TOY II

![Image of TOY II](image-url)
LINC
LINC
What We've Learned About TOY

Data representation. Binary and hex.

TOY.

• Box with switches and lights.
• 16-bit memory locations, 16-bit registers, 8-bit pc.
• 4,328 bits = (255 × 16) + (15 × 16) + (8) = 541 bytes!
• von Neumann architecture.

TOY instruction set architecture. 16 instruction types.

TOY machine language programs. Variables, arithmetic, loops.
Quick Review: Multiply

| 0A: 0003 | 3       | ← inputs |
| 0B: 0009 | 9       | ← output |
| 0C: 0000 | 0       | ← constants |
| 0D: 0000 | 0       |
| 0E: 0001 | 1       |

| 10: 8A0A | RA ← mem[0A] | a |
| 11: 8B0B | RB ← mem[0B] | b |
| 12: 8C0D | RC ← mem[0D] | c = 0 |
| 13: 810E | R1 ← mem[0E] | always 1 |

| 14: CA18 | if (RA == 0) pc ← 18 |
| 15: 1CCB | RC ← RC + RB |
| 16: 2AA1 | RA ← RA - R1 |
| 17: C014 | pc ← 14 |
| 18: 9C0C | mem[0C] ← RC |
| 19: 0000 | halt |

multiply.toy
What We Do Today

Data representation. Negative numbers.

Input and output. Standard input, standard output.

Manipulate addresses. References (pointers) and arrays.

TOY simulator in Java and implications.
Data Representation
Data is a sequence of bits. (interpreted in different ways)

- Integers, real numbers, characters, strings, ...
- Documents, pictures, sounds, movies, Java programs, ...

Ex. 01110101

- As binary integer: $1 + 4 + 16 + 32 + 64 = 117$ (base ten).
- As character: $117^{th}$ Unicode character = 'u'.
- As music: $117/256$ position of speaker.
- As grayscale value: 45.7% black.

```java
public class HelloWorld {
    public static void main(String[] args) {
        System.out.println("Hello, World");
    }
}
```
Decimal and binary addition.

```
013 0 0 0 0 1 1 0 1
+ 0 92 + 0 1 0 1 1 1 0 0
105 0 1 1 0 1 0 0 1
```

But what about subtraction? Just add a negative integer.

```
e.g., 6 - 4 = 6 + (-4))
```

Q. OK, but how to represent negative integers?
Representing Negative Integers

TOY words are 16 bits each.

- We could use 16 bits to represent 0 to $2^{16} - 1$.
- We want negative integers too.
- Reserving half the possible bit-patterns for negative seems fair.

Highly desirable property. If $x$ is an integer, then the representation of $-x$, when added to $x$, yields zero.

$$
\begin{array}{c}
x \\
+ (-x) \\
\hline
0
\end{array}
\quad
\begin{array}{c}
0 0 1 1 0 1 0 0 \\
\hline
0 0 0 0 0 0 0 0
\end{array}
$$

-x: flip bits and add 1

$$
\begin{array}{c}
x \\
+ 1 1 0 0 1 0 1 1 \\
\hline
1 1 1 1 1 1 1 1
\end{array}
\quad
\begin{array}{c}
1 1 1 1 1 1 1 1 \\
+ \\
\hline
1
\end{array}
\quad
\begin{array}{c}
0 \\
+ 0 0 0 0 0 0 0 0
\hline
0 0 0 0 0 0 0 0
\end{array}
$$
“Two's Complement” Integers

To compute \(-x\) from \(x\):

- **Start with \(x\).**
  
  \[
  +4 \quad 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0
  \]

- **Flip bits.**
  
  \[
  -5 \quad 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 0 \ 1 \ 1
  \]

- **Add one.**
  
  \[
  -4 \quad 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 0 \ 0
  \]
## Two's Complement Integers

<table>
<thead>
<tr>
<th>dec</th>
<th>hex</th>
<th>binary</th>
</tr>
</thead>
<tbody>
<tr>
<td>+32767</td>
<td>7FFF</td>
<td>0 1 1 1 1 1 1 1 1 1 1 1 1 1 1</td>
</tr>
<tr>
<td>+4</td>
<td>0004</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 1 0 0</td>
</tr>
<tr>
<td>+3</td>
<td>0003</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 0 1 1</td>
</tr>
<tr>
<td>+2</td>
<td>0002</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 0 1 0</td>
</tr>
<tr>
<td>+1</td>
<td>0001</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 0 0 1</td>
</tr>
<tr>
<td>+0</td>
<td>0000</td>
<td>0 0 0 0 0 0 0 0 0 0 0 0 0 0 0</td>
</tr>
<tr>
<td>-1</td>
<td>FFFF</td>
<td>1 1 1 1 1 1 1 1 1 1 1 1 1 1 1</td>
</tr>
<tr>
<td>-2</td>
<td>FFFE</td>
<td>1 1 1 1 1 1 1 1 1 1 1 1 1 1 0</td>
</tr>
<tr>
<td>-3</td>
<td>FFFD</td>
<td>1 1 1 1 1 1 1 1 1 1 1 1 1 0 1</td>
</tr>
<tr>
<td>-4</td>
<td>FFFC</td>
<td>1 1 1 1 1 1 1 1 1 1 1 1 1 0 0</td>
</tr>
</tbody>
</table>

...
Properties of Two's Complement Integers

Properties.
- Leading bit (bit 15 in Toy) signifies sign.
- Addition and subtraction are easy.
- 0000000000000000 represents zero.
- Negative integer \(-x\) represented by \(2^{16} - x\).
- Not symmetric: can represent \(-32,768\) but not \(32,768\).

Java. Java's int data type is a 32-bit two's complement integer.

Ex. 2147483647 + 1 equals \(-2147483648\).
Properties of Two's Complement Integers

Properties.

- Leading bit (bit 15 in Toy) signifies sign.
- Addition and subtraction are easy.
- 0000000000000000 represents zero.
- Negative integer \(-x\) represented by \(2^{16} - x\).
- Not symmetric: can represent \(-32,768\) but not \(32,768\).

Java. Java's int data type is a 32-bit two's complement integer.

Ex. 2147483647 + 1 equals \(-2147483648\).

```java
public class OhYesItDoes {
    public static void main(String[] args){
        int x = 2147483647;
        System.out.println(x + 1);
    }
}
```

> java OhYesItDoes

-2147483648
Representing Other Primitive Data Types in TOY

**Bigger integers.** Use two 16-bit words per int.

**Real numbers.**
- Use "floating point" (like scientific notation).
- Use four 16-bit words per double.

**Characters.**
- Use ASCII code (8 bits / character).
- Pack two characters per 16-bit word.

**Note.** Real microprocessors add hardware support for int and double.
Standard Input and Output
Standard Output

Standard output.

- Writing to memory location FF sends one word to TOY stdout.
- Ex. 9AFF writes the integer in register A to stdout.

<table>
<thead>
<tr>
<th>Address</th>
<th>Binary</th>
<th>Value</th>
<th>Instruction</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>00:</td>
<td>0000</td>
<td>0</td>
<td></td>
<td></td>
</tr>
<tr>
<td>01:</td>
<td>0001</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>10:</td>
<td>8A00</td>
<td>RA ← mem[00]</td>
<td>a = 0</td>
<td></td>
</tr>
<tr>
<td>11:</td>
<td>8B01</td>
<td>RB ← mem[01]</td>
<td>b = 1</td>
<td></td>
</tr>
<tr>
<td>12:</td>
<td>9AFF</td>
<td>write RA to stdout</td>
<td>print a</td>
<td></td>
</tr>
<tr>
<td>13:</td>
<td>1AAB</td>
<td>RA ← RA + RB</td>
<td>a = a + b</td>
<td></td>
</tr>
<tr>
<td>14:</td>
<td>2BAB</td>
<td>RB ← RA - RB</td>
<td>b = a - b</td>
<td></td>
</tr>
<tr>
<td>15:</td>
<td>DA12</td>
<td>if (RA &gt; 0) goto 12</td>
<td>} while (a &gt; 0)</td>
<td></td>
</tr>
<tr>
<td>16:</td>
<td>0000</td>
<td>halt</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Standard Output

Standard output.

- Writing to memory location FF sends one word to TOY stdout.
- Ex. 9AFF writes the integer in register A to stdout.

```
00: 0000 0
01: 0001 1
10: 8A00 RA ← mem[00] a = 0
11: 8B01 RB ← mem[01] b = 1
do {
12: 9AFF write RA to stdout print a
13: 1AAB RA ← RA + RB a = a + b
14: 2BAB RB ← RA - RB b = a - b
15: DA12 if (RA > 0) goto 12 } while (a > 0)
16: 0000 halt
```
Standard Input

Standard input.

• Loading from memory address FF loads one word from TOY stdin.
• Ex. 8AFF reads an integer from stdin and store it in register A.

Ex: read in a sequence of integers and print their sum.

• In Java, stop reading when EOF.
• In TOY, stop reading when user enters 0000.

```java
while (!StdIn.isEmpty()) {
    a = StdIn.readInt();
    sum = sum + a;
}
StdOut.println(sum);
```
Standard Input and Output: Implications

Standard input and output enable you to:

▪ Put information from real world into machine.
▪ Get information out of machine.
▪ Process more information than fits in memory.
▪ Interact with the computer while it is running.

Information can be instructions!

▪ Booting a computer.
▪ Sending programs over the Internet
▪ Sending viruses over the Internet
Load Address (a.k.a. Load Constant)

**Load address.** [opcode 7]

- Loads an 8-bit integer into a register.
- 7A30 means load the value 30 into register A.

**Applications.**

- Load a small **constant** into a register.
- Load an 8-bit **memory address** into a register.

![Register stores "pointer" to a memory cell](image)

<table>
<thead>
<tr>
<th>15</th>
<th>14</th>
<th>13</th>
<th>12</th>
<th>11</th>
<th>10</th>
<th>9</th>
<th>8</th>
<th>7</th>
<th>6</th>
<th>5</th>
<th>4</th>
<th>3</th>
<th>2</th>
<th>1</th>
<th>0</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

\[ a = \text{0x30}; \]

Java code (NOTE hex literal)

Register stores "pointer" to a memory cell

**Table:**

<table>
<thead>
<tr>
<th>opcode</th>
<th>dest d</th>
<th>addr</th>
</tr>
</thead>
<tbody>
<tr>
<td>7_16</td>
<td>A_16</td>
<td>3_16</td>
</tr>
</tbody>
</table>

![Table](image)
Arrays in TOY

TOY main memory is a giant array.

- Can access memory cell $30$ using load and store.
- $8C30$ means load $\text{mem}[30]$ into register $C$.
- Goal: access memory cell $i$ where $i$ is a variable.

**Load indirect.** [opcode A]

- $AC06$ means load $\text{mem}[R6]$ into register $C$.

**Store indirect.** [opcode B]

- $BC06$ means store contents of register $C$ into $\text{mem}[R6]$. 

<table>
<thead>
<tr>
<th>TOY memory</th>
</tr>
</thead>
<tbody>
<tr>
<td>30</td>
</tr>
<tr>
<td>31</td>
</tr>
<tr>
<td>32</td>
</tr>
<tr>
<td>33</td>
</tr>
<tr>
<td>34</td>
</tr>
<tr>
<td>35</td>
</tr>
<tr>
<td>36</td>
</tr>
<tr>
<td>37</td>
</tr>
<tr>
<td>...</td>
</tr>
</tbody>
</table>
Example: Reverse an array

TOY implementation of reverse.

- Read in a sequence of integers and store in memory 30, 31, 32, ...
- Stop reading if 0000.
- Print sequence in reverse order.

Java version:

```java
int n = 0;
while (!StdIn.isEmpty())
{
    a[n] = StdIn.readInt();
    n++;
}

while (n > 0)
{
    n--;
    StdOut.println(a[n]);
}
(We'll just assume a[] is big enough)
```
TOY Implementation of Reverse

TOY implementation of reverse.

• Read in a sequence of integers and store in memory 30, 31, 32, ...
• Stop reading if 0000.
• Print sequence in reverse order.

10: 7101 R1 ← 0001 constant 1
11: 7A30 RA ← 0030 a[]
12: 7B00 RB ← 0000 n

while(true) {
13: 8CFF read RC c = StdIn.readInt();
14: CC19 if (RC == 0) goto 19 if (c == 0) break;
15: 16AB R6 ← RA + RB memory address of a[n]
16: BC06 mem[R6] ← RC a[n] = c;
17: 1BB1 RB ← RB + R1 n++;
18: C013 goto 13 }

read in the data
TOY Implementation of Reverse

TOY implementation of reverse.

• Read in a sequence of integers and store in memory 30, 31, 32, ...
• Stop reading if 0000.
• Print sequence in reverse order.

```
10: 7101  R1 ← 0001  // constant 1
11: 7A30  RA ← 0030  // a[]
12: 7B00  RB ← 0000  // n

while(true) {
    19: CB20  if (RB == 0) goto 20  // if (n == 0) break;
    1A: 16AB  R6 ← RA + RB  // memory address of a[n]
    1B: 2661  R6 ← R6 - R1  // n--;
    1C: AC06  RC ← mem[R6]  // c = a[n];
    1D: 9CFF  write RC  // StdOut.print(c);
    1E: 2BB1  RB ← RB - R1  // n--;
    1F: C019  goto 19  // }
```

print in reverse order

Unsafe Code at any Speed

Q. What happens if we make array start at 00 instead of 30?

```
10: 7101  R1 ← 0001    constant 1
11: 7A00  RA ← 0000    a[]
12: 7B00  RB ← 0000    n

while(true) {
    13: 8CFF  read RC     c = StdIn.readInt();
    14: CC19  if (RC == 0) goto 19    if (c == 0) break;
    15: 16AB  R6 ← RA + RB    address of a[n]
    16: BC06  mem[R6] ← RC    a[n] = c;
    17: 1BB1  RB ← RB + R1    n++;
    18: C013  goto 13
}
```
Unsafe Code at any Speed

```

00: 0000 08: 0000
01: 0000 09: 0000
02: 0000 0A: 0000
03: 0000 0B: 0000
04: 0000 0C: 0000
05: 0000 0D: 0000
06: 0000 0E: 0000
07: 0000 0F: 0000
10: 7101 R1 ← 0001
11: 7A00 RA ← 0000
12: 7B00 RB ← 0000
13: 8CFF read RC
14: CC19 if (RC == 0) goto 19
15: 16AB R6 ← RA + RB
16: BC06 mem[R6] ← RC
17: 1BB1 RB ← RB + R1
18: C013 goto 13

constant 1
a[]
n
while(true) {
  c = StdIn.readInt();
  if (c == 0) break;
  address of a[n]
  a[n] = c;
  n++;
}
```
Unsafe Code at any Speed

Machine is Owned

while (true) { x = 8888; writeln(x);

if (c == 0) break;
address of a[n]
a[n] = c;
n++; }
Buffer overflow.
- Array buffer[] has size 100.
- User might enter 200 characters.
- Might lose control of machine behavior.

Consequences. Viruses and worms.

Java enforces security.
- Type safety.
- Array bounds checking.
- Not foolproof.
Buffer Overflow Attacks

Stuxnet worm. [July 2010]

- Step 1. Natanz centrifuge fuel-refining plant employee plugs in USB flash drive.
- Step 2. Data becomes code by exploiting Windows buffer overflow; machine is Owned.
- Step 3. Uranium enrichment in Iran stalled.

More buffer overflow attacks: Morris worm, Code Red, SQL Slammer, iPhone unlocking, Xbox softmod, JPEG of death [2004], . . .

Lesson.

- Not easy to write error-free software.
- Embrace Java security features.
- Keep your OS patched.
Q. Work all day to develop operating system. How to save it?

A. Write short program `dump.toy` and run it to dump contents of memory onto tape.

```
00: 7001  R1 ← 0001  i = 10
01: 7210  R2 ← 0010
02: 73FF  R3 ← 00FF
03: AA02  RA ← mem[R2]  a = mem[i]
04: 9AFF  write RA    print a
05: 1221  R2 ← R2 + R1  i++
06: 2432  R4 ← R3 - R2
07: D403  if (R4 > 0) goto 03
08: 0000  halt
```

dump.toy
Q. How do you get it back?

A. Write short program `boot.toy` and run it to read contents of memory from tape.

```
00: 7001 R1 ← 0001
01: 7210 R2 ← 0010
02: 73FF R3 ← 00FF
03: 8AFF read RA
04: BA02 mem[R2] ← RA
05: 1221 R2 ← R2 + R1
06: 2432 R4 ← R3 - R2
07: D403 if (R4 > 0) goto 03
08: 0000 halt
```

boot.toy
Simulating the TOY machine
TOY Simulator

Goal. Write a program to "simulate" the behavior of the TOY machine.

- TOY simulator in Java.

```java
public class TOY {
    public static void main(String[] args) {
        int pc = 0x10; // program counter
        int[] R = new int[16]; // registers
        int[] mem = new int[256]; // main memory

        // READ .toy FILE into mem[]
        while (true) {
            int inst = mem[pc++]; // fetch, increment
            // DECODE
            // EXECUTE
        }
    }
}
```

% more add-stdin.toy
10: 8C00
11: 8AFF
12: CA15
13: 1CCA
14: C011
15: 9CFF
16: 0000

% java TOY add-stdin.toy
00AE
0046
0003
0000
00F7
Ex. Extract destination register of \texttt{1CAB} by shifting and masking.

\begin{verbatim}
int inst = mem[pc++]; // fetch and increment
int op = (inst >> 12) & 15; // opcode (bits 12-15)
int d = (inst >> 8) & 15; // dest d (bits 08-11)
int s = (inst >> 4) & 15; // source s (bits 04-07)
int t = (inst >> 0) & 15; // source t (bits 00-03)
int addr = (inst >> 0) & 255; // addr (bits 00-07)
\end{verbatim}
if (op == 0) break; // halt

switch (op)
{
    case 1: R[d] = R[s] + R[t]; break;
    case 2: R[d] = R[s] - R[t]; break;
    case 3: R[d] = R[s] & R[t]; break;
    case 4: R[d] = R[s] ^ R[t]; break;
    case 5: R[d] = R[s] << R[t]; break;
    case 6: R[d] = R[s] >> R[t]; break;
    case 7: R[d] = addr; break;
    case 8: R[d] = mem[addr]; break;
    case 9: mem[addr] = R[d]; break;
    case 10: R[d] = mem[R[t]]; break;
    case 11: mem[R[t]] = R[d]; break;
    case 12: if (R[d] == 0) pc = addr; break;
    case 13: if (R[d] > 0) pc = addr; break;
    case 14: pc = R[d]; break;
    case 15: R[d] = pc; pc = addr; break;
}
Omitted details.

• Register 0 is always 0.
  - reset \( R[0] = 0 \) after each fetch-execute step

• Standard input and output.
  - if \( \text{addr} \) is FF and opcode is load (indirect) then read in data
  - if \( \text{addr} \) is FF and opcode is store (indirect) then write out data

• TOY registers are 16-bit integers; program counter is 8-bit.
  - Java \text{int} \ is 32-bit; Java \text{short} \ is 16-bit
  - use casts and bit-whacking

Complete implementation. See TOY.java on booksite.
Simulation

Building a new computer? Need a plan for old software.

Two possible approaches

- Rewrite software (costly, error-prone, boring, and time-consuming).
- Simulate old computer on new computer.

Ancient programs still running on modern computers.

- Payroll
- Power plants
- Air traffic control
- Ticketron.
- Games.