

# The MapReduce programming model

**Input** a list of (key, value) pairs

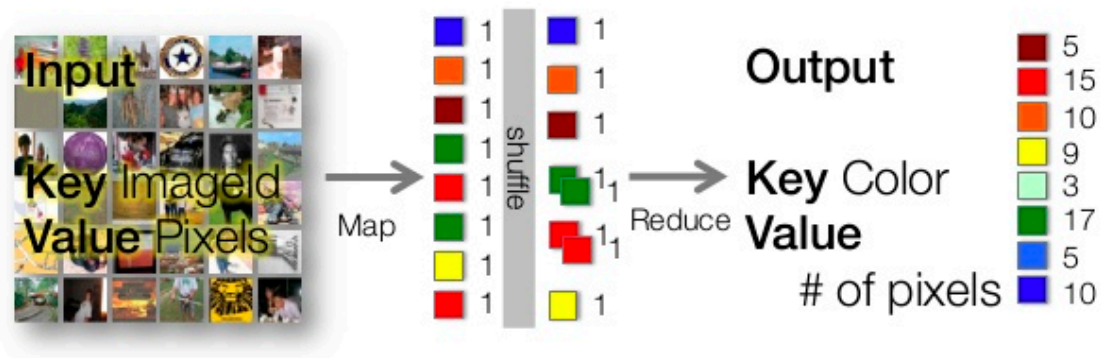
**Map** apply a function  $f$  to all pairs

**Reduce** apply a function  $g$  to  
all values with key  $k$  (for all  $k$ )

**Output** a list of (key, value) pairs

## Computing a histogram

### A simple MapReduce example



Map(ImageId, Pixels)

for each pixel

emit

Key = (r,g,b)

Value = 1

Reduce(Color, Values)

emit

Key = Color

Value = sum(Values)

## Many matrix computations are possible in MapReduce

$A_{11}$	$A_{12}$	$A_{13}$	$A_{14}$
$A_{21}$	$A_{22}$	$A_{23}$	$A_{24}$
$A_{31}$	$A_{32}$	$A_{33}$	$A_{34}$
$A_{41}$	$A_{42}$	$A_{43}$	$A_{44}$

$(3,4) \rightarrow 5$   
 $(1,2) \rightarrow -6.0$   
 $(2,3) \rightarrow -1.2$   
 $(1,1) \rightarrow 3.14$

“Coordinate storage”

### Column sums are easy

Input Key  $(i,j)$  Value  $A_{ij}$

**Map** $((i,j), val)$       **Reduce** $(j, Values)$

emit      emit

Key =  $j$ , Value =  $val$       Key =  $j$ , Value =  $sum(Values)$

### Other basic methods

can use common parallel/out-of-core algs

Sparse matrix-vector products  $\mathbf{y} = \mathbf{Ax}$

Sparse matrix-matrix products  $\mathbf{C} = \mathbf{AB}$

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**Input** a list of (key, value) pairs

**Map** apply a function  $f$  to all pairs

**Reduce** apply a function  $g$  to  
all values with key  $k$  (for all  $k$ )

**Output** a list of (key, value) pairs

Map function  $f$  must be side-effect free  
*All map functions run in parallel*

Reduce function  $g$  must be side-effect free  
*All reduce functions run in parallel*