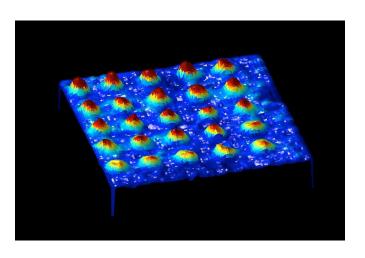
# 1.4 Arrays



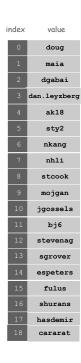
## Arrays

This lecture. Store and manipulate huge quantities of data.

Array. Indexed sequence of values of the same type.

## Examples.

- 52 playing cards in a deck.
- 5 thousand undergrads at Princeton.
- 1 million characters in a book.
- 10 million audio samples in an MP3 file.
- 4 billion nucleotides in a DNA strand.
- 1.3 trillion Google queries per year.
- 50 trillion cells in the human body.
- $6.02 \times 10^{23}$  particles in a mole.



# any program you might want to write objects functions and modules graphics, sound, and image I/O arrays conditionals and loops Math text I/O primitive data types assignment statements

# Many Variables of the Same Type

Goal. 10 variables of the same type.

```
// Tedious and error-prone code.
double a0, a1, a2, a3, a4, a5, a6, a7, a8, a9;
a0 = 0.0;
a1 = 0.0;
a2 = 0.0;
a3 = 0.0;
a4 = 0.0;
a5 = 0.0;
a6 = 0.0;
a7 = 0.0;
a8 = 0.0;
a9 = 0.0;
...
a4 = 3.0;
...
double x = a4 + a8;
```

# Many Variables of the Same Type

Goal. 10 variables of the same type (e.g.).

```
// Easy alternative.
double[] a = new double[10];
...
a[4] = 3.0;
...
a[8] = 8.0;
...
double x = a[4] + a[8];
```

## Many Variables of the Same Type

Goal. 1 million variables of the same type.

```
// Scales to handle large arrays.
double[] a = new double[1000000];
...
a[234567] = 3.0;
...
a[876543] = 8.0;
...
double x = a[234567] + a[876543];
```

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# Arrays in Java

Java has special language support for arrays.

- To make an array: declare, create, and initialize it.
- To access element i of array named a, use a[i].
- Array indices start at 0.

Compact alternatives: Declare, create, and initialize in one statement.

• Default: all entries automatically set to 0.

```
double[] a = new double[1000];

• Initialize to literal values

double[] x = { 0.3, 0.6, 0.1 };

double[] x = new double[3];
x[0] = 0.3; x[1] = 0.6; x[2] = 0.1;
```

Sample Array Code: Vector Dot Product

Dot product. Given two vectors x[] and y[] of length n, their dot product is the sum of the products of their corresponding components.

```
double[] x = { 0.3, 0.6, 0.1 };
double[] y = { 0.5, 0.1, 0.4 };

double sum = 0.0;
for (int i = 0; i < N; i++)
    sum += x[i] * y[i];</pre>
```

i	x[i]	y[i]	x[i]*y[i]	sum
				0
0	.30	.50	.15	.15
1	. 60	.10	.06	.21
2	.10	.40	.04	.25
				.25

# Array Processing Examples

```
double[] a = new double[N];
for (int i = 0; i < N; i++)
   a[i] = Math.random();</pre>
```

create an array with N random values

```
for (int i = 0; i < N; i++)
    System.out.println(a[i]);</pre>
```

print the array values, one per line

```
double max = Double.NEGATIVE_INFINITY;
for (int i = 0; i < N; i++)
  if (a[i] > max) max = a[i];
```

find the maximum of the array values

```
double[] b = new double[N];
for (int i = 0; i < N; i++)
  b[i] = a[i];</pre>
```

copy to another array

```
double sum = 0.0;
for (int i = 0; i < N; i++)
    sum += a[i];
double average = sum / N;
```

compute the average of the array values

```
for (int i = 0; i < N/2; i++)
{
   double temp = b[i];
   b[i] = b[N-i-1];
   b[N-i-1] = temp;
}</pre>
```

reverse the elements within the array

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# Shuffling a Deck



## Mumbo-Jumbo Demystification, Part 1

```
public class Gambler {
   public static void main(String[] args) {
     int stake = Integer.parseInt(args[0]);
     int goal = Integer.parseInt(args[1]);
     int trials = Integer.parseInt(args[2]);
     . . .
     . . .
}
```

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# Setting Array Values at Compile Time

Fx Print a random card

```
String[] rank =
{
    "2", "3", "4", "5", "6", "7", "8", "9",
    "10", "Jack", "Queen", "King", "Ace"
};

String[] suit =
{
    "clubs", "diamonds", "hearts", "spades"
};

int i = (int) (Math.random() * 13); // between 0 and 12
int j = (int) (Math.random() * 4); // between 0 and 3

System.out.println(rank[i] + " of " + suit[j]);
```

## Setting Array Values at Compile Time

#### Want to initialize a whole deck? How about this:

```
String[] deck =
   "2 of clubs", "3 of clubs", "4 of clubs", "5 of clubs",
   "6 of clubs", "7 of clubs", "8 of clubs", "9 of clubs",
   "10 of clubs", "Jack of clubs", "Queen of clubs",
   "King of clubs", "Ace of clubs", "2 of diamonds",
   "3 of diamonds", "4 of diamonds", "5 of diamonds",
   "6 of diamonds", "7 of diamonds", "8 of diamonds",
   "9 of diamonds", "10 of diamonds", "Jack of diamonds",
   "Queen of diamonds", "King of diamonds", "Ace of diamonds",
   "2 of hearts", "3 of hearts", "4 of hearts", "5 of hearts",
  "6 of hearts", "7 of hearts", "8 of hearts", "9 of hearts",
  "10 of hearts", "Jack of hearts", "Queen of hurts",
   "King of hearts", "Ace of hearts", "2 of spades",
   "3 of spades", "4 of spades", "5 of spades",
   "6 of spades", "7 of spades", "8 of spades", "9 of spades",
   "10 of spades", "Jack of spades", "Queen of spades",
   "King of spades", "Ace of spades",
};
```

## Setting Array Values at Run Time

#### This method saves ink:

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# Array Challenge 1

The following code sets array values to the 52 card values and prints them. In which order are they printed?

```
      A. 2 of clubs
      B. 2 of clubs

      2 of diamonds
      3 of clubs

      2 of hearts
      4 of clubs

      2 of spades
      5 of clubs

      3 of clubs
      6 of clubs
```

# Array Challenge 2

Swap the for statements: rank index in inner loop, suit index in outer loop. Now, in which order are they printed?

```
String[] rank = { "2", "3" ..., "King", "Ace" };
String[] suit =
    { "clubs", "diamonds", "hearts", "spades" };

String[] deck = new String[52];
for (int j = 0; j < 4; j++)
    for (int i = 0; i < 13; i++)
        deck[4*i + j] = rank[i] + " of " + suit[j];

for (int i = 0; i < 52; i++)
    System.out.println(deck[i]);</pre>
```

```
A. 2 of clubs
    2 of diamonds
    2 of hearts
    2 of spades
    3 of clubs
    5 of clubs
    ...
    ...
```

# Array Challenge 3

The following code sets array values to the 52 card values and prints them. What change to the code will produce the "B" order?

```
String[] rank = { "2", "3" ..., "King", "Ace" };
String[] suit =
    { "clubs", "diamonds", "hearts", "spades" };

String[] deck = new String[52];
for (int i = 0; i < 13; i++)
    for (int j = 0; j < 4; j++)
        deck[4*i + j] = rank[i] + " of " + suit[j];

for (int i = 0; i < 52; i++)
    System.out.println(deck[i]);</pre>
```

```
      A. 2 of clubs
      B. 2 of clubs

      2 of diamonds
      3 of clubs

      2 of hearts
      4 of clubs

      2 of spades
      5 of clubs

      3 of clubs
      6 of clubs
```

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# Shuffle an Array

#### Shuffle a deck of cards

- In ith iteration, put a random element from remainder of deck at index i.
- -choose random integer r between i and N-1
- -swap values in positions r and i

Array index	0	1	2	3	4	5	6	7	8	9
Value	9*	3*	4%	5*	6%	7 <b>.</b>	8•	24	10%	J.
	1							1		

random integer = 7

# Shuffling

Goal. Given an array, rearrange its elements in random order.

## Shuffling algorithm.

- In iteration i, pick random card from deck[i] through deck[N-1], with each card equally likely.
- Exchange it with deck[i].

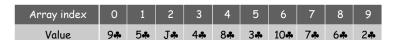
```
int N = deck.length;
for (int i = 0; i < N; i++)
{
    int r = i + (int) (Math.random() * (N-i));
    String t = deck[r];
    deck[r] = deck[i];
    deck[i] = t;
}</pre>
```

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# Shuffle an Array

## Shuffle a deck of cards.

- In i<sup>th</sup> iteration, put a random element from remainder of deck at index i.
- -choose random integer r between i and N-1
- -swap values in positions r and i



# Shuffling a Deck of Cards

```
public class Deck
  public static void main(String[] args)
      String[] suit = { "Clubs", "Diamonds", "Hearts", "Spades" };
      String[] rank = { "2", "3", "4", "5", "6", "7", "8", "9",
                        "10", "Jack", "Queen", "King", "Ace"
     int SUITS = suit.length;
      int RANKS = rank.length;
                                        avoid "hardwired" constants like 52, 4, and 13.
     int N = SUITS * RANKS;
      String[] deck = new String[N];
                                                                     build the deck
      for (int i = 0; i < RANKS; i++)
         for (int j = 0; j < SUITS; j++)
            deck[SUITS*i + j] = rank[i] + " of " + suit[j];
      for (int i = 0; i < N; i++)
                                                                         shuffle
         int r = i + (int) (Math.random() * (N-i));
         String t = deck[r];
         deck[r] = deck[i];
         deck[i] = t;
      for (int i = 0; i < N; i++)
                                                                 print shuffled deck
         System.out.println(deck[i]);
```

# Shuffling a Deck of Cards

% java Deck 5 of Clubs Jack of Hearts 9 of Spades 10 of Spades 9 of Clubs 7 of Spades 6 of Diamonds 7 of Hearts 7 of Clubs 4 of Spades Queen of Diamonds 10 of Hearts 5 of Diamonds Jack of Clubs Ace of Hearts 5 of Spades

% java Deck 10 of Diamonds King of Spades 2 of Spades 3 of Clubs 4 of Spades Queen of Clubs 2 of Hearts 7 of Diamonds 6 of Spades Queen of Spades 3 of Spades Jack of Diamonds 6 of Diamonds 8 of Spades 9 of Diamonds 10 of Spades

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# Coupon Collector



# Coupon Collector Problem

Coupon collector problem. Given  ${\tt N}$  different card types, how many do you have to collect before you have (at least) one of each type?



assuming each possibility is equally likely for each card that you collect

Simulation algorithm. Repeatedly choose an integer  ${\tt i}$  between 0 and N-1. Stop when we have at least one card of every type.

- Q. How to check if we've seen a card of type i?
- A. Maintain a boolean array so that found[i] is true if we've already collected a card of type i.

# Coupon Collector: Java Implementation

```
public class CouponCollector
  public static void main(String[] args)
      int N = Integer.parseInt(args[0]);
      int cardcnt = 0; // number of cards collected
      int valcnt = 0;
                         // number of distinct cards seen so far
      // Do simulation.
      boolean[] found = new boolean[N];
      while (valcnt < N)
         int val = (int) (Math.random() * N);
         cardcnt++;
                                                type of next card
         if (!found[val])
                                                (between 0 and N-1)
            valcnt++;
            found[val] = true;
      // all N distinct cards found
      System.out.println(cardcnt);
```

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# Coupon Collector: Mathematical Context

Coupon collector problem. Given N different possible cards, how many do you have to collect before you have (at least) one of each type?

Ex. N = 30 baseball teams. Expect to wait  $\approx$  120 years before all teams win a World Series.

Coupon Collector: Debugging

Debugging. Add code to print contents of all variables.

val	found						valcnt	cardent	
Val	0	1	2	3	4	5	valent	Cardent	
	F	F	F	F	F	F	0	0	
2	F	F	T	F	F	F	1	1	
0	T	F	T	F	F	F	2	2	
4	T	F	T	F	T	F	3	3	
0	T	F	T	F	T	F	3	4	
1	T	T	T	F	T	F	4	5	
2	T	T	T	F	T	F	4	6	
5	T	Т	Т	F	Т	T	5	7	
0	T	Т	Т	F	Т	T	5	8	
1	T	Т	Т	F	Т	T	5	9	
3	Т	T	T	T	T	T	6	10	

Challenge. Debugging with arrays requires tracing many variables.

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# Coupon Collector: Scientific Context

- Q. Given a sequence from nature, does it have same characteristics as a random sequence?
- A. No easy answer many tests have been developed.

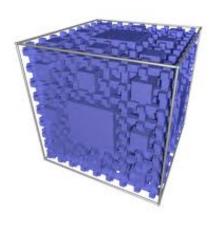
Coupon collector test. Compare number of elements that need to be examined before all values are found against the corresponding answer for a random sequence.







# Multidimensional Arrays



# Two Dimensional Arrays in Java

a[][]

Declare, create, initialize. Like 1D, but add another pair of brackets.

```
int M = 10;
int N = 3;
double[][] a = new double[M][N];
```

## Array access.

Use a[i][j] to access entry in row i and column j Both indices start at 0.

## Initialize.

This code is implicit (sets all entries to 0).

	a[U][U]	a[0][1]	a[0][2]			
	a[1][0]	a[1][1]	a[1][2]			
	a[2][0]	a[2][1]	a[2][2]			
j.	a[3][0]	a[3][1]	a[3][2]			
	a[4][0]	a[4][1]	a[4][2]			
	a[5][0]	a[5][1]	a[5][2]			
[6] -	a[6][0]	a[6][1]	a[6][2]			
	a[7][0]	a[7][1]	a[7][2]			
	a[8][0]	a[8][1]	a[8][2]			
	a[9][0]	a[9][1]	a[9][2]			
A 10-by-3 array						

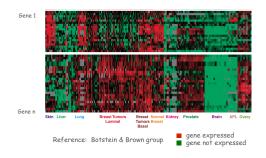
Warning. This implicit code might slow down your program for very big arrays.

# Two Dimensional Arrays

## Two dimensional arrays.

- Table of data for each experiment and outcome.
- Table of grades for each student and assignments.
- Table of grayscale values for each pixel in a 2D image.

Mathematical abstraction. Matrix. Java abstraction. 2D array.



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# Setting 2D Array Values at Compile Time

Initialize 2D array by listing values.

```
double[][] p =
{
    { .92, .02, .02, .02, .02 },
    { .02, .92, .32, .32 },
    { .02, .02, .02, .92, .02 },
    { .92, .02, .02, .02, .02 },
    { .47, .02, .47, .02, .02 },
};
```

## Matrix Addition

Matrix addition. Given two N-by-N matrices a and b, define c to be the N-by-N matrix where c[i][j] is the sum a[i][j] + b[i][j].

```
double[][] c = new double[N][N];
for (int i = 0; i < N; i++)
   for (int j = 0; j < N; j++)
      c[i][j] = a[i][j] + b[i][j];</pre>
```

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# Array Challenge 4

How many multiplications to multiply two N-by-N matrices?

```
double[][] c = new double[N][N];
for (int i = 0; i < N; i++)
  for (int j = 0; j < N; j++)
    for (int k = 0; k < N; k++)
        c[i][j] += a[i][k] * b[k][j];</pre>
```

- A. N
- B. N<sup>2</sup>
- C. N<sup>3</sup>
- D. N<sup>4</sup>

# Matrix Multiplication

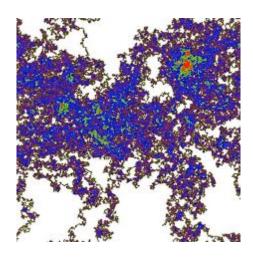
Matrix multiplication. Given two N-by-N matrices a and b, define c to be the N-by-N matrix where c[i][j] is the dot product of the  $i^{th}$  row of a and the  $j^{th}$  column of b.

```
a[][] .70 .2<u>0 .10</u>
                                                      .30 .60 .10 ←row 1
                         all values initialized to 0
                                                      .50 .10 .40
double[][] c = new double[N][N];
                                                            column 2
for (int i = 0; i < N; i++)
   for (int j = 0; j < N; j++)
                                                b[][]
                                                      .80 .30 .50
      for (int k = 0; k < N; k++)
                                                      .10 .40 .10
          c[i][j] += a[i][k] * b[k][j];
                                                      .10 .30 .40
                                                             c[11[2] = .3 *.5
                                               c[][] .59 .32 .41
```

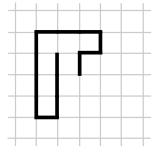
4

.31 .36 <mark>.25</mark> .45 .31 .42

# Application: 2D Random Walks



# Application: Self-Avoiding Walks





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# Self-Avoiding Walk

#### Model.

- N-by-N lattice.
- Start in the middle.
- Randomly move to a neighboring intersection, avoiding all previously visited intersections.
- Two possible outcomes: escape and dead end





Applications. Polymers, statistical mechanics, etc.

- Q. What fraction of time will you escape in an 5-by-5 lattice?
- Q. In an N-by-N lattice?
- Q. In an N-by-N-by-N lattice?

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# Self-Avoiding Walk: Implementation

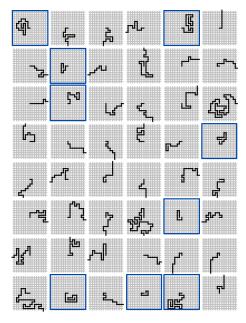
```
public class SelfAvoidingWalk
   public static void main(String[] args)
                                            // lattice size
      int N = Integer.parseInt(args[0]);
      int T = Integer.parseInt(args[1]);
                                             // number of trials
      int deadEnds = 0;
                                             // trials ending at dead end
      for ( each trial )
         boolean[][] a = new boolean[N][N]; // intersections visited
         int x = N/2, y = N/2;
                                              // current position
         while ( you're still inside the lattice )
            if ( you're at a dead end )
                                                                              dead end
            { deadEnds++; break; }
            a[x][y] = true;
                                             // mark as visited
            double r = Math.random();
                    (r < 0.25) \{ if (!a[x+1][y]) x++; \}
                                                                             take a random
            else if (r < 0.50) { if (!a[x-1][y]) x--; }
                                                                              step to a new
            else if (r < 0.75) { if (!a[x][y+1]) y++; }
                                                                              intersection
            else if (r < 1.00) { if (!a[x][y-1]) y--; }
      System.out.println(100*deadEnds/T + "% dead ends");
```

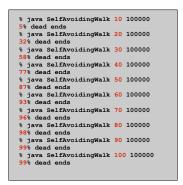
# Self-Avoiding Walk: Implementation

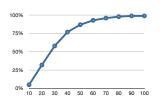
```
public class SelfAvoidingWalk
   public static void main(String[] args)
                                             // lattice size
      int N = Integer.parseInt(args[0]);
      int T = Integer.parseInt(args[1]);
                                             // number of trials
      int deadEnds = 0;
                                             // trials ending at dead end
      for (int t = 0; t < T; t++)
         boolean[][] a = new boolean[N][N]; // intersections visited
         int x = N/2, y = N/2;
                                              // current position
         while (x > 0 && x < N-1 && y > 0 && y < N-1)
            if (a[x-1][y] \&\& a[x+1][y] \&\& a[x][y-1] \&\& a[x][y+1])
                                                                              dead end
            { deadEnds++; break; }
                                             // mark as visited
            a[x][y] = true;
            double r = Math.random();
                    (r < 0.25) \{ if (!a[x+1][y]) x++; \}
                                                                              take a random
            else if (r < 0.50) { if (!a[x-1][y]) x--; }
                                                                              step to a new
            else if (r < 0.75) { if (!a[x][y+1]) y++; }
                                                                              intersection
            else if (r < 1.00) { if (!a[x][y-1]) y--; }
      System.out.println(100*deadEnds/T + "% dead ends");
```

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# Self-Avoiding Walks







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# Summary

### Arrays.

- Organized way to store huge quantities of data.
- Almost as easy to use as primitive types.
- You can directly (and very quickly) access an element given its index.
- You can have as many dimensions as you like!

#### Caveats:

- Need to fix size of array ahead of time.
- Don't forget to allocate memory with new.
- Indices start at 0 not 1.
- Out-of-bounds to access a[-1] or a[N] of N element array.
- -in Java: ArrayIndexOutOfBoundsException
- in C: "ghastly error"

Ahead. Reading in large quantities of data from a file into an array.