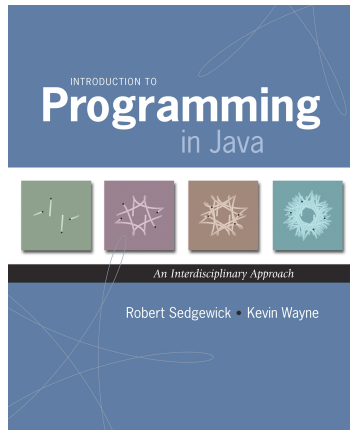


## 4.3 Stacks and Queues

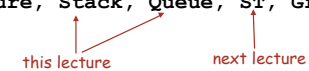


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## Data Types and Data Structures

**Data types.** Set of values and operations on those values.

- Some are built into the Java language: int, double[], String, ...
- Most are not: Complex, Picture, Stack, Queue, ST, Graph, ...



**Data structures.**

- Represent data or relationships among data.
- Some are built into Java language: arrays.
- Most are not: linked list, circular list, tree, sparse array, graph, ...



## Collections

**Fundamental data types.**

- Set of operations (add, remove, test if empty) on generic data.
- Intent is clear when we insert.
- Which item do we remove?

**Stack.** [LIFO = last in first out]

← this lecture

- Remove the item most recently added.
- Ex: cafeteria trays, Web surfing.

**Queue.** [FIFO = first in, first out]

← this lecture

- Remove the item least recently added.
- Ex: Hoagie Haven line.

**Symbol table.**

← next lecture

- Remove the item with a given key.
- Ex: Phone book.

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## Stacks

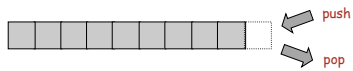


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## Stack API

```
public class *StackOfStrings
    *StackOfStrings() create an empty stack
    boolean isEmpty() is the stack empty?
    void push(String item) push a string onto the stack
    String pop() pop the stack
```



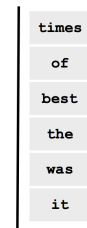
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## Stack Client Example 1: Reverse

```
public class Reverse {
    public static void main(String[] args) {
        StackOfStrings stack = new StackOfStrings();
        while (!StdIn.isEmpty()) {
            String s = StdIn.readString();
            stack.push(s);
        }
        while (!stack.isEmpty()) {
            String s = stack.pop();
            StdOut.println(s);
        }
    }
}
```

```
% more tiny.txt
it was the best of times

% java Reverse < tiny.txt
times of best the
was it
```



← stack contents when standard input is empty

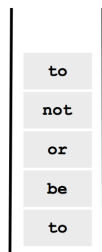
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## Stack Client Example 2: Test Client

```
public static void main(String[] args) {
    StackOfStrings stack = new StackOfStrings();
    while (!StdIn.isEmpty()) {
        String s = StdIn.readString();
        if (s.equals("-"))
            StdOut.println(stack.pop());
        else
            stack.push(s);
    }
}
```

```
% more test.txt
to be or not to - be - - that - - - is

% java StackOfStrings < test.txt
to be not that or be
```



← stack contents just before first pop operation

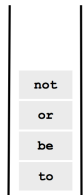
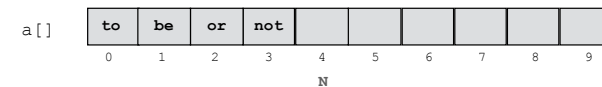
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## Stack: Array Implementation

### Array implementation of a stack.

- Use array `a[]` to store `N` items on stack.
- `push()` add new item at `a[N]`.
- `pop()` remove item from `a[N-1]`.

how big to make array? [stay tuned]



```
public class ArrayStackOfStrings {
    private String[] a;
    private int N = 0;
    public ArrayStackOfStrings(int max) { a = new String[max]; }
    public boolean isEmpty() { return (N == 0); }
    public void push(String item) { a[N++] = item; }
    public String pop() { return a[--N]; }
}
```

temporary solution: make client provide capacity

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## Array Stack: Test Client Trace

	StdIn	StdOut	N	a[]				
				0	1	2	3	4
			0					
push	to		1	to				
	be		2	to	be			
	or		3	to	be	or		
	not		4	to	be	or	not	
	to		5	to	be	or	not	to
pop	-	to	4	to	be	or	not	to
	be		5	to	be	or	not	be
	-	be	4	to	be	or	not	be
	-	not	3	to	be	or	not	be
	that		4	to	be	or	that	be
	-	that	3	to	be	or	that	be
	-	or	2	to	be	or	that	be
	-	be	1	to	be	or	that	be
	is		2	to	is	or	that	to

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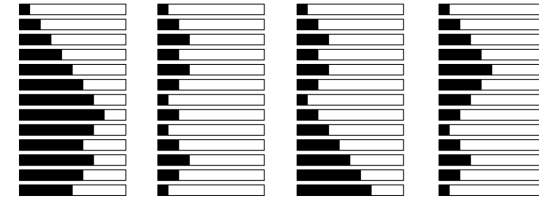
## Array Stack: Performance

Running time. Push and pop take constant time.

Memory. Proportional to client-supplied capacity, not number of items.

Problem.

- Original API does not take capacity as argument (bad to change API).
- Client might not know what capacity to use.
- Client might use multiple stacks.



Challenge. Stack where capacity is not known ahead of time.

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## Linked Lists

## Sequential vs. Linked Allocation

Sequential allocation. Put items one after another.

- TOY: consecutive memory cells.
- Java: array of objects.

Linked allocation. Include in each object a link to the next one.

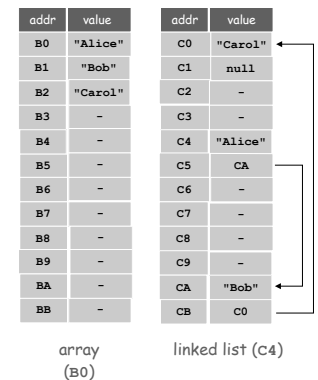
- TOY: link is memory address of next item.
- Java: link is reference to next item.

Key distinctions.

- Array: random access, fixed size.
- Linked list: sequential access, variable size.

↖ get i<sup>th</sup> item

↖ get next item



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## Linked Lists

### Linked list.

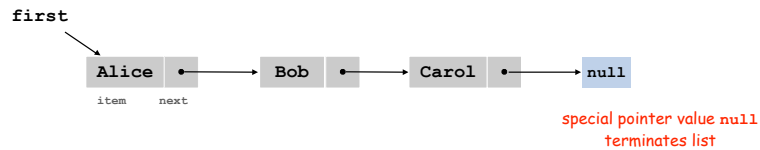
- A recursive data structure.
- An item plus a pointer to another linked list (or empty list).
- Unwind recursion: linked list is a sequence of items.

why private?  
stay tuned

### Node data type.

- A reference to a string.
- A reference to another Node.

```
private class Node {
    private String item;
    private Node next;
}
```



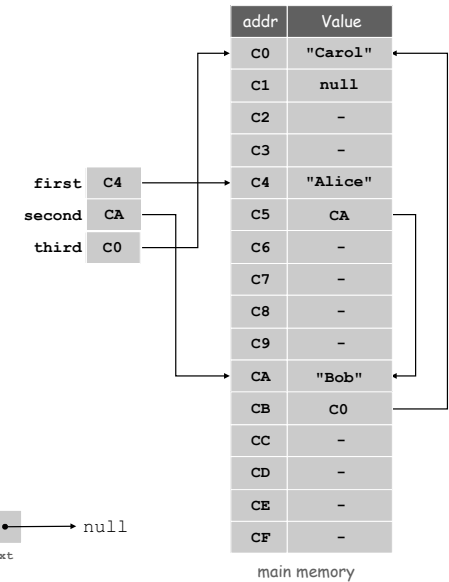
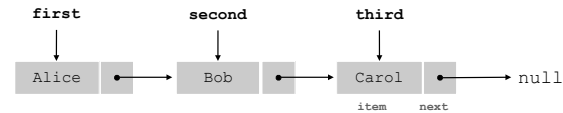
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## Building a Linked List

```
Node third = new Node();
third.item = "Carol";
third.next = null;

Node second = new Node();
second.item = "Bob";
second.next = third;

Node first = new Node();
first.item = "Alice";
first.next = second;
```



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## List Processing Challenge 1

Q. What does the following code fragment do?

```
Node last = new Node();
last.item = StdIn.readString();
last.next = null;
Node first = last;
while (!StdIn.isEmpty()) {
    last.next = new Node();
    last = last.next;
    last.item = StdIn.readString();
    last.next = null;
}
```

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## List Processing Challenge 2

Q. What does the following code fragment do?

```
for (Node x = first; x != null; x = x.next) {
    StdOut.println(x.item);
}
```



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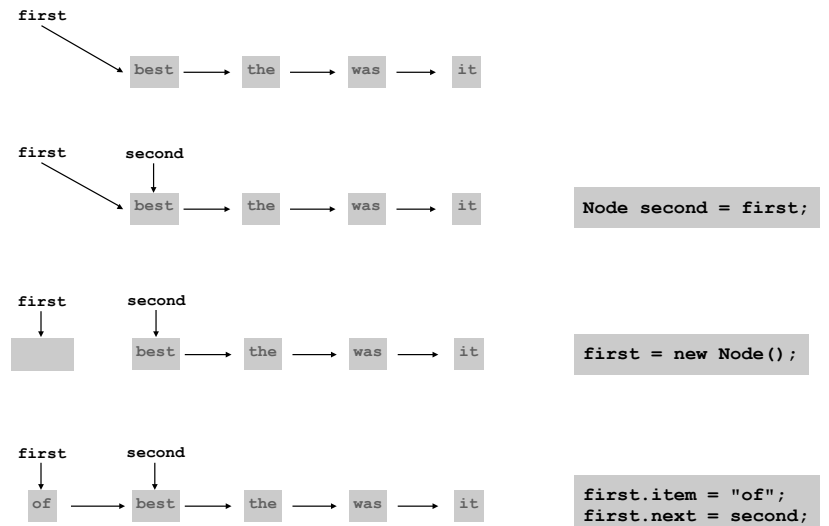
## Enough with the Idioms

How about this idea:

- Use a linked list to implement a stack

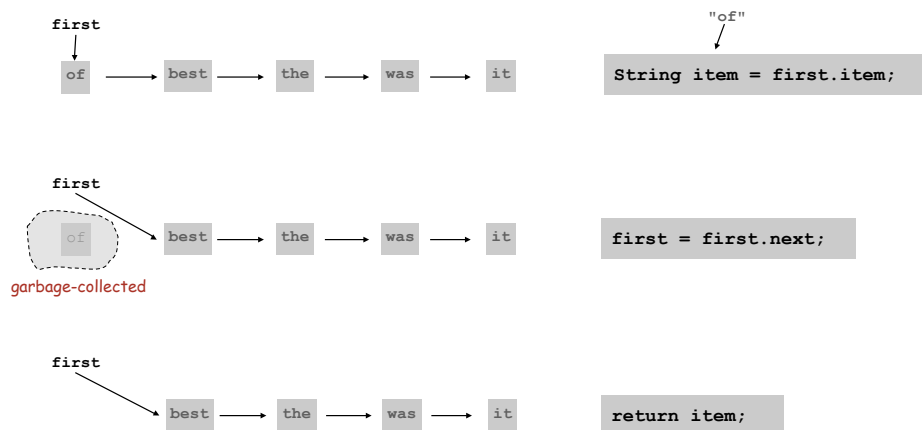
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## Stack Push: Linked List Implementation



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## Stack Pop: Linked List Implementation



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## Stack: Linked List Implementation

```
public class LinkedStackOfStrings {  
    private Node first = null;
```

```
private class Node {  
    private String item;  
    private Node next;  
}
```

*special reserved name*

*"inner class"*

```
public boolean isEmpty() { return first == null; }
```

```
public void push(String item) {  
    Node second = first;  
    first = new Node();  
    first.item = item;  
    first.next = second;  
}
```

```
public String pop() {  
    String item = first.item;  
    first = first.next;  
    return item;  
}
```

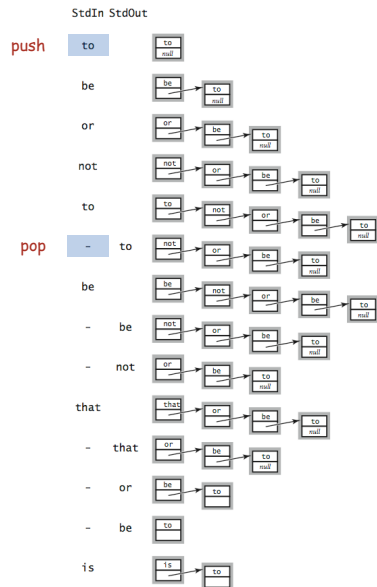
```
}
```

stack and linked list contents  
after 4<sup>th</sup> push operation

```
not  
or  
be  
to
```

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## Linked List Stack: Test Client Trace



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## Stack Data Structures: Tradeoffs

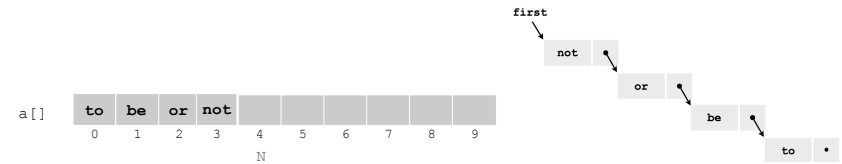
Two data structures to implement stack data type.

### Array.

- Every push/pop operation take constant time.
- **But...** must fix maximum capacity of stack ahead of time.

### Linked list.

- Every push/pop operation takes constant time.
- Memory is proportional to number of items on stack.
- **But...** uses extra space and time to deal with references.



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## Parameterized Data Types

## Stack: Linked List Implementation

```
public class LinkedStackOfStrings {
    private Node first = null;

    private class Node {
        private String item;
        private Node next;
    }
    "inner class"

    public boolean isEmpty() { return first == null; }

    public void push(String item) {
        Node second = first;
        first = new Node();
        first.item = item;
        first.next = second;
    }

    public String pop() {
        String item = first.item;
        first = first.next;
        return item;
    }
}
```

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## Parameterized Data Types

We just implemented: `StackOfStrings`.

We also want: `StackOfInts`, `StackOfURLs`, `StackOfVans`, ...

**Strawman.** Implement a separate stack class for each type.

- Rewriting code is tedious and **error-prone**.
- Maintaining cut-and-pasted code is tedious and **error-prone**.



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## Generics

**Generics.** Parameterize stack by a single type.

```
Stack<Apple> stack = new Stack<Apple>();
Apple a = new Apple();
Orange b = new Orange();
stack.push(a);
stack.push(b); // compile-time error
a = stack.pop();
```

"stack of apples" (points to Stack<Apple>)

parameterized type (points to <Apple>)

sample client (points to the entire code block)

can't push an orange onto a stack of apples (points to stack.push(b);)

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## Generic Stack: Linked List Implementation

```
public class Stack<Item> {
    private Node first = null;

    private class Node {
        private Item item;
        private Node next;
    }

    public boolean isEmpty() { return first == null; }

    public void push(Item item) {
        Node second = first;
        first = new Node();
        first.item = item;
        first.next = second;
    }

    public Item pop() {
        Item item = first.item;
        first = first.next;
        return item;
    }
}
```

parameterized type name (chosen by programmer) (points to Item)

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## Autoboxing

**Generic stack implementation.** Only permits reference types.

**Wrapper type.**

- Each primitive type has a **wrapper** reference type.
- Ex: `Integer` is wrapper type for `int`.

**Autoboxing.** Automatic cast from primitive type to wrapper type.

**Autounboxing.** Automatic cast from wrapper type to primitive type.

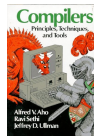
```
Stack<Integer> stack = new Stack<Integer>();
stack.push(17); // autobox (int -> Integer)
int a = stack.pop(); // auto-unbox (Integer -> int)
```

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## Stack Applications

### Real world applications.

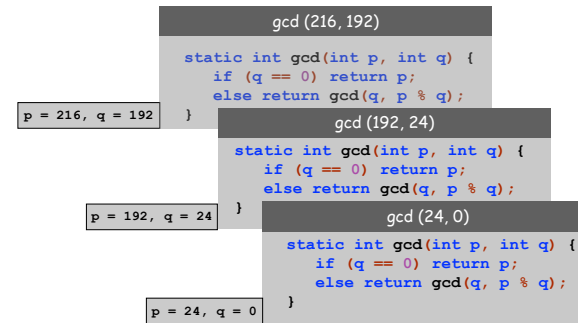
- Parsing in a compiler.
- Java virtual machine.
- Undo in a word processor.
- Back button in a Web browser.
- PostScript language for printers.
- Implementing function calls in a compiler.



## Function Calls

### How a compiler implements functions.

- Function call: **push** local environment and return address.
- Return: **pop** return address and local environment.



Recursive function. Function that calls itself.

Note. Can always use an explicit stack to remove recursion.

## Arithmetic Expression Evaluation

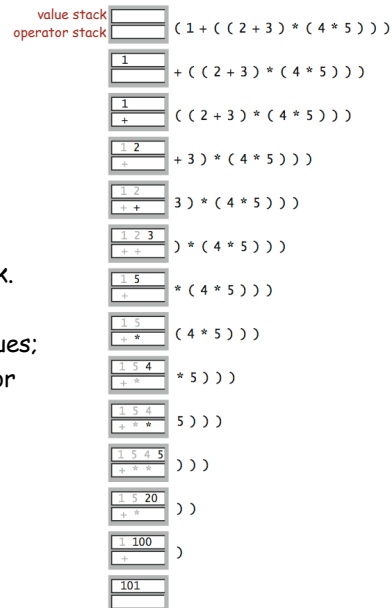
### Goal. Evaluate infix expressions.

( 1 + ( ( 2 + 3 ) \* ( 4 \* 5 ) ) )

↑ operand                      ↑ operator

### Two stack algorithm. [E. W. Dijkstra]

- Value: push onto the value stack.
- Operator: push onto the operator stack.
- Left parens: ignore.
- Right parens: pop operator and two values; push the result of applying that operator to those values onto the value stack.



Context. An interpreter!

## Arithmetic Expression Evaluation

```
public class Evaluate {
    public static void main(String[] args) {
        Stack<String> ops = new Stack<String>();
        Stack<Double> vals = new Stack<Double>();
        while (!StdIn.isEmpty()) {
            String s = StdIn.readString();
            if (s.equals("(")) ;
            else if (s.equals("+")) ops.push(s);
            else if (s.equals("*")) ops.push(s);
            else if (s.equals(")")) {
                String op = ops.pop();
                if (op.equals("+")) vals.push(vals.pop() + vals.pop());
                else if (op.equals("*")) vals.push(vals.pop() * vals.pop());
            }
            else vals.push(Double.parseDouble(s));
        }
        StdOut.println(vals.pop());
    }
}
```

```
% java Evaluate
( 1 + ( ( 2 + 3 ) * ( 4 * 5 ) ) )
101.0
```



## Correctness

**Why correct?** When algorithm encounters an operator surrounded by two values within parentheses, it leaves the result on the value stack.

```
( 1 + ( ( 2 + 3 ) * ( 4 * 5 ) ) )
```

So it's as if the original input were:

```
( 1 + ( 5 * ( 4 * 5 ) ) )
```

Repeating the argument:

```
( 1 + ( 5 * 20 ) )  
( 1 + 100 )  
101
```

**Extensions.** More ops, precedence order, associativity, whitespace.

```
1 + ( 2 - 3 - 4 ) * 5 * sqrt(6*6 + 7*7)
```

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## Stack-Based Programming Languages

**Observation 1.** Remarkably, the 2-stack algorithm computes the same value if the operator occurs **after** the two values.

```
( 1 ( ( 2 3 + ) ( 4 5 * ) * ) + )
```

**Observation 2.** All of the parentheses are redundant!

```
1 2 3 + 4 5 * * +
```

**Bottom line.** Postfix or "reverse Polish" notation.

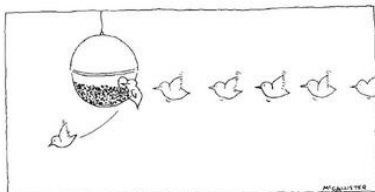
**Applications.** Postscript, Forth, calculators, Java virtual machine, ...



Jan Lukasiewicz

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## Queues



Drawing by McCallister, © 1977 The New Yorker Magazine, Inc.



(CHIRPAB HQ23N2)

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## Queue API

```
public class Queue<Item>
```

```
    Queue<Item>() create an empty queue
```

```
    boolean isEmpty() is the queue empty?
```

```
    void enqueue(Item item) enqueue an item
```

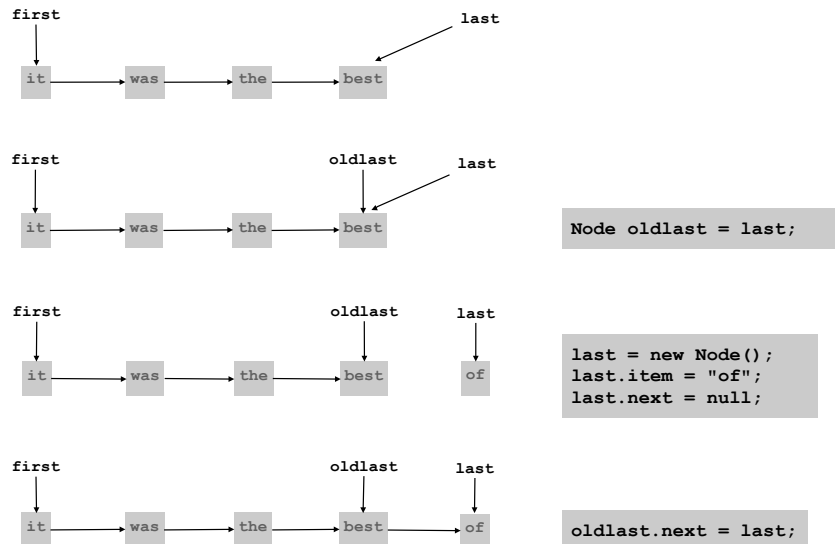
```
    Item dequeue() dequeue an item
```

enqueue →  → dequeue

```
public static void main(String[] args) {  
    Queue<String> q = new Queue<String>();  
    q.enqueue("Vertigo");  
    q.enqueue("Just Lose It");  
    q.enqueue("Pieces of Me");  
    q.enqueue("Pieces of Me");  
    while(!q.isEmpty())  
        StdOut.println(q.dequeue());  
}
```

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## Enqueue: Linked List Implementation



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## Dequeue: Linked List Implementation



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## Queue: Linked List Implementation

```

public class Queue<Item> {
    private Node first, last;

    private class Node { Item item; Node next; }

    public boolean isEmpty() { return first == null; }

    public void enqueue(Item item) {
        Node oldlast = last;
        last = new Node();
        last.item = item;
        last.next = null;
        if (isEmpty()) first = last;
        else oldlast.next = last;
    }

    public Item dequeue() {
        Item item = first.item;
        first = first.next;
        if (isEmpty()) last = null;
        return item;
    }
}
    
```

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## Queue Applications

### Some applications.

- iTunes playlist.
- Data buffers (iPod, TiVo).
- Asynchronous data transfer (file IO, pipes, sockets).
- Dispensing requests on a shared resource (printer, processor).

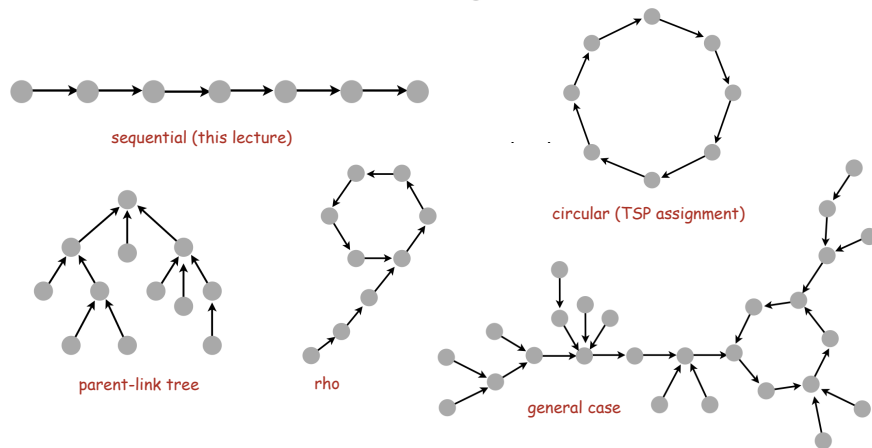
### Simulations of the real world.

- Guitar string.
- Traffic analysis.
- Waiting times of customers at call center.
- Determining number of cashiers to have at a supermarket.

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## Singly-Linked Data Structures

From the point of view of a particular object:  
all of these structures look the same. ● →



**Multiply-linked data structures.** Many more possibilities.

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## Conclusions

Stacks and Queues are fundamental ADTs.  
Sequential allocation: supports indexing, fixed size.  
Linked allocation: variable size, supports sequential access.

Linked structures are a central programming tool.

- Linked lists.
- Binary trees.
- Graphs.
- Sparse matrices.
- ...

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