

Client, implementation, interface

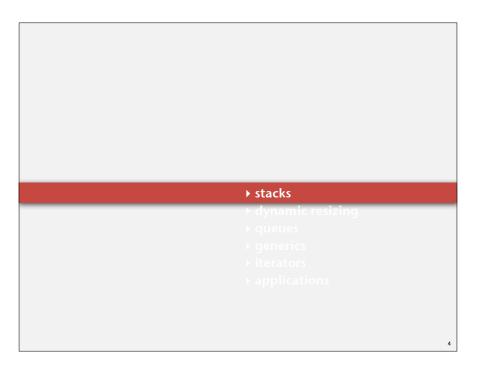
Separate interface and implementation.

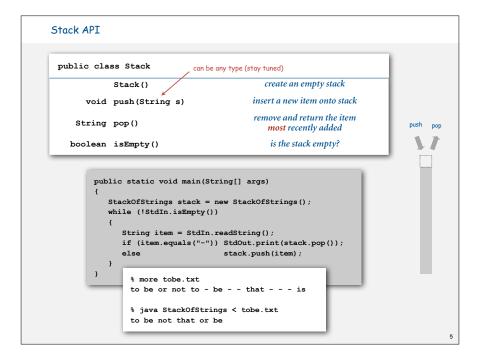
Ex: stack, queue, priority queue, symbol table, union-find,

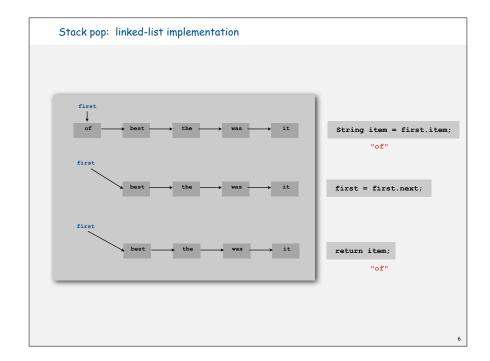
Benefits.

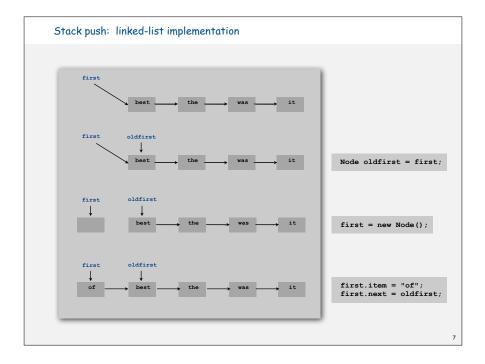
- Client can't know details of implementation ⇒
 client has many implementation from which to choose.
- Implementation can't know details of client needs ⇒ many clients can re-use the same implementation.
- Design: creates modular, reusable libraries.
- Performance: use optimized implementation where it matters.

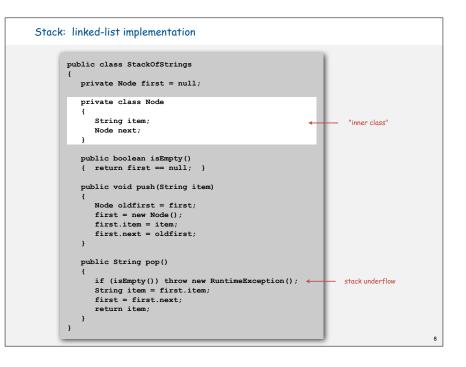
Client: program using operations defined in interface. Implementation: actual code implementing operations. Interface: description of data type, basic operations.

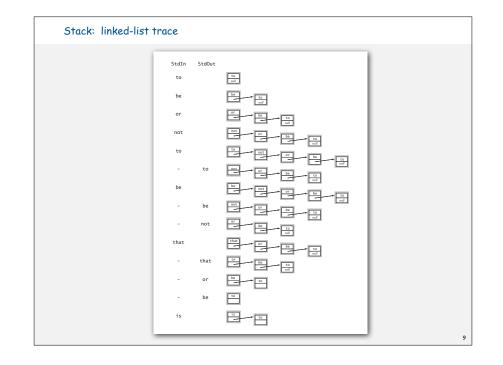


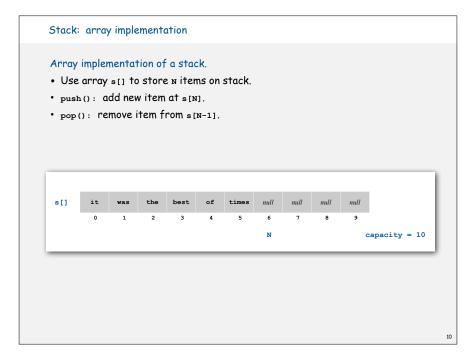


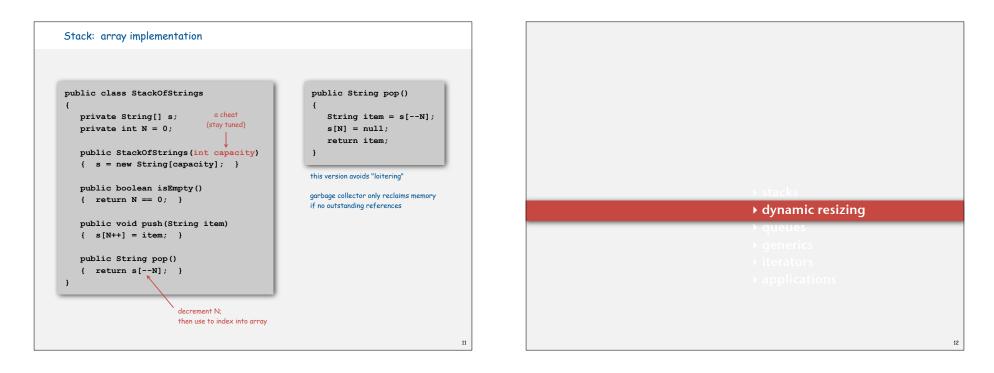


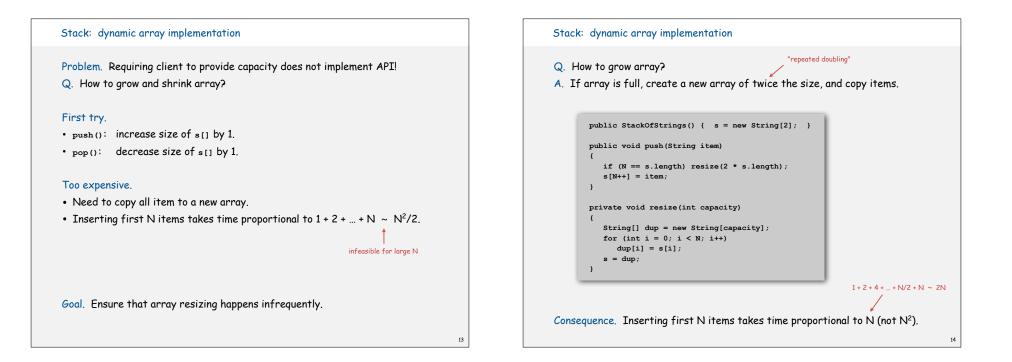












Stack: dynamic array implementation

Q. How to shrink array?

First try.

- push(): double size of s[] when array is full.
- pop(): halve size of s[] when array is half full.

Too expensive

- · Consider push-pop-push-pop-... sequence when array is full.
- Takes time proportional to N per operation.



"thrashing"

Stack: dynamic array implementation Q. How to shrink array? Efficient solution. • push(): double size of s[] when array is full. • pop(): halve size of s[] when array is one-quarter full. public String pop() { string item = s[--N]; s[N] = null; if (N > 0 & & N == s.length/4) resize(s.length / 2); return item; }

16

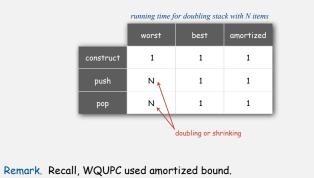
Invariant. Array is always between 25% and 100% full.

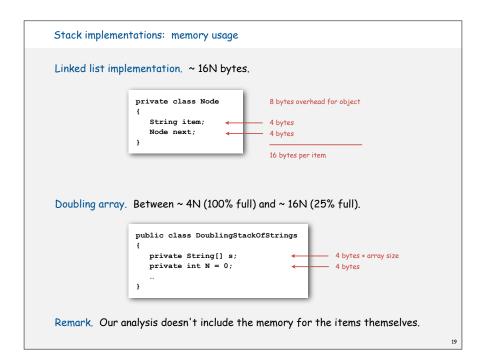
StdIn	StdOut	Ν	a.length	0	1	а 2	3	4	5	6	7
		0	1	null							
to		1		to							
be		2	2	to	be						
or		3	4	to		or	null				
not		4	4	to			not				
to		5	8	to			not	to	null	null	null
-	to	4	8	to			not	null			
be		5	8	to			not	be			
-	be	4	8	to			not	null			
-	not	3	8	to			null				
that		4	8	to			that				
-	that	3	8	to			null				
-	or	2	4	to		null	null				
-	be	1	2	to	null						
is		2	2	to	is						

Amortized analysis

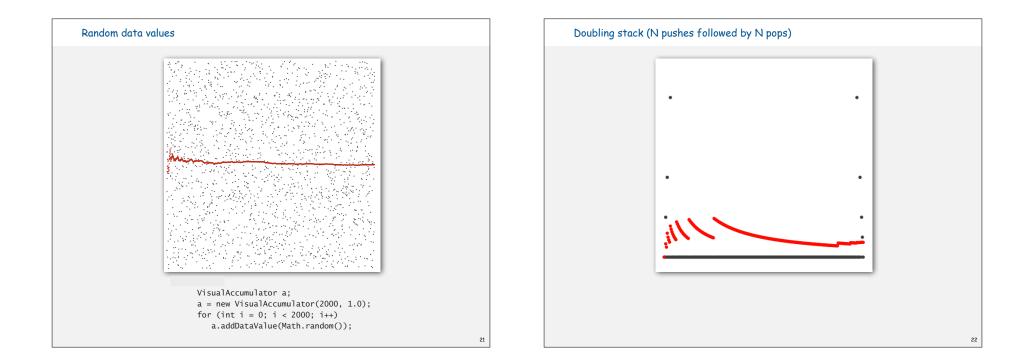
Amortized analysis. Average running time per operation over a worst-case sequence of operations.

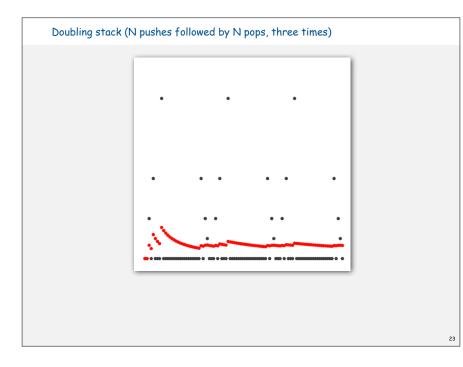
Proposition. Starting from empty stack, any sequence of M push and pop ops takes time proportional to M.





Amortized analysis	
Often useful to compute average cost per operation	n over a sequence of ops
<pre>public class VisualAccumulator { private double total; private int N;</pre>	
<pre>public VisualAccumulator(int maxN, double max) { StdDraw.setXscale(0, maxN); StdDraw.setYscale(0, max); StdDraw.setPenRadius(.005); }</pre>	height of Nth red dot from the left is the average of the heights of the leftmost N gray dots
<pre>public void addDataValue(double val) { N++; total += val; StdDraw.setPenColor(StdDraw.DARK_GRAY); StdDraw.point(N, val); StdDraw.setPenColor(StdDraw.RED); StdDraw.point(N, total/N); } }</pre>	• height of gray dot is the data point value Visual accumulator plot
	20







Stack implementations: dynamic array vs. linked List

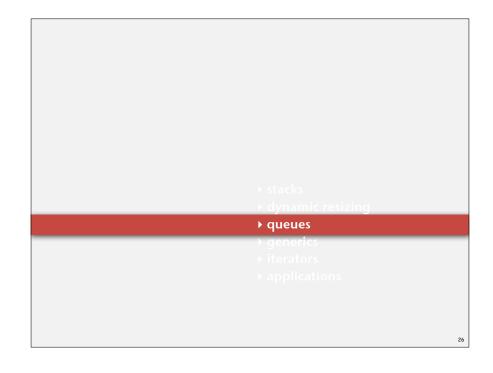
Tradeoffs. Can implement with either array or linked list; client can use interchangeably. Which is better?

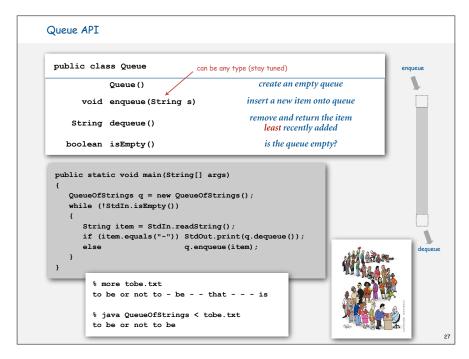
Linked list.

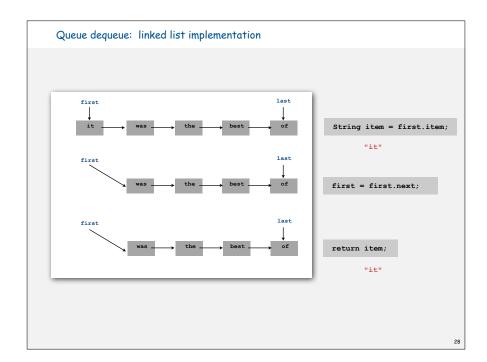
- Every operation takes constant time in worst-case.
- Uses extra time and space to deal with the links.

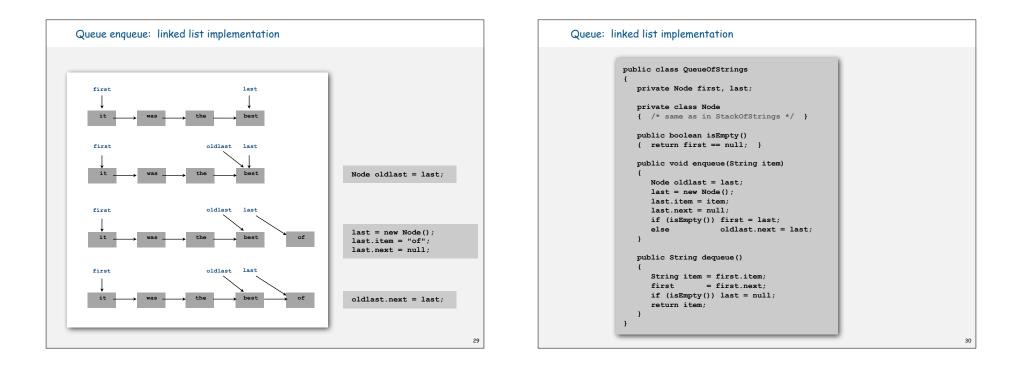
Array.

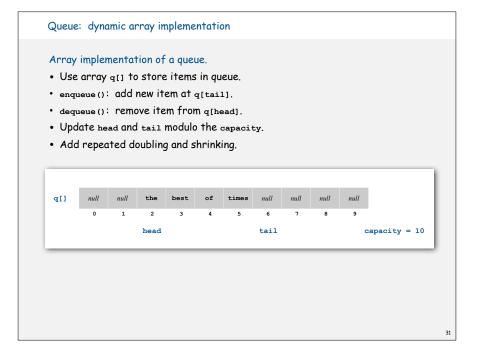
- Every operation takes constant amortized time.
- Less wasted space.

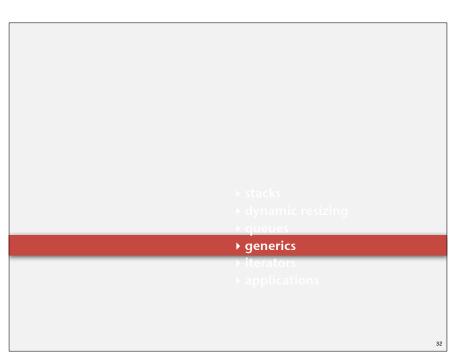












Parameterized stack

We implemented: stackOfstrings.

We also want: StackOfURLs, StackOfCustomers, StackOfInts, etc?

Attempt 1. Implement a separate stack class for each type.

- Rewriting code is tedious and error-prone.
- · Maintaining cut-and-pasted code is tedious and error-prone.

@#\$*! most reasonable approach until Java 1.5. [hence, used in Algorithms in Java, 3rd edition]

Parameterized stack

We implemented: stackofstrings.

We also want: StackOfURLs, StackOfCustomers, StackOfInts, etc?

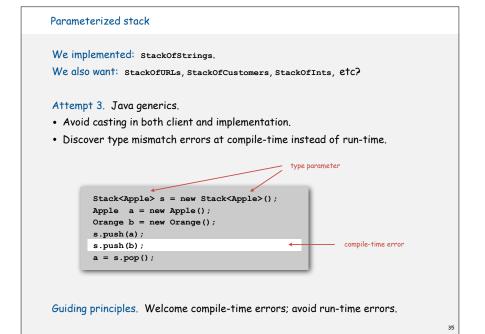
Attempt 2. Implement a stack with items of type object.

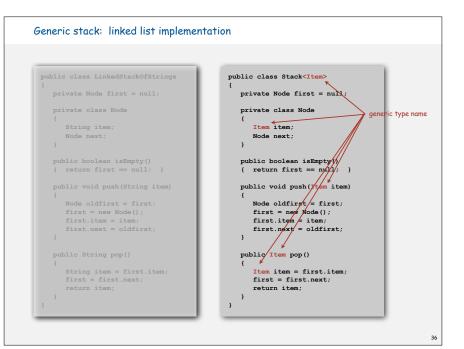
• Casting is required in client.

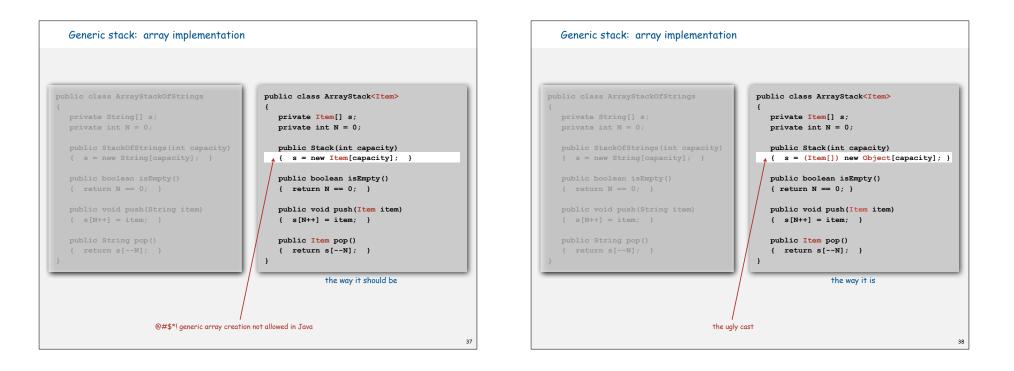
33

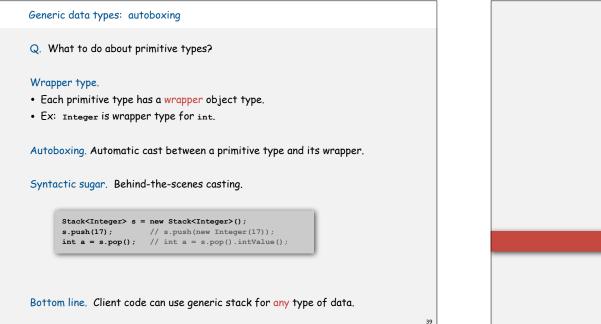
• Casting is error-prone: run-time error if types mismatch.

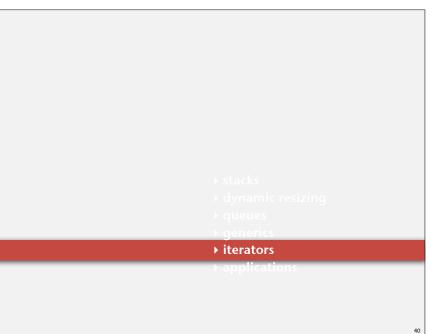
StackOfObjects s = new StackOfObjects(); Apple a = new Apple(); Orange b = new Orange(); s.push(a); s.push(b); a = (Apple) (s.pop());

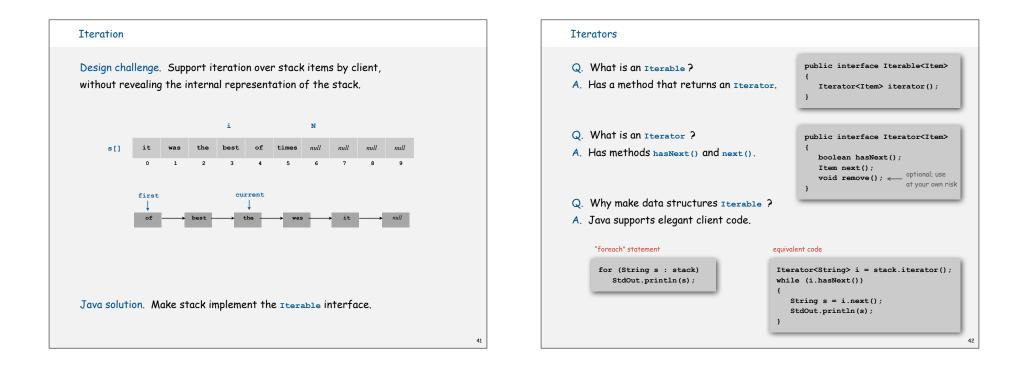


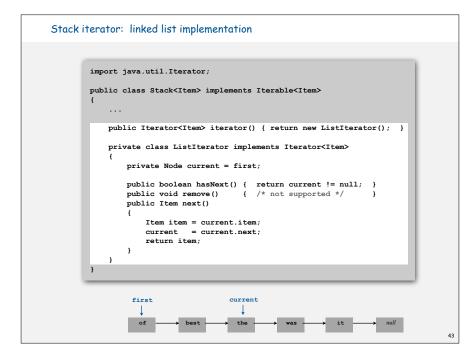




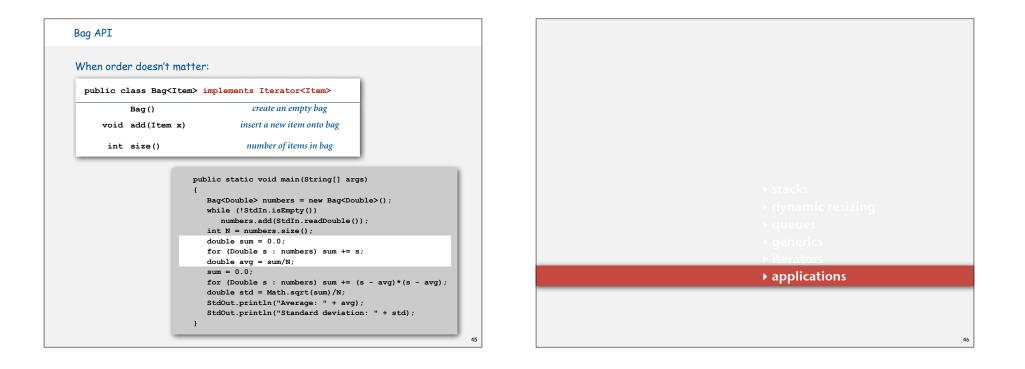








Stack iterat	or: array	impleme	ntation								
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	private cl {	lass Array	Iterator	imple	ements	Iterat	or <ite< td=""><td>n></td><td></td><td></td><td></td></ite<>	n>			
	-	te int i =	N;								
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}	5										
_			_	_	_	_	_	_	_	_	
			i			N					
s[]	it	was the	best	of	times	null	null	null	null		
	0	1 2	3	4	5	6	7	8	9		
											44



Java collections library

java.util.List API.

- boolean isEmpty()
- int size()
- void add(Item item)
- void add(int index, Item item) Insert item at specified index.
- Item get(int index)
- Item remove(int index)
- Item set(int index Item item)
- boolean contains(Item item)
- Iterator<Item> iterator()
- ...

Implementations.

- java.util.ArrayList implements API using an array.
- java.util.LinkedList implements API using a (doubly) linked list.

Is the list empty?

Return iterator.

Return number of items on the list.

Return and delete item at given index.

Insert a new item to end of list.

Replace element at given index.

Does the list contain the item?

Return item at given index.

Java collections library

java.util.Stack.

- Supports push(), pop(), size(), isEmpty(), and iteration.
- Also implements java.util.List interface from previous slide,
 e.g., set(), get(), and contains().
- Bloated and poorly-designed API \Rightarrow don't use.

java.util.Queue.

• An interface, not an implementation of a queue.

Best practices. Use our implementations of stack, Queue, and Bag.

War story (from COS 226)

Generate random open sites in an N-by-N percolation system.

- Jenny: pick (i, j) at random; if closed, repeat. Takes ~ c1 N² seconds.
- Kenny: maintain a java.util.ArrayList of open sites.
 Pick an index at random and delete.
 Takes ~ c₂ N⁴ seconds.
- Q. Why is Kenny's code so slow?

Lesson. Don't use a library until you understand its API! COS 226. Can't use a library until we've implemented it in class.

Stack applications

49

51

Real world applications.

- Parsing in a compiler.
- Java virtual machine.
- Undo in a word processor.
- Back button in a Web browser.
- PostScript language for printers.
- Implementing function calls in a compiler.

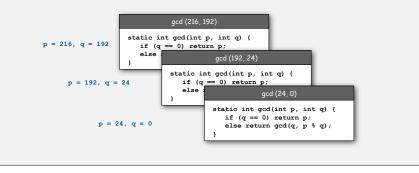
Function calls

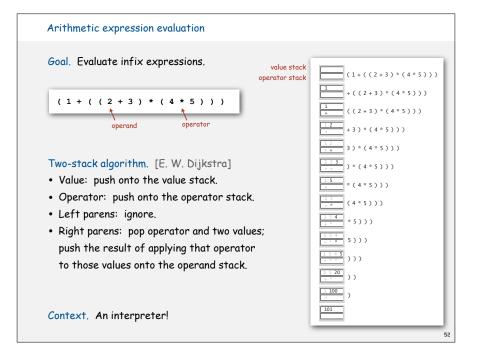
How a compiler implements a function.

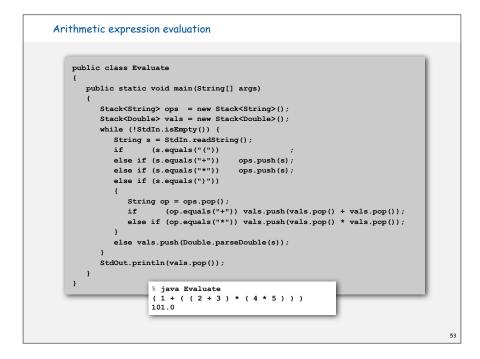
- Function call: push local environment and return address.
- Return: pop return address and local environment.

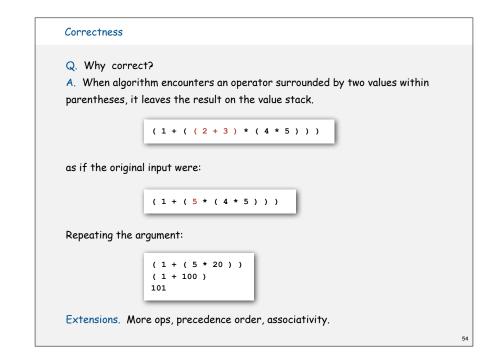
Recursive function. Function that calls itself.

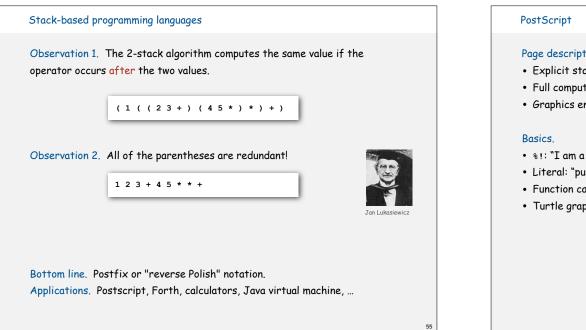
Note. Can always use an explicit stack to remove recursion.



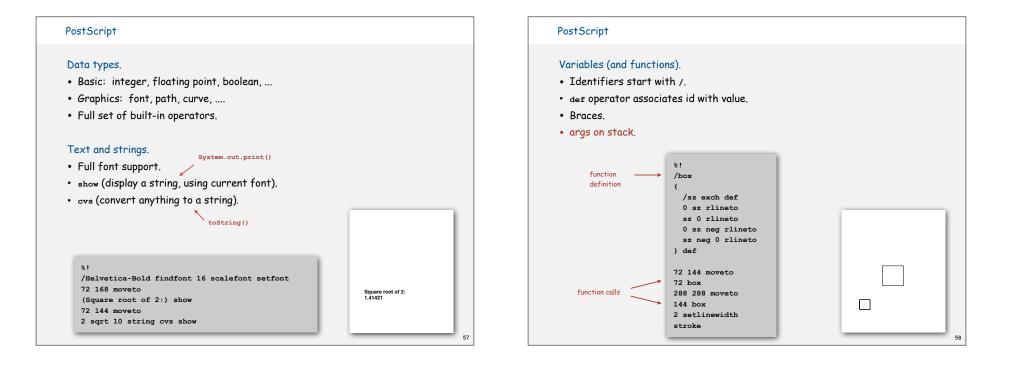








PostScript	
 Page description language. Explicit stack. Full computational model Graphics engine. Basics. %!: "I am a PostScript program." Literal: "push me on the stack." Function calls take arguments from stack. Turtle graphics built in. 	a PostScript program %! 72 72 moveto 0 72 rlineto 72 0 rlineto 0 -72 0 rlineto 2 setlinewidth stroke

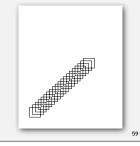


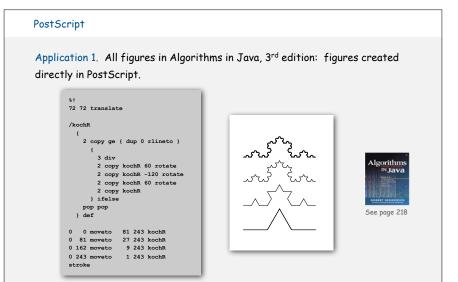


- Alternatives in braces.
- if operator.

... (hundreds of operators)







Application 2. All figures in Algorithms, 4th edition: enhanced version of stdDraw saves to PostScript for vector graphics.

Queue applications

Familiar applications.

- iTunes playlist.
- Data buffers (iPod, TiVo).
- Asynchronous data transfer (file IO, pipes, sockets).
- Dispensing requests on a shared resource (printer, processor).

Simulations of the real world.

- Traffic analysis.
- Waiting times of customers at call center.
- Determining number of cashiers to have at a supermarket.



M/M/1 queue.

61

- Customers arrive according to Poisson process at rate of λ per minute.
- Customers are serviced with rate of μ per minute.

Infinite queue	Server

