# COS 426, Spring 2011 Midterm 1

Name:

NetID:

Honor Code pledge:

Signature:

This exam consists of 6 questions. Do all of your work on these pages (use the back for scratch space), giving the answer in the space provided. This is a closed-book exam, but you may use one page of notes during the exam. **Put your NetID on every page (1 point), and write out and sign the Honor Code pledge before turning in the test:** 

"I pledge my honor that I have not violated the Honor Code during this examination."

Question	Score
1	
2	
3	
4	
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6	
NetID on	
every page	
Total	

#### 1. Color (15 points)

a) For each statement, list *all* the colorspaces from the following list to which it applies: RGB, HSV, XYZ, CMY

- Can represent all pure spectral colors with positive values:
- Represents white with (0,0,0):
- Is a linear transformation of RGB:
- Is an affine transformation of RGB:
- Is especially well suited for sending colors to printers:
- Represents each color uniquely:

b) The U-store is designing orange-tinted sunglasses to sell to rabid Princeton fans, and receives two samples of "orange" color filters: filter A and filter B. You look through each filter at a white wall and, sure enough, it appears orange through both. However, when looking at a red car, you notice that it appears red through filter material A and black through filter material B. Explain why this may be the case. (Hint: think spectrally.)

2. Signal processing (15 points)Complete the following sentences:a) A *pixel* is ...

b) *Dithering* is used to ...

c) For a signal with bandwidth *b*, the *Nyquist rate* is ...

d) *Aliasing* can occur when ...

and may have some of the following manifestations:

e) *Resampling* is used to ...

#### 3. Morphing (25 points)

Beier and Neely, in their 1992 paper, determined warps based on line correspondences. What if they had used point correspondences instead? Let us try to devise a morphing method for a user interface that only provides point correspondences. Keep in mind that there are several equally good ways to solve this problem.

**Notation:** given source image A(x, y) and target image B(x, y) with source points  $(a_1, a_2, ..., a_n)$  and corresponding target points  $(b_1, b_2, ..., b_n)$ , determine the intermediate image  $I_t(x, y)$  at some time 0 < t < 1.

In case you find it useful, here is equation 4 of the Beier-Neely paper:

weight = 
$$\left(\frac{\text{length }^p}{a + \text{dist}}\right)^b$$
.

a) Suppose n = 1 (i.e., one point correspondence is specified). Describe how would you find  $I_t(x, y)$ . Give an exact formula in terms of A, B,  $a_1$ , and  $b_1$ .

b) For arbitrary *n* and some time *t*, describe how you would find the intermediate locations of feature points  $(i_1(t), i_2(t), \dots, i_n(t))$ .

c) Now describe how you would find  $I_t(x, y)$  for an arbitrary number of corresponding points. You can re-use formulas you defined in (a) and (b).

d) Describe the difference, if any, between the Beier-Neely method with a single line correspondence, and your scheme with n = 1 point.

e) Describe the difference, if any, between the Beier-Neely method with a single line correspondence, and your scheme with n = 2 points.

f) What are the advantages and disadvantages, if any, of using points over lines? If applicable, describe potential scenarios in which points or lines would work better.

### 4. 3D Representations (8 points)

After graduating from Princeton and earning multiple metric tons of money, you decide to have a custom jet designed for you. Of the following 3D representations:

implicit function, triangle mesh, B-spline

which one will your private horde of engineers find most convenient for performing each of the following tasks? Choose the *single best* answer for each question.

- Efficient graphics-hardware-based rendering:
- During an airflow simulation, checking whether a 3D point is inside or outside the airplane:
- Ensuring that the wing design is  $C^2$  continuous:
- Given separate models of the wings and fuselage, combining them into a single model of the surface of the whole airplane:
- Representing the final shape of the fuselage as exactly and compactly as possible:
- Ensuring that, when part of the design is outsourced, what comes back is guaranteed to be a valid manifold surface:
- Accurately representing the crease between the wing and fuselage:
- Finding the exact curve representing the wing's leading edge:

## **5. Half-edge data structure** (16 points)

Consider the following patch of a polygonal mesh.



a) Draw and number the half-edges in the diagram.

b) Write out the complete contents of the half-edge, face, and vertex tables (omitting the vertex coordinates) for this mesh. Make your arrays 0-based, and use indices instead of pointers.

c) Suppose that vertex v4 is removed from the mesh. Which half-edges must be removed from your data structure?

d) For the scenario in (c), list all other changes that must be made to your half-edge, face, and vertex tables.

### 6. Transformations (20 points)

a) Write down a 2 × 2 transformation matrix that reflects a 2-D point (represented as a 2 × 1 column vector) about the line ax + by = 0 (assuming  $a^2 + b^2 = 1$ ).

b) Sketch a proof that the composition of any two such reflections is a rotation about the origin. (The proof need not use the matrix formula you derived above; it is fine to argue geometrically.) What is the angle of the resulting rotation, as a function of the angle between the two lines?