



Program Verification

Agenda



Famous bugs

Common bugs

Testing (from lecture 6)

Reasoning about programs

Techniques for program verification

Famous Bugs

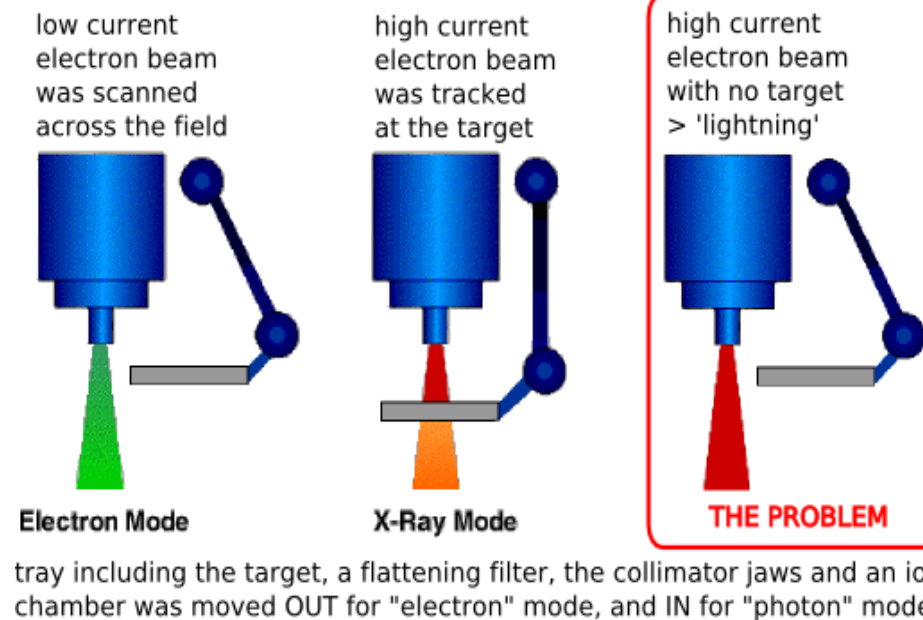


0800 Gordon started
 1000 stopped - Gordon ✓
 11:00 AM MP-AC
 010 POC
 020 POC
 2.13000000
 2.13000000
 Relay 6-2 in 022 failed signal input lead
 in relay - new lead -
 Relay changed
 11:00 Started Coinc. Tape (Sine check)
 15:00 Started Multi-Plexer Test
 15:05  Relay → 70 Panel F
 (auth) in relay.
 First actual case of bug being found.
 17:00 Relay started.
 17:00 closed down.

The first bug: A moth in a relay (1945)
At the Smithsonian (currently not on display)

(in)Famous Bugs

- Safety-critical systems



Therac-25 medical radiation device (1985)

At least 5 deaths attributed to a race condition in software

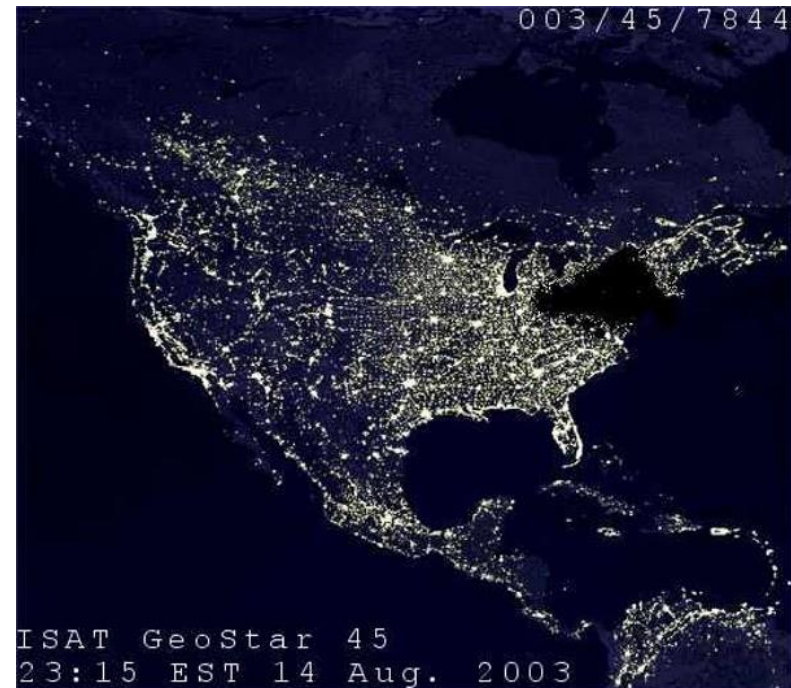
(in)Famous Bugs



- Mission-critical systems



Ariane-5 self-destruction (1995)
SW interface issue, backup failed
Cost: \$400M payload



The Northeast Blackout (2003)
Race condition in power control software
Cost: \$4B

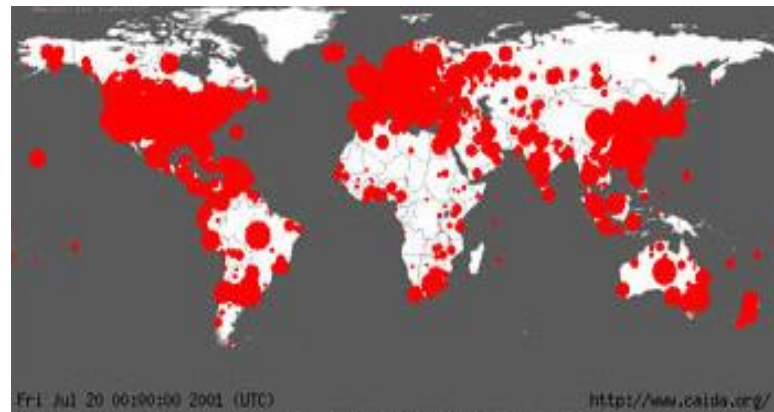
(in)Famous Bugs



- Commodity hardware / software



Pentium bug (1994)
Float computation errors
Cost: \$475M



Code Red worm on MS IIS server (2001)
Buffer overflow exploited by worm
Infected 359k servers
Cost: >\$2B



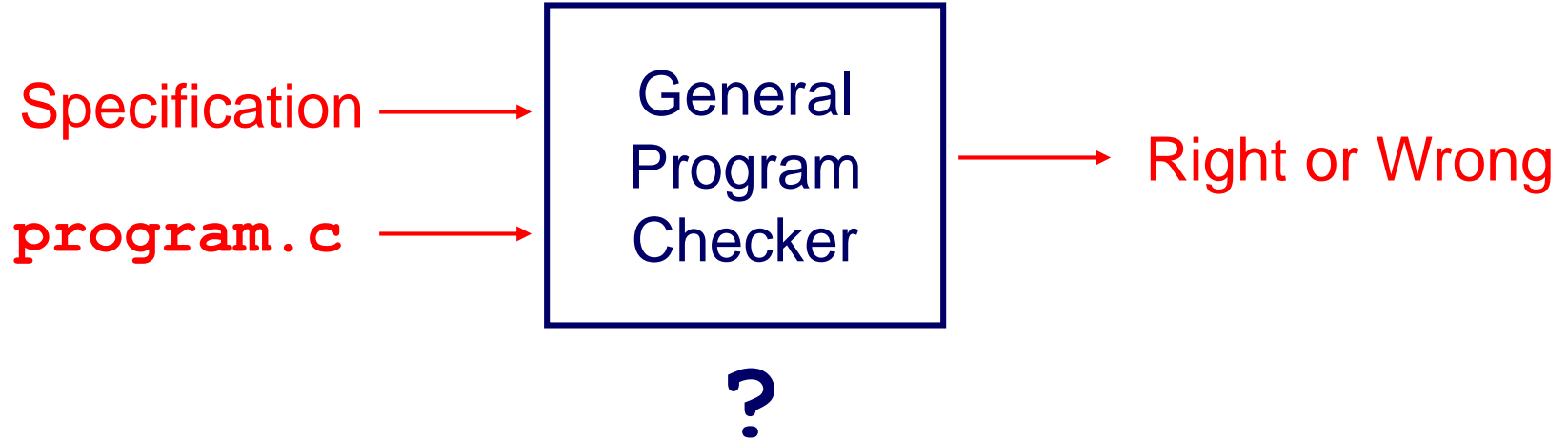
Common Bugs

- **Runtime bugs**
 - Null pointer dereference (access via a pointer that is Null)
 - Array buffer overflow (out of bound index)
 - Can lead to security vulnerabilities
 - Uninitialized variable
 - Division by 0
- **Concurrency bugs**
 - Race condition (flaw in accessing a shared resource)
 - Deadlock (no process can make progress)
- **Functional correctness bugs**
 - Input-output relationships
 - Interface properties
 - Data structure invariants
 - ...



Program Verification

Ideally: Prove that any given program is correct



In general: Undecidable

This lecture: For some (kinds of) properties, a Program Verifier can provide a proof (if right) or a counterexample (if wrong)

Program Testing (Lecture 6)



Pragmatically: Convince yourself that a **specific** program **probably** works



“Program testing can be quite effective for showing the presence of bugs, but is hopelessly inadequate for showing their absence.”

– Edsger Dijkstra

Path Testing Example (Lecture 6)



Example pseudocode:

```
if (condition1)
    statement1;
else
    statement2;
...
if (condition2)
    statement3;
else
    statement4;
...
```

Path testing:

Should make sure all logical paths are executed

How many passes through code are required?

Four paths for four combinations of (condition1, condition 2): TT, TF, FT, FF

- Simple programs => maybe reasonable
- Complex program => combinatorial explosion!!!
 - Path test code fragments

Agenda



Famous bugs

Common bugs

Testing (from lecture 6)

Reasoning about programs

Techniques for program verification



Reasoning about Programs

```
1 int factorial(int x) {  
2     int y = 1;  
3     int z = 0;  
4     while (z != x) {  
5         z = z + 1;  
6         y = y * z;  
7     }  
8     return y;  
9 }
```

Example:
factorial program

Check:
If $x \geq 0$, then $y = \text{fac}(x)$
(fac is the mathematical function)

- Try out the program, say for $x=3$
 - At line 4, before executing the loop: $x=3$, $y=1$, $z=0$
 - Since $z \neq x$, we will execute the while loop
 - At line 4, after 1st iteration of loop: $x=3$, $z=1$, $y=1$
 - At line 4, after 2nd iteration of loop: $x=3$, $z=2$, $y=2$
 - At line 4, after 3rd iteration of loop: $x=3$, $z=3$, $y=6$
 - Since $z == x$, exit loop, return 6: It works!

Reasoning about Programs



```
1 int factorial(int x) {  
2     int y = 1;  
3     int z = 0;  
4     while (z != x) {  
5         z = z + 1;  
6         y = y * z;  
7     }  
8     return y;  
9 }
```

Example:
factorial program

Check:
If $x \geq 0$, then $y = \text{fac}(x)$

- Try out the program, say for $x=4$
 - At line 4, before executing the loop: $x=4$, $y=1$, $z=0$
 - Since $z \neq x$, we will execute the while loop
 - At line 4, after 1st iteration of loop: $x=4$, $z=1$, $y=1$
 - At line 4, after 2nd iteration of loop: $x=4$, $z=2$, $y=2$
 - At line 4, after 3rd iteration of loop: $x=4$, $z=3$, $y=6$
 - At line 4, after 4th iteration of loop: $x=4$, $z=4$, $y=24$
 - Since $z == x$, exit loop, return 24: It works!



Reasoning about Programs

```
1 int factorial(int x) {  
2     int y = 1;  
3     int z = 0;  
4     while (z != x) {  
5         z = z + 1;  
6         y = y * z;  
7     }  
8     return y;  
9 }
```

Example:
factorial program

Check:
If $x \geq 0$, then $y = \text{fac}(x)$

- Try out the program, say for $x=1000$
 - At line 4, before executing the loop: $x=1000$, $y=1$, $z=0$
 - Since $z \neq x$, we will execute the while loop
 - At line 4, after 1st iteration of loop: $x=1000$, $z=1$, $y=1$
 - At line 4, after 2nd iteration of loop: $x=1000$, $z=2$, $y=2$
 - At line 4, after 3rd iteration of loop: $x=1000$, $z=3$, $y=6$
 - At line 4, after 4th iteration of loop: $x=1000$, $z=4$, $y=24$

Want to keep going on???

Lets try some mathematics ...



```
1 int factorial(int x) {
2     int y = 1;
3     int z = 0;
4     while (z != x) {
5         z = z + 1;
6         y = y * z;
7     }
8     return y;
9 }
```

Example:
factorial program

Check:
If $x \geq 0$, then $y = \text{fac}(x)$

- Annotate the program with “assertions” [Floyd 67]
 - Assertions (at program lines) are expressed as (logic) formulas
 - Here, we will use standard arithmetic
 - Meaning: Assertions hold before that line is executed
- For loops, we will use an assertion called a “loop invariant”
 - Invariant means that the assertion holds in each iteration of loop
 - We can prove this by using induction



Loop Invariant

```
1 int factorial(int x) {  
2     int y = 1;  
3     int z = 0;  
4     while (z != x) {  
5         z = z + 1;  
6         y = y * z;  
7     }  
8     return y;  
9 }
```



Example:
factorial program

Check:
If $x \geq 0$, then $y = \text{fac}(x)$

- Loop invariant (assertion at line 4): $y = \text{fac}(z)$
- Try to *prove by induction* that the loop invariant holds
 - Base case: First time at line 4, $z=0$, $y=1$, $\text{fac}(0)=1$, $y=\text{fac}(z)$ holds \checkmark
 - Induction hypothesis: Suppose $y = \text{fac}(z)$ at line 4
 - Induction step: In next iteration of the loop (when $z \neq x$)
 - $z' = z+1$ and $y' = \text{fac}(z) * z + 1 = \text{fac}(z')$ (z'/y' denote updated values)
 - Therefore, at line 4, $y' = \text{fac}(z')$, i.e., loop invariant holds again \checkmark



Proof of Correctness

```
1 int factorial(int x) {  
2     int y = 1;  
3     int z = 0;  
4     while (z != x) {  
5         z = z + 1;  
6         y = y * z;  
7     }  
8     return y;  
9 }
```

Example:
factorial program

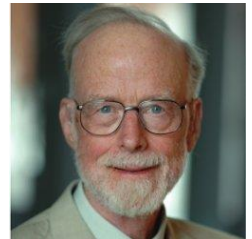
Check:
If $x \geq 0$, then $y = \text{fac}(x)$

- Loop invariant (assertion at line 4): $y = \text{fac}(z)$ ✓
- What should we do now?
 - If loop condition is true, i.e., if $(z \neq x)$, execute loop again, $y = \text{fac}(z)$
 - If the loop condition is false, i.e., if $(z == x)$, exit the loop
 - At line 8, we now know that $y = \text{fac}(z)$ AND $z == x$, i.e., $y = \text{fac}(x)$
 - Thus, at return, $y = \text{fac}(x)$
- Proof of correctness of the factorial program is now done ✓

Program Verification



- Rich history in computer science
- *Assigning Meaning to Programs* [Floyd, 1967]
 - Program is annotated with assertions (formulas in logic)
 - Program is proved correct by reasoning about assertions
- *An Axiomatic Basis for Computer Programming* [Hoare, 1969]
 - Hoare Triple: $\{P\} S \{Q\}$
 - S: statement (or fragments) in program
 - P: precondition (formula in logic)
 - Q: postcondition (formula in logic)
 - Meaning: If S executes from a state where P is true, and if S terminates, then Q is true in the resulting state
 - This is called “partial correctness”
 - does not guarantee termination of S
 - For our example: $\{x \geq 0\} y = \text{factorial}(x) \{y = \text{fac}(x)\}$



Program Verification



- **Proof Systems**

- Perform reasoning using logic formulas and rules of inference
 - Soundness: If assertion A is proved, then A is true
 - Completeness: If assertion A is true, then A can be proved

- **Hoare Logic**

[Hoare 69]

- Inference rules for assignments, conditionals, loops, sequence
- Given a program annotated with preconditions, postconditions, and loop invariants
 - Verification Condition (VC) can be generated automatically
 - If VC is “valid”, then program is correct
 - Validity of VC can be checked by a theorem-prover
- **Question: Can these preconditions/postconditions/loop invariants be generated automatically?**

Automatic Program Verification



- Question: Can these preconditions/postconditions/loop invariants be generated automatically?
- Answer: Yes! (in many cases)
- Techniques for deriving the assertions automatically
 - Model checking: based on exploring “states” of programs
 - Abstract interpretation: based on static analysis using “abstractions” of programs
 - ... many other techniques
- Still an active area of research (after more than 45 years)!

Model Checking



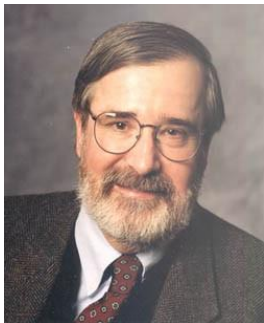
- Temporal logic

- Used for specifying correctness properties
- [Pnueli, 1977]



- Model checking

- Verifying temporal logic properties by state space exploration
- [Clarke & Emerson, 1981] and [Queille & Sifakis, 1981]

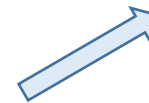
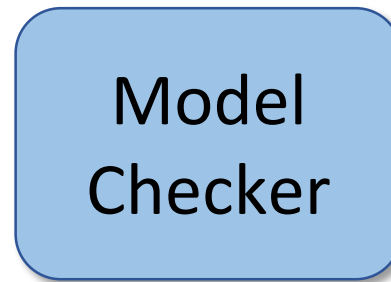
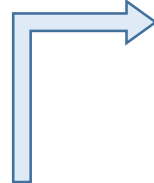




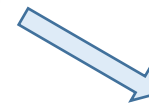
Model Checker

- Model checker performs automatic state space exploration
 - If all reachable states are visited and error state is not reached, then property is proved correct
 - Otherwise, it provides a counterexample (trace to error state)

```
1 int factorial(int x) {  
2   int y = 1;  
3   int z = 0;  
4   while (z != x) {  
5     z = z + 1;  
6     y = y * z;  
7   }  
8   return y;  
9 }
```



(may run out of memory)



Property holds
Proof

Property fails
Counterexample

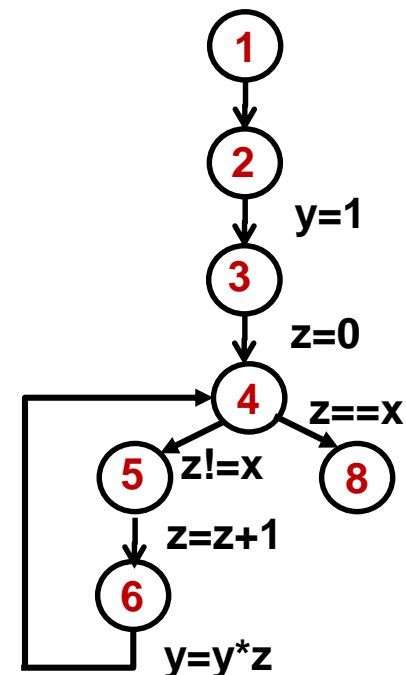
Property: formula
Is error state reachable?
(Example: error state is where $y \neq \text{fac}(x)$ at return)



Model Checking (simplified)

- Consider viewing a program *like* a DFA (not quite, ...)
 - “State” in a program
 - Line number
 - Value of each program variable (not shown below)
 - “Transition” in a program
 - Statement in program (updates state)
- Example: factorial program

```
1 int factorial(int x) {  
2   int y = 1;  
3   int z = 0;  
4   while (z != x) {  
5     z = z + 1;  
6     y = y * z;  
7   }  
8   return y;  
9 }
```

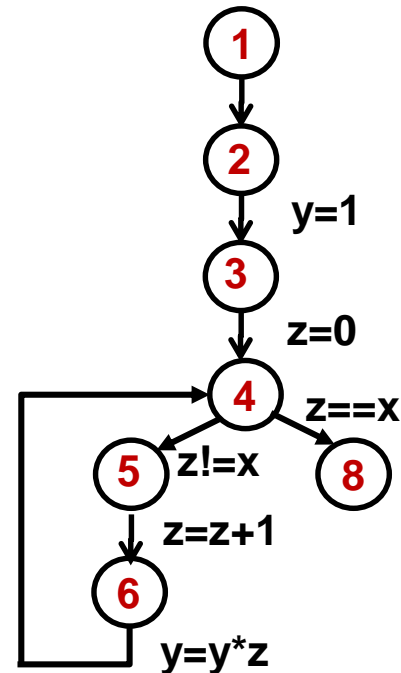




Model Checking (simplified)

- Example: factorial program

```
1 int factorial(int x) {  
2   int y = 1;  
3   int z = 0;  
4   while (z != x) {  
5     z = z + 1;  
6     y = y * z;  
7   }  
8   return y;  
9 }
```



- Number of program states

- 9 (lines)*(states of x)*(states of y)*(states of z): $9 * 2^{32} * 2^{32} * 2^{32}$
- States are not represented explicitly, but *symbolically* as formulas
 - e.g. $(z < y)$ represents all program states where z is less than y

- Many other enhancements are used ...



F-Soft Model Checker

Automatic tool for finding bugs in large C/C++ programs (NEC)

```
1: void pivot_sort(int A[], int n){
2: int pivot=A[0], low=0, high=n;
3: while ( low < high ) {
4:   do {
5:     low++;
6:   } while ( A[low] <= pivot );
7:   do {
8:     high -- ;
9:   } while ( A[high] >= pivot );
10:  swap(&A[low],&A[high]);
11: }
12: }
```

Array Buffer Overflow?

F-Soft



counterexample trace

```
Line 1: n=2, A[0]=10, A[1]=10
Line 2: pivot=10, low=0, high=2
Line 3: low < high ?      YES
Line 5: low = 1
Line 6: A[low] <= pivot ?  YES
Line 5: low = 2
Line 6: A[low] <= pivot ?
```

Buffer Overflow!!!

Summary



- Program verification
 - Provide *proofs of correctness* for classes of properties & programs
 - Testing *cannot* provide proofs of correctness (unless exhaustive)
- Proof systems based on logic
 - Users annotate the program with assertions
 - Theorem-provers perform search for proofs (with user guidance)
- Automatic verification techniques
 - Program assertions are derived automatically
 - But, scalability is an issue
 - Explosion in sets of reachable states
 - Worse for concurrent multi-threaded programs
 - Need to explore all possible interleavings of different threads
- *COS 597B in Fall '15: Automatic Reasoning about Software*

Course Summary



We have covered:

Programming in the large

- The C programming language
- Testing
- Building
- Debugging
- Program & programming style
- Data structures
- Modularity
- Performance

Course Summary



We have covered (cont.):

Under the hood

- Number systems
- Language levels tour
 - Assembly language
 - Machine language
 - Assemblers and linkers
- Service levels tour
 - Exceptions and processes
 - Storage management
 - Dynamic memory management
 - Process management
 - I/O management
 - Signals

The Rest of the Course



Assignment 7

- Due on Dean's Date (5/12) at 5PM
- Cannot submit late (University regulations)
- Cannot use late pass

Office hours and exam prep sessions

- Will be announced on Piazza

Final exam

- When: Tuesday 5/19, 1:30 PM
- Where: Friend Center 101
- Closed book, closed notes, no electronic devices



Thank you!