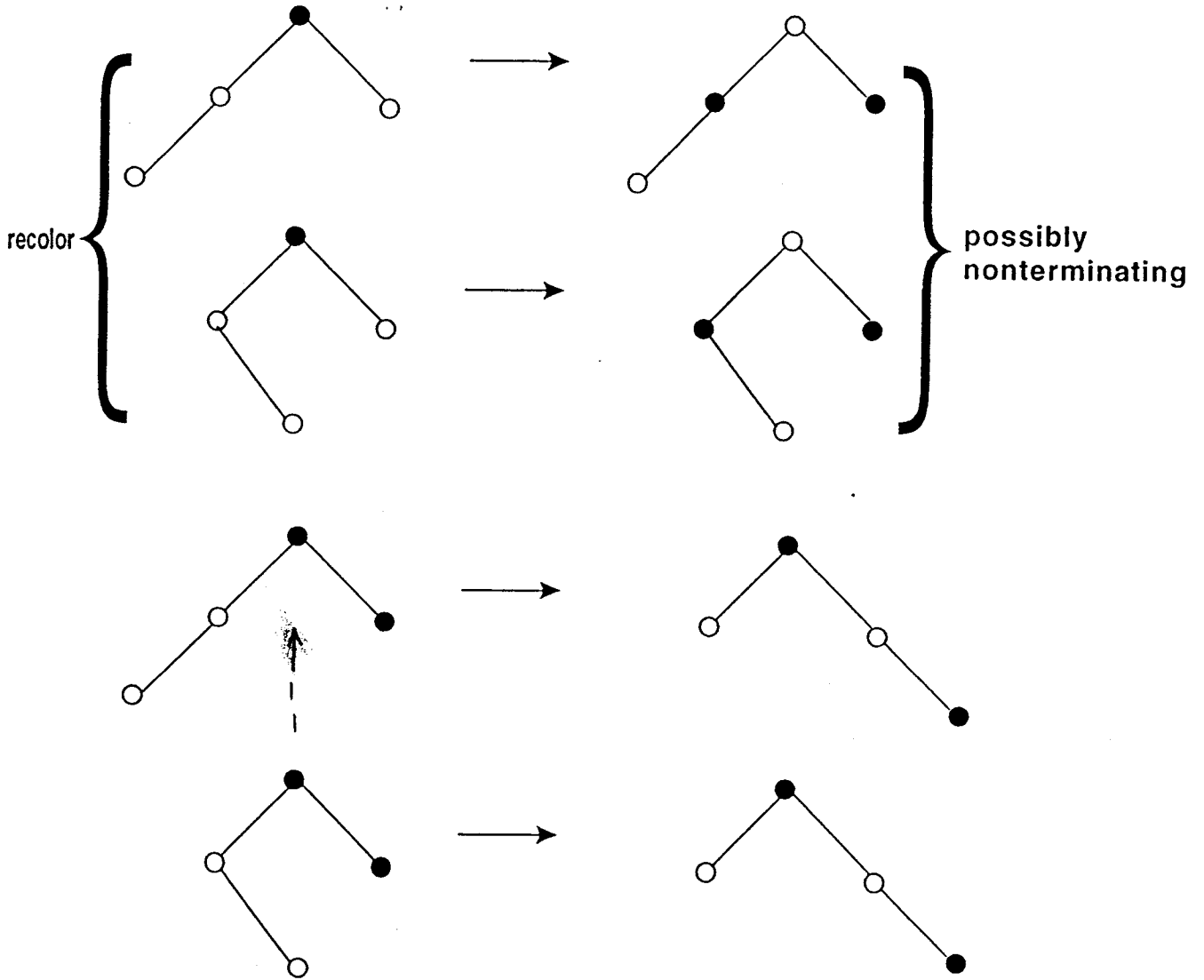


Red-black tree updates

● black

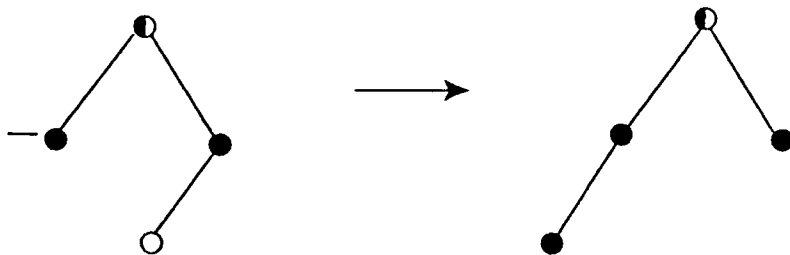
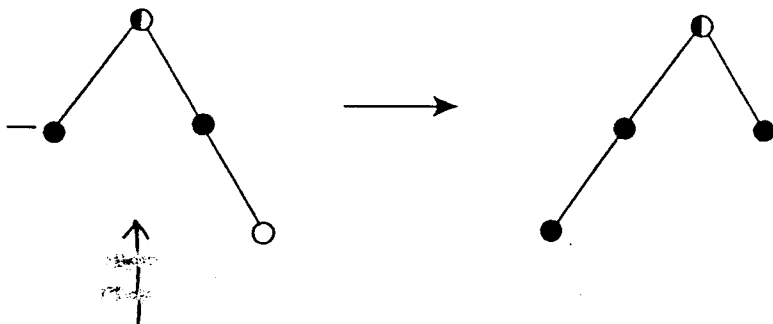
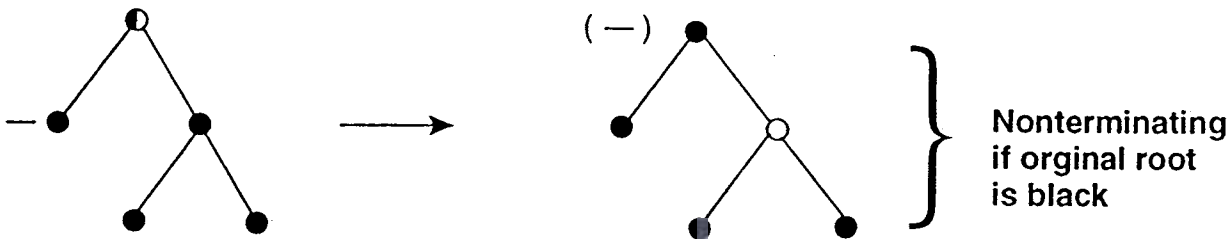
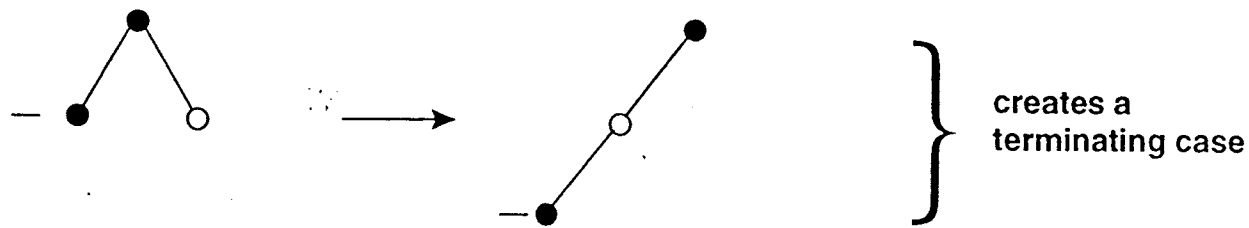
○ red

Insert ○ root → ●



**Delete** — short node (all paths down lack one black node)

- red or black node (color preserved)
- root  $\longrightarrow$  ●
- $\longrightarrow$  ●



$O(\log n)$  recolorings; 0, 1, 2, or 3 rotations

$O(1)$  amortized recoloring time for insert/delete:

$\Phi = 2$  for ,  $1$  for