

# **Character Animation**

COS 426, Spring 2015 Princeton University

## **Computer Animation**

- Animation
  - Make objects change over time according to scripted actions

- Simulation / dynamics
  - Predict how objects change over time according to physical laws



University of Illinois



Pixar

## **Computer Animation**



 Describing how 3D objects (& cameras) move over time



Pixar

## **Computer Animation**

- Challenge is balancing between ...
  - Animator control
  - Physical realism



## **Character Animation Methods**



- Keyframing / Forward Kinematics
- Inverse Kinematics
- Dynamics
- Motion capture





 Define character poses at specific time steps called "keyframes"



Lasseter `87



 Interpolate variables describing keyframes to determine poses for character in between



Lasseter `87



- Inbetweening:
  - Linear interpolation usually not enough continuity





- Inbetweening:
  - Spline interpolation maybe good enough



#### **Example: Ball Boy**





## **Articulated Figures**



 Character poses described by set of rigid bodies connected by "joints"



## **Articulated Figures**



2 DOF

3 DOF

3 DOF

> 2 DOF

2 DOF

1 DOF

2 DOF

Rose et al. '96

2 DOF

• Well-suited for humanoid characters



#### **Example: Ice Skating**





(Mao Chen, Zaijin Guan, Zhiyan Liu, Xiaohu Qie, CS426, Fall98, Princeton University)

## **Articulated Figures**



Animation focuses on joint angles



Watt & Watt

#### **Forward Kinematics**



Describe motion of articulated character



## **Forward Kinematics**



- Animator specifies joint angles:  $\Theta_1$  and  $\Theta_2$
- Computer finds positions of end-effector: X



 $X = (l_1 \cos \Theta_1 + l_2 \cos(\Theta_1 + \Theta_2), l_1 \sin \Theta_1 + l_2 \sin(\Theta_1 + \Theta_2))$ 

#### **Forward Kinematics**



Joint motions specified e.g. by spline curves





• Articulated figure:



Watt & Watt



Hip joint orientation:





• Knee joint orientation:



Watt & Watt



• Ankle joint orientation:



Watt & Watt

## **Example: walk cycle**





#### Lague: www.youtube.com/watch?v=DuUWxUitJos

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Angel Plate 1



• What if animator knows position of "end-effector"?





- Animator specifies end-effector positions: X
- Computer finds joint angles:  $\Theta_1$  and  $\Theta_2$ :





 End-effector postions can be specified by spline curves





- Problem for more complex structures
  - System of equations is usually under-constrained
  - Multiple solutions





- Solution for more complex structures:
  - Find best solution (e.g., minimize energy in motion)
  - Non-linear optimization



## **Kinematics**

- Advantages
  - Simple to implement
  - Complete animator control
- Disadvantages
  - Motions may not follow physical laws
  - Tedious for animator





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Angel Plate 1

## **Dynamics**



• Simulation of physics ensures realism of motion



Lasseter `87



- Animator specifies constraints:
  - What the character's physical structure is
    » e.g., articulated figure
  - What the character has to do (keyframes)
    » e.g., jump from here to there within time t
  - What other physical structures are present
    » e.g., floor to push off and land
  - How the motion should be performed
    - » e.g., minimize energy





- Computer finds the "best" physical motion satisfying constraints
- Example: particle with jet propulsion
  - $\mathbf{x}(t)$  is position of particle at time t
  - $\circ$  **f**(t) is force of jet propulsion at time t
  - Particle's equation of motion is:

$$mx''-f-mg=0$$

 Suppose we want to move from a to b within t<sub>0</sub> to t<sub>1</sub> with minimum jet fuel:

Minimize 
$$\int_{t_0}^{t_1} |f(t)|^2 dt$$
 subject to  $x(t_0) = a$  and  $x(t_1) = b$   
Witkin & Kass `88

 Solve with iterative optimization methods











Witkin & Kass `88



- Advantages:
  - Free animator from having to specify details of physically realistic motion with spline curves
  - Easy to vary motions due to new parameters and/or new constraints

#### • Challenges:

- Specifying constraints and objective functions
- Avoiding local minima during optimization



Adapting motion:



Original Jump



Heavier Base

Witkin & Kass `88



• Adapting motion:





Adapting motion:





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Angel Plate 1



 Measure motion of real characters and then simply "play it back" with kinematics



Gleicher



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- Advantage:
  - Physical realism
- Challenge:
  - Animator control







• Retargeting motion:

Original motion data + constraints:



New motion data:



Gleicher

## **Beyond Skeletons...**



- Skinning
- Motion blur

### **Kinematic Skeletons**

- Hierarchy of transformations ("bones")
  - Changes to parent affect all descendent bones
- So far: bones affect objects in scene or parts of a mesh
  - Equivalently, each point on a mesh acted upon by one bone
  - Leads to discontinuities when parts of mesh animated
- Extension: each point on a mesh acted upon by more than one bone





## **Linear Blend Skinning**



- Each vertex of skin potentially influenced by all bones
  - Normalized weight vector  $w^{(v)}$  gives influence of each bone transform
  - When bones move, influenced vertices also move
- Computing a transformation  $T_v$  for a skinned vertex
  - For each bone
    - » Compute global bone transformation T<sub>b</sub> from transformation hierarchy
  - For each vertex
    - » Take a linear combination of bone transforms
    - » Apply transformation to vertex in original pose

$$T_v = \sum_{b \in B} w_b^{(v)} T_b$$

 Equivalently, transformed vertex position is weighted combination of positions transformed by bones

$$v_{transformed} = \sum_{b \in B} w_b^{(v)} (T_b v)$$



# Assigning Weights: "Rigging"

- Painted by hand
- Automatic: function of relative distances to nearest bones
  - Smoothness of skinned surface depends on smoothness of weights!



#### **Beyond Skeletons...**



- Skinning
- Motion blur





## Summary



- Kinematics
  - Animator specifies poses (joint angles or positions) at keyframes and computer determines motion by kinematics and interpolation
- Dynamics
  - Animator specifies physical attributes, constraints, and starting conditions and computer determines motion by physical simulation
- Motion capture
  - Compute captures motion of real character and provides tools for animator to edit it