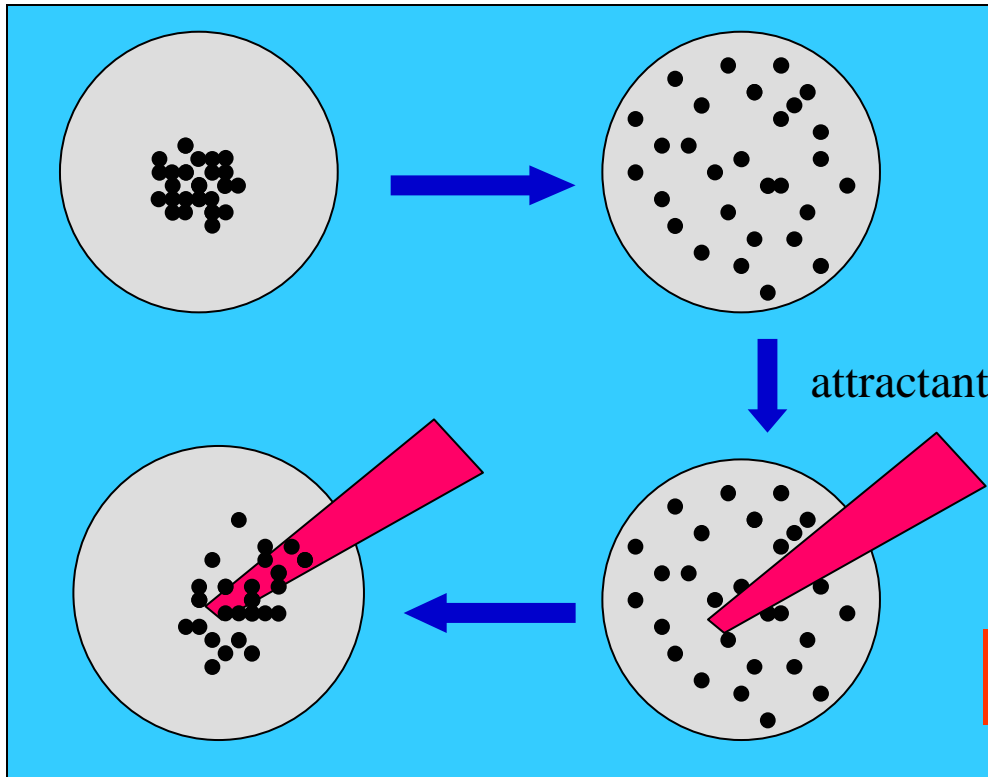


Bacterial Chemotaxis

Bacteria can be attracted/repelled by chemicals



Mechanism ?

“Chemoreceptors in bacteria.”

Adler, 1969 “Science” – **READ!**

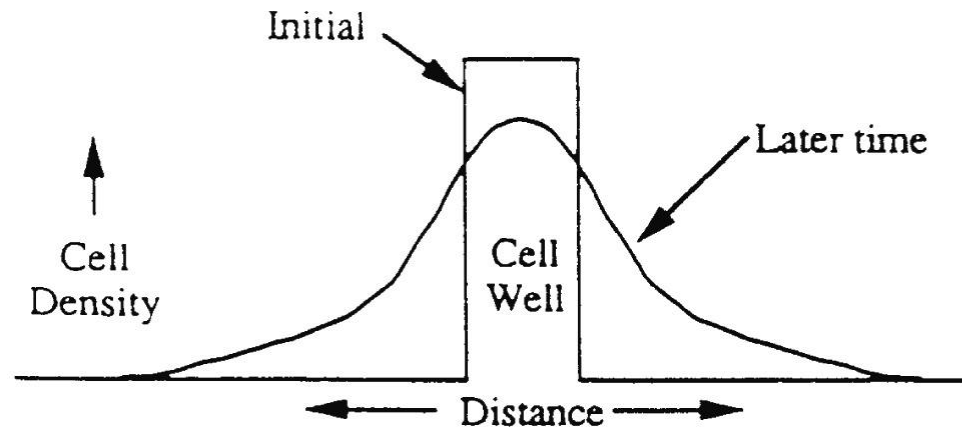
This is sensing, not metabolism

**Based on genetic approach!!!
No molecules yet**

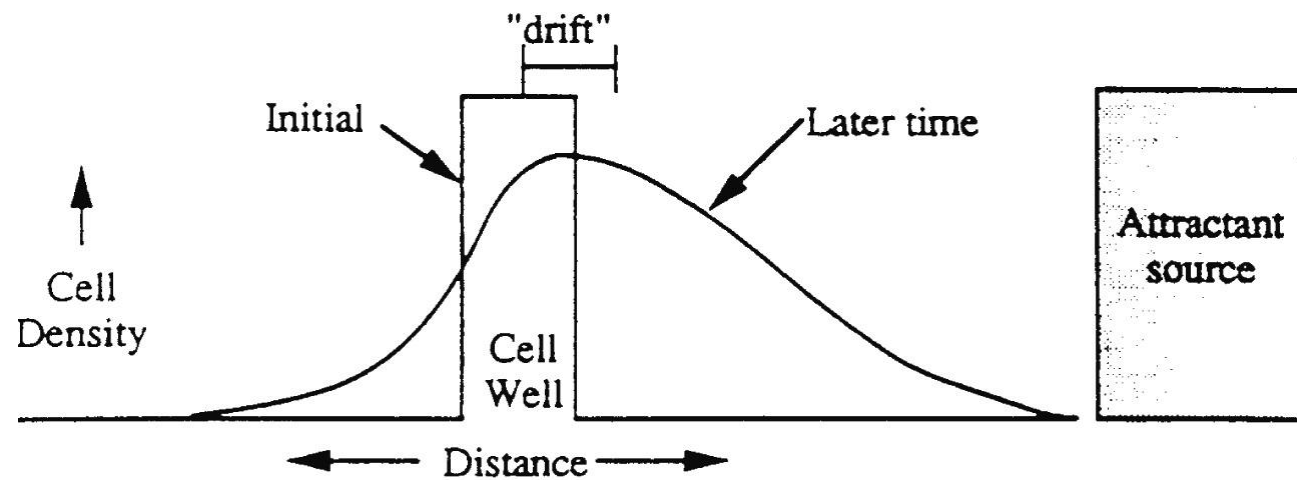
Macroscopic phenomenon:

flux of bacteria = $F(\text{gradient of chemicals})$

Random Motility and Chemotaxis

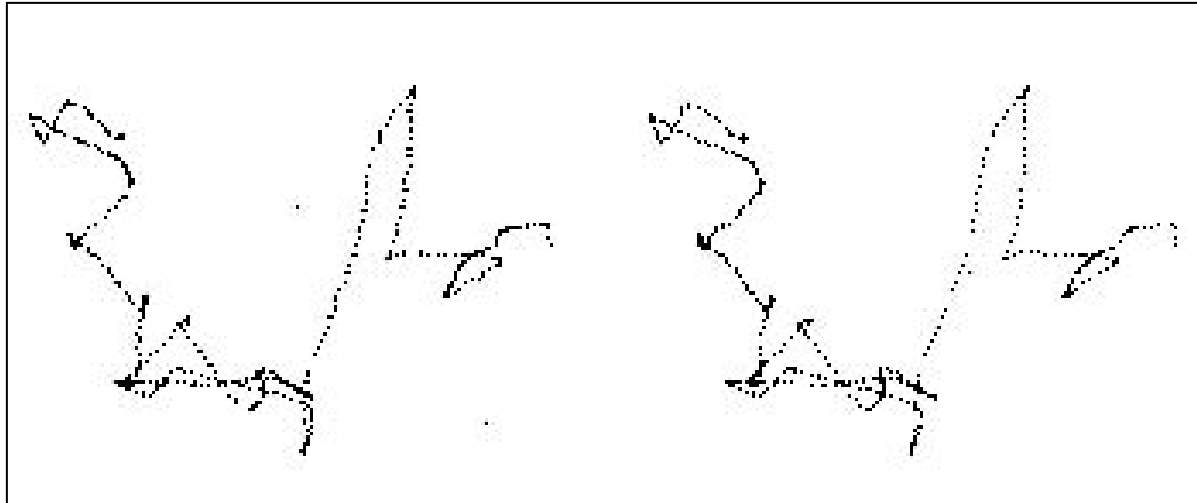


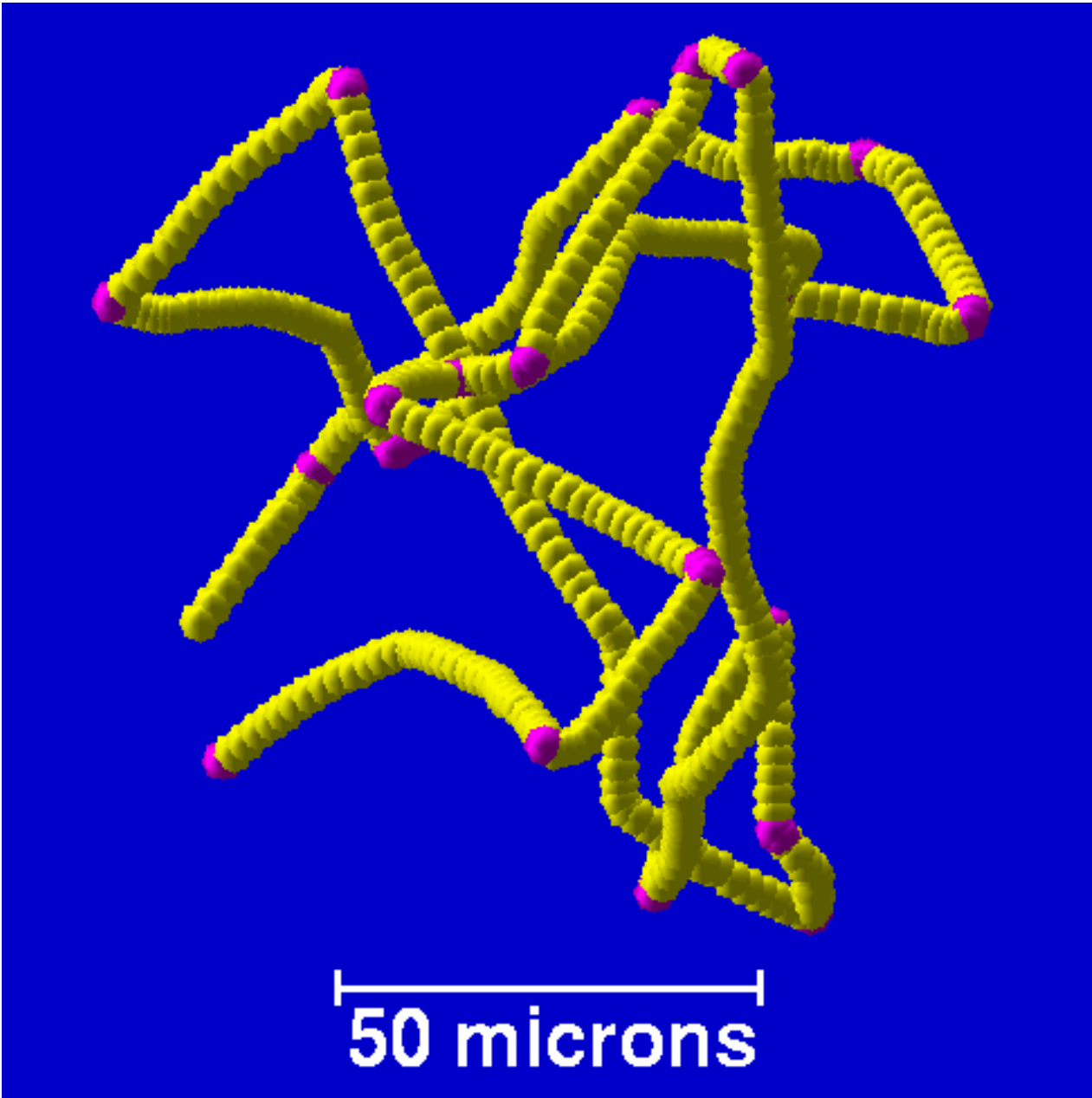
b. Migration in a chemical attractant gradient:
Random motility (μ), chemokinesis ($\frac{d\mu}{da}$) and chemotaxis (χ)



Trajectories

In the absence of chemical gradients, a swimming bacterium executes a three-dimensional random walk consisting of **runs of swimming** in a straight line **punctuated by tumbles**

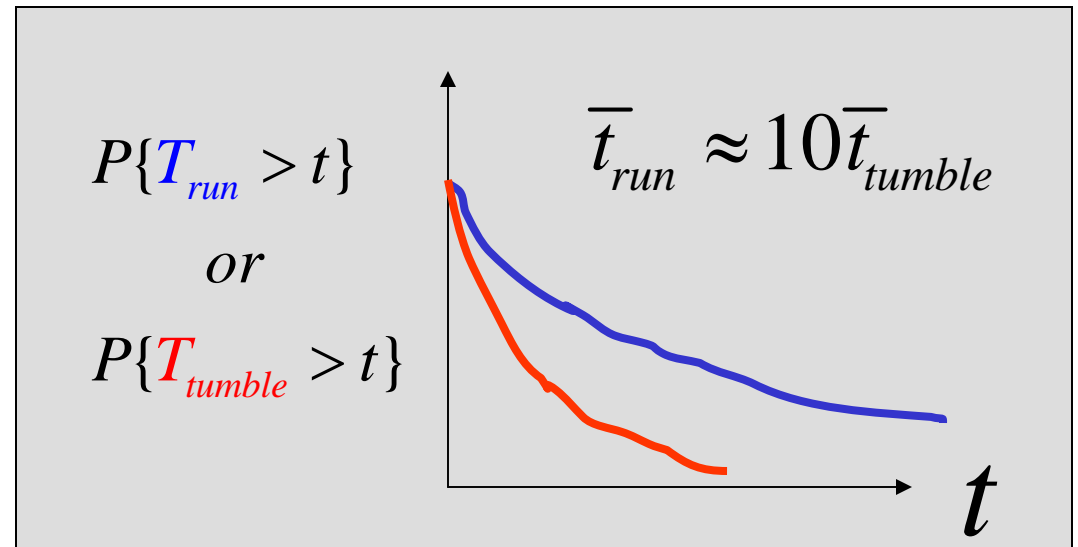
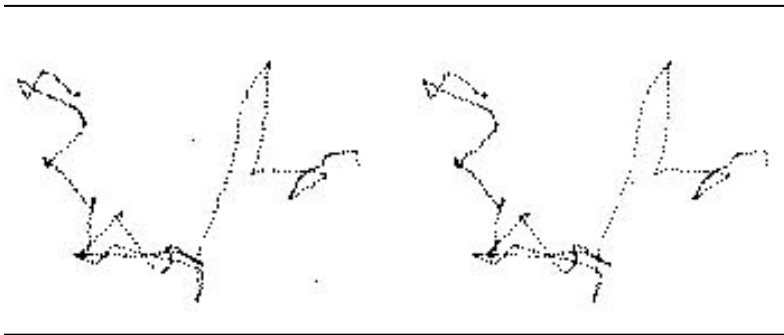




From Trajectories to Microscopic Parameters of Cell Migration

(Velocity Jump Process)

Berg and Brown, 1972

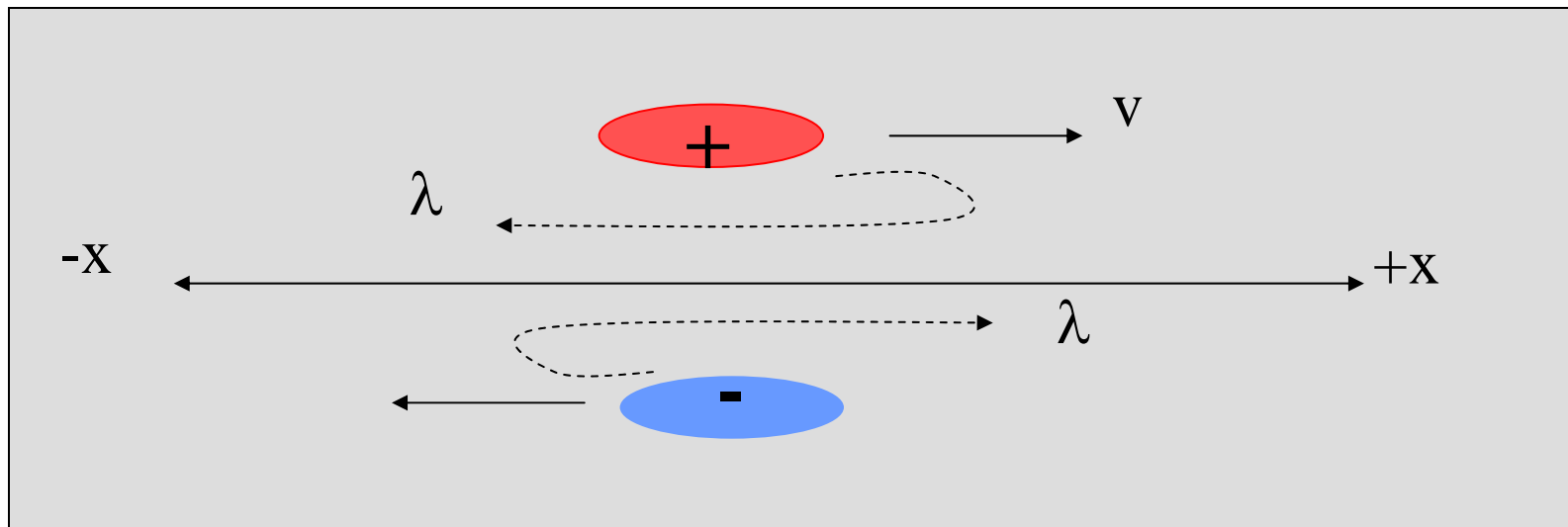


1. Runs punctuated by tumbles
2. Both runs and tumbles are exponentially distributed
3. Runs are longer than tumbles
4. Constant velocity

MODEL: instantaneous tumbles (neglect tumble time)

MODEL: instantaneous tumbles (neglect tumble time)

Velocity Jump Process



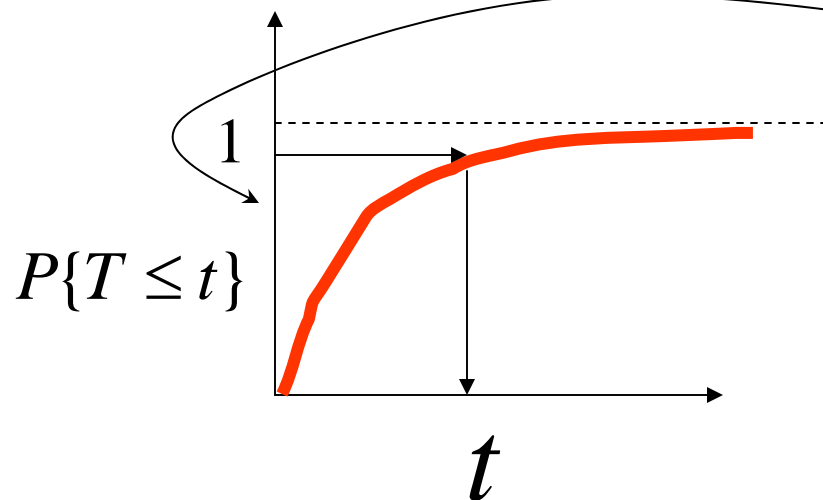
1. Continuous space & Continuous time
2. At every point: right- and left-moving cells
3. Follow a single cell & a population of cells

Velocity Jump Process

$$P\{T \leq t\} = 1 - \exp(-\lambda t)$$

$$v = \pm V$$

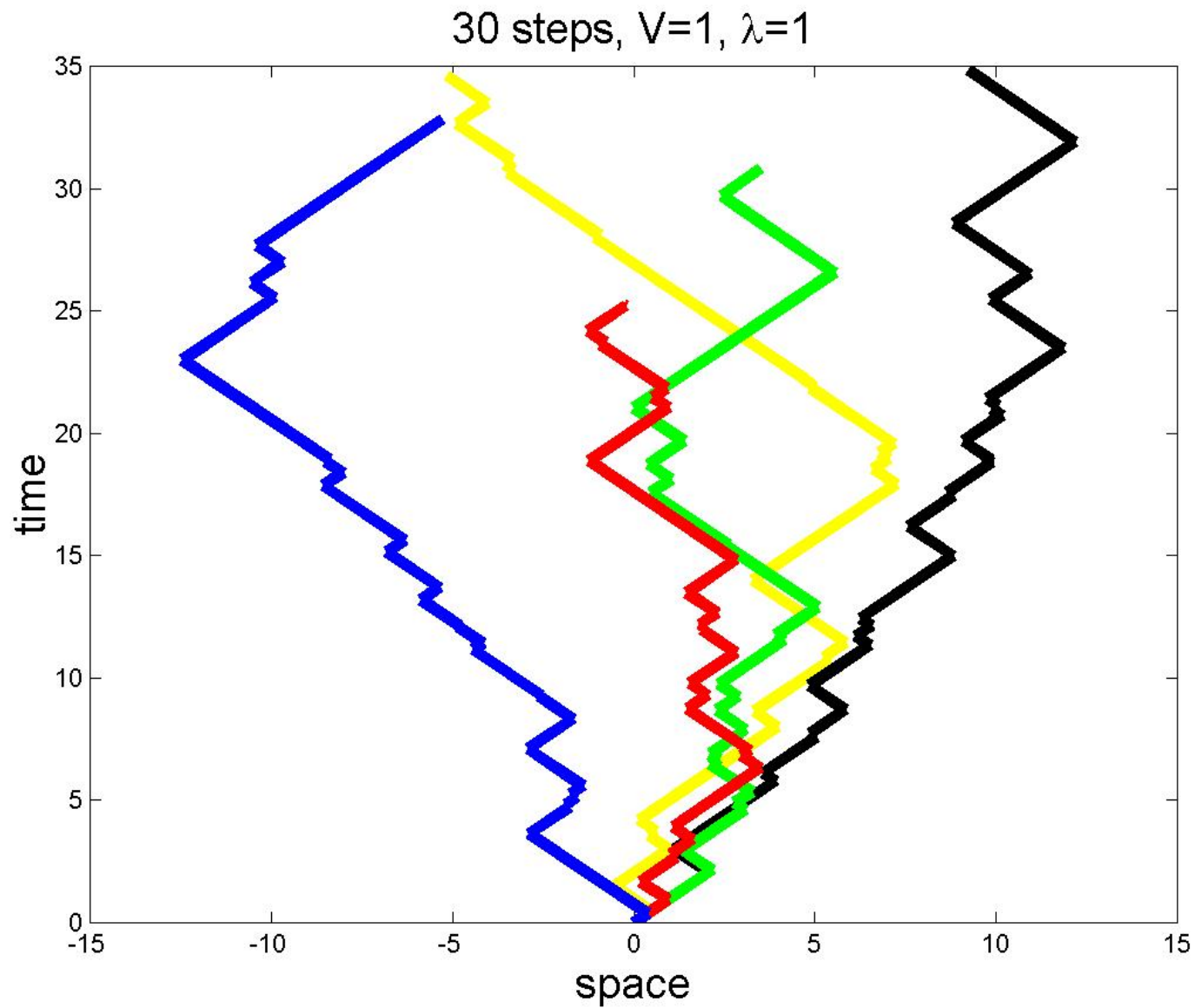
Inversion method



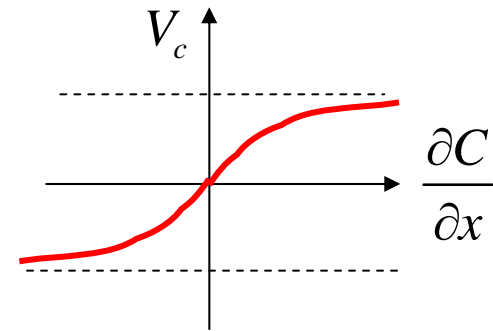
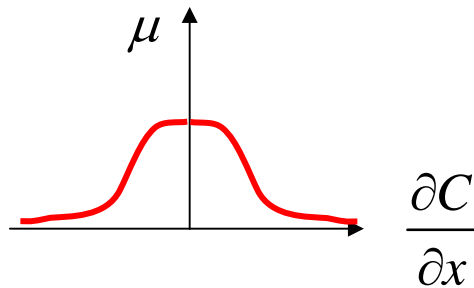
Simulation

```
λ =1; t=[0];  
x=[0]; V=1; STEPS=30  
for j=1:5  
    for i=1:STEPS;  
        T=-log(1-rand(1))/λ;  
        N=length(t);  
        t=[t;t(N)+T];  
        x=[x;x(N)+V*T];  
        V=-V;  
    end; plot(x,t); hold on;  
end;
```

Velocity Jump Process



Flux in a 1D Gradient (4): Analysis



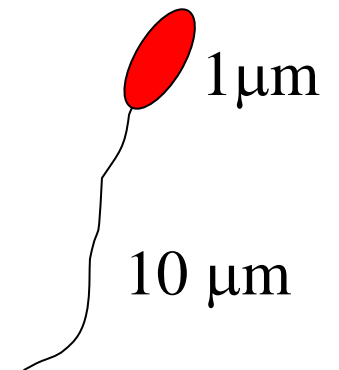
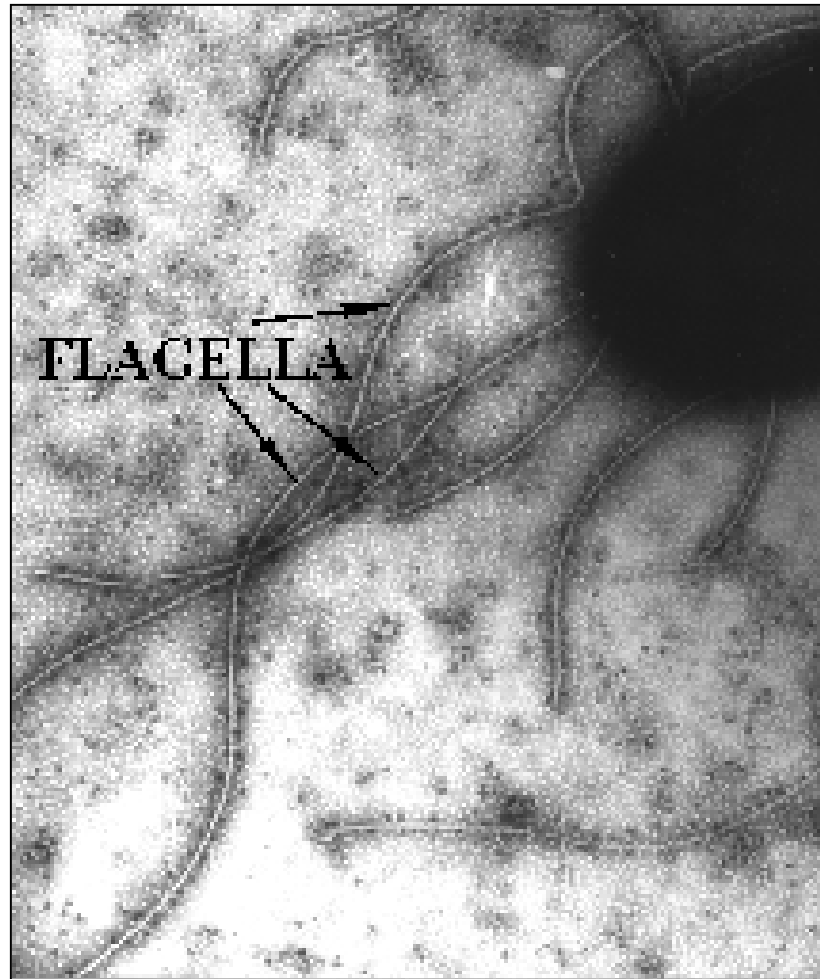
1. Random motility coefficient is a decreasing function of spatial gradient: at large gradients all cells swim in one direction
2. Chemotactic velocity has a limiting value: the population can not move faster than the maximal cell speed

E. Coli swims by rotating its flagella

Flagellar rotation
as a means of
bacterial motility

1974

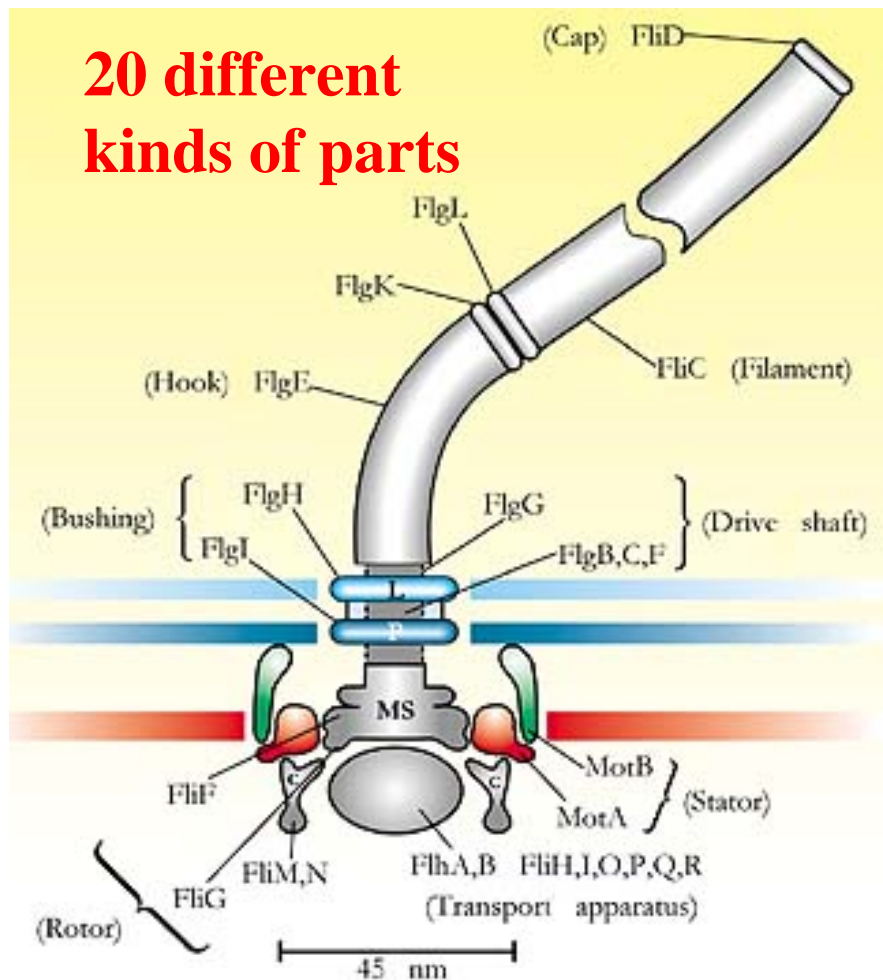
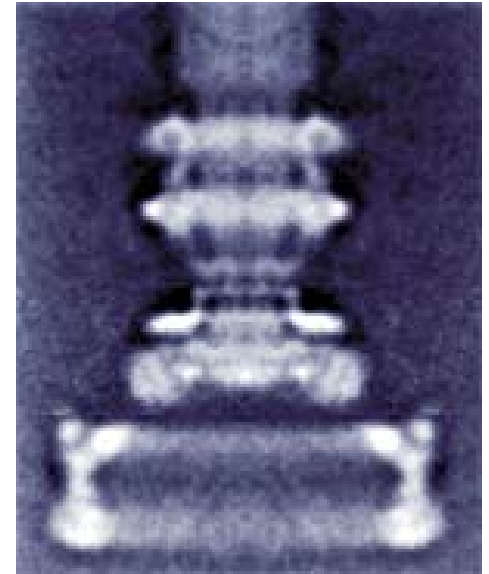
Speed: 20-30 $\mu\text{m/s}$



Propulsive unit: a bundle of bacteria

The motor 1974: These observations suggest that the hook is driven in a rotary fashion, probably by the mechanism anchored to cell body at the base of the flagellum.

... the cell has the capacity to vary the direction of the rotation and the speed as well as the frequency of stopping.
(Silverman and Simon, 1994, Nature, 249, 73)



The flagellum is an organelle that has three parts (as figure 2 shows).

There is a basal body consisting of a reversible rotary motor embedded in the cell wall, beginning within the cytoplasm and ending at the outer membrane.

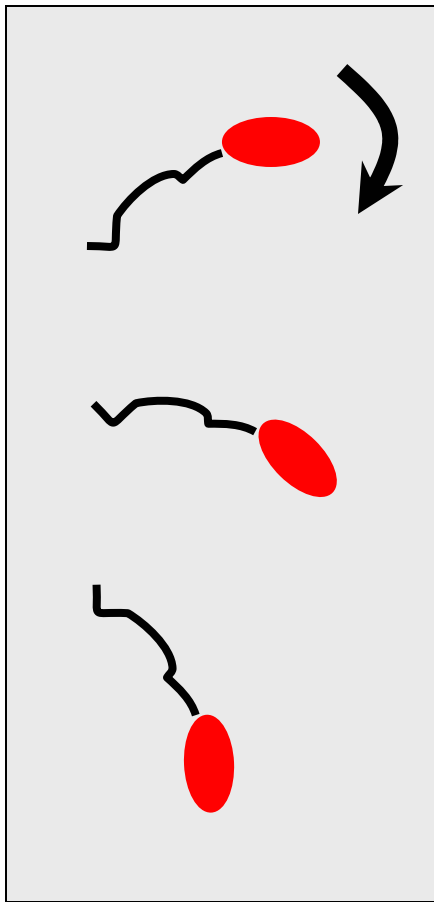
There is a short proximal hook, which is a flexible coupling or universal joint.

And there is a long helical filament, which is a propeller.

Proteins forming the motor have been identified

The motor can rotate in 2 directions – CW and CCW – viewed from the end of the flagella

Experiments with tethered cells: bacterium is attached to a slide. The whole cell rotates. (Silverman and Simon, Adler et al, 1974, “Nature”)



Change in direction of flagellar rotation is the basis of the chemotactic response in E. Coli, 1974, Adler et al

- 1972: Chemotaxis is produced by variation in the tumbling frequency
- 1974: Tumbling frequency is produced by the CW rotation of the flagella
- **Rotation bias is affected by chemicals**
- **Tumbling frequency is affected by chemicals**

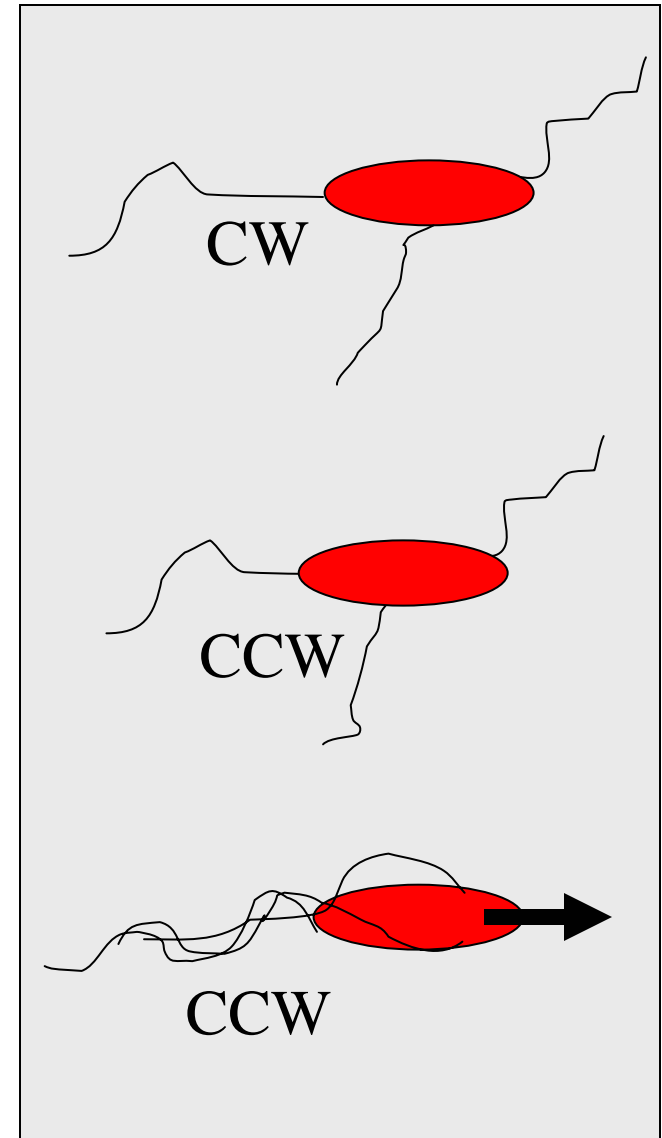
CW rotation – tumble
CCW – swimming

Same pattern of attractant responses for
CW/CW and tumble/run

But this is for one flagella.
The propulsive unit is a bundle
How does it form?

Hydrodynamic forces can
bundle individual flagella

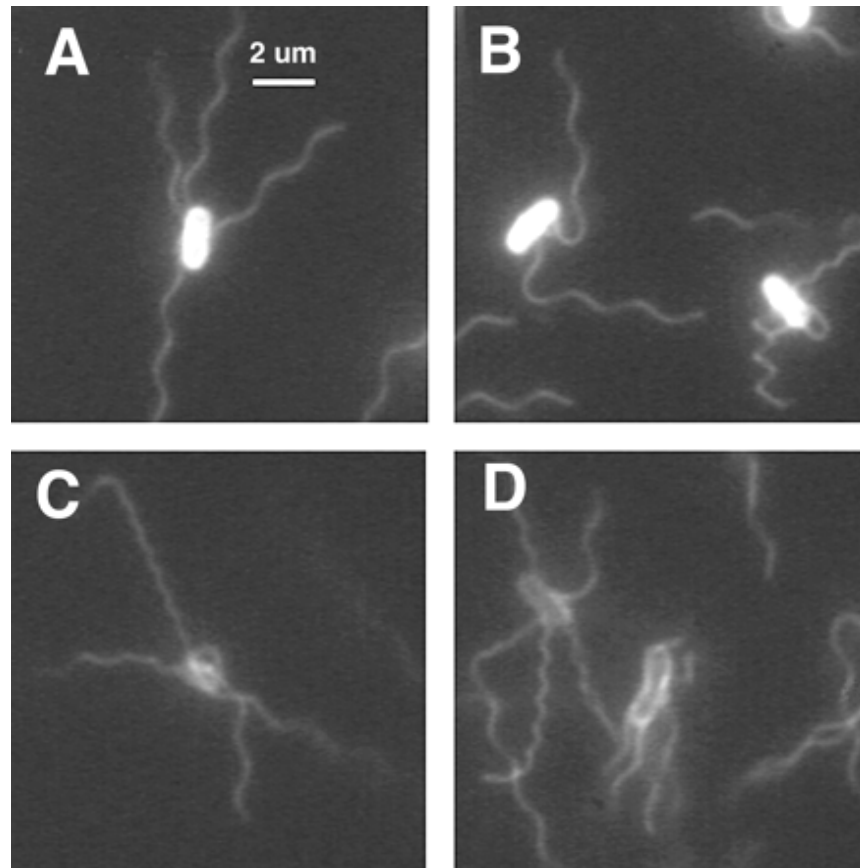
(large reduction in power dissipation for synchronous rotation within a bundle)
Many other examples of hydrodynamics-based synchronization



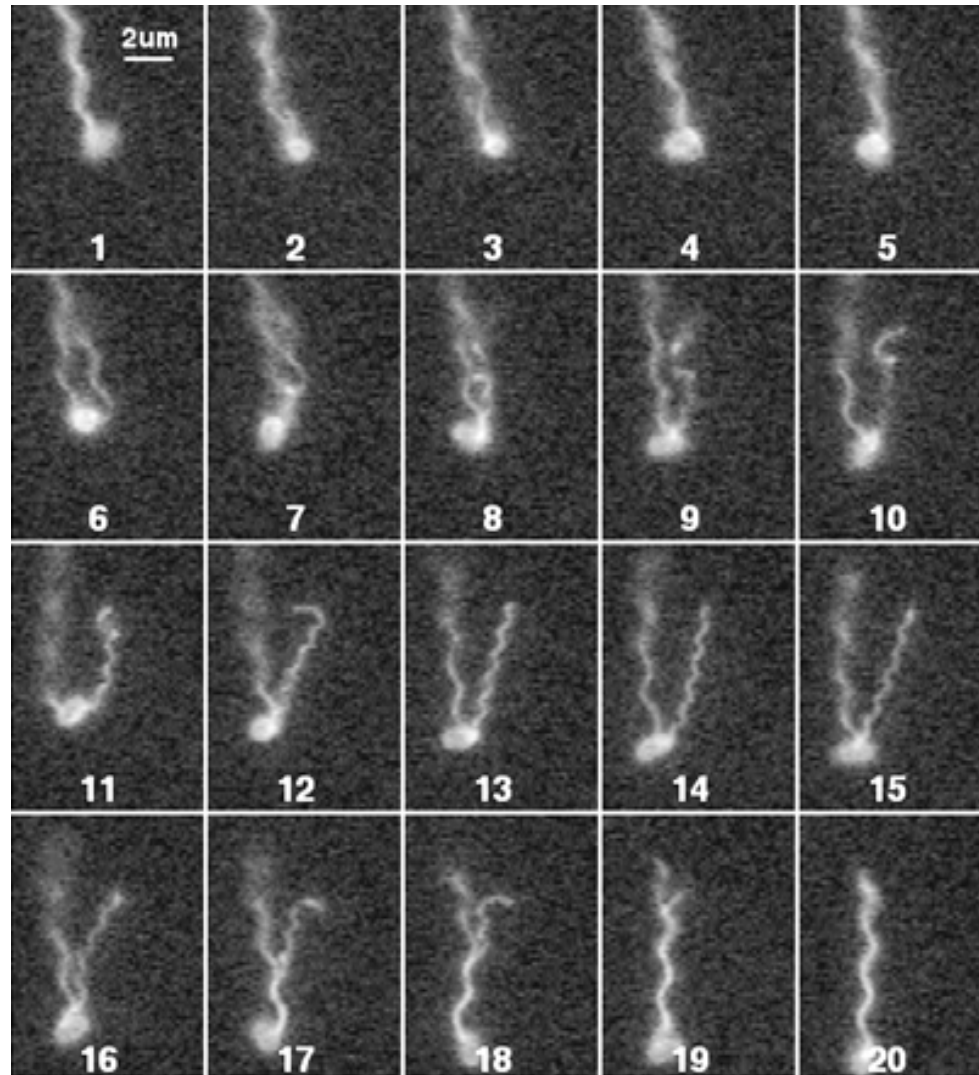
Is it just a theory ?

Real-time imaging of fluorescent flagellar filaments

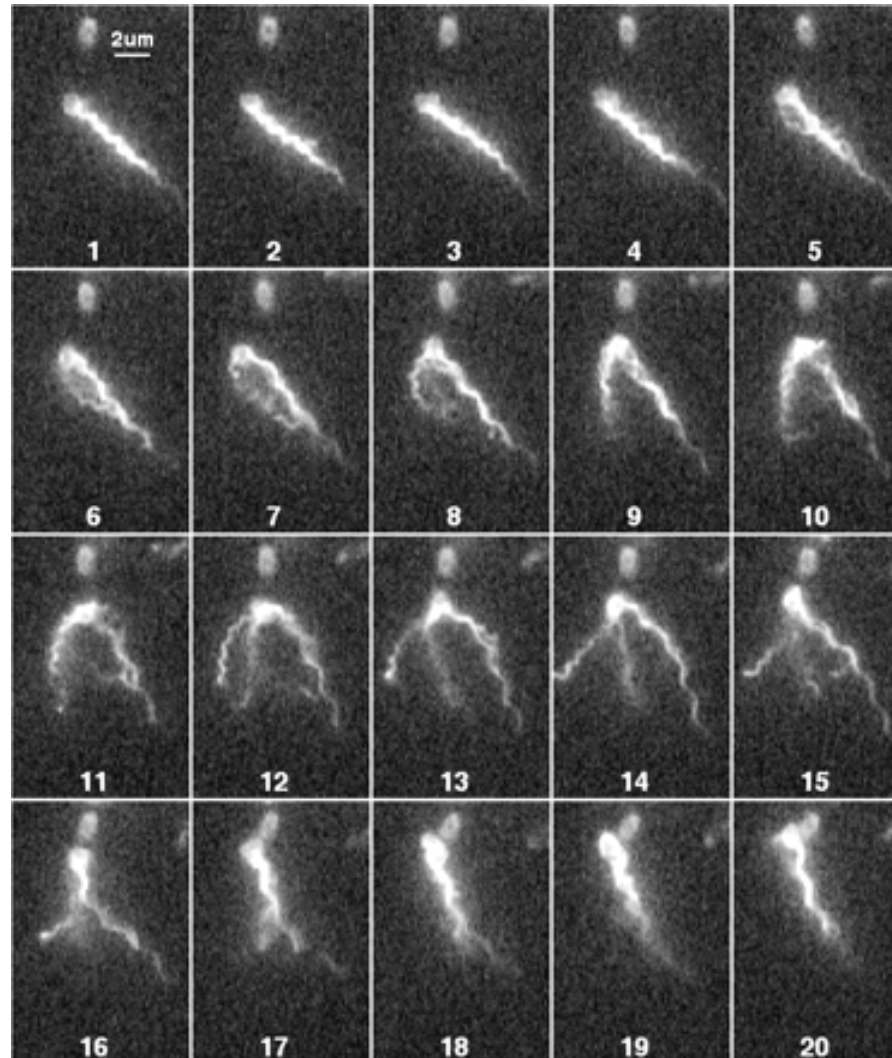
Turner, Ryu, and Berg, J. Bacteriology, 182, 10, 2783, 2000



2 flagella



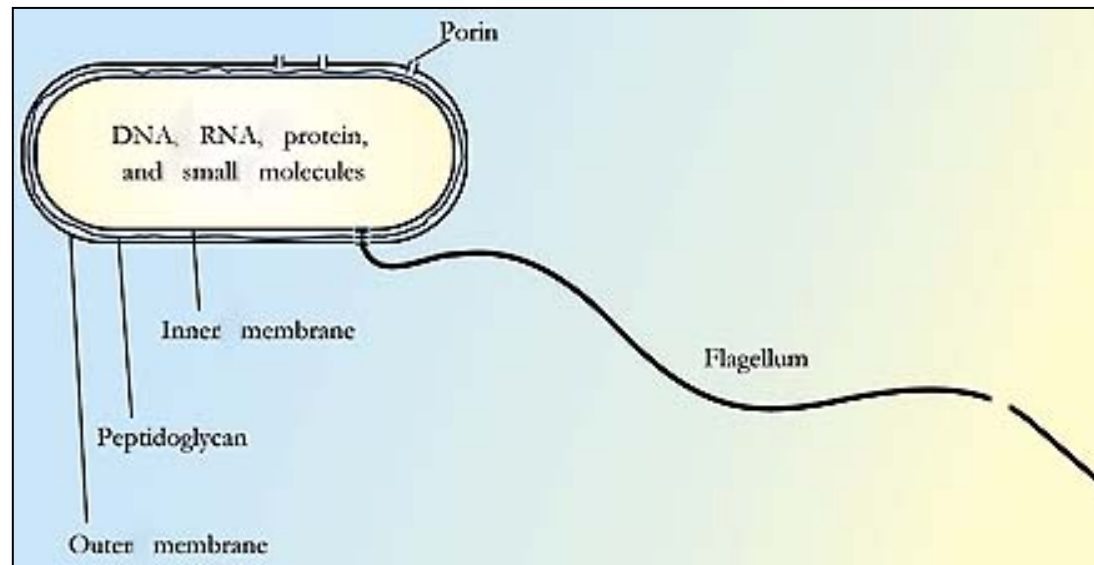
Several
flagella



- Not all flagella have to rotate CCW for the cell to “run”
- Only several flagella can rotate CW to cause tumbling
- Different motors behave “independently”

Attractants/repellants modify rotational bias

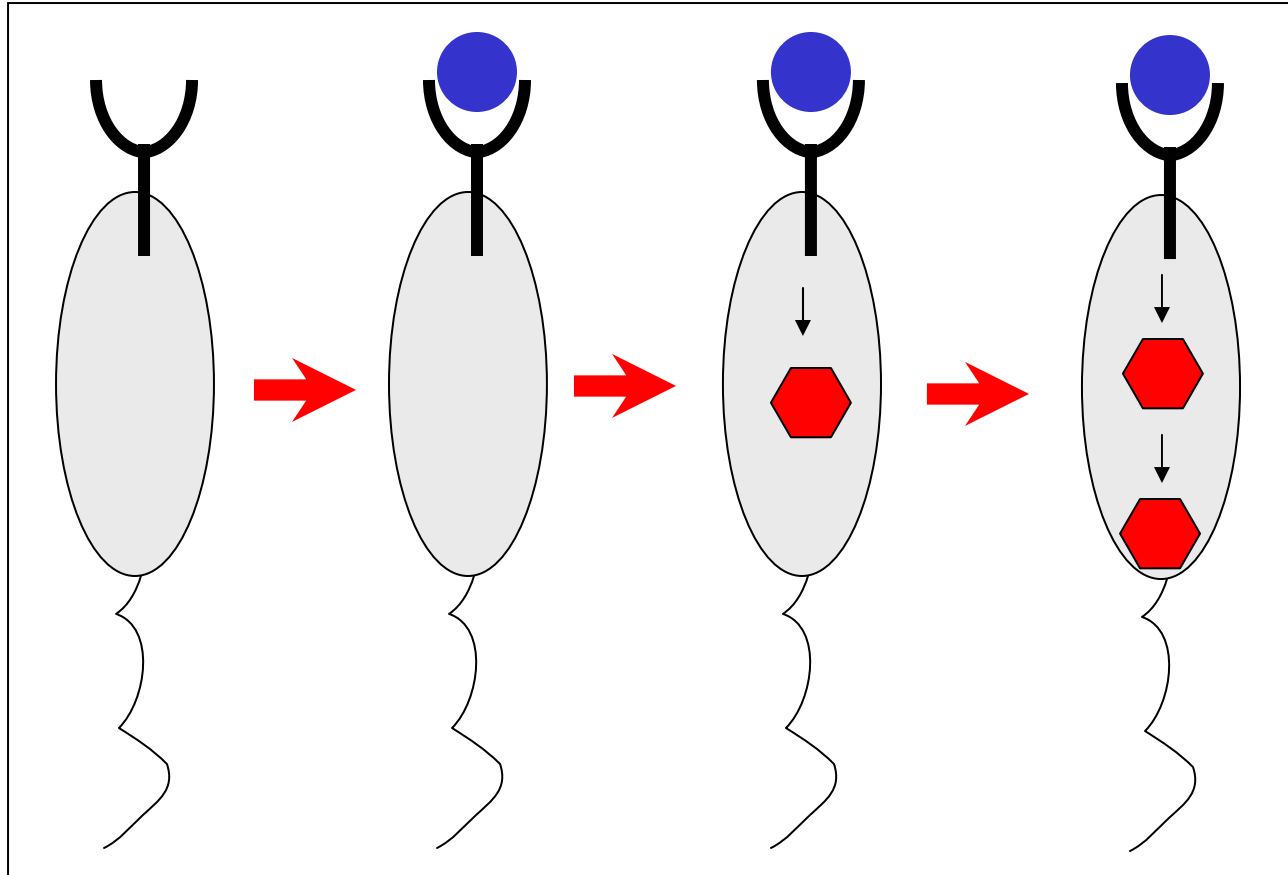
How is it accomplished?



Look inside the cell

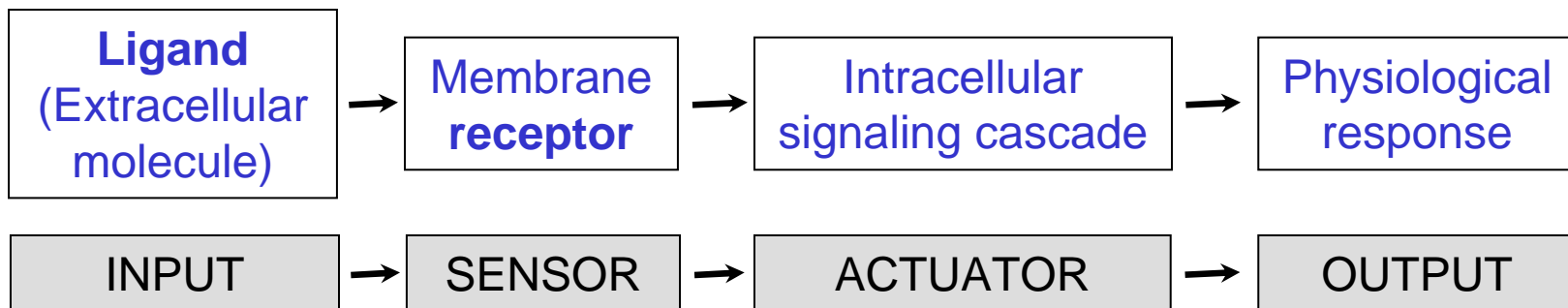
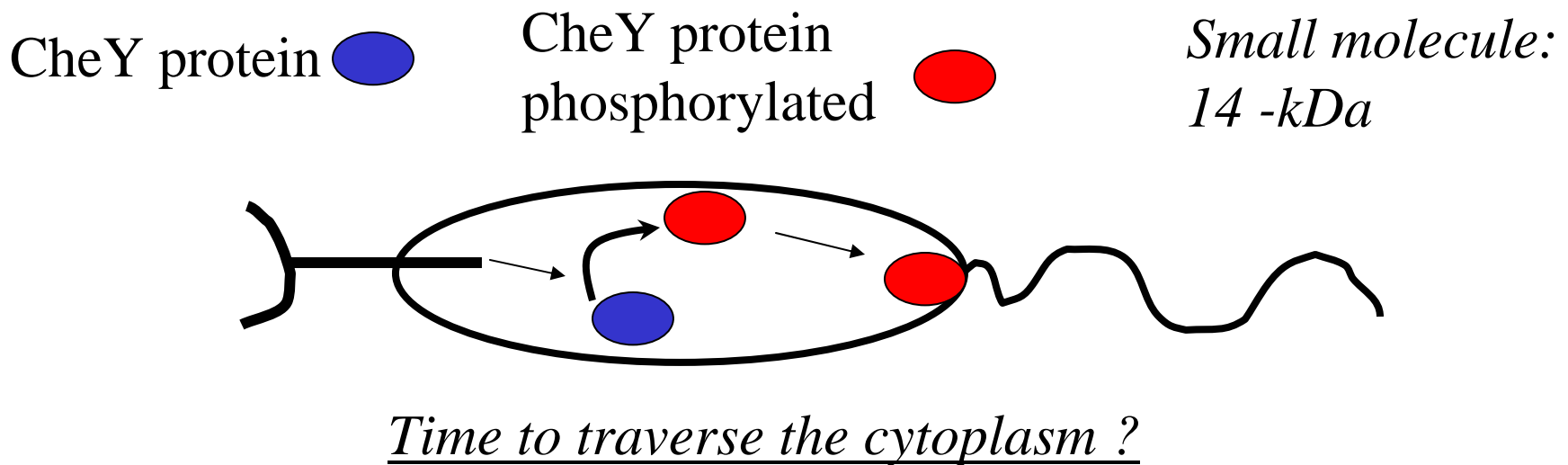
What happens when ligand binds?

- Receptor directly linked to the motor – NO
- Electric signal generated – NO
- **Diffusing messenger (~1985)**



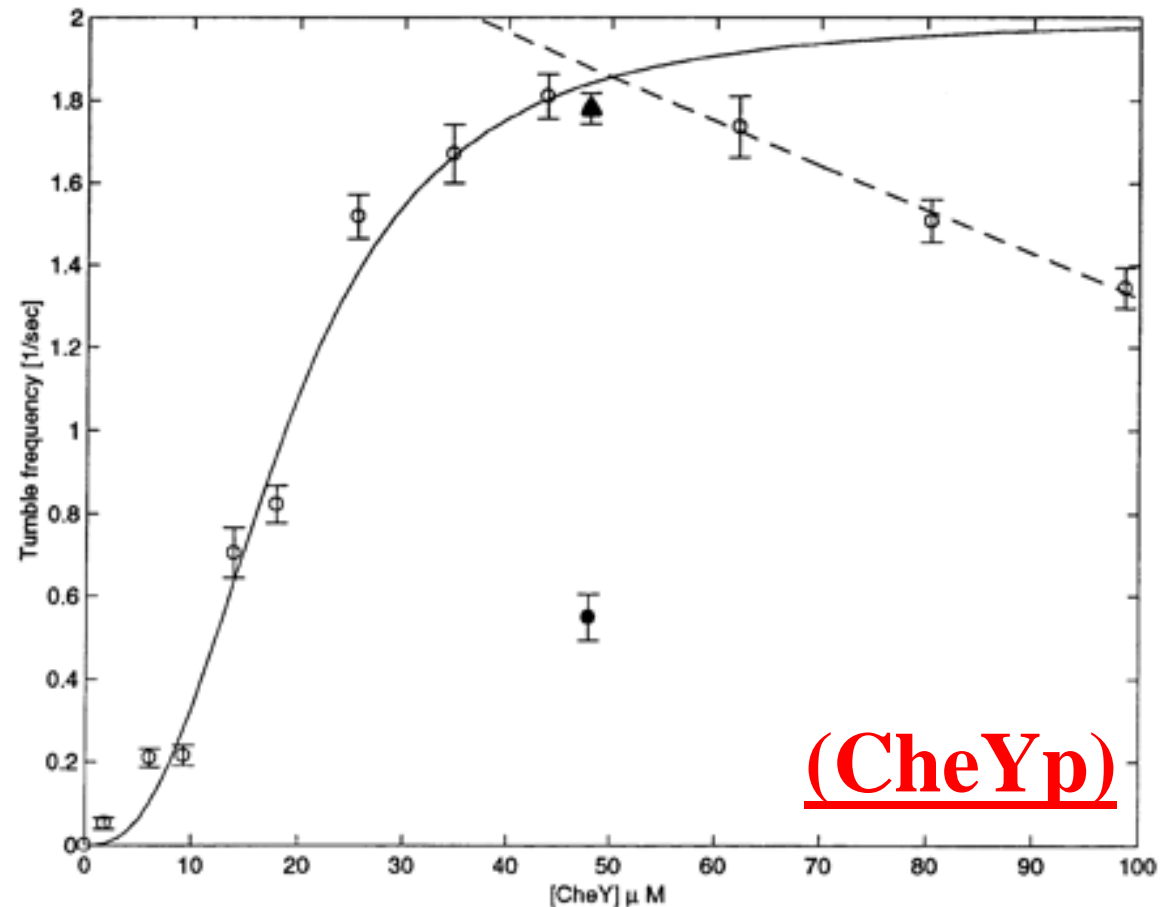
**Signal
transduction**

Concentration of an active form of a cytoplasmic protein regulates the rotational bias of the motor



Input/output behavior quantified: Motor bias = $F(\bullet)$

Tumbling
frequency

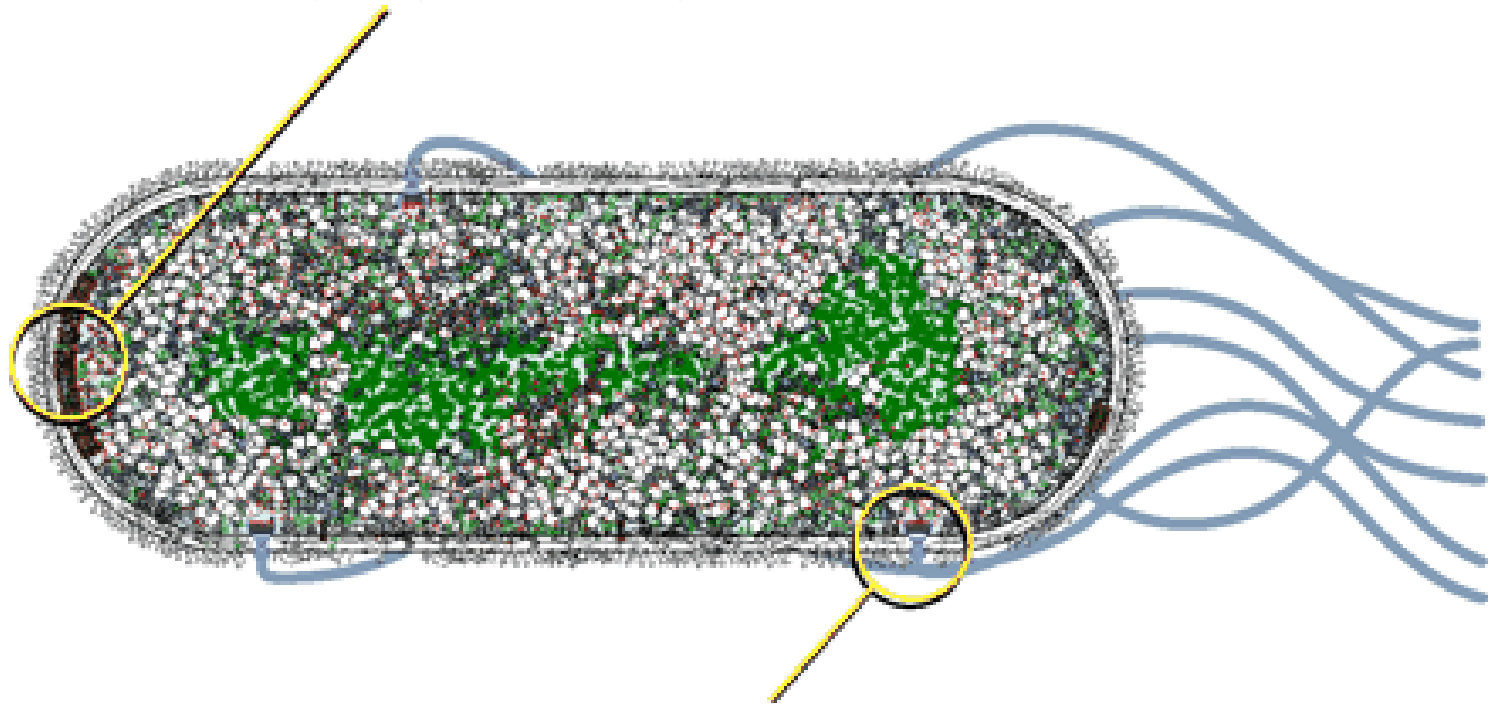


Alon U, Camarena L, Surette MG, Aguera y Arcas B, Liu Y, Leibler S, Stock JB.
Response regulator output in bacterial chemotaxis.
EMBO J. 1998 Aug 3;17(15):4238-48.

Scharf BE, Fahrner KA, Turner L, Berg HC.
Control of direction of flagellar rotation in bacterial chemotaxis
Proc Natl Acad Sci U S A. 1998 Jan 6;95(1):201-6.

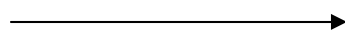
Gradient of chemical \rightarrow Flux of bacteria
CheY concentration \rightarrow statistics of motor reversals

Swimming bacterium encounters aspartate.
Occupancy of the receptor Tar increases.

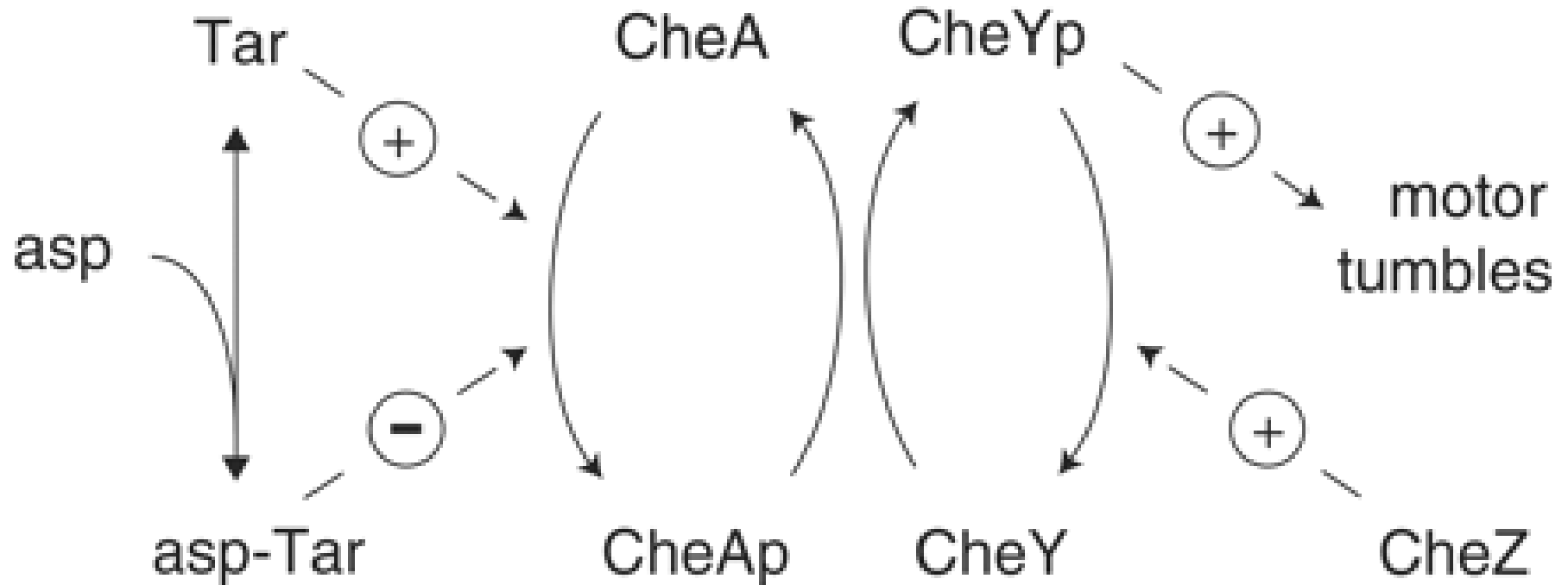


Concentration of cytosolic CheYp falls.
Probability of motor CCW rotation (bias) increases.

receptor



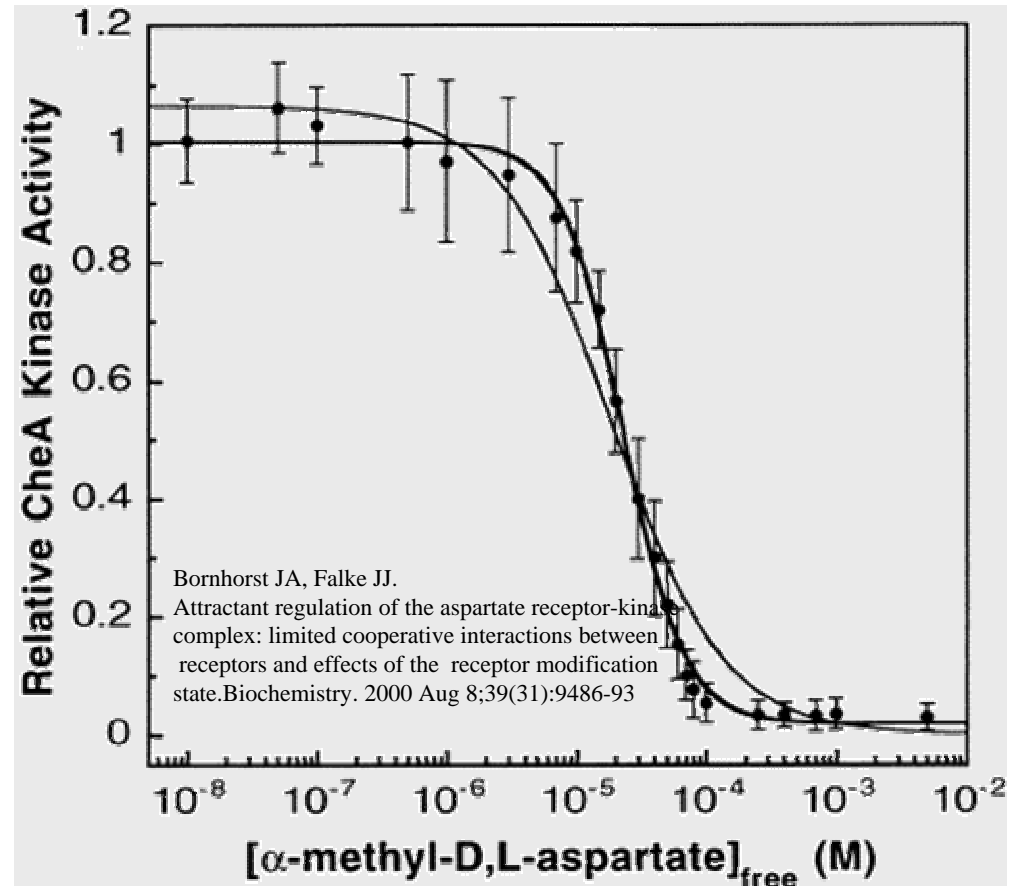
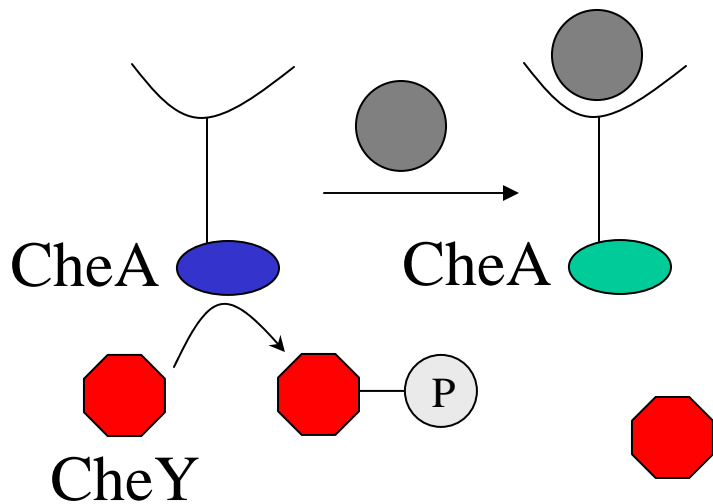
messenger



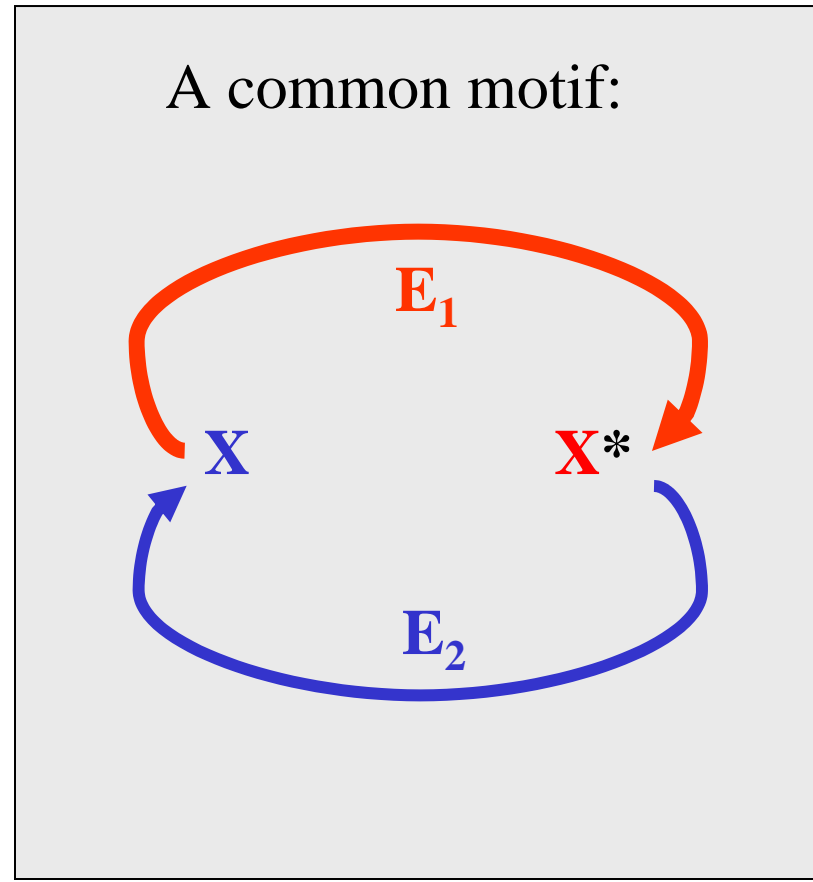
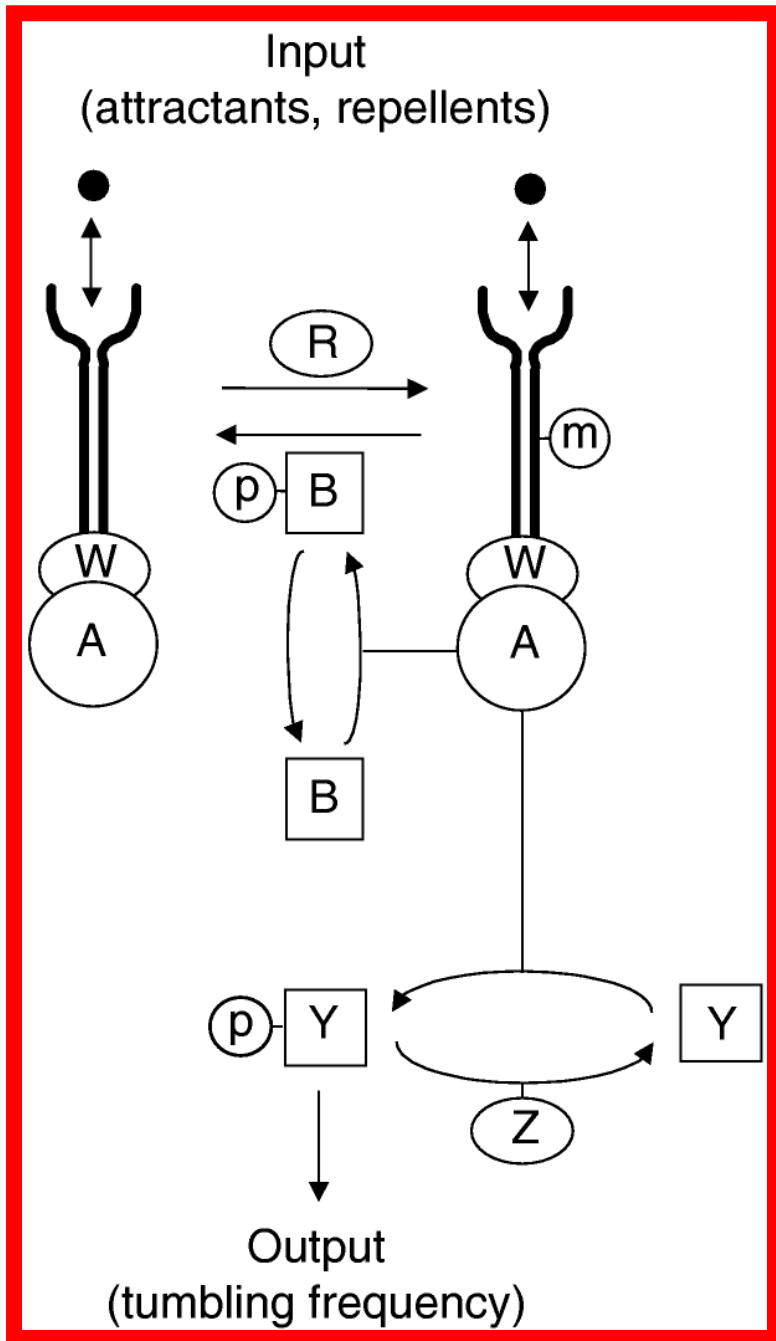
regulator

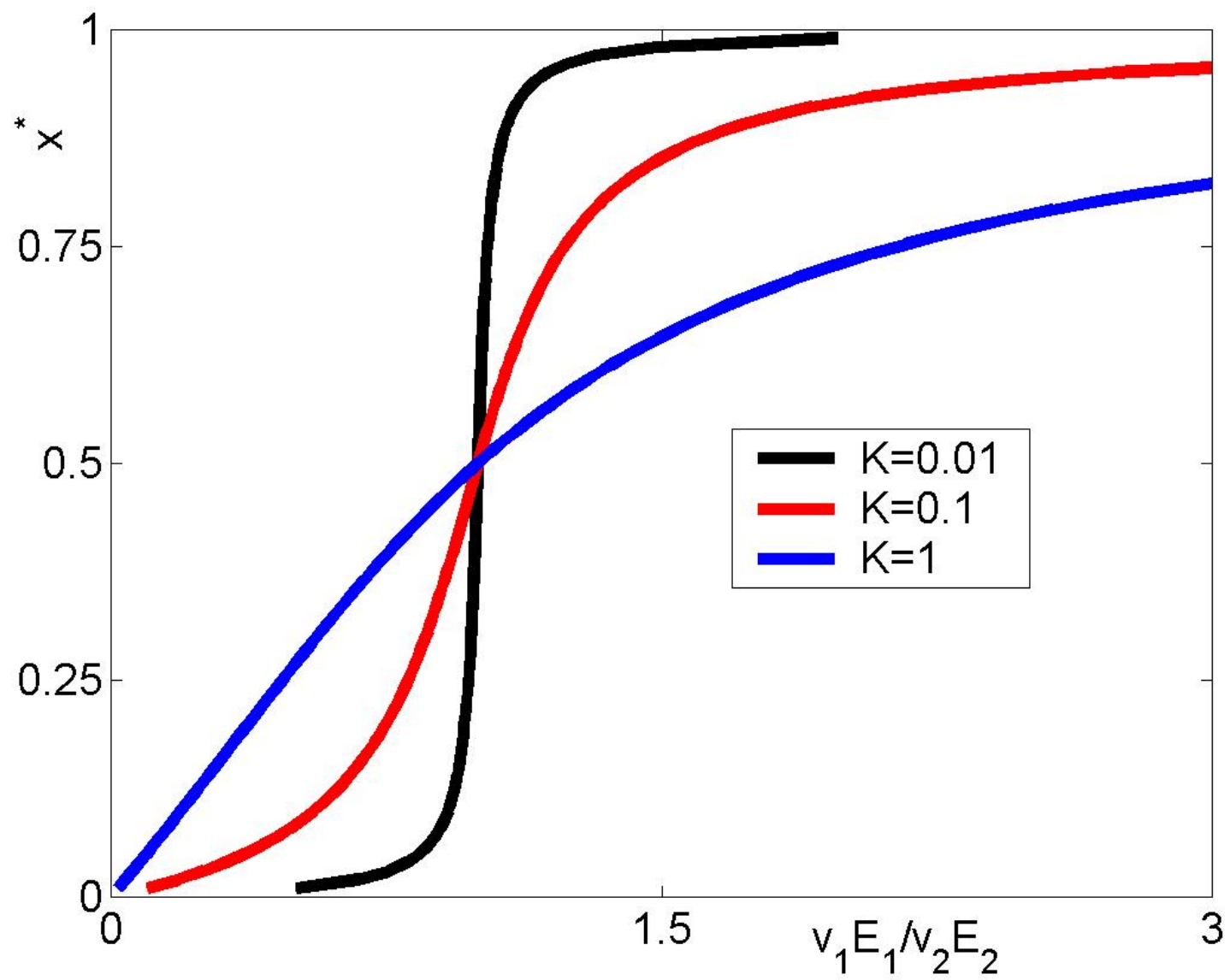
CheY is phosphorylated by a receptor-linked kinase (**regulator**)

Ligand binding negatively regulates kinase activity



This is only an input to the network that regulates CheY-P





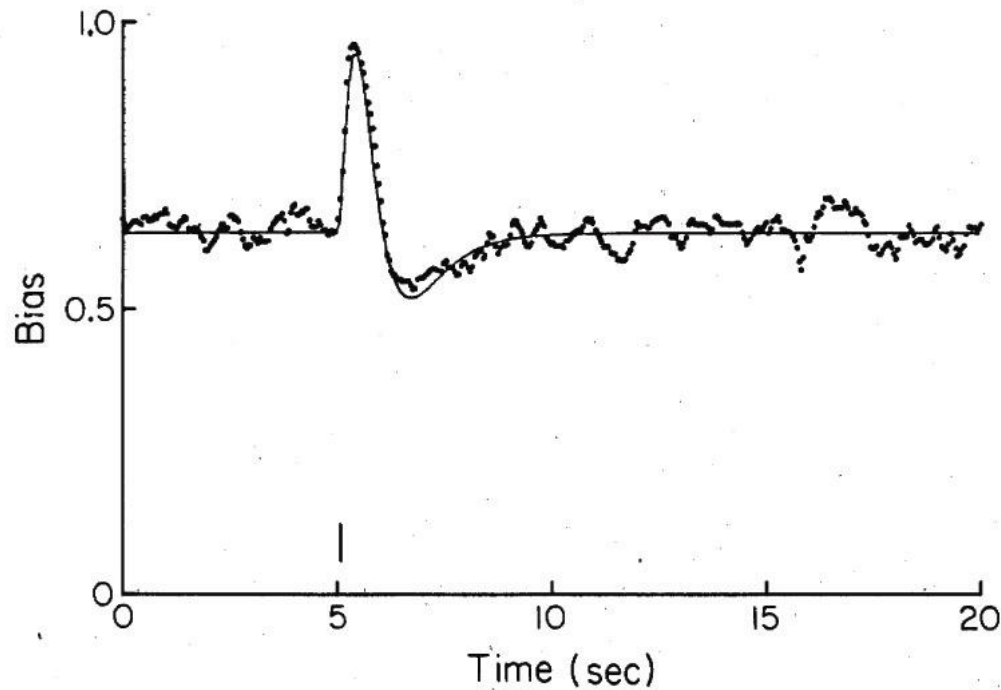


FIG. 1. Impulse response to attractant in wild-type cells. The dotted curve is the probability, determined from repetitive stimulation, that tethered cells of strain AW405 spin CCW when exposed to pulses of L-aspartate or α -methyl-DL-aspartate beginning at 5.06 sec (vertical bar). The smooth curve is a fit to a sum of exponentials (see text). For methods, see refs. 14 and 16. Pipettes containing aspartate (1 mM) were pulsed for 0.02 sec at -25 to -100 nA, and pipettes containing methylaspartate (1–3 mM, with 1.6 mM in the bath) were pulsed for 0.12 sec at -100 nA, both at 32°C . Some pipettes containing 1–7 mM methylaspartate were pulsed for 0.03–0.12 sec at -50 to -100 nA at 22°C . The curve was constructed from 378 records comprising 7566 reversals of 17 cells. Points were determined every 0.05 sec.

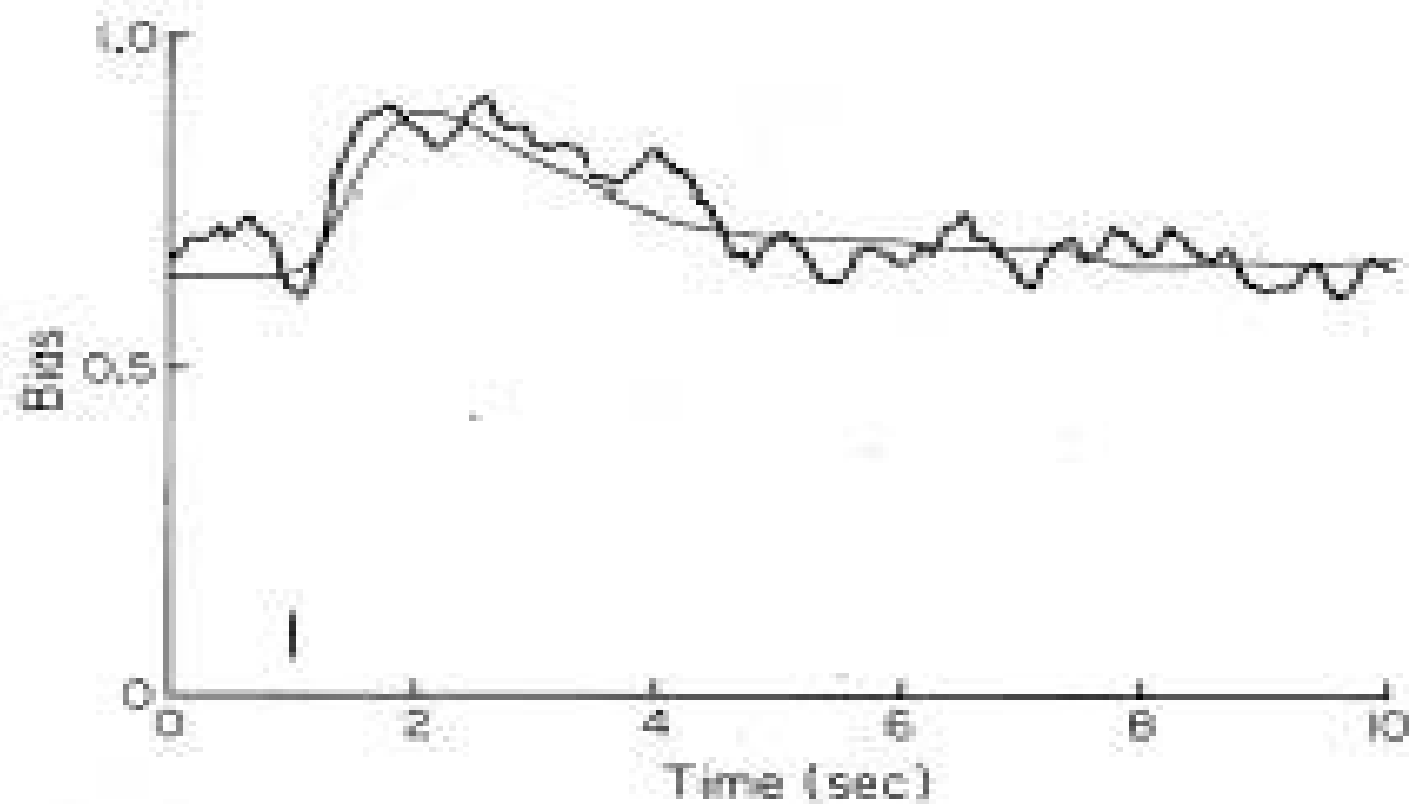
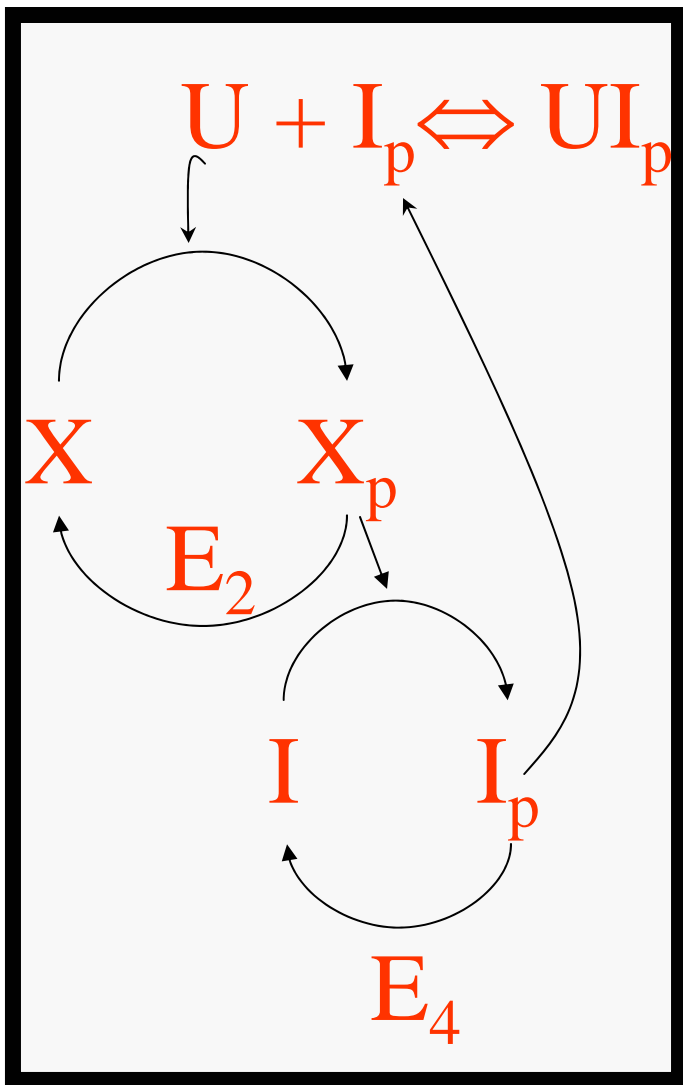


FIG. 2. Step response to attractant in wild-type cells. The thick line is the probability that cells of strain AW405 spin CCW when



$$\frac{dX_p}{dt} = \frac{u}{1 + G * I_p} \frac{X}{K_1 + X} - \frac{V_2 X_p}{K_2 + X_p}$$

$$\frac{dI_p}{dt} = \frac{V_3 X_p I}{K_3 + I} - \frac{V_4 I_p}{K_4 + I_p}$$

$$1 = I + I_p, \quad K_3 \text{ \& } K_4 \ll 1$$

$$1 = X + X_p$$

At steady state:

$$X_p \approx \frac{V_4}{V_3} \text{ independently of } u, K_1, K_2$$

make $\frac{V_4}{V_3}$ small

```
function y = feedback(t,x,flag,p)

u=p(1); g=p(2);
K=0.1; I=x(2); X=x(1);

y(1,1) = 0.1*((u/(1+p(2)*I))*(1-X)/(K+1-X) - X/(K+X));
y(2,1) = (X - 0.01*I/(0.01+I));

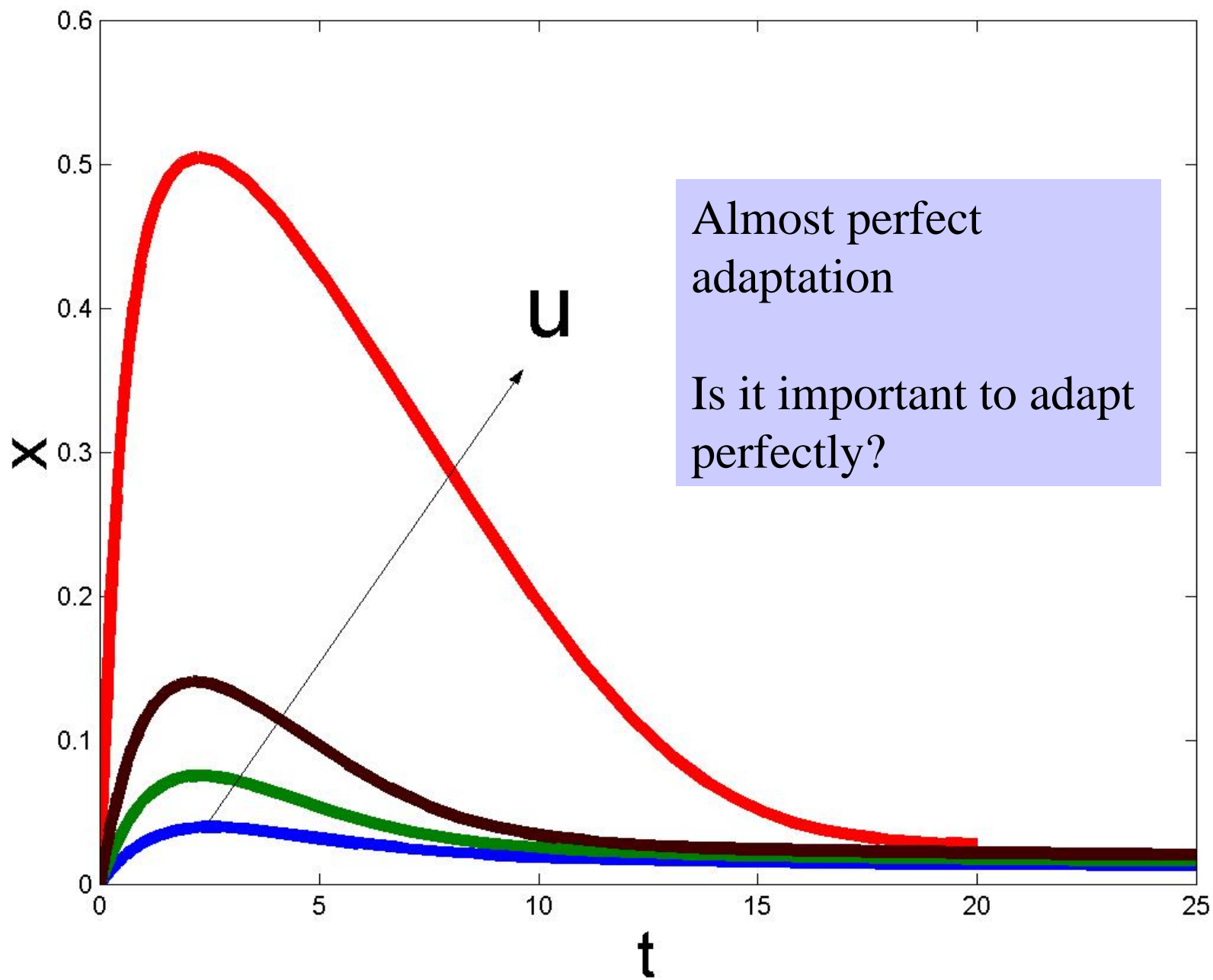
return;

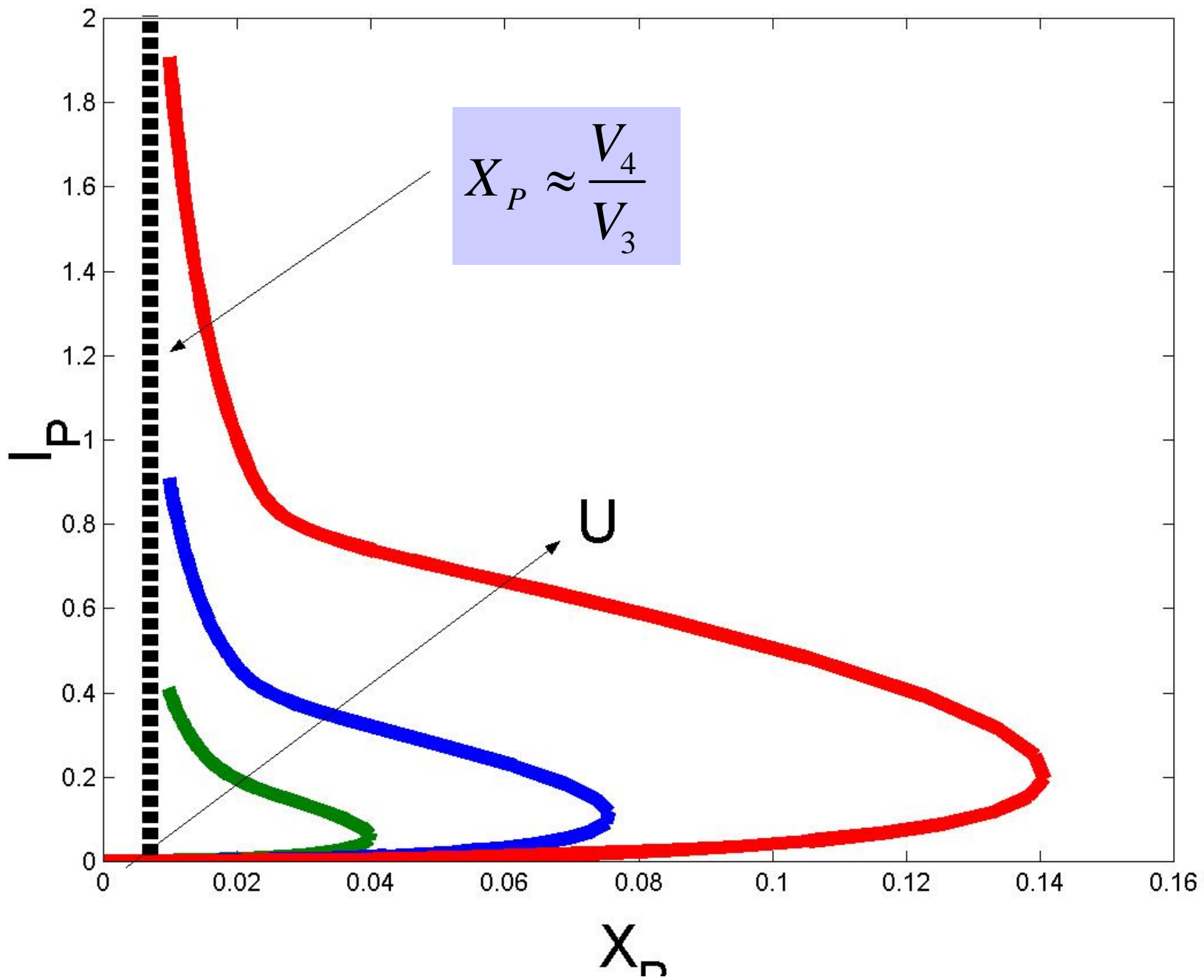
U=[0,0.5,1,2];

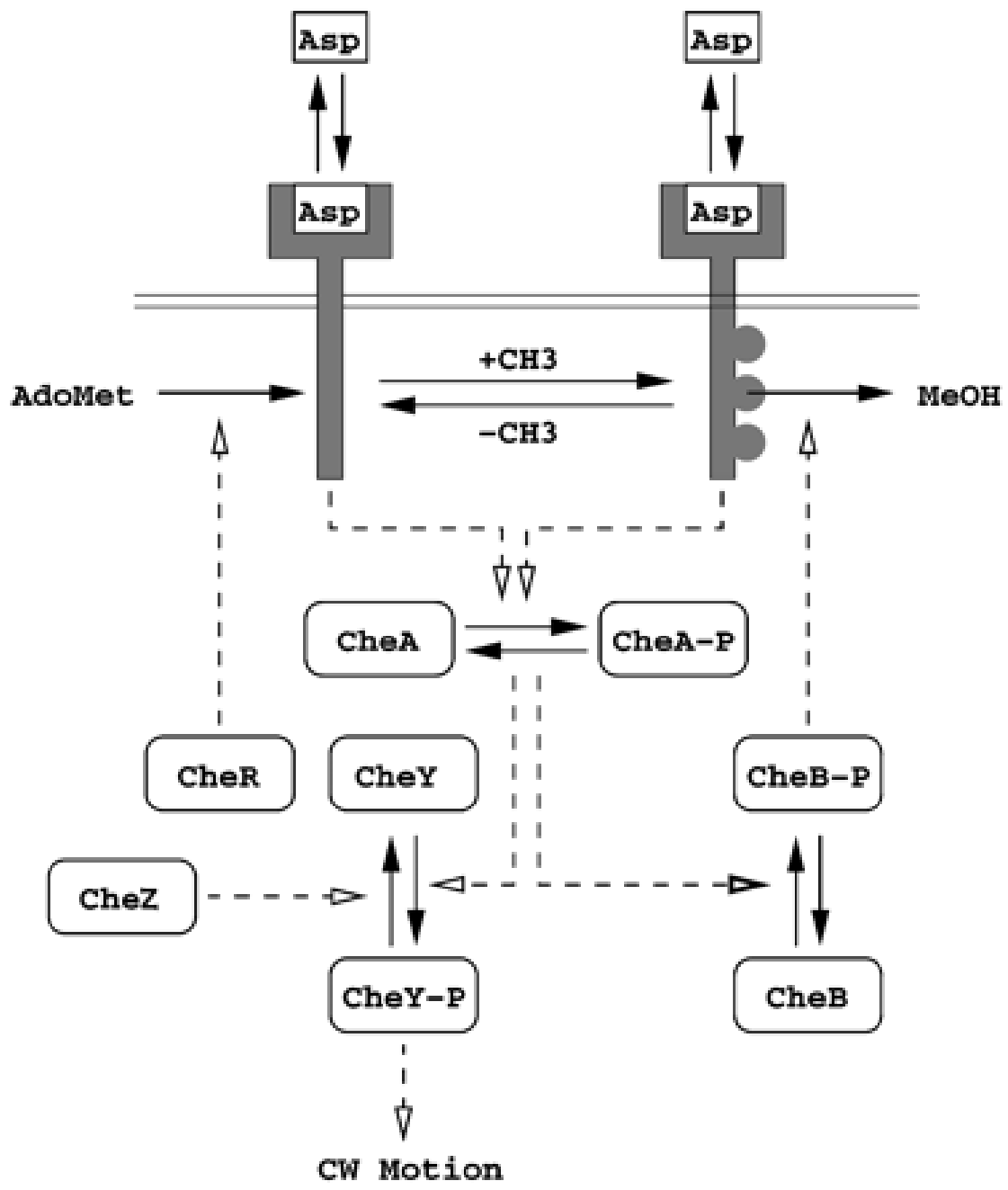
for i=1:length(U)

    x0=[0;0]; u=U(i); g=10.0; P=[u;g];
    [t,y]=ode23s('feedback',[0,7000],x0,[],P);
    plot(y(:,1),y(:,2)); hold on;

end;
```

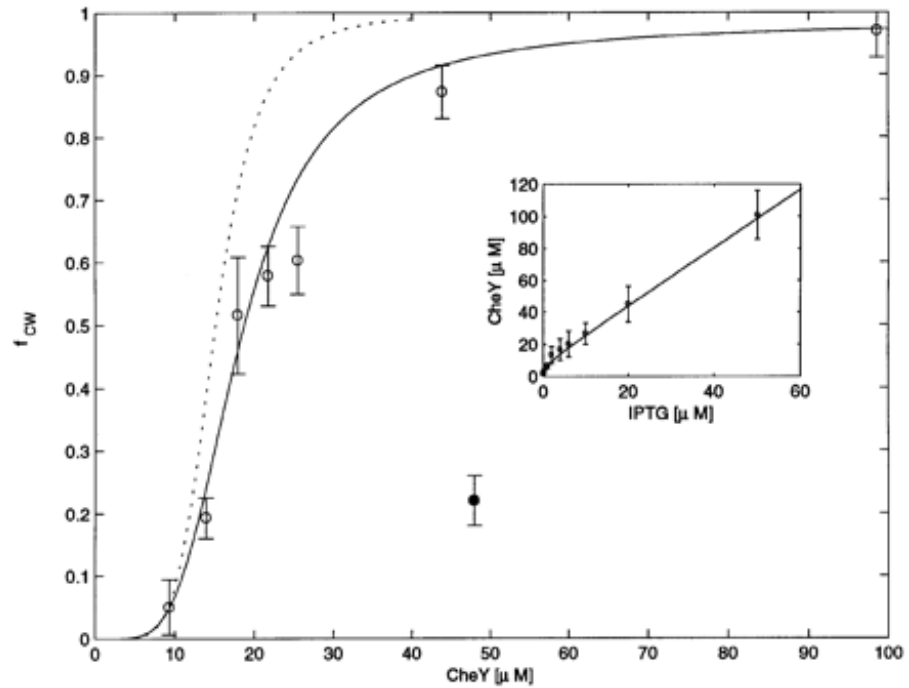
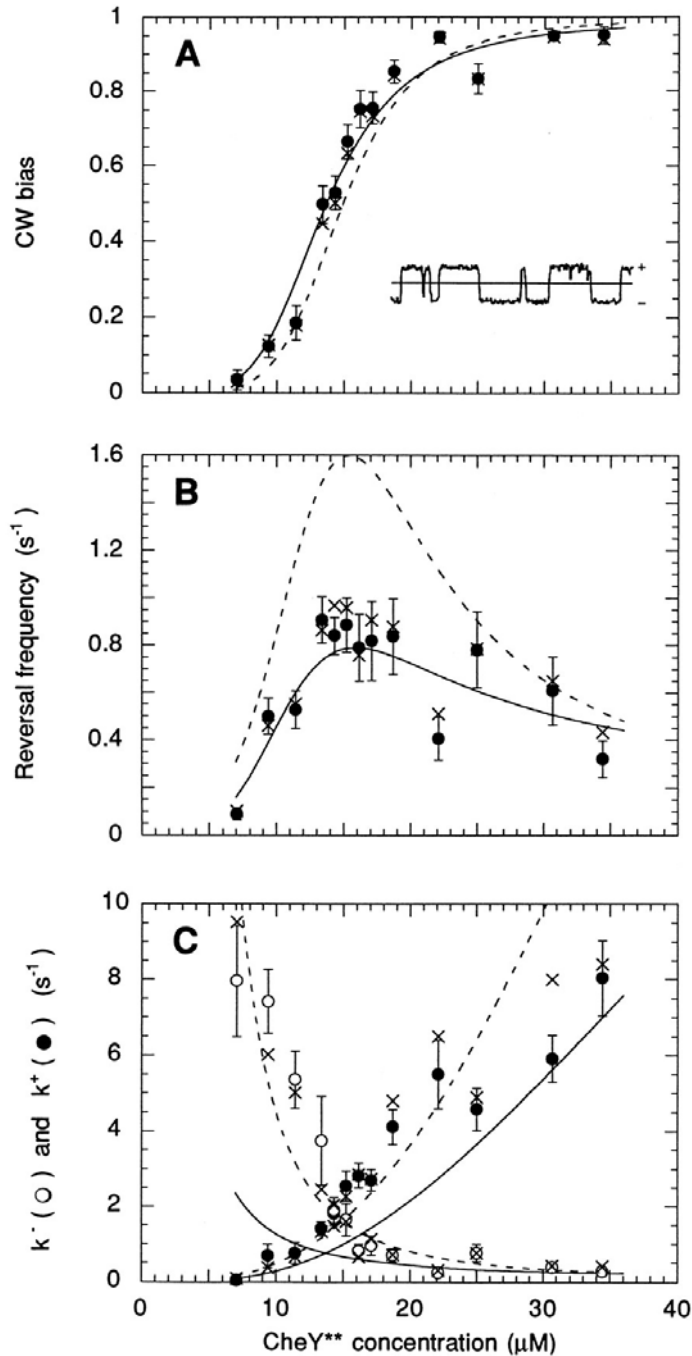






Input/output behavior was quantified:
 Motor bias = $F(\bullet)$

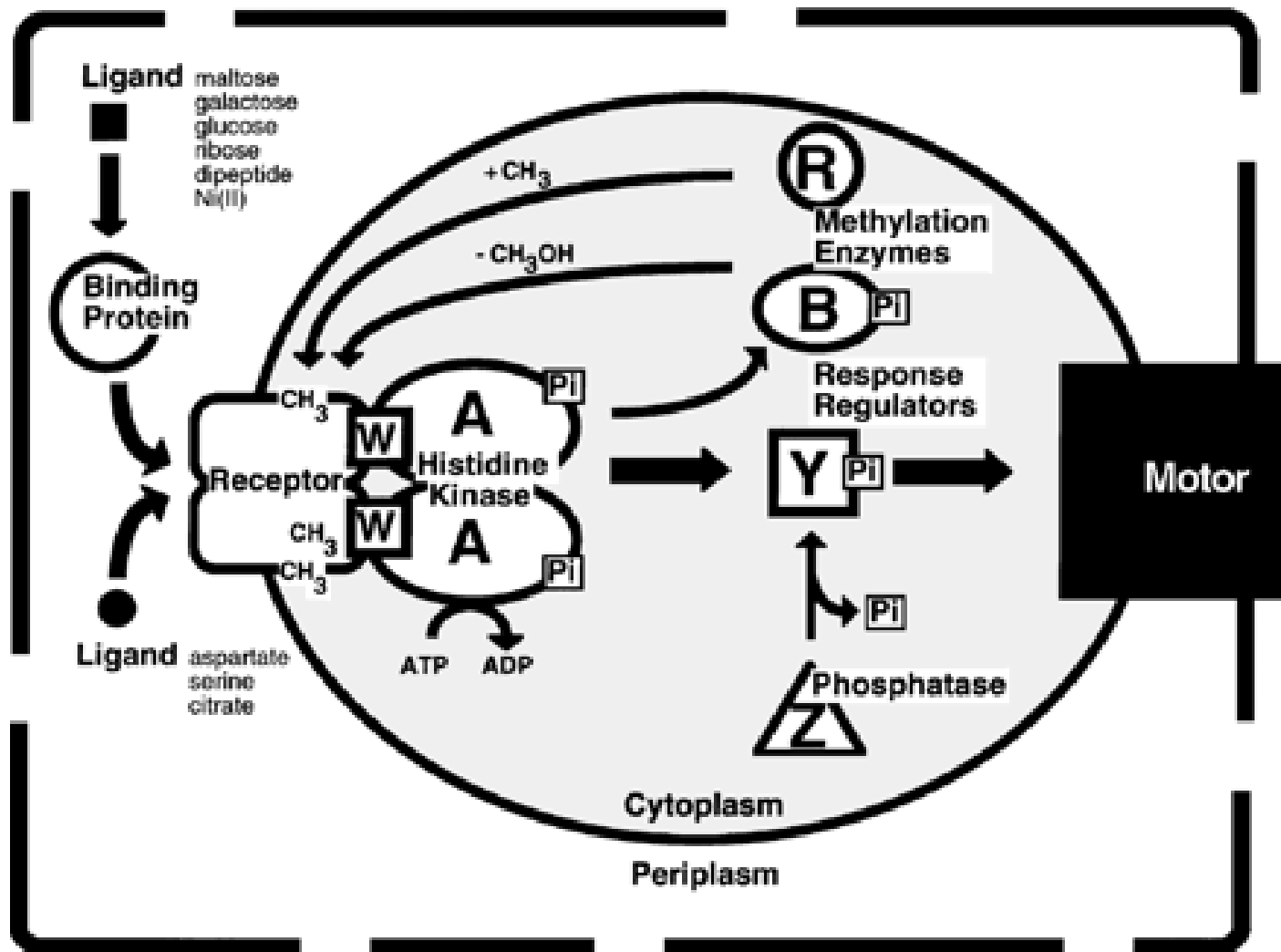
1998

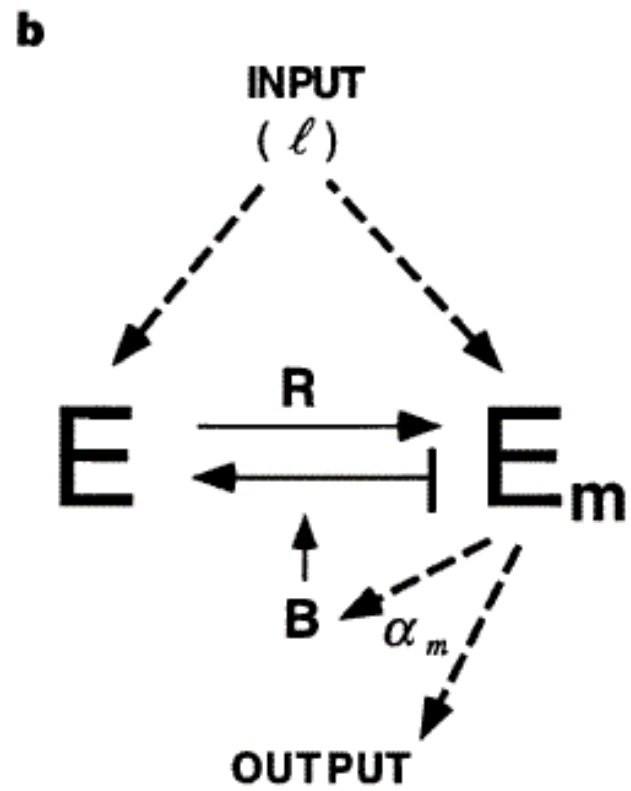
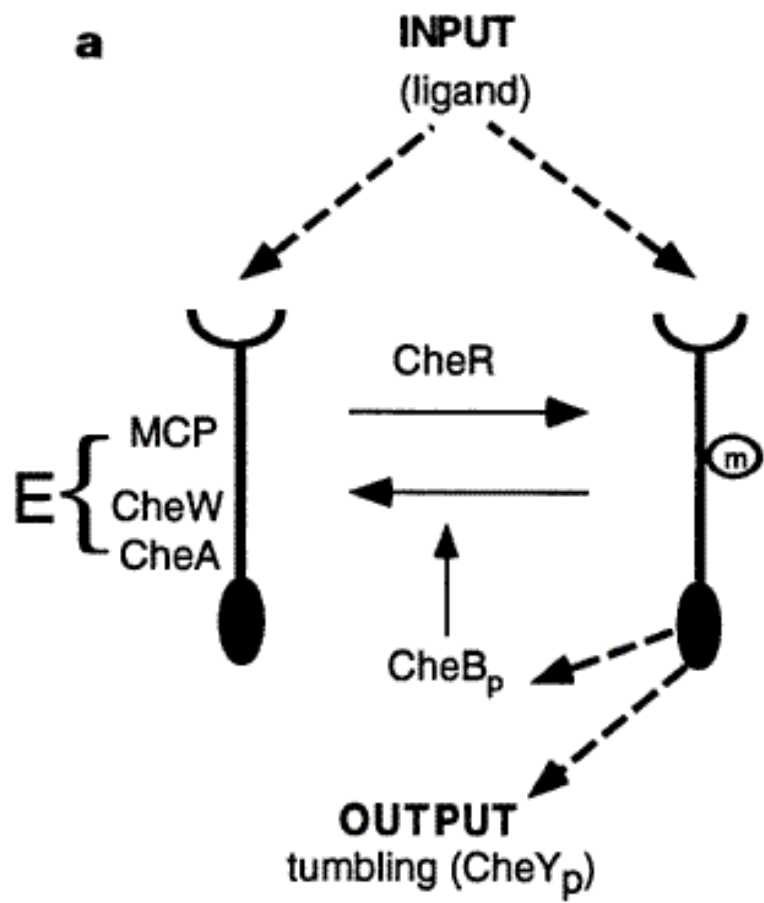


Alon U, Camarena L, Surette MG, Aguera y Arcas B, Liu Y, Leibler S, Stock JB.
 Response regulator output in bacterial chemotaxis.
 EMBO J. 1998 Aug 3;17(15):4238-48.

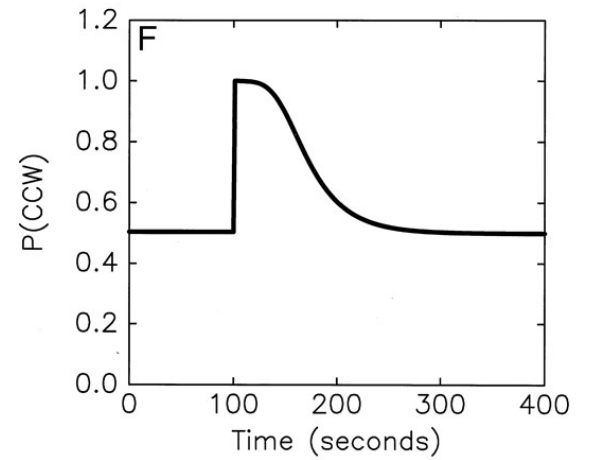
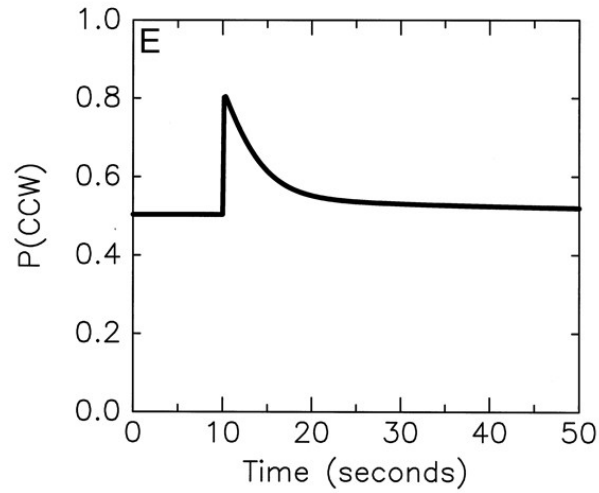
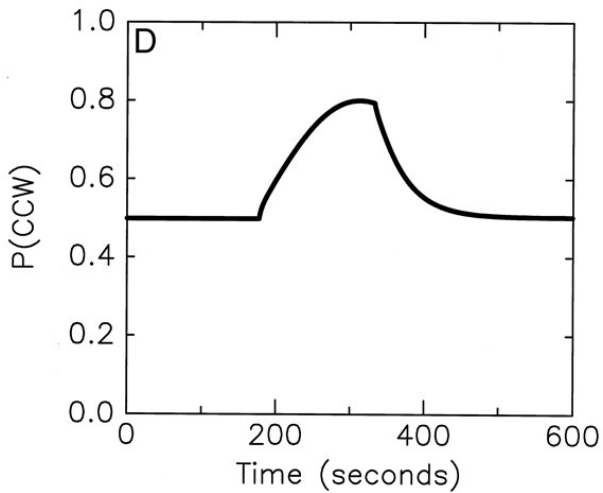
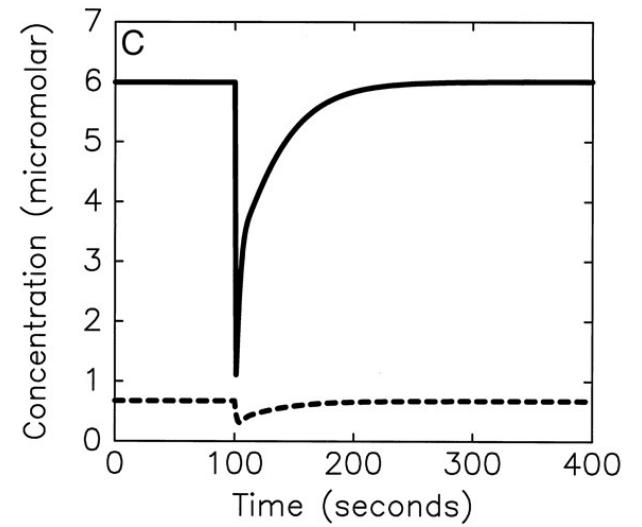
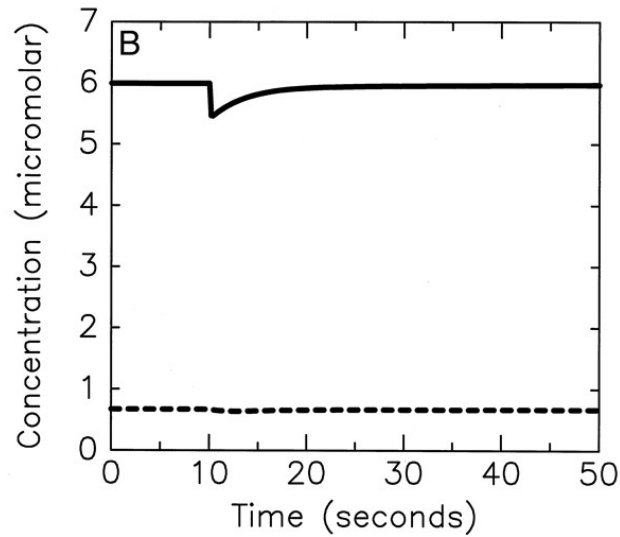
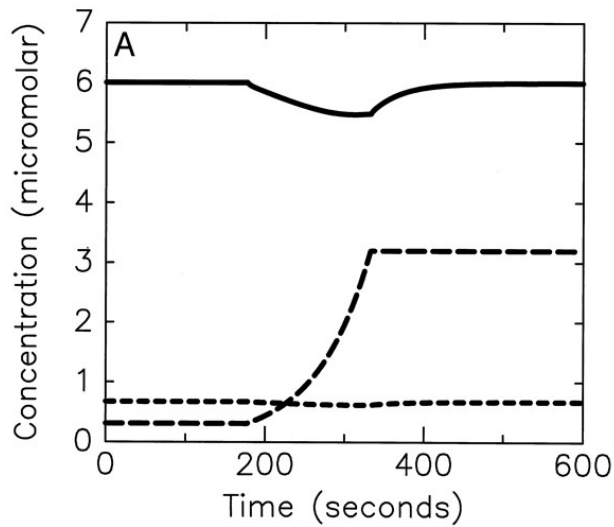
Scharf BE, Fahrner KA, Turner L, Berg HC.
 Control of direction of flagellar rotation in bacterial chemotaxis
 Proc Natl Acad Sci U S A. 1998 Jan 6;95(1):201-6.

Chemotaxis Network

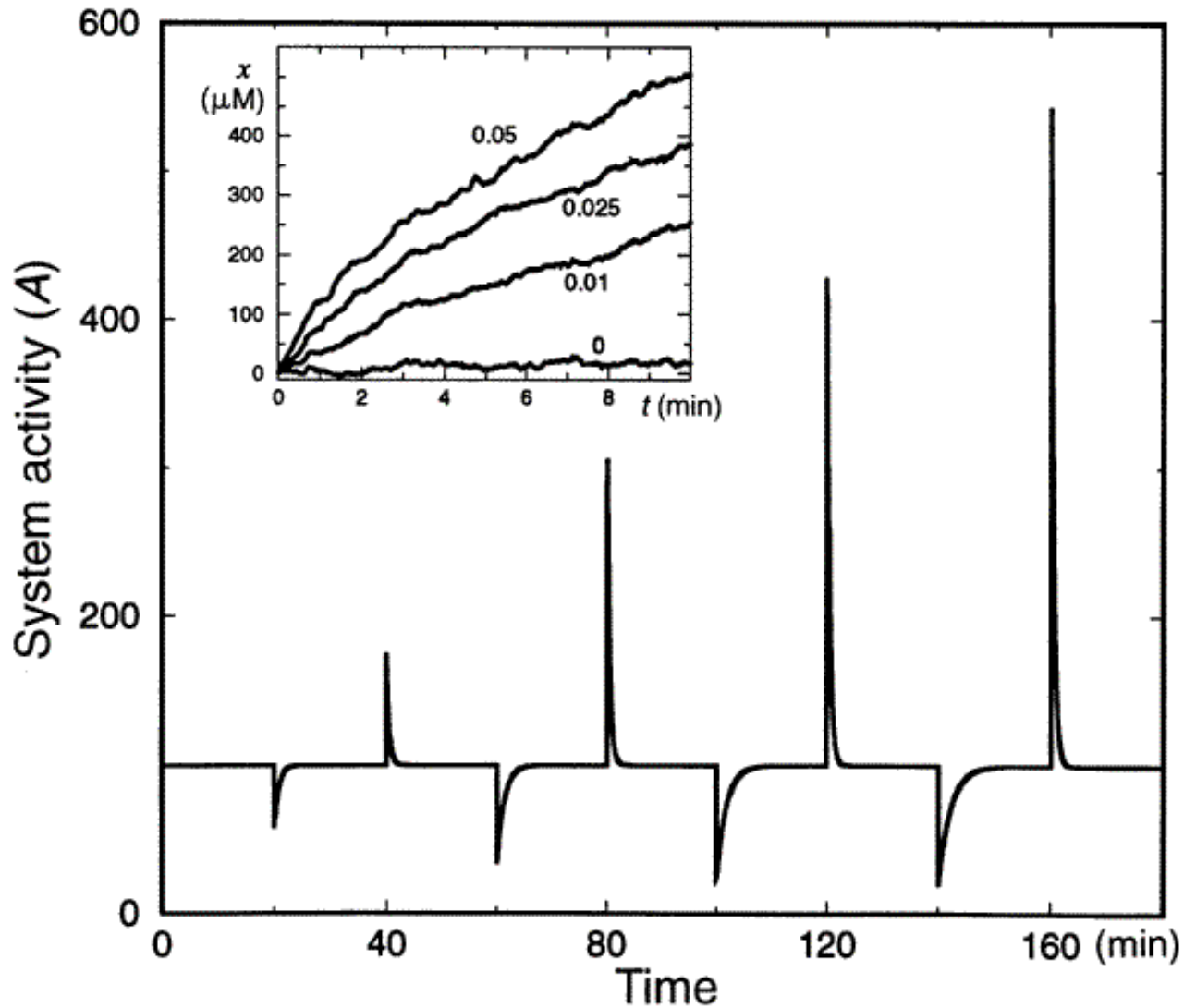




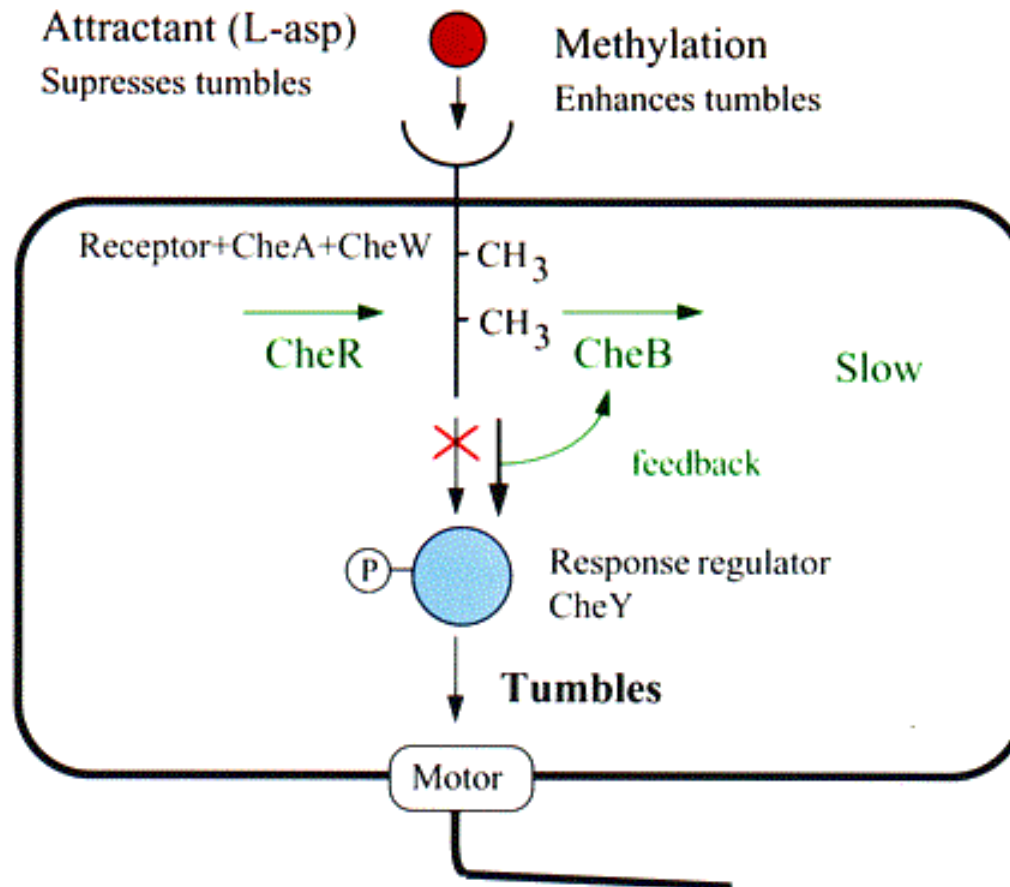
Spiro, Othmer, Parkinson, 1997



Bacterial chemotaxis became a honey pot for modelers

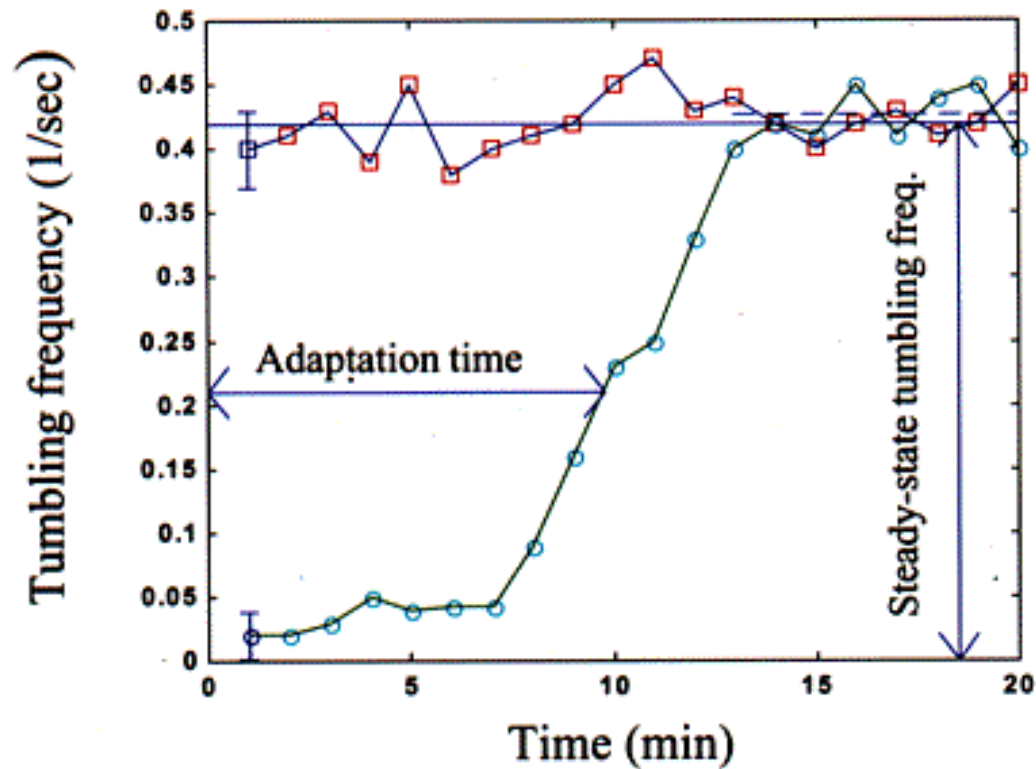


Adaptation is Precise



<http://online.itp.ucsb.edu/online/infobio01/alon1/oh/116.html>

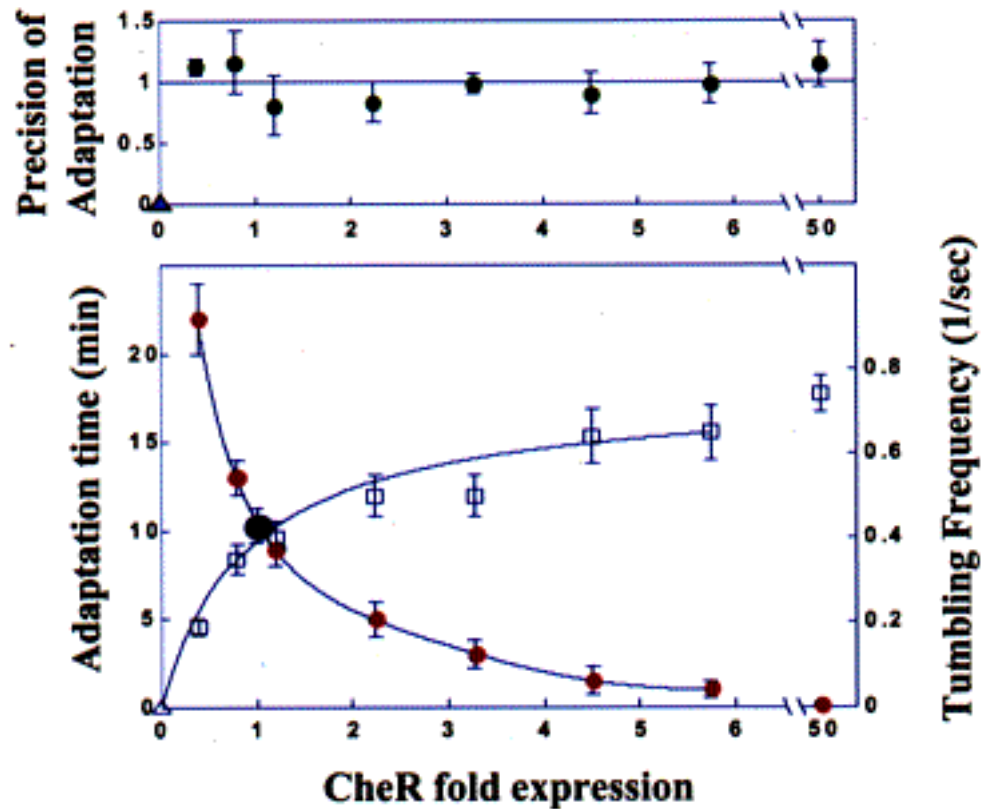
Response and adaptation to attractant



E. coli RP437

<http://online.itp.ucsb.edu/online/infobio01/alon1/oh/116.html>

Effect of varying CheR concentration

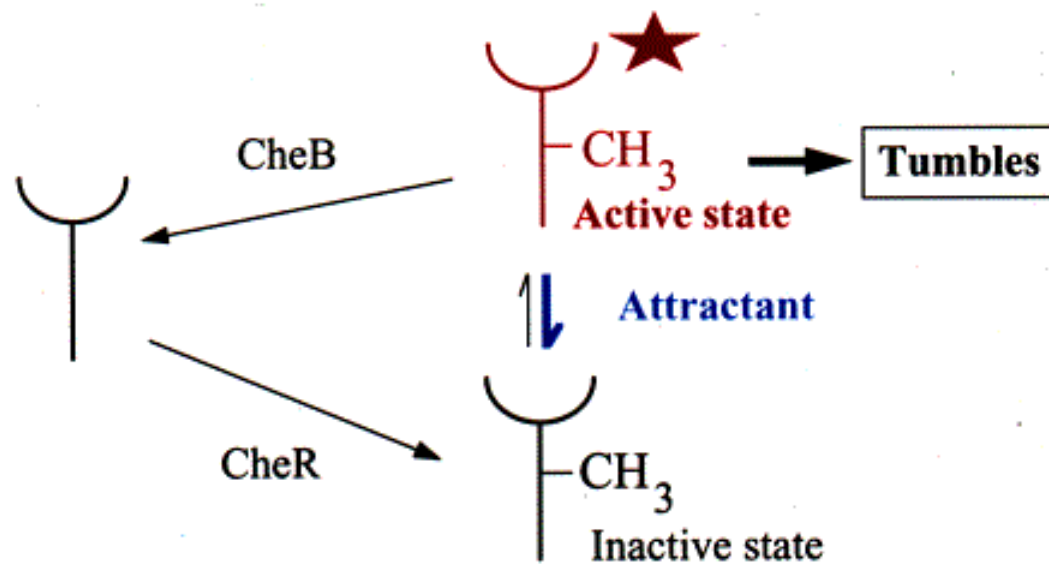


RP4968(Δ cheR) + p lac-CheR

<http://online.itp.ucsb.edu/online/infobio01/alon1/oh/116.html>

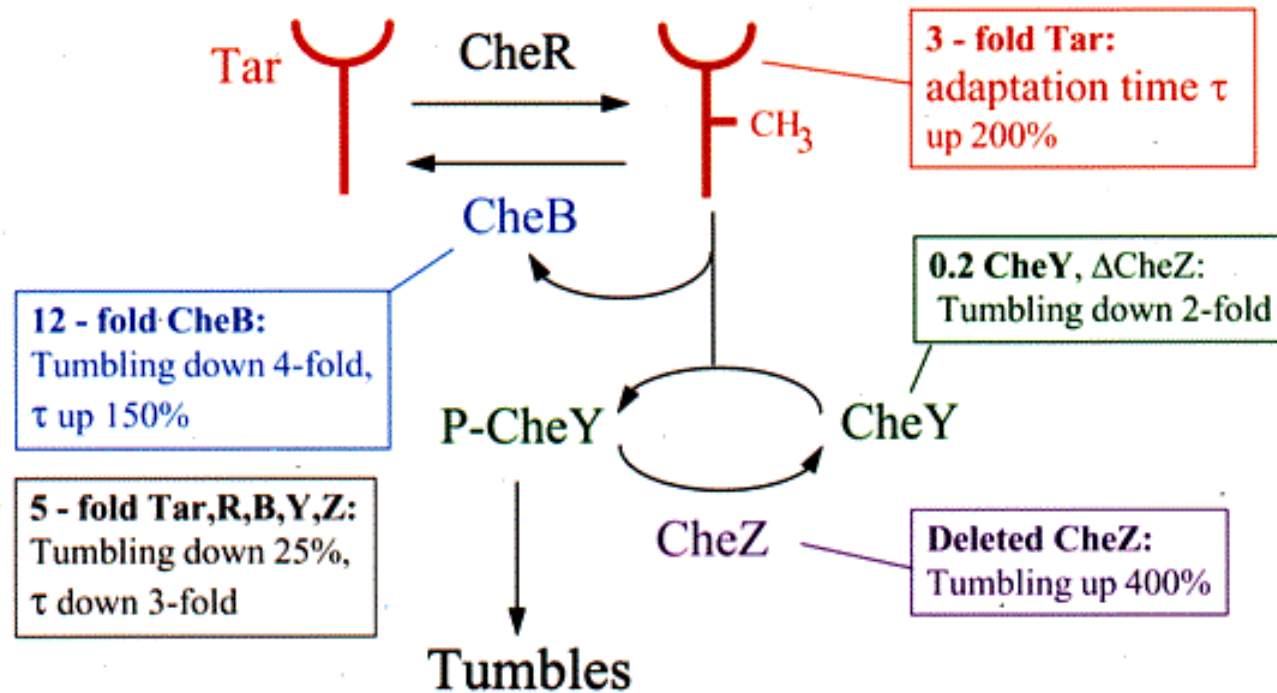
Robust Mechanism for Adaptation

Barkai & Leibler 1997



Two-state receptors: Asakura, Honda 1984.
Stock, Surette 1996.

Varying different proteins in the network



Adaptation precise to within 10% in all cases

<http://online.itp.ucsb.edu/online/infobio01/alon1/oh/116.html>

The gain is huge

Experiment 1:

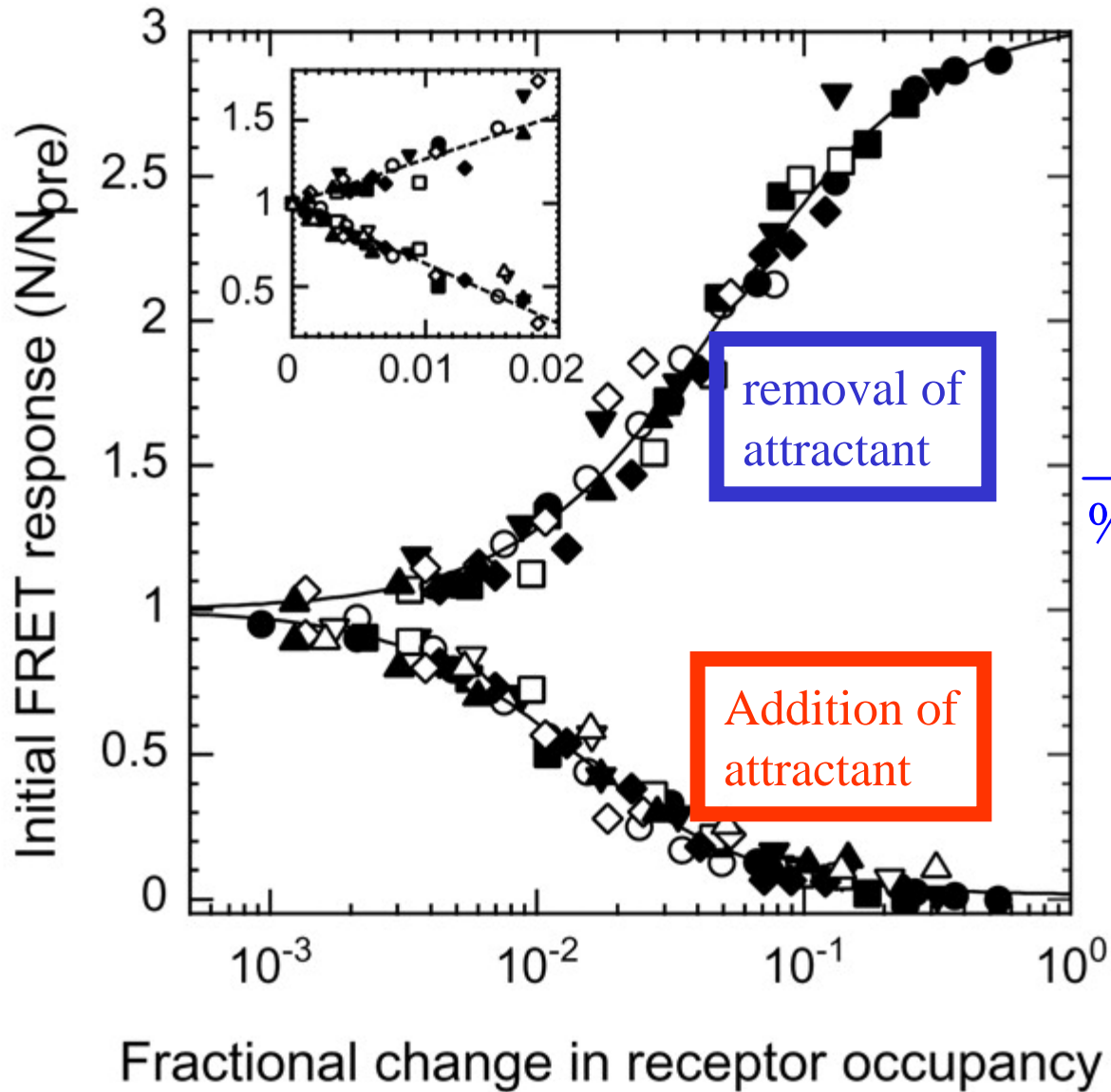
- Cells tracked ~6mm from the capillary with 1mM aspartate:
- Gradient: 0.02 $\mu\text{M}/\mu\text{m}$
- Mean concentration: 8 μM
- Run length 10 μm
- Fractional change in concentration: 2.5%
- Fractional change in receptor occupancy: 0.003
- Runs up the gradient increased in length by 30%

Experiment 2:

- Tethered cell
- Fractional change in receptor occupancy: 0.002
- Rotational bias 0.23

The gain is prodigious

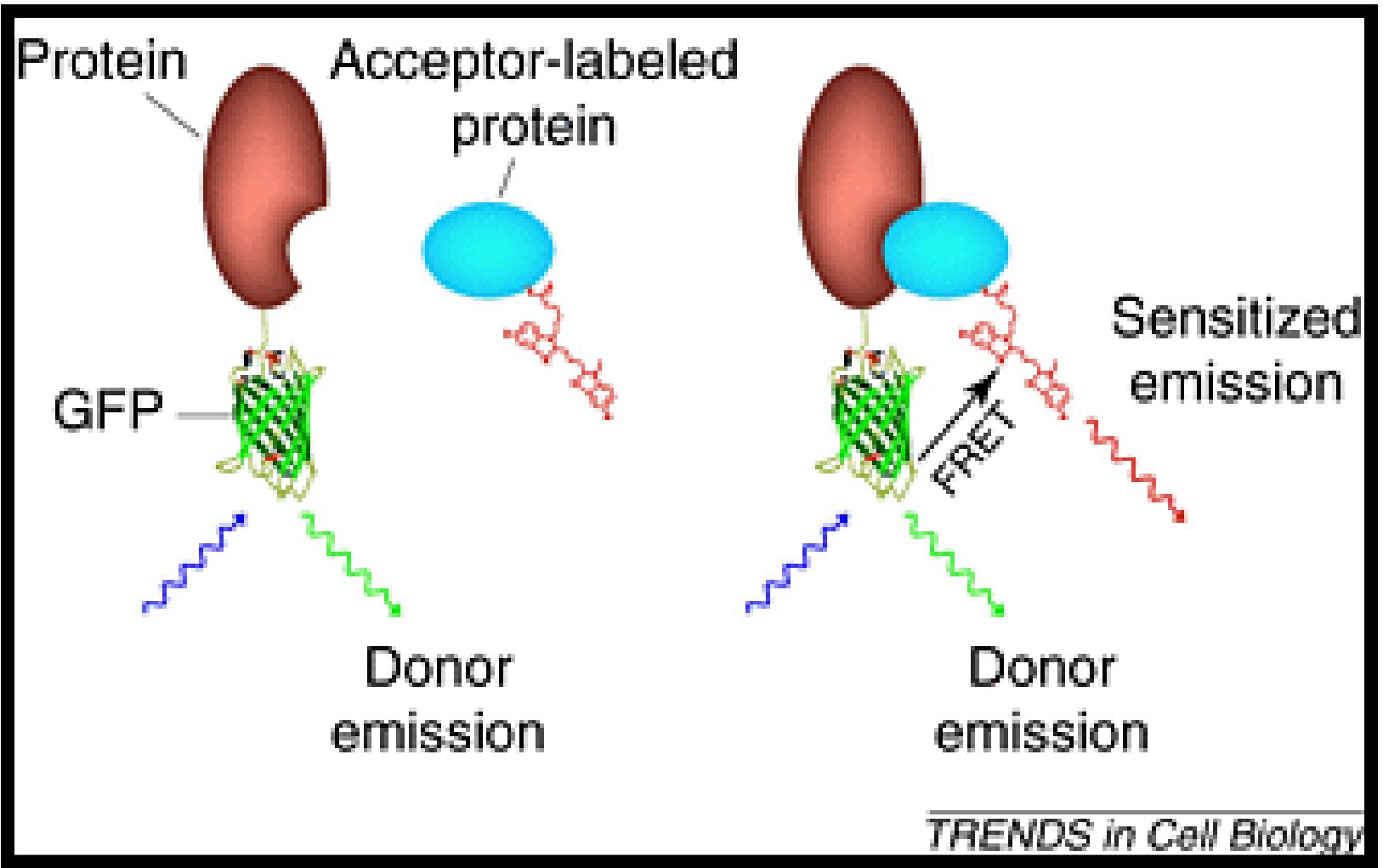
c



$$\frac{\% \Delta CheY - P}{\% \Delta \text{Occupied receptors}} > 30$$

Experiment:
FRET for protein/protein
Interactions

Berg & Sourjik, 2002

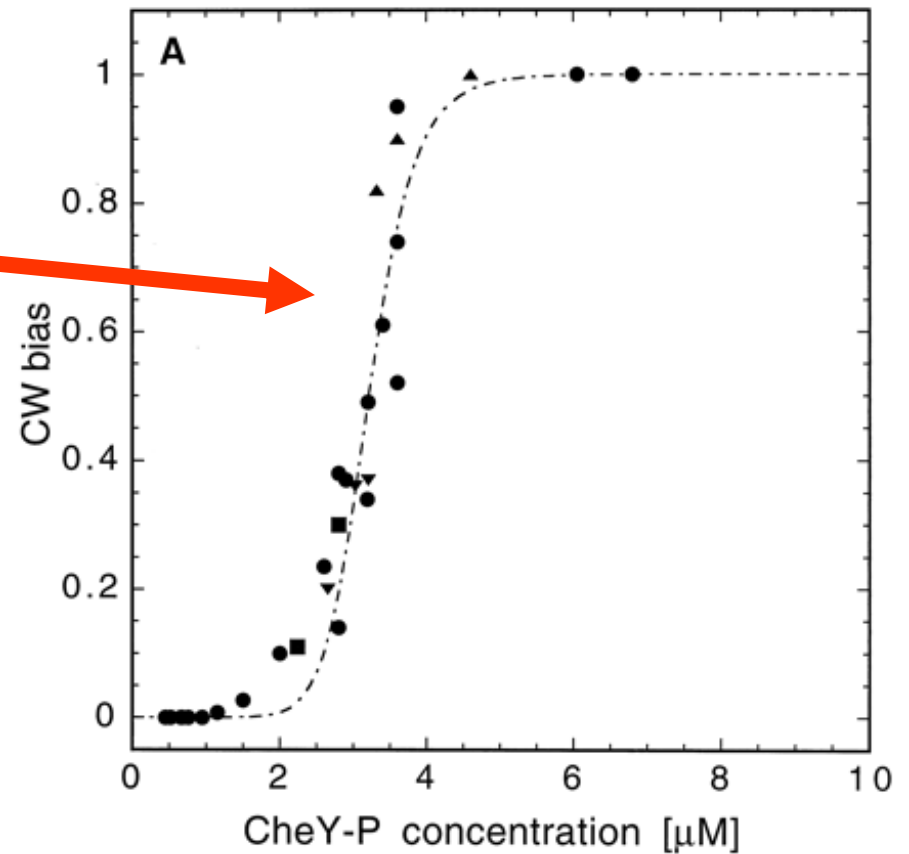


What keeps the gain large
over the range of concentrations ?

How is it used?

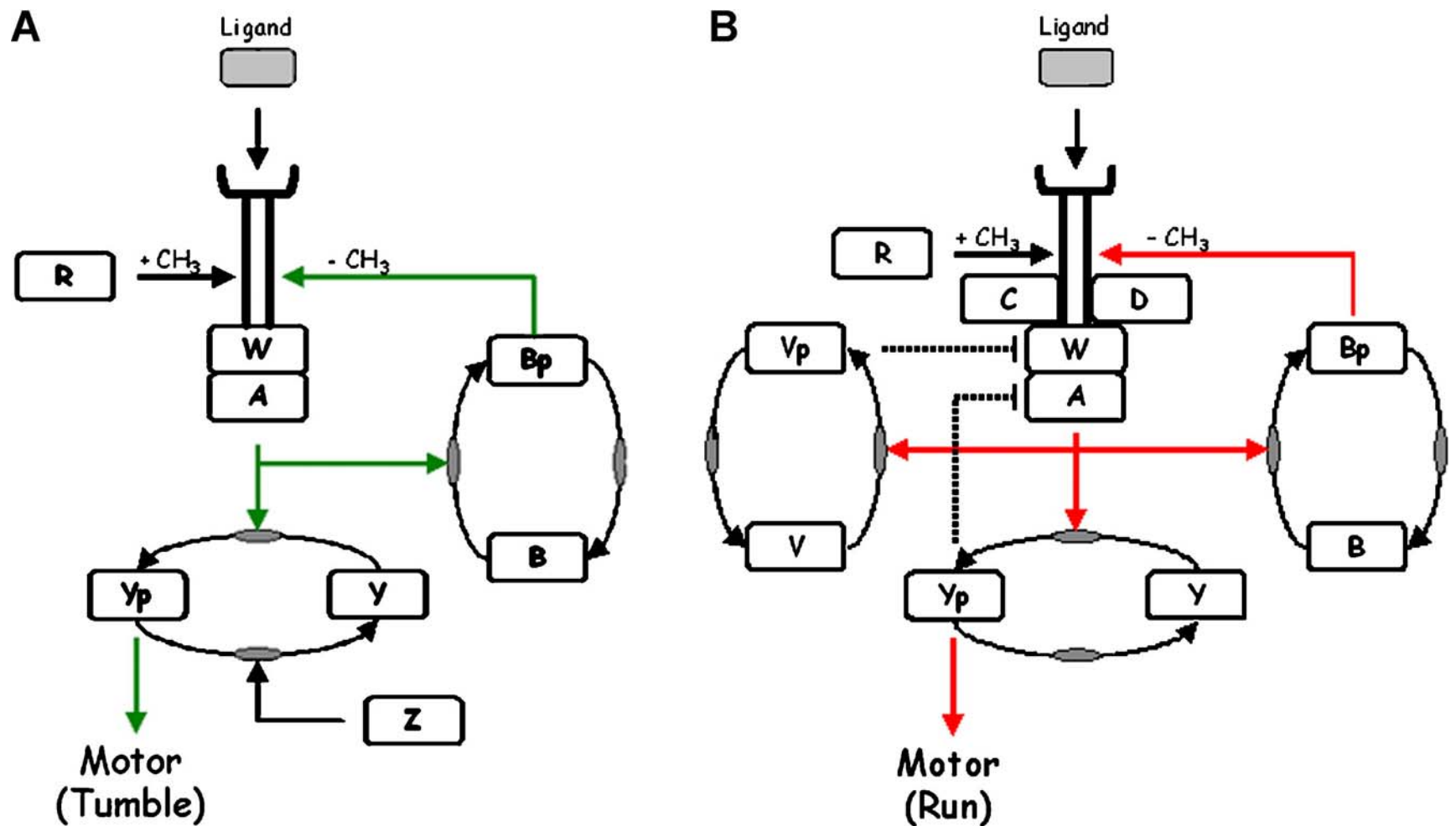
The motor appears to be
ultrasensitive (Cluzel, Surette, Leibler, 2000)

The Che-Yp in a fully adapted cell
appears to be near the
threshold



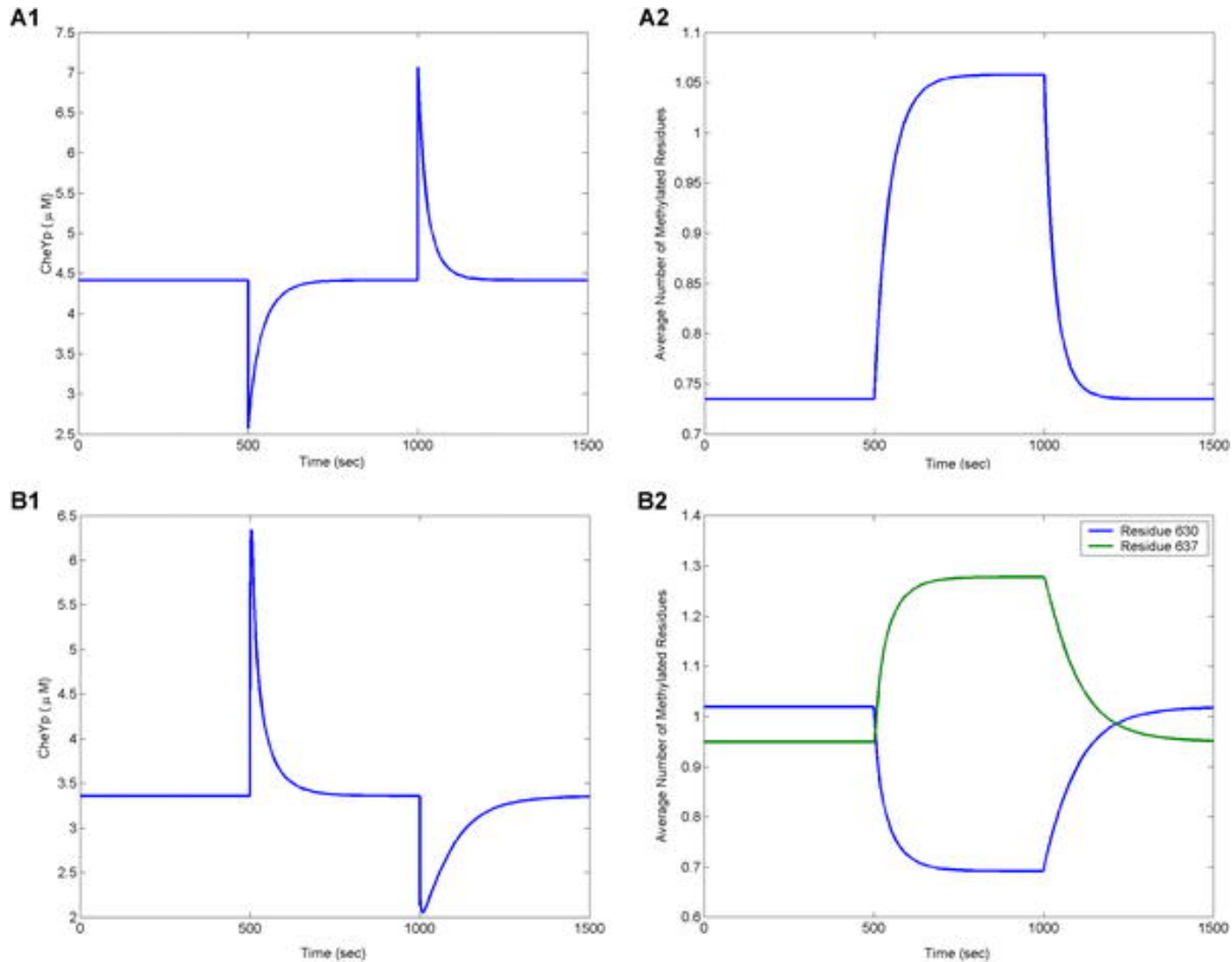
(Cluzel, Surette, Leibler, 2000)

Chemotaxis network in different species



Rao CV, Kirby JR, Arkin AP. Design and Diversity in Bacterial Chemotaxis: A Comparative Study in *Escherichia coli* and *Bacillus subtilis*. PLoS Biol. 2004 Feb;2(2):E49.

Both networks can robustly adapt



Rao CV, Kirby JR, Arkin AP. Design and Diversity in Bacterial Chemotaxis: A Comparative Study in *Escherichia coli* and *Bacillus subtilis*. PLoS Biol. 2004 Feb;2(2):E49.