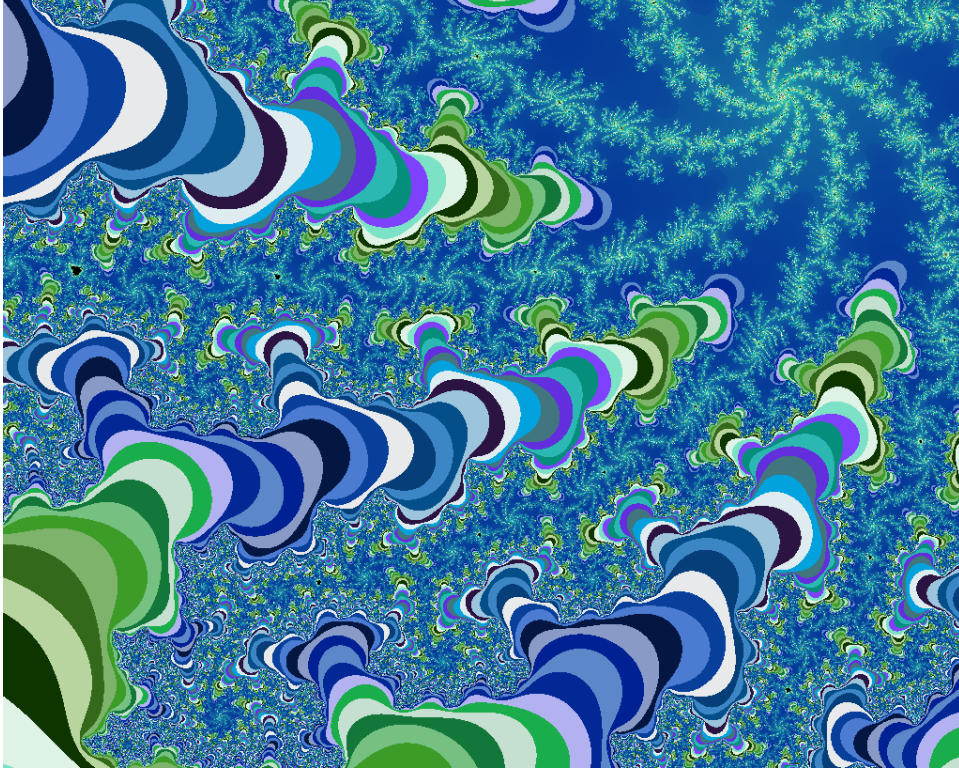
Data type. Set of values and collection of operations on those values.

Simulating the physical world.

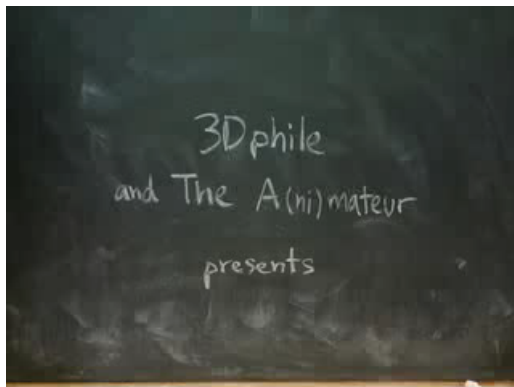
- Java objects model real-world objects.
- Not always easy to make model reflect reality.
- Ex: charged particle, molecule, COS 126 student,

Extending the Java language.

- Java doesn't have a data type for every possible application.
- Data types enable us to add our own abstractions.
- Ex: complex, vector, polynomial, matrix,



Mandelbrot Set Music Video



[http://www.jonathancoulton.com/songdetails/Mandelbrot Set](http://www.jonathancoulton.com/songdetails/Mandelbrot%20Set)