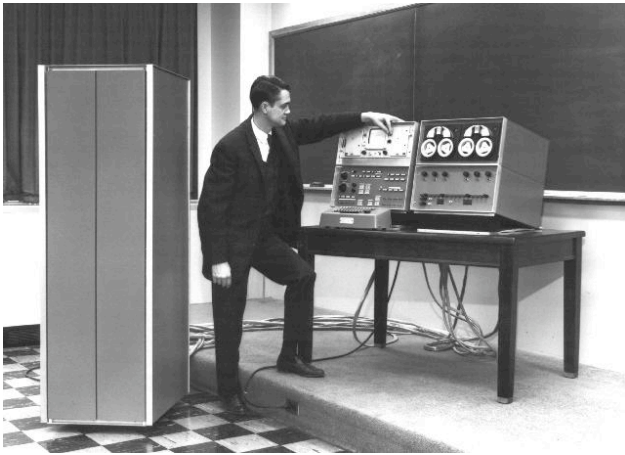


TOY II



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Data representation. Binary and hex.

TOY.

- Box with switches and lights.
- 16-bit memory locations, 16-bit registers, 8-bit pc.
- $4,328 \text{ bits} = (255 \times 16) + (15 \times 16) + (8) = 541 \text{ bytes!}$
- von Neumann architecture.

TOY instruction set architecture. 16 instruction types.

TOY machine language programs. Variables, arithmetic, loops.



What We Do Today

Data representation. Negative numbers.

Input and output. Standard input, standard output.

Manipulate addresses. References (pointers) and arrays.

TOY simulator in Java.



Negative Numbers

How to add and subtract binary numbers

Binary addition facts:

- 0 + 0 = 0
- 0 + 1 = 1 + 0 = 1
- 1 + 1 = 10
- 1 + 1 + 1 = 11 (needed for carries)

Bigger numbers example:

$$\begin{array}{r}
 \begin{array}{cccccccc}
 & & & & & & & 1 \\
 & & & & & & & \swarrow \text{carries} \\
 & & & & & & & \searrow \\
 1 & & & & & & & 1\ 1 \\
 013 & & & & & & & 0\ 0\ 0\ 0\ 1\ 1\ 0\ 1 \\
 + 092 & & & & & & & + 0\ 1\ 0\ 1\ 1\ 1\ 0\ 0 \\
 \hline
 105 & & & & & & & 0\ 1\ 1\ 0\ 1\ 0\ 0\ 1
 \end{array}
 \end{array}$$

OK, but: subtract?

- Subtract by adding a negative integer (e.g., $6 - 4 = 6 + (-4)$)
- OK, but: negative integers?

Representing Negative Integers

TOY words are 16 bits each.

- We could use 16 bits to represent 0 to $2^{16} - 1$.
- We want negative integers too.
- Reserving half the possible bit-patterns for negative seems fair.

Highly desirable property. If x is an integer, then the representation of $-x$, when added to x , is zero.

$$\begin{array}{r}
 \begin{array}{cccccccc}
 x & & & & & & & 0\ 0\ 1\ 1\ 0\ 1\ 0\ 0 \\
 + (-x) & & & & & & & +\ ?\ ?\ ?\ ?\ ?\ ?\ ? \\
 \hline
 0 & & & & & & & 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0
 \end{array} \\
 \\
 \begin{array}{r}
 x & & & & & & & 0\ 0\ 1\ 1\ 0\ 1\ 0\ 0 \\
 + (-x) & & & & & & & +\ 1\ 1\ 0\ 0\ 1\ 0\ 1\ 1 \\
 \hline
 0 & & & & & & & 1\ 1\ 1\ 1\ 1\ 1\ 1\ 1 \\
 & & & & & & & + \\
 & & & & & & & 1 \\
 \hline
 0 & & & & & & & 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0
 \end{array}
 \end{array}$$

flip bits and add 1

"Two's Complement" Integers

Properties:

- Leading bit (bit 15) signifies sign.
- Negative integer $-N$ represented by $2^{16} - N$.
- Trick to compute $-N$:

1. Start with N.

	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	
+4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0

2. Flip bits.

	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	1
--	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

3. Add 1.

-4	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0
----	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Two's Complement Integers

dec	hex	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	
+32767	7FFF	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
...																		
+4	0004	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	
+3	0003	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	
+2	0002	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0
+1	0001	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1
+0	0000	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
-1	FFFF	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
-2	FFFE	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
-3	FFFD	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1
-4	FFFC	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	0
...																		
-32768	8000	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Properties of Two's Complement Integers

Nice properties:

- 0000000000000000 represents 0.
- -0 and +0 are the same.
- Addition is easy (see next slide).
- Checking for arithmetic overflow is easy.

Not-so-nice properties.

- Can represent one more negative integer than positive integer. (-32,768 = -2^{15} but not $32,768 = 2^{15}$).

Two's Complement Arithmetic

Addition is carried out as if all integers were positive.

- It usually works.

-3	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0	1	
+																		
4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0
=																		
1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1

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Two's Complement Arithmetic

Addition is carried out as if all integers were positive.

- It usually works.
- But overflow can occur:
 - carry into sign (left most) bit with no carry out

+32,767	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
+																		
2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0
=																		
-32,767	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1

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Representing Other Primitive Data Types

Negative integers. TOY uses two's complement integers.

Big integers.

- Can use "multiple precision."
- Use two 16-bit words per integer.

Real numbers.

- Can use "floating point" (like scientific notation).
- Double word for extra precision.

Characters.

- Can use ASCII code (8 bits / character).
- Can pack two characters into one 16-bit word.

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Standard Input and Output

Standard output.

- Writing to memory location `FF` sends one word to TOY stdout.
- Ex. `9AFF` writes the integer in register `A` to stdout.

```

00: 0000  0
01: 0001  1

10: 8A00  RA ← mem[00]      a = 0
11: 8B01  RB ← mem[01]      b = 1
12: 9AFF  write RA to stdout  print a
13: 1AAB  RA ← RA + RB          a = a + b
14: 2BAB  RB ← RA - RB          b = a - b
15: DA12  if (RA > 0) goto 12 } while (a > 0)
16: 0000  halt

```

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Standard Input

Standard input.

- Loading from memory address `FF` loads one word from TOY stdin.
- Ex. `8AFF` reads an integer from stdin and store it in register `A`.

Ex: read in a sequence of integers and print their sum.

- In Java, stop reading when EOF.
- In TOY, stop reading when user enters `0000`.

```

while (!StdIn.isEmpty()) {
    a = StdIn.readInt();
    sum = sum + a;
}
StdOut.println(sum);

```

```

00: 0000  0
10: 8C00  RC ← mem[00]
11: 8AFF  read RA from stdin
12: CA15  if (RA == 0) pc ← 15
13: 1CCA  RC ← RC + RA
14: C011  pc ← 11
15: 9CFF  write RC
16: 0000  halt

```

```

00AE
0046
0003
0000
00F7

```

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Standard Input and Output: Implications

Standard input and output enable you to:

- Put information from real world into machine.
- Get information out of machine.
- Process more information than fits in memory.
- Interact with the computer while it is running.

Information can be instructions!

- Booting a computer.
- Sending programs over the Internet
- Sending **viruses** over the Internet

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Pointers

Load address. [opcode 7]

- Loads an 8-bit integer into a register.
- 7A30 means load the value 30 into register A.

Applications.

- Load a small **constant** into a register.
- Load a 8-bit **memory address** into a register.

`a = 0x30;`

Java code

register stores "pointer" to a memory cell

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	1	1	1	1	0	1	0	0	0	1	1	0	0	0	0
7 ₁₆				A ₁₆				3 ₁₆				0 ₁₆			
opcode				dest d				addr							

Arrays in TOY

TOY main memory is a giant array.

- Can access memory cell 30 using load and store.
- 8C30 means load mem[30] into register C.
- Goal: access memory cell *i* where *i* is a variable.

...	...
30	0000
31	0001
32	0001
33	0002
34	0003
35	0005
36	0008
37	000D
...	...

TOY memory

Load indirect. [opcode A] ← a variable index

- AC06 means load mem[R6] into register C.

Store indirect. [opcode B]

- BC06 means store contents of register C into mem[R6].

← a variable index

```
for (int i = 0; i < N; i++)
    a[i] = StdIn.readInt();

for (int i = 0; i < N; i++)
    StdOut.println(a[N-i-1]);
```

TOY Implementation of Reverse

TOY implementation of reverse.

- ⇒ Read in a sequence of integers and store in memory 30, 31, 32, ...
- Stop reading if 0000.
- Print sequence in reverse order.

<pre>10: 7101 R1 ← 0001 11: 7A30 RA ← 0030 12: 7B00 RB ← 0000 13: 8CFF read RC 14: CC19 if (RC == 0) goto 19 15: 16AB R6 ← RA + RB 16: BC06 mem[R6] ← RC 17: 1BB1 RB ← RB + R1 18: C013 goto 13</pre>	<pre>constant 1 a[] n while(true) { c = StdIn.readInt(); if (c == 0) break; memory address of a[n] a[n] = c; n++; }</pre>
--	--

read in the data

TOY implementation of reverse.

- Read in a sequence of integers and store in memory 30, 31, 32, ...
- Stop reading if 0000.
- ➔ ▪ Print sequence in reverse order.

```

19: CB20  if (RB == 0) goto 20      while (n > 0) {
1A: 16AB  R6 ← RA + RB                  address of a[n]
1B: 2661  R6 ← R6 - R1              address of a[n-1]
1C: AC06  RC ← mem[R6]           c = a[n-1];
1D: 9CFE  write RC                  StdOut.println(c);
1E: 2BB1  RB ← RB - R1           n--;
1F: C019  goto 19                }
20: 0000  halt
    
```

print in reverse order

Q. What happens if we make array start at 00 instead of 30?

A. Self modifying program; can overflow buffer and run arbitrary code!

```

10: 7101  R1 ← 0001              constant 1
11: 7A00  RA ← 0000              a[]
12: 7B00  RB ← 0000              n

13: 8CFF  read RC                while(true) {
14: CC19  if (RC == 0) goto 19   c = StdIn.readInt();
15: 16AB  R6 ← RA + RB           if (c == 0) break;
16: BC06  mem[R6] ← RC           address of a[n]
17: 1BB1  RB ← RB + R1          a[n] = c;
18: C013  goto 13                n++;
    }
    
```

```

% more crazy8.txt
1 1 1 1 1 1 1 1
1 1 1 1 1 1 1 1
8888 8810
98FF C011
    
```

What Can Happen When We Lose Control (in C or C++)?

Buffer overrun.

- Array `buffer[]` has size 100.
- User might enter 200 characters.
- Might lose control of machine behavior.

```

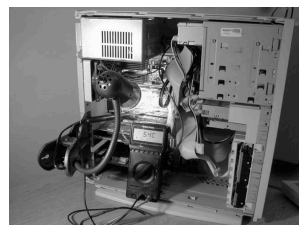
#include <stdio.h>
int main(void) {
    char buffer[100];
    scanf("%s", buffer);
    printf("%s\n", buffer);
    return 0;
}
    
```

unsafe C program

Consequences. Viruses and worms.

Java enforces security.

- Type safety.
- Array bounds checking.
- Not foolproof.



shine 50W bulb at DRAM [Appel-Govindavajhala '03]

Buffer Overrun Example: JPEG of Death

Microsoft Windows JPEG bug. [September, 2004]

- Step 1. User views malicious JPEG in IE or Outlook.
- Step 2. Machine is Owned.
- Data becomes code by exploiting buffer overrun in GDI+ library.



Fix. Update old library with patched one.

but many applications install independent copies of GDI library

Moral.

- Not easy to write error-free software.
- Embrace Java security features.
- Don't try to maintain several copies of the same file.
- Keep your OS patched.

Dumping

Q. Work all day to develop operating system. How to save it?

A. Write short program `dump.toy` and run it to dump contents of memory onto tape.

```
00: 7101  R1 ← 0001
01: 7210  R2 ← 0010          i = 10
02: 73FF  R3 ← 00FF

do {
03: AA02  RA ← mem[R2]      a = mem[i]
04: 9AFF  write RA          print a
05: 1221  R2 ← R2 + R1      i++
06: 2432  R4 ← R3 - R2
07: D403  if (R4 > 0) goto 03    } while (i < 255)
08: 0000  halt
```

`dump.toy`

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Booting

Q. How do you get it back?

A. Write short program `boot.toy` and run it to read contents of memory from tape.



```
00: 7101  R1 ← 0001
01: 7210  R2 ← 0010          i = 10
02: 73FF  R3 ← 00FF

do {
03: 8AFF  read RA          read a
04: BA02  mem[R2] ← RA     mem[i] = a
05: 1221  R2 ← R2 + R1      i++
06: 2432  R4 ← R3 - R2
07: D403  if (R4 > 0) goto 03    } while (i < 255)
08: 0000  halt
```

`boot.toy`

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TOY Simulator

Goal. Write a program to "simulate" the behavior of the TOY machine.

- TOY simulator in Java.

```
public class TOY {
    public static void main(String[] args) {
        int pc = 0x10; // program counter
        int[] R = new int[16]; // registers
        int[] mem = new int[256]; // main memory

        // READ IN .toy FILE

        while (true) {
            // FETCH INSTRUCTION and DECODE
            ...
            // EXECUTE
            ...
        }
    }
}
```

```
% java TOY add-stdin.toy
A012
002B
A03D
```

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Fetch. Extract destination register of 1CAB by shifting and masking.

0	0	0	1	1	1	0	0	1	0	1	0	1	0	1	1	inst
1 ₁₆				C ₁₆				A ₁₆				B ₁₆				
0	0	0	0	0	0	0	0	0	0	0	1	1	1	0	0	inst >> 8
0 ₁₆				0 ₁₆				1				C ₁₆				
0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	15
0 ₁₆				0 ₁₆				0 ₁₆				F ₁₆				
0	0	0	0	0	0	0	0	0	0	0	0	1	1	0	0	(inst >> 8) & 15
0 ₁₆				0 ₁₆				0				C ₁₆				

```
int inst = mem[pc++];           // fetch and increment
int op  = (inst >> 12) & 15;   // opcode (bits 12-15)
int d   = (inst >> 8) & 15;    // dest d (bits 08-11)
int s   = (inst >> 4) & 15;    // source s (bits 04-07)
int t   = (inst >> 0) & 15;    // source t (bits 00-03)
int addr = (inst >> 0) & 255; // addr (bits 00-07)
```

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```
if (op == 0) break;           // halt

switch (op) {
  case 1: R[d] = R[s] + R[t];   break;
  case 2: R[d] = R[s] - R[t];   break;
  case 3: R[d] = R[s] & R[t];   break;
  case 4: R[d] = R[s] ^ R[t];   break;
  case 5: R[d] = R[s] << R[t];  break;
  case 6: R[d] = R[s] >> R[t];  break;
  case 7: R[d] = addr;         break;
  case 8: R[d] = mem[addr];     break;
  case 9: mem[addr] = R[d];     break;
  case 10: R[d] = mem[R[t]];    break;
  case 11: mem[R[t]] = R[d];    break;
  case 12: if (R[d] == 0) pc = addr; break;
  case 13: if (R[d] > 0) pc = addr; break;
  case 14: pc = R[d];          break;
  case 15: R[d] = pc; pc = addr; break;
}
```

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TOY Simulator: Omitted Details

Omitted details.

- Register 0 is always 0.
 - reset $R[0]=0$ after each fetch-execute step
- Standard input and output.
 - if addr is FF and opcode is load (indirect) then read in data
 - if addr is FF and opcode is store (indirect) then write out data
- TOY registers are 16-bit integers; program counter is 8-bit.
 - Java int is 32-bit; Java short is 16-bit
 - use casts and bit-whacking

Complete implementation. See TOY.java on booksite.

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Simulation

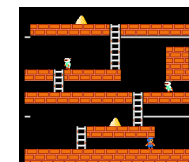
Consequences of simulation.

- Test out new machine or microprocessor using simulator.
 - cheaper and faster than building actual machine
- Easy to add new functionality to simulator.
 - trace, single-step, breakpoint debugging
 - simulator more useful than TOY itself
- Reuse software from old machines.



Ancient programs still running on modern computers.

- Ticketron.
- Lode Runner on Apple IIe.



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