

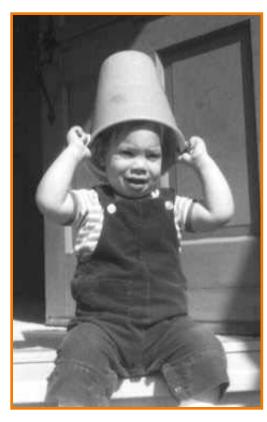
Image Processing

COS 426

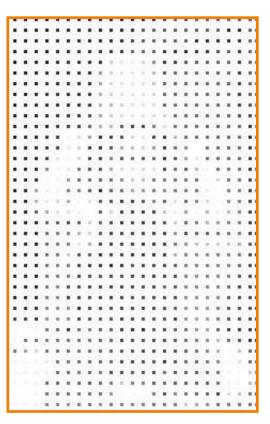
What is a Digital Image?



A digital image is a discrete array of samples representing a continuous 2D function



Continuous function



Discrete samples

Limitations on Digital Images



- Spatial discretization
- Quantized intensity
- Approximate color (RGB)
- (Temporally discretized frames for digital video)

Image Processing



- Changing intensity/color Moving image locations
 - Linear: scale, offset, etc.
 - Nonlinear: gamma, saturation, etc.
 - Add random noise
- Filtering over neighborhoods
 - Blur
 - Detect edges
 - Sharpen
 - **Emboss**
 - Median

- - Scale
 - Rotate
 - Warp
- Combining images
 - Composite
 - Morph

Similar to Analog / Continuous



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Account for Limitations of Digital



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Inherently New Digital Operations



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- Quantization
- Spatial / intensity tradeoff
 - Dithering

Digital Image Processing



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Adjusting Brightness



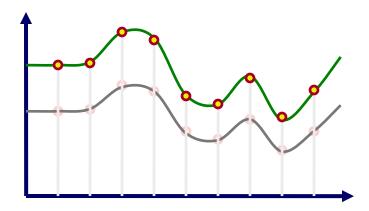
- Simply scale pixel components
 - o Must clamp to range, e.g. [0..1] or [0..255]



Original



Brighter

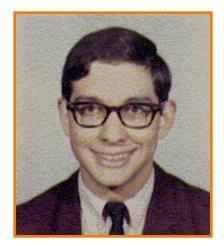


Note: this is "contrast" on your monitor! "Brightness" adjusts black level (offset)

Adjusting Contrast



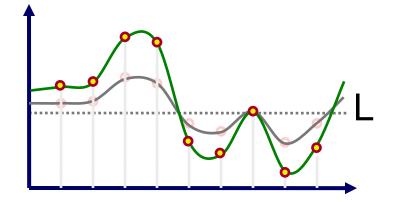
- Compute mean luminance L for all pixels
 o luminance = 0.30*r + 0.59*g + 0.11*b
- Scale deviation from L for each pixel component
 o Must clamp to range (e.g., 0 to 1)



Original

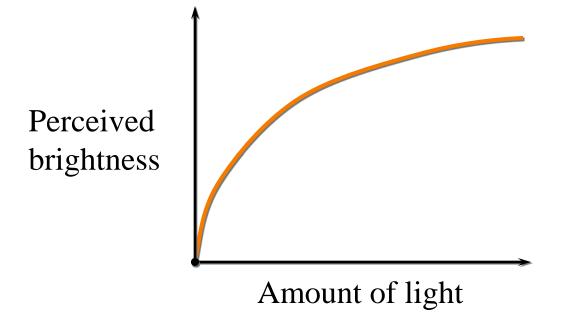


More Contrast



Digression: Perception of Intensity

Perception of intensity is nonlinear



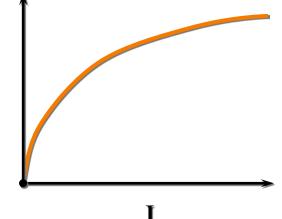
Modeling Nonlinear Intensity Response

 Brightness (B) usually modeled as a logarithm or power law of intensity (I)

 \mathbf{B}

$$B = k \log I$$

$$B = I^{1/3}$$



 Exact curve varies with ambient light, adaptation of eye

Cameras

 Original cameras based on Vidicon obey power law for Voltage (V) vs. Intensity (I):

$$V = I^{\gamma}$$

$$\gamma \approx 0.45$$

CRT Response

Power law for Intensity (I) vs.
 applied voltage (V)

$$I = V^{\gamma}$$

$$\gamma \approx 2.5$$

- Vidicon + CRT = almost linear!
- Other displays (e.g. LCDs) contain electronics to emulate this law

CCD Cameras

- Camera gamma codified in NTSC standard
- CCDs have linear response to incident light
- Electronics to apply required power law

- So, pictures from most cameras (including digital still cameras) will have $\gamma = 0.45$
 - sRGB standard: partly-linear, partly power-law curve well approximated by $\gamma = 1 / 2.2$

Digital Image Processing



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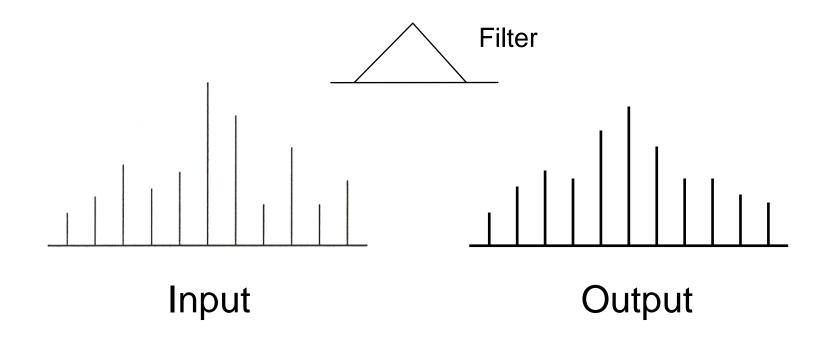
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- Spatial / intensity tradeoff
 - Dithering

Basic Operation: Convolution



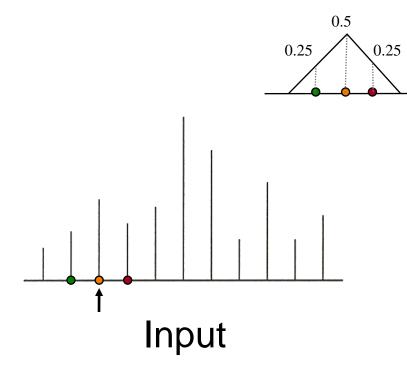
Output value is weighted sum of values in neighborhood of input image

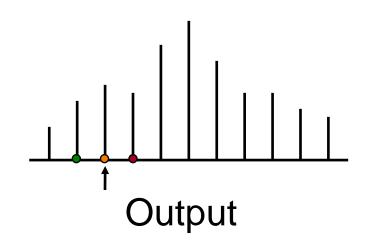
Pattern of weights is the "filter" or "kernel"



Filter

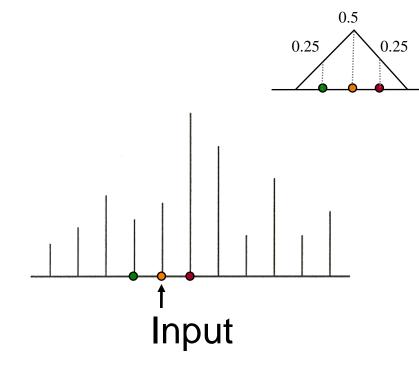


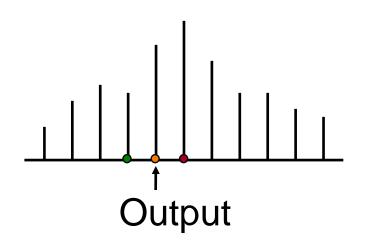




Filter



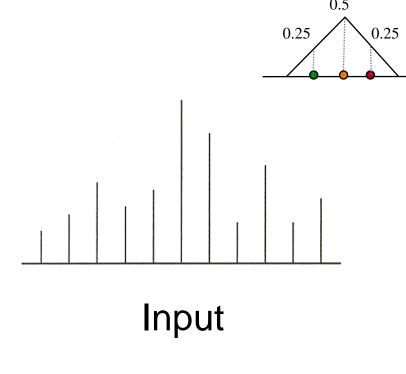


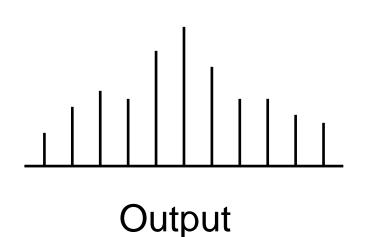


Filter



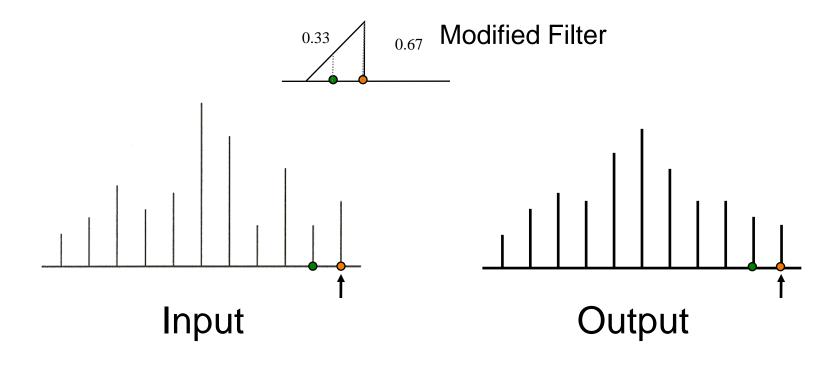
What if the filter runs off the end?





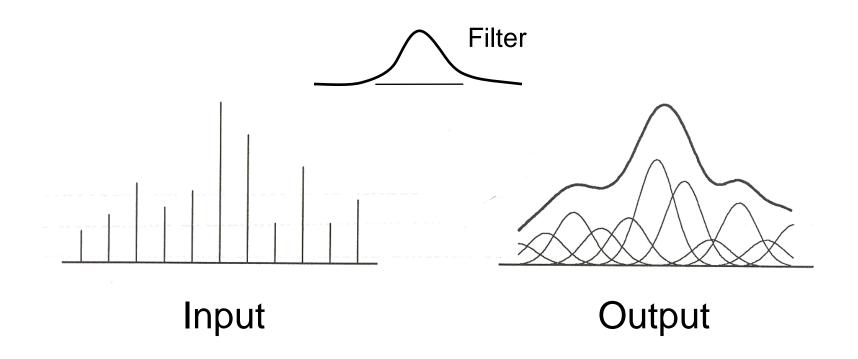


Common option: normalize the filter



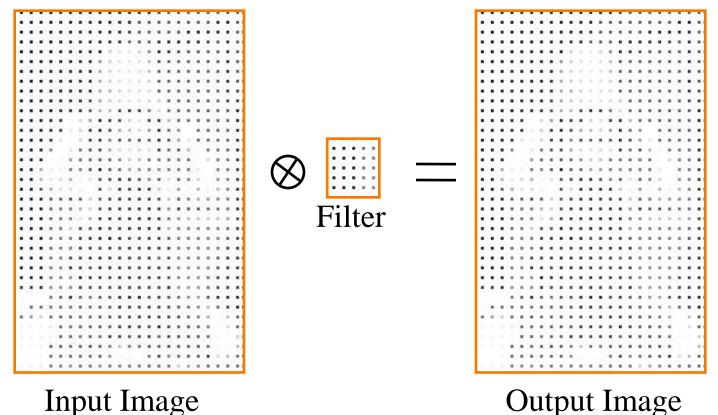
Convolution with a Gaussian Filter







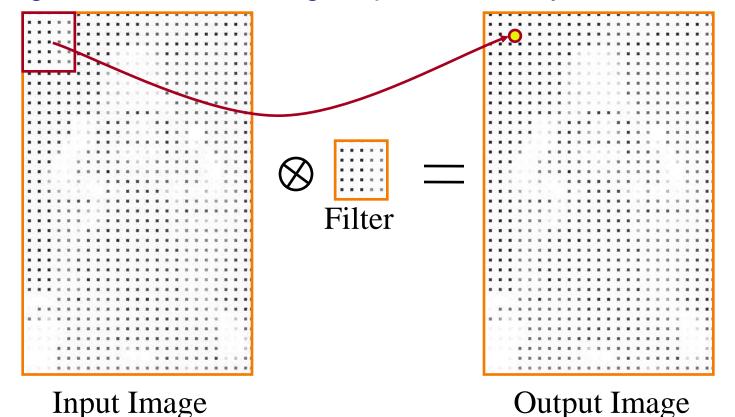
2D Convolution







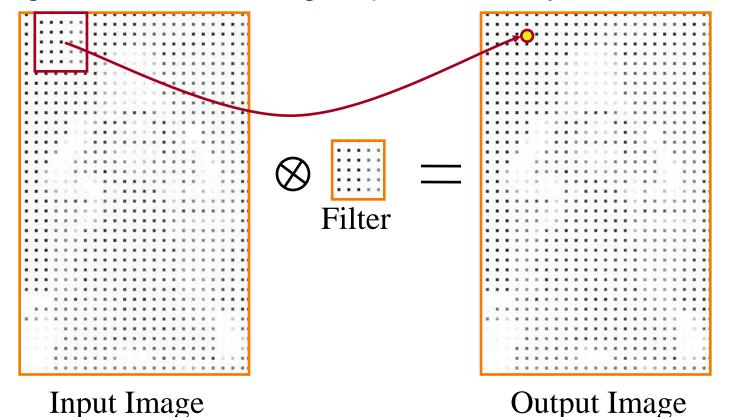
2D Convolution





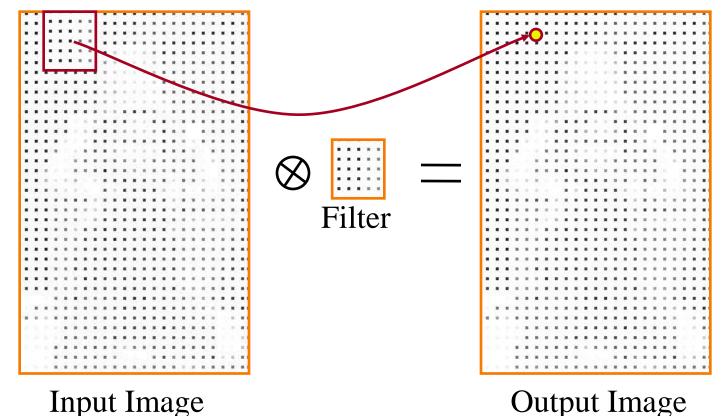


2D Convolution





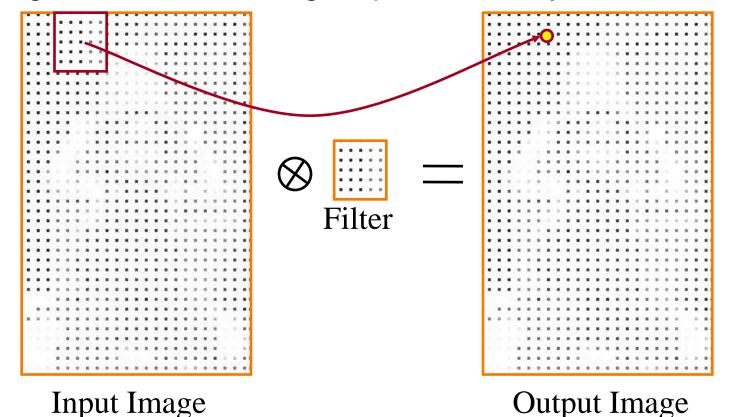
2D Convolution







2D Convolution

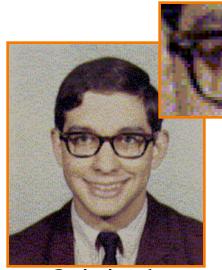




Blur



Convolve with a filter whose entries sum to one o Each pixel becomes a weighted average of its neighbors



Original



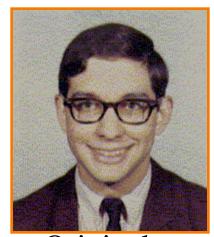
Blur

Filter =
$$\begin{bmatrix} 1/& 2/& 1/\\ /16 & /16 & /16 \\ 2/& 4/& 2/\\ /16 & /16 & /16 \\ 1/& 2/& 1/\\ /16 & /16 & /16 \end{bmatrix}$$

Edge Detection



Convolve with a filter that finds differences between neighbor pixels



Original



Detect edges

Filter =
$$\begin{bmatrix} -1 & -1 & -1 \\ -1 & +8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$

Sharpen



Sum detected edges with original image



Original



Sharpened

Filter =
$$\begin{bmatrix} -1 & -1 & -1 \\ -1 & +9 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$

Emboss



Convolve with a filter that highlights gradients in particular directions



Original



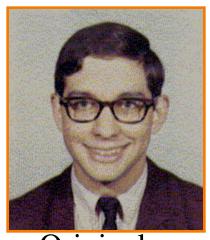
Embossed

$$Filter = \begin{bmatrix} -1 & -1 & 0 \\ -1 & 0 & 1 \\ 0 & 1 & 1 \end{bmatrix}$$

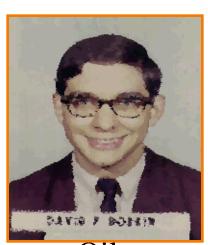
Non-Linear Filtering



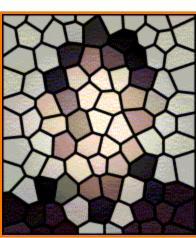
Each output pixel is a non-linear function of input pixels in neighborhood (filter depends on input)



Original



Oil



Stained Glass

Digital Image Processing



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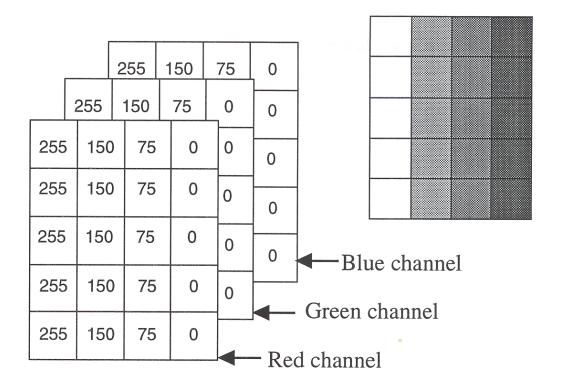
- - Scale
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- Quantization
- Spatial / intensity tradeoff
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Quantization



Reduce intensity resolution

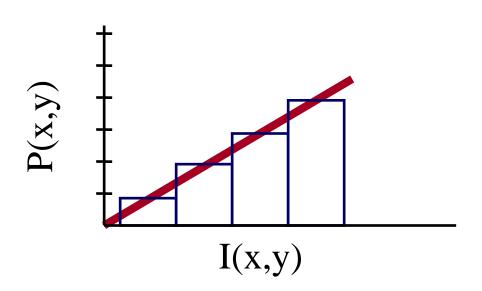
- o Frame buffers have limited number of bits per pixel
- o Physical devices have limited dynamic range



Uniform Quantization

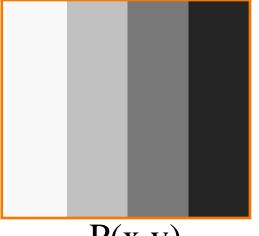


P(x, y) = round(I(x, y))
where round() chooses nearest
value that can be represented.





I(x,y)

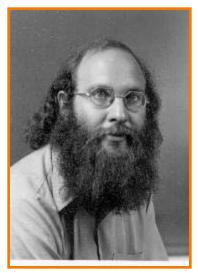


P(x,y) (2 bits per pixel)

Uniform Quantization



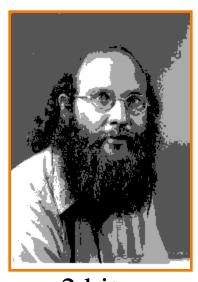
Images with decreasing bits per pixel:



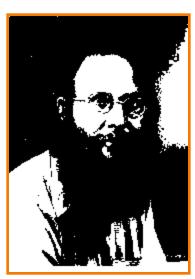
8 bits



4 bits



2 bits



1 bit

Notice contouring.

Reducing Effects of Quantization



- Intensity resolution / spatial resolution tradeoff
- Dithering
 - o Random dither
 - o Ordered dither
 - o Error diffusion dither
- Halftoning
 - o Classical halftoning

Dithering

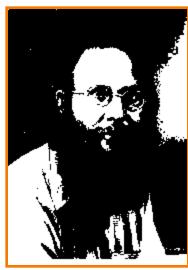


Distribute errors among pixels

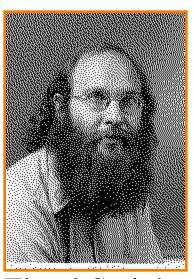
- o Exploit spatial integration in our eye
- o Display greater range of perceptible intensities



Original (8 bits)



Uniform
Quantization
(1 bit)



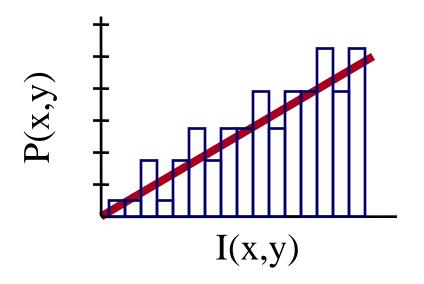
Floyd-Steinberg
Dither
(1 bit)

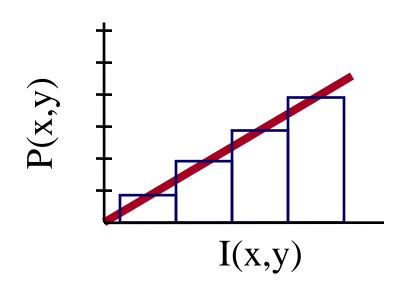
Random Dither



Randomize quantization errors

o Errors appear as noise

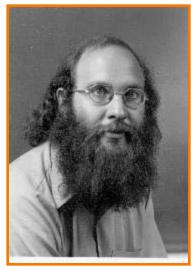




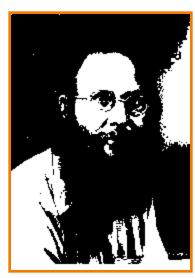
$$P(x, y) = round(I(x, y) + noise(x,y))$$

Random Dither

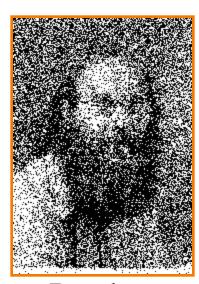




Original (8 bits)



Uniform
Quantization
(1 bit)



Random
Dither
(1 bit)

Ordered Dither



Pseudo-random quantization errors

o Matrix stores pattern of threshholds

$$i = x \mod n$$

 $j = y \mod n$
 $e = I(x,y) - trunc(I(x,y))$
 $threshold = (D(i,j)+1)/(n^2+1)$
 $if (e > threshold)$
 $P(x,y) = ceil(I(x,y))$
 $else$
 $P(x,y) = floor(I(x,y))$

Ordered Dither



Bayer's ordered dither matrices

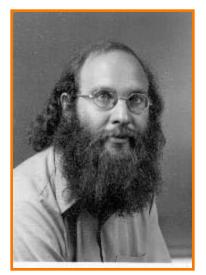
$$D_{n} = \begin{bmatrix} 4D_{n/2} + D_{2}(1,1)U_{n/2} & 4D_{n/2} + D_{2}(1,2)U_{n/2} \\ 4D_{n/2} + D_{2}(2,1)U_{n/2} & 4D_{n/2} + D_{2}(2,2)U_{n/2} \end{bmatrix}$$

$$D_2 = \begin{bmatrix} 3 & 1 \\ 0 & 2 \end{bmatrix}$$

$$D_2 = \begin{bmatrix} 3 & 1 \\ 0 & 2 \end{bmatrix} \qquad D_4 = \begin{bmatrix} 15 & 7 & 13 & 5 \\ 3 & 11 & 1 & 9 \\ 12 & 4 & 14 & 6 \\ 0 & 8 & 2 & 10 \end{bmatrix}$$

Ordered Dither

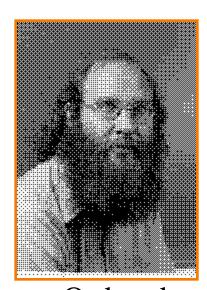




Original (8 bits)



Random Dither (1 bit)



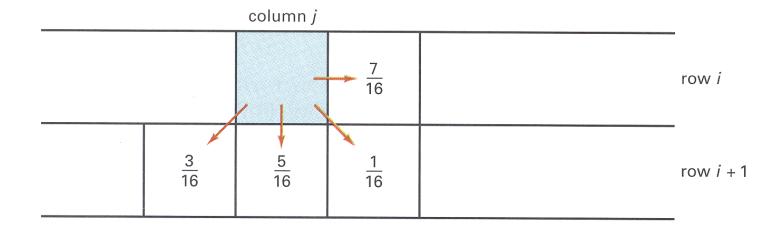
Ordered
Dither
(1 bit)

Error Diffusion Dither



Spread quantization error over neighbor pixels

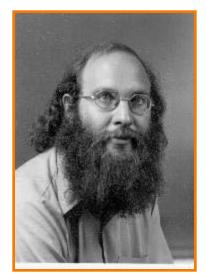
- o Error dispersed to pixels right and below
- o Floyd-Steinberg weights:



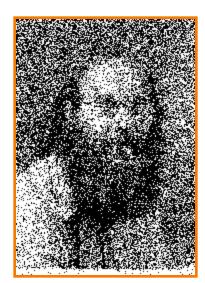
$$3/16 + 5/16 + 1/16 + 7/16 = 1.0$$

Error Diffusion Dither

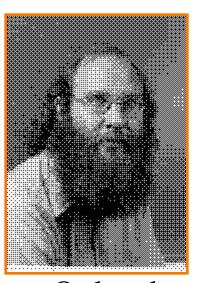




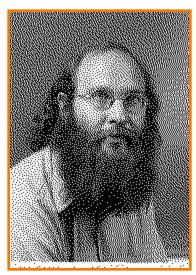
Original (8 bits)



Random
Dither
(1 bit)



Ordered Dither (1 bit)



Floyd-Steinberg
Dither
(1 bit)

Reducing Effects of Quantization

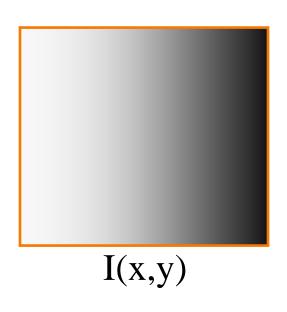


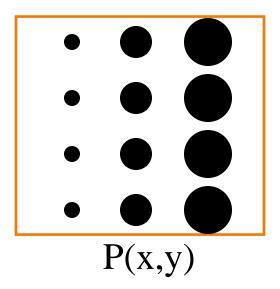
- Dithering
 - o Random dither
 - o Ordered dither
 - o Error diffusion dither
- Halftoning
 - o Classical halftoning

Classical Halftoning



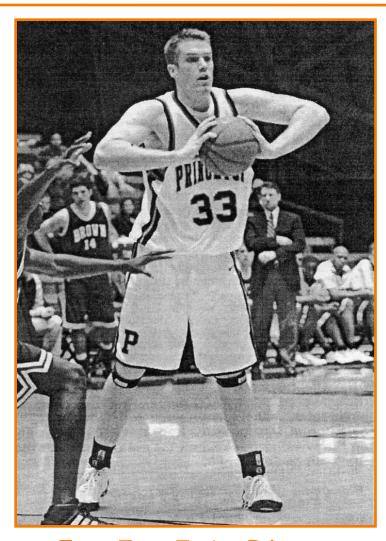
Use dots of varying size to represent intensities of Area of dots proportional to intensity in image



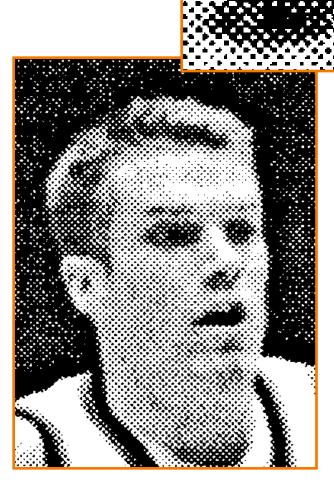


Classical Halftoning





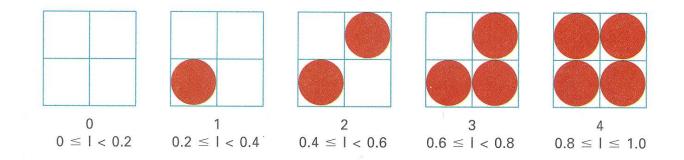
From Town Topics, Princeton



Digital Halftone Patterns



Use cluster of pixels to represent intensity



Q: In this case, would we use four "halftoned" pixels in place of one original pixel?

Summary



- Image filtering
 - o Compute new values for image pixels based on function of old values
- Halftoning and dithering
 - o Reduce visual artifacts due to quantization
 - o Distribute errors among pixels
 - » Exploit spatial integration in our eye

Next Time...



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