

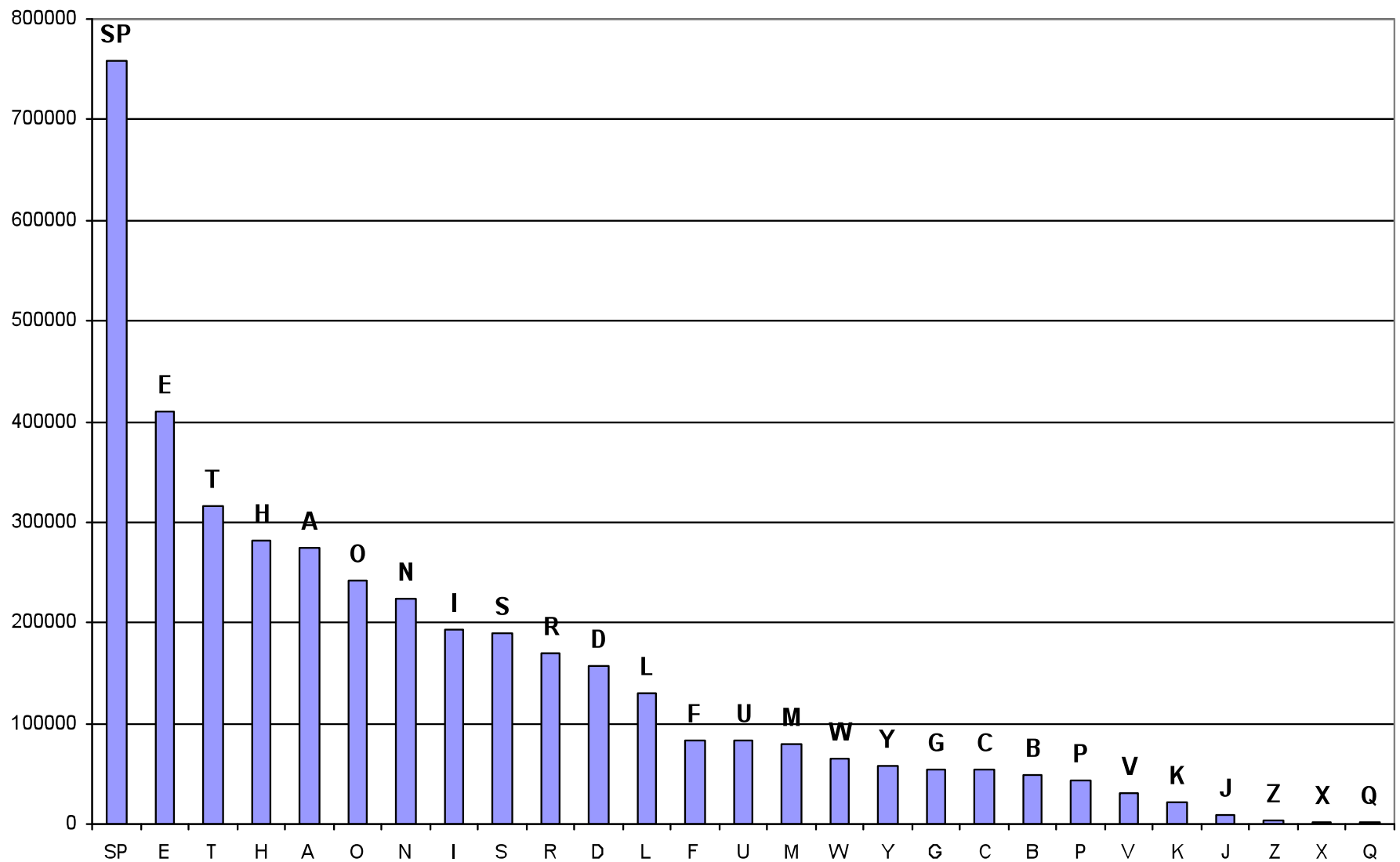
# Compression; Error detection & correction

- **compression: squeeze out redundancy**
  - to use less memory and/or use less network bandwidth,
  - encode the same information in fewer bits
    - some bits carry no information
    - some bits can be computed or inferred from others
    - some bits don't matter to the recipient and can be dropped entirely
- **error detection & correction: add redundancy**
  - to detect and fix up loss or damage
  - add carefully defined, systematic redundancy
  - with enough of the right redundancy,
    - can detect damaged bits
    - can correct errors

# Compressing English text

- **letters do not occur equally often**
- **encode frequent letters with fewer bits,**
- **encode less frequent letters with more bits**
- **trades complexity against space**
  - e.g., Morse code, Huffman code, ...
- **run-length encoding**
  - encode runs of identical things with a count
  - e.g., World Wide Web Consortium => WWWWC => W3C
- **words do not occur equally often**
- **encode whole words or phrases, not just letters**
  - e.g., abbreviations for frequent words or sequences
  - acronyms, shorthands, ...

# Letter frequencies in King James bible (4.1M chars)



# Lempel-Ziv coding; adaptive compression algorithms

- **build a dictionary of recently occurring data**
- **replace subsequent occurrences by (shorter) reference to the dictionary entry**
- **dictionary adapts as more input is seen**
  - compression adapts to properties of particular input
  - algorithm is independent of nature of input
- **dictionary is included in the compressed data**
- **Lempel-Ziv is the basis of PKZip, Winzip, gzip, GIF**
  - compresses Bible from 4.1 MB to 1.2 MB (typical for text)
- **Lempel-Ziv is a lossless compression scheme**
  - compression followed by decompression reproduces the input exactly
- **lossy compression: may do better if can discard some information**
  - commonly used for pictures, sounds, movies

# **JPEG** (Joint Photographic Experts Group) **picture compression**

- **a lossy compression scheme, based on how our eyes work**
- **digitize picture into pixels**
- **discard some color information (use fewer distinct colors)**
  - eye is less sensitive to color variation than brightness
- **discard some fine detail**
  - decompressed image is not quite as sharp as original
- **discard some fine gradations of color and brightness**
  
- **use Huffman code, run-length encoding, etc., to compress resulting stream of numeric values**
  
- **compression is usually 10:1 to 20:1 for pictures**
- **used in web pages, digital cameras, ...**

# **MPEG** (Moving Picture Experts Group) **movie compression**

- **MPEG-4: lossy compression scheme, based on human perceptions**
  - H.264 is most-used current version
- **uses JPEG for individual frames (spatial redundancy)**
- **adds compression of temporal redundancy**
  - look at image in blocks
  - if a block hasn't changed, just transmit that fact, not the content
  - if a block has moved, transmit amount of motion
  - motion prediction (encode expected differences plus correction)
  - separate moving parts from static background
  - ...
- **used in phones, DVD, TV, Internet video, video games, ...**
- **rate depends on resolution, frame rate, ...**

# MP3 (MPEG Audio Layer-3) sound compression

- **movies have sound as well as motion; this is the audio part**
- **3 levels, with increasing compression, increasing complexity**
- **based on "perceptual noise shaping":**
  - use characteristics of the human ear to compress better:**
    - human ear can't hear some sounds (e.g., very high frequencies)
    - human ear hears some sounds better than others
    - louder sounds mask softer sounds
- **break sound into different frequency bands**
- **encode each band separately**
- **encode 2 stereo channels as 1 plus difference**
- **gives about 10:1 compression over CD-quality audio**
  - 1 MB/minute instead of 10 MB/minute
  - can trade quality against compression

# Summary of compression

- **eliminate / reduce redundancy**
  - more frequent things encoded with fewer bits
  - use a dictionary of encoded things, and refer to it (Lempel-Ziv)
  - encode repetitions with a count
- **not everything can be compressed**
  - something will be bigger
- **lossless vs lossy compression**
  - lossy discards something that is not needed by recipient
- **tradeoffs**
  - encoding time and complexity vs decoding time and complexity
  - encoding is usually slower and more complicated (done once)
  - parameters in lossy compressions
    - size, speed, quality



# Error detection and correction

- **systematic use of redundancy to defend against errors**
- **some common numbers have no redundancy**
  - and thus can't detect when an error might have occurred
  - e.g., SSN -- any 9-digit number is potentially valid
- **if some extra data is added or if some possible values are excluded, this can be used to detect and even correct errors**
- **common examples include**
  - ATM & credit card numbers
  - ISBN for books
  - bar codes for products

# ATM card checksum

- **credit card / ATM card checksum:**  
starting at rightmost digit:
  - multiply digit alternately by 1 or 2
  - if result is  $> 9$  subtract 9
  - add the resulting digitssum should be divisible by 10

e.g., 12345678 is invalid

$$8 + (14-9) + 6 + (10-9) + 4 + 6 + 2 + 2 = 34$$

but 42345678 is valid

$$8 + (14-9) + 6 + (10-9) + 4 + 6 + 2 + 8 = 40$$

- **defends against transpositions and many single digit errors**
  - these are the most common errors



# Parity & other binary codes

- **parity bit: use one extra bit so total number of 1-bits is even**

0110100 => 01101001

0110101 => 01101010

- detects any single-bit error

- **more elaborate codes can detect and even correct errors**
- **basic idea is to add extra bits systematically so that legal values are uniformly spread out, so any small error converts a legal value into an illegal one**
  - some schemes correct random isolated errors
  - some schemes correct bursts of errors (used in CD-ROM and DVD)
- **no error correcting code can detect/correct all errors**
  - a big enough error can convert one legal pattern into another one

