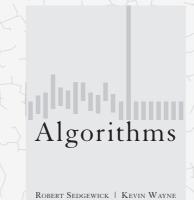


5.1 STRING SORTS

- strings in Java
- key-indexed counting
- LSD radix sort
- MSD radix sort
- 3-way radix quicksort
- suffix arrays



http://algs4.cs.princeton.edu

5.1 STRING SORTS

- strings in Java
- key-indexed counting
- ISD radix sort
- MSD radix sort
- 3-way radix quicksort
- > suffix arrays

String processing

String. Sequence of characters.

Important fundamental abstraction.

- Programming systems (e.g., Java programs).
- Communication systems (e.g., email).
- · Information processing.
- Genomic sequences.
- ...

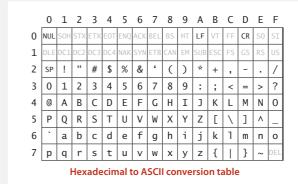
"The digital information that underlies biochemistry, cell biology, and development can be represented by a simple string of G's, A's, T's and C's. This string is the root data structure of an organism's biology." — M. V. Olson



The char data type

C char data type. Typically an 8-bit integer.

- Supports 7-bit ASCII.
- Can represent at most 256 characters.



 $\text{A \'a} \stackrel{\text{\'a}}{\text{\tiny U+0041}} \stackrel{\text{\'a}}{\text{\tiny U+00E1}} \stackrel{\text{\o}}{\text{\tiny U+2202}} \stackrel{\text{\o}}{\text{\tiny U+1D50A}}$

some Unicode characters

Java char data type. A 16-bit unsigned integer.

- Supports original 16-bit Unicode.
- Supports 21-bit Unicode 3.0 (awkwardly).

I ♥ Unicode



The String data type

String data type in Java. Immutable sequence of characters.

Length. Number of characters.

Indexing. Get the *i*th character.

Concatenation. Concatenate one string to the end of another.



The String data type: immutability

Q. Why immutable?

A. All the usual reasons.

- Can use as keys in symbol table.
- Don't need to defensively copy.
- · Ensures consistent state.
- Supports concurrency.
- Improves security.

```
public class FileInputStream
{
    private String filename;
    public FileInputStream(String filename)
    {
        if (!allowedToReadFile(filename))
            throw new SecurityException();
        this.filename = filename;
    }
    ...
}
```

attacker could bypass security if string type were mutable

The String data type: representation

Representation (Java 7). Immutable char[] array + cache of hash.

operation	Java	running time
length	s.length()	1
indexing	s.charAt(i)	1
concatenation	s + t	M + N
÷		÷

String performance trap

Q. How to build a long string, one character at a time?

```
public static String reverse(String s)
{
    String rev = "";
    for (int i = s.length() - 1; i >= 0; i--)
        rev += s.charAt(i);
    return rev;
}
```

A. Use StringBuilder data type (mutable char[] resizing array).

```
public static String reverse(String s)
{
    StringBuilder rev = new StringBuilder();
    for (int i = s.length() - 1; i >= 0; i--)
        rev.append(s.charAt(i));
    return rev.toString();
}
```

Alphabets

Digital key. Sequence of digits over fixed alphabet. Radix. Number of digits *R* in alphabet.

name	R()	lgR()	characters
BINARY	2	1	01
OCTAL	8	3	01234567
DECIMAL	10	4	0123456789
HEXADECIMAL	16	4	0123456789ABCDEF
DNA	4	2	ACTG
LOWERCASE	26	5	abcdefghijklmnopqrstuvwxyz
UPPERCASE	26	5	ABCDEFGHIJKLMNOPQRSTUVWXYZ
PROTEIN	20	5	ACDEFGHIKLMNPQRSTVWY
BASE64	64	6	ABCDEFGHIJKLMNOPQRSTUVWXYZabcdef ghijklmnopqrstuvwxyz0123456789+/
ASCII	128	7	ASCII characters
EXTENDED_ASCII	256	8	extended ASCII characters
UNICODE16	65536	16	Unicode characters

Comparing two strings

Q. How many character compares to compare two strings, each of length W?

s.compareTo(t)

s	р	r	е	f	е	t	С	h
	0	1	2	3	4	5	6	7
t	р	r	е	f	i	Х	е	S

Running time. Proportional to length of longest common prefix.

- Proportional to W in the worst case.
- But, often sublinear in W.

5.1 STRING SORTS

strings in Java
key-indexed counting
LSD radix sort

MSD radix sort

3-way radix-quicksort

http://algs4.cs.princeton.edu

Review: summary of the performance of sorting algorithms

Frequency of operations.

algorithm	guarantee	random	extra space	stable?	operations on keys
insertion sort	½ N²	½ N ²	1	~	compareTo()
mergesort	$N \lg N$	$N \lg N$	N	V	compareTo()
quicksort	1.39 N lg N*	1.39 N lg N	c lg N*		compareTo()
heapsort	2 N lg N	$2 N \lg N$	1		compareTo()

* probabilistic

Lower bound. $\sim N \lg N$ compares required by any compare-based algorithm.

Q. Can we do better (despite the lower bound)?

A. Yes, if we don't depend on key compares. \leftarrow

use array accesses to make R-way decisions (instead of binary decisions)

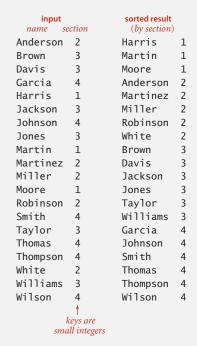
Key-indexed counting: assumptions about keys

Assumption. Keys are integers between 0 and R - 1. Implication. Can use key as an array index.

Applications.

- Sort string by first letter.
- · Sort class roster by section.
- Sort phone numbers by area code.
- Subroutine in a sorting algorithm. [stay tuned]

Remark. Keys may have associated data \Rightarrow can't just count up number of keys of each value.



Key-indexed counting demo

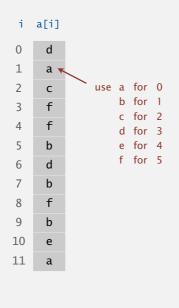
Goal. Sort an array a[] of N integers between 0 and R-1.





- Compute frequency cumulates which specify destinations.
- Access cumulates using key as index to move items.
- Copy back into original array.

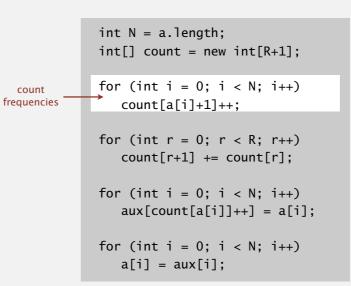
```
int N = a.length;
int[] count = new int[R+1];
for (int i = 0; i < N; i++)
  count[a[i]+1]++;
for (int r = 0; r < R; r++)
  count[r+1] += count[r];
for (int i = 0; i < N; i++)
  aux[count[a[i]]++] = a[i];
for (int i = 0; i < N; i++)
  a[i] = aux[i];
```

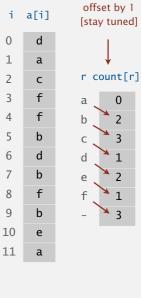


Key-indexed counting demo

Goal. Sort an array a[] of N integers between 0 and R - 1.

- Count frequencies of each letter using key as index.
- Compute frequency cumulates which specify destinations.
- Access cumulates using key as index to move items.
- Copy back into original array.

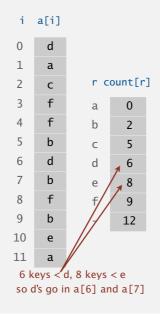




Key-indexed counting demo

Goal. Sort an array a[] of N integers between 0 and R-1.

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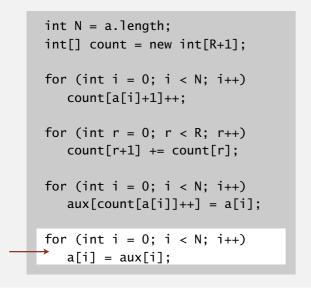


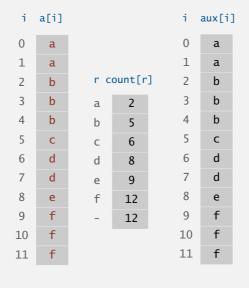
Key-indexed counting demo

Goal. Sort an array a[] of N integers between 0 and R-1.

- Count frequencies of each letter using key as index.
- Compute frequency cumulates which specify destinations.
- Access cumulates using key as index to move items.
- Copy back into original array.

copy back



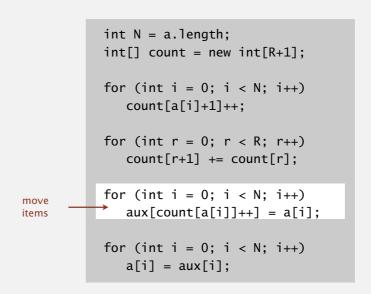


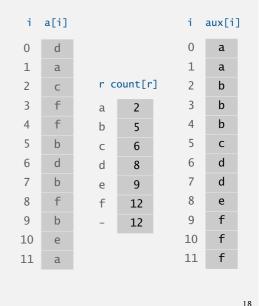
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Key-indexed counting demo

Goal. Sort an array a[] of N integers between 0 and R-1.

- Count frequencies of each letter using key as index
- Compute frequency cumulates which specify destinations.
- Access cumulates using key as index to move items.
- Copy back into original array.



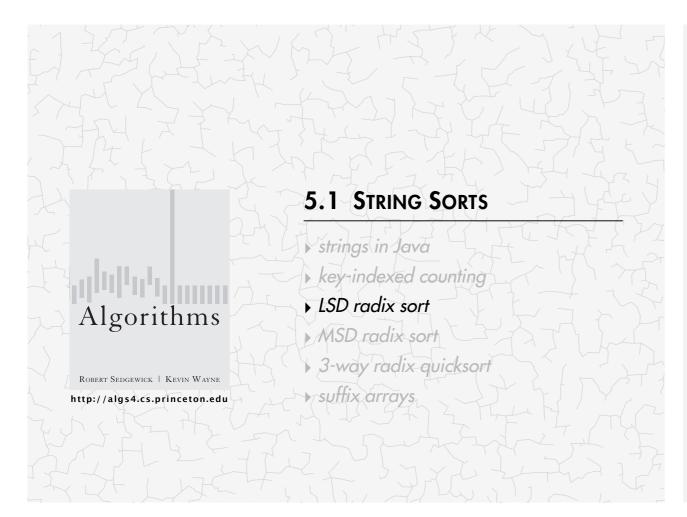


Radix sorting: quiz 1

Which of the following are properties of key-indexed counting?

- A. Time proportional to N + R.
- B. Extra space proportional to N + R.
- C. Stable.
- D. All of the above.
- E. I don't know.

a[0] Anderson	2 \	Harris	1 aux[0]
a[1] Brown	3	Martin	1 aux[1]
a[2] Davis	3 \\ X	Moore	1 aux[2]
a[3] Garcia	4	Anderson	2 aux[3]
a[4] Harris	1 \\\	Martinez	2 aux[4]
a[5] Jackson	3 \ \\	Miller	2 aux[5]
a[6] Johnson	4 \ \ \ \	Robinson	2 aux[6]
a[7] Jones	3 \	White	2 aux[7]
a[8] Martin	1/\\\	∬Brown	3 aux[8]
a[9] Martinez	2 / / /	Davis	3 aux[9]
a[10] Miller	2 // \	Jackson	3 aux[10]
a[11] Moore	1// \	Jones	3 aux[11]
a[12] Robinson	2 / /	Taylor	3 aux[12]
a[13] Smith	4	/Williams	3 aux[13]
a[14] Taylor	3	Garcia	4 aux[14]
a[15] Thomas	4 /	Johnson	4 aux[15]
a[16] Thompson	4	Smith	4 aux[16]
a[17] White	2	Thomas	4 aux[17]
a[18] Williams	3	Thompson	4 aux[18]
a[19] Wilson	4	→ Wilson	4 aux[19]



LSD string sort: correctness proof

Proposition. LSD sorts fixed-length strings in ascending order.

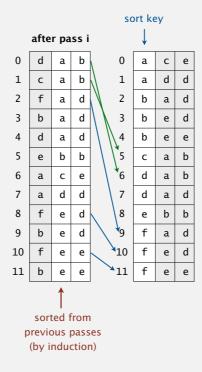
Pf. [by induction on i]

After pass i, strings are sorted by last i characters.

- If two strings differ on sort key, key-indexed sort puts them in proper relative order.
- If two strings agree on sort key,
 stability keeps them in proper relative order.

Proposition. LSD sort is stable.

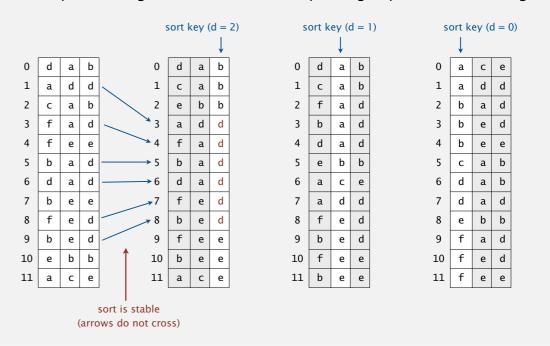
Pf. Key-indexed counting is stable.



Least-significant-digit-first string sort

LSD string (radix) sort.

- · Consider characters from right to left.
- Stably sort using d^{th} character as the key (using key-indexed counting).



LSD string sort: Java implementation

```
public class LSD
   public static void sort(String[] a, int W)
                                                                fixed-length W strings
                                                                radix R
      int R = 256;
      int N = a.length;
      String[] aux = new String[N];
                                                                do key-indexed counting
      for (int d = W-1; d >= 0; d--)
                                                                for each digit from right to left
         int[] count = new int[R+1];
         for (int i = 0; i < N; i++)
            count[a[i].charAt(d) + 1]++;
         for (int r = 0; r < R; r++)
            count[r+1] += count[r];
                                                                 key-indexed counting
         for (int i = 0; i < N; i++)
            aux[count[a[i].charAt(d)]++] = a[i];
         for (int i = 0; i < N; i++)
            a[i] = aux[i];
```

Summary of the performance of sorting algorithms

Frequency of operations.

algorithm	guarantee	random	extra space	stable?	operations on keys
insertion sort	½ N ²	½ N ²	1	V	compareTo()
mergesort	$N \lg N$	N lg N	N	V	compareTo()
quicksort	1.39 N lg N*	1.39 N lg N	c lg N		compareTo()
heapsort	2 N lg N	2 N lg N	1		compareTo()
LSD sort †	2 W(N+R)	2 W(N+R)	N + R	~	charAt()

^{*} probabilistic

Q. What if strings are not all of same length?



Radix sorting: quiz 2

Which sorting method to use to sort 1 million 32-bit integers?

- A. Insertion sort.
- B. Mergesort.
- C. Quicksort.
- D. LSD radix sort.
- E. I don't know.



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SORT ARRAY OF 128-BIT NUMBERS

Problem. Sort huge array of random 128-bit numbers.

Ex. Supercomputer sort, internet router.

Which sorting method to use?

- Insertion sort.
- · Mergesort.
- Quicksort.
- · Heapsort.
- LSD string sort.



[†] fixed-length W keys

1880 Census. Took 1500 people 7 years to manually process data.

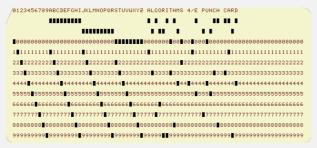


Herman Hollerith. Developed a tabulating and sorting machine.

- Use punch cards to record data (e.g., sex, age).
- Machine sorts one column at a time (into one of 12 bins).
- Typical question: how many women of age 20 to 30?



Hollerith tabulating machine and sorter



punch card (12 holes per column)

1890 Census. Finished in 1 year (and under budget)!

How to get rich sorting in 1900s?

Punch cards. [1900s to 1950s]

- Also useful for accounting, inventory, and business processes.
- · Primary medium for data entry, storage, and processing.

Hollerith's company later merged with 3 others to form Computing Tabulating Recording Corporation (CTRC); company renamed in 1924.



E R

IBM 80 Series Card Sorter (650 cards per minute)

Algorithms

ROBERT SEDGEWICK | KEVIN WAYNE

http://algs4.cs.princeton.edu

LSD string sort: a moment in history (1960s)



card punch



punched cards



card reader



mainframe



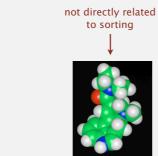
line printer

To sort a card deck

- start on right column
- put cards into hopper
- machine distributes into bins
- pick up cards (stable)
- move left one column
- continue until sorted



card sorter



Lysergic Acid Diethylamide (Lucy in the Sky with Diamonds)

5.1 STRING SORTS

strings in Java

key-indexed counting

ISD radix sort

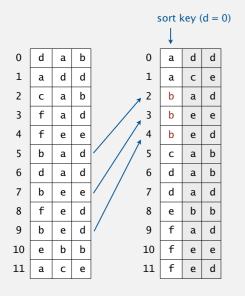
MSD radix sort

3-way radix-quicksort

suffix arrays

Reverse LSD

- · Consider characters from left to right.
- Stably sort using d^{th} character as the key (using key-indexed counting).



sort key (d = 1)						
	↓					
0	b	a	d			
1	С	a	b			
2	d	a	b			
3	d	a	d			
4	f	a	d			
5	e	b	b			
6	a	С	е			
7	a	d	d			
8	b	е	е			
9	b	е	d			
10	f	e	е			
11	f	e	d			
6 7 8 9 10	a a b b	c d e e	e d e d			

sort key (d = 2)							
	\downarrow						
0	С	a	b				
1	d	a	b				
2	e	b	b				
3	b	a	d				
4	d	a	d				
5	f	a	d				
6	a	d	d				
7	b	е	d				
8	f	е	d				
9	a	С	е				
10	b	е	е				
11	f	е	е				
not sorted!							

33

35

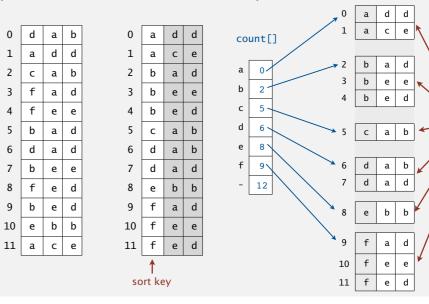
MSD string sort: example



Most-significant-digit-first string sort

MSD string (radix) sort.

- Partition array into R pieces according to first character (use key-indexed counting).
- · Recursively sort all strings that start with each character (key-indexed counts delineate subarrays to sort).

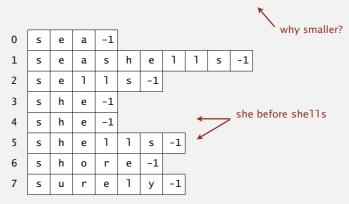


sort subarrays

recursively

Variable-length strings

Treat strings as if they had an extra char at end (smaller than any char).



```
private static int charAt(String s, int d)
   if (d < s.length()) return s.charAt(d);</pre>
   else return -1;
```

C strings. Have extra char '\0' at end \Rightarrow no extra work needed.

MSD string sort: Java implementation

```
public static void sort(String[] a) 
                                                         recycles aux[] array
                                                         but not count[] array
  aux = new String[a.length];
  sort(a, aux, 0, a.length - 1, 0);
private static void sort(String[] a, String[] aux, int lo, int hi, int d)
   if (hi <= lo) return;
  int[] count = new int[R+2];
                                                                 key-indexed counting
  for (int i = lo; i <= hi; i++)
     count[charAt(a[i], d) + 2]++;
  for (int r = 0; r < R+1; r++)
     count[r+1] += count[r];
  for (int i = lo; i <= hi; i++)
     aux[count[charAt(a[i], d) + 1]++] = a[i];
  for (int i = lo; i <= hi; i++)
     a[i] = aux[i - lo];
  for (int r = 0; r < R; r++)
                                                            sort R subarrays recursively
      sort(a, aux, lo + count[r], lo + count[r+1] - 1, d+1);
```

Cutoff to insertion sort

Solution. Cutoff to insertion sort for small subarrays.

• Insertion sort, but start at *d*th character.

```
private static void sort(String[] a, int lo, int hi, int d)
{
   for (int i = lo; i <= hi; i++)
      for (int j = i; j > lo && less(a[j], a[j-1], d); j--)
            exch(a, j, j-1);
}
```

• Implement less() so that it compares starting at *d*th character.

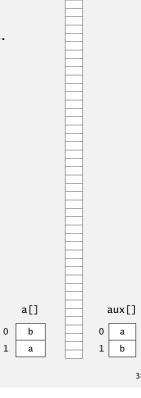
```
private static boolean less(String v, String w, int d)
{
   for (int i = d; i < Math.min(v.length(), w.length()); i++)
   {
      if (v.charAt(i) < w.charAt(i)) return true;
      if (v.charAt(i) > w.charAt(i)) return false;
   }
   return v.length() < w.length();
}</pre>
```

MSD string sort: potential for disastrous performance

Observation 1. Much too slow for small subarrays.

- Each function call needs its own count[] array.
- ASCII (256 counts): 100x slower than copy pass for N = 2.
- Unicode (65,536 counts): 32,000x slower for N = 2.

Observation 2. Huge number of small subarrays because of recursion.



count[]

MSD string sort: performance

Number of characters examined.

- MSD examines just enough characters to sort the keys.
- Number of characters examined depends on keys.
- Can be sublinear in input size!

compareTo() based sorts can also be sublinear!

Random (sublinear)	Non-random with duplicates (nearly linear)	Worst case (linear)
1E I0402	are	1DNB377
1H YL490	by	1DNB377
1R 0Z572	sea	1DNB377
2H XE734	seashells	1DNB377
2I YE230	seashells	1DNB377
2XOR846	sells	1DNB377
3CDB573	sells	1DNB377
3CVP720	she	1DNB377
3I GJ319	she	1DNB377
3KNA382	shells	1DNB377
3TAV879	shore	1DNB377
4 C QP781	surely	1DNB377
4Q GI284	the	1DNB377
4Y HV229	the	1DNB377

Characters examined by MSD string sort

Summary of the performance of sorting algorithms

Frequency of operations.

algorithm	guarantee	random	extra space	stable?	operations on keys
insertion sort	½ N ²	½ N ²	1	V	compareTo()
mergesort	$N \lg N$	$N \lg N$	N	V	compareTo()
quicksort	1.39 N lg N *	1.39 N lg N	$c \lg N^*$		compareTo()
heapsort	2 N lg N	2 N lg N	1		compareTo()
LSD sort †	2 W(N+R)	2 W(N+R)	N + R	V	charAt()
MSD sort ‡	2 W(N+R)	$N \log_R N$	N + D R 1	V	charAt()
			n-call stack depth gest prefix matcl	, h) † fi	robabilistic ixed-length W keys verage-length W keys

Engineering a radix sort (American flag sort)

Optimization 0. Cutoff to insertion sort.

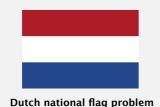
Optimization 1. Replace recursion with explicit stack.

- Push subarrays to be sorted onto stack.
- Now, one count[] array suffices.

Optimization 2. Do *R*-way partitioning in place.

- Eliminates aux[] array.
- · Sacrifices stability.





Engineering Radix Sort

Peter M. McIlroy and Keith Bostic University of California at Berkeley; and M. Douglas McIlroy AT&T Bell Laboratories

ABSTRACT: Radix sorting methods have excellent asymptotic performance on string data, for which comparison is not a unit-time operation. Attractive for use in large byte-addressable memories, these methods have nevertheless long been eclipsed by more easily programmed algorithms. Three ways to sort strings by bytes left to right—a stable list sort, a stable two-array sort, and an in-place "American flag" sort—are illustrated with practical C programs. For heavy-duty sorting, all three perform comparably, usually running at least twice as fast as a good quicksort. We recommend American flag sort for general use.

MSD string sort vs. quicksort for strings

Disadvantages of MSD string sort.

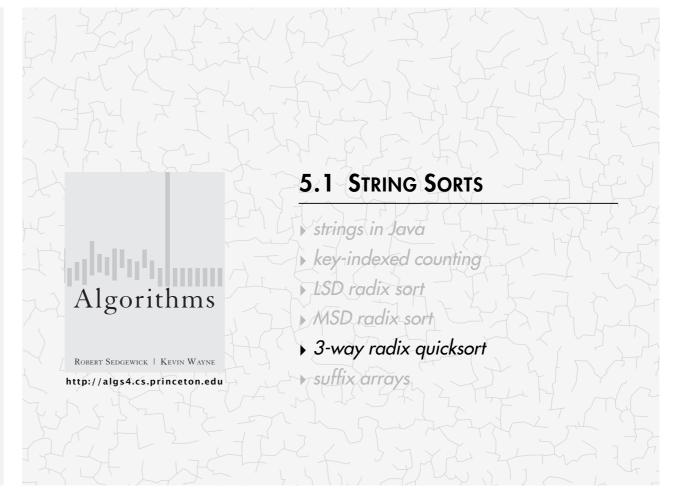
- Extra space for aux[].
- Extra space for count[].
- Inner loop has a lot of instructions.
- · Accesses memory "randomly" (cache inefficient).

Disadvantage of quicksort.

- · Linearithmic number of string compares (not linear).
- Has to rescan many characters in keys with long prefix matches.



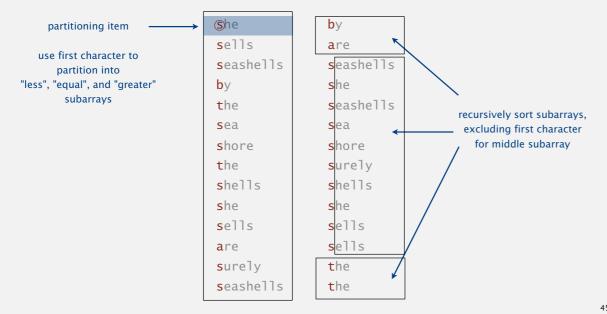
Goal. Combine advantages of MSD and quicksort.



3-way string quicksort (Bentley and Sedgewick, 1997)

Overview. Do 3-way partitioning on the d^{th} character.

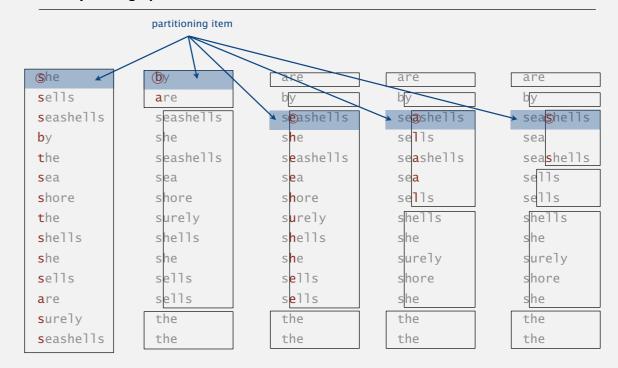
- Less overhead than R-way partitioning in MSD radix sort.
- Does not re-examine characters equal to the partitioning char. (but does re-examine characters not equal to the partitioning char)



3-way string quicksort: Java implementation

```
private static void sort(String[] a)
{ sort(a, 0, a.length - 1, 0); }
private static void sort(String[] a, int lo, int hi, int d)
   if (hi <= lo) return;</pre>
                                                        3-way partitioning
   int lt = lo, gt = hi;
                                                        (using dth character)
   int v = charAt(a[lo], d);
   int i = lo + 1;
   while (i <= gt)
                                           to handle variable-length strings
      int t = charAt(a[i], d);
              (t < v) exch(a, 1t++, i++);
      else if (t > v) exch(a, i, gt--);
      else
   sort(a, lo, lt-1, d);
   if (v \ge 0) sort(a, lt, gt, d+1); \leftarrow sort 3 subarrays recursively
   sort(a, gt+1, hi, d);
```

3-way string quicksort: trace of recursive calls



Trace of first few recursive calls for 3-way string quicksort (subarrays of size 1 not shown)

3-way string quicksort vs. standard quicksort

Standard quicksort.

- Uses $\sim 2N \ln N$ string compares on average.
- Costly for keys with long common prefixes (and this is a common case!)

3-way string (radix) quicksort.

- Uses $\sim 2 N \ln N$ character compares on average for random strings.
- Avoids re-comparing long common prefixes.

Fast Algorithms for Sorting and Searching Strings

Jon L. Bentley* Robert Sedgewick#

We present theoretical algorithms for sorting and implementations for applications in which keys are characradix sort, it is competitive with the best known C sort space-efficient than multiway trees, and support codes. The searching algorithm blends tries and binary

that is competitive with the most efficient string sorting programs known. The second program is a symbol table searching multikey data, and derive from them practical C implementation that is faster than hashing, which is commonly regarded as the fastest symbol table implementa ter strings. The sorting algorithm blends Quicksort and tion. The symbol table implementation is much more advanced searches

3-way string quicksort vs. MSD string sort

MSD string sort.

- Is cache-inefficient.
- Too much memory storing count[].
- Too much overhead reinitializing count[] and aux[].

3-way string quicksort.

- Is in-place.
- Is cache-friendly.
- · Has a short inner loop.
- · But not stable.



library of Congress call numbers

Bottom line. 3-way string quicksort is method of choice for sorting strings.

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Summary of the performance of sorting algorithms

Frequency of operations.

algorithm	guarantee	random	extra space	stable?	operations on keys
insertion sort	½ N ²	½ N ²	1	V	compareTo()
mergesort	N lg N	N lg N	N	V	compareTo()
quicksort	1.39 N lg N *	1.39 N lg N	$c \lg N^*$		compareTo()
heapsort	2 N lg N	$2 N \lg N$	1		compareTo()
LSD sort †	2 W(N+R)	2 W (N+R)	N + R	V	charAt()
MSD sort ‡	2 W(N+R)	$N \log_R N$	N + DR	V	charAt()
3-way string quicksort	1.39 <i>W N</i> lg <i>R</i> *	1.39 <i>N</i> lg <i>N</i>	$\log N + W^*$		charAt()

^{*} probabilistic

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Keyword-in-context search

Given a text of *N* characters, preprocess it to enable fast substring search (find all occurrences of query string context).

% more tale.txt it was the best of times it was the worst of times it was the age of wisdom it was the age of foolishness it was the epoch of belief it was the epoch of incredulity it was the season of light it was the season of darkness it was the spring of hope it was the winter of despair :

5.1 STRING SORTS

strings in Java

key-indexed counting

ISD radix sort

MSD radix sort

3-way radix quicksort

suffix arrays

Algorithms ROBERT SEDGEWICK | KEVIN WAYNE http://algs4.cs.princeton.edu

[†] fixed-length W keys

[‡] average-length W keys

Keyword-in-context search

Given a text of *N* characters, preprocess it to enable fast substring search (find all occurrences of query string context).

Applications. Linguistics, databases, web search, word processing,

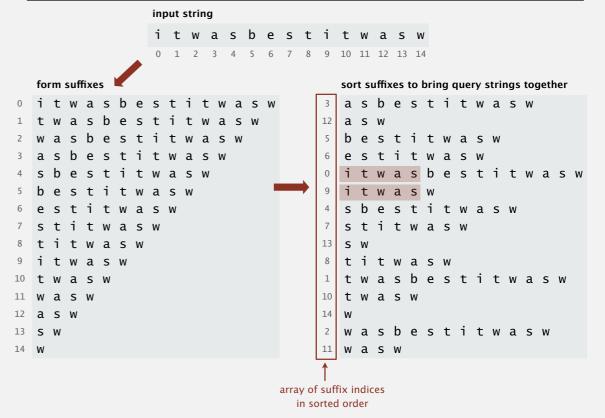
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Keyword-in-context search: suffix-sorting solution

- Preprocess: suffix sort the text.
- Query: binary search for query; scan until mismatch.

KWIC search for "search" in Tale of Two Cities

Suffix sort



War story

Q. How to efficiently form (and sort) suffixes?

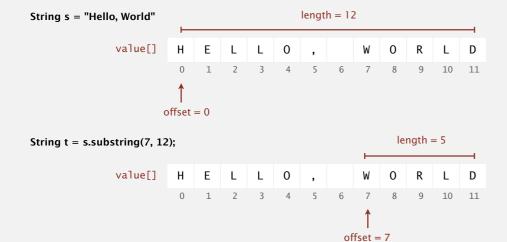
```
String[] suffixes = new String[N];
for (int i = 0; i < N; i++)
    suffixes[i] = s.substring(i, N);
Algorithms
Arrays.sort(suffixes);</pre>
```

3rd printing (2012)

input file	characters	Java 7u5	Java 7u6
amendments.txt	18 thousand	0.25 sec	2.0 sec
aesop.txt	192 thousand	1.0 sec	out of memory
mobydick.txt	1.2 million	7.6 sec	out of memory
chromosome11.txt	7.1 million	61 sec	out of memory

The String data type: Java 7u5 implementation

```
public final class String implements Comparable<String>
{
   private char[] value; // characters
   private int offset; // index of first char in array
   private int length; // length of string
   private int hash; // cache of hashCode()
   ...
```



The String data type: performance

String data type (in Java). Sequence of characters (immutable). Java 7u5. Immutable char[] array, offset, length, hash cache. Java 7u6. Immutable char[] array, hash cache.

operation	Java 7u5	Java 7u6	
length	1	1	
indexing	1	1	
substring extraction	1	N	
concatenation	M + N	M + N	
immutable?	V	V	
memory	64 + 2N	56 + 2N	

The String data type: Java 7u6 implementation

```
public final class String implements Comparable<String>
{
   private char[] value; // characters
   private int hash; // cache of hashCode()
   ...
```

String s = "Hello, World"

```
        value[]
        H
        E
        L
        L
        O
        ,
        W
        O
        R
        L
        D
```

String t = s.substring(7, 12);

```
value[] W O R L D
0 1 2 3 4
```

A Reddit exchange

I'm the author of the substring() change. As has been suggested in the analysis here there were two motivations for the change

- Reduce the size of String instances. Strings are typically 20-40% of common apps footprint.
- Avoid memory leakage caused by retained substrings holding the entire character array.



Changing this function, in a bugfix release no less, was totally irresponsible. It broke backwards compatibility for numerous applications with errors that didn't even produce a message, just freezing and timeouts... All pain, no gain. Your work was not just vain, it was thoroughly destructive, even beyond its immediate effect.



 $http://www.reddit.com/r/programming/comments/1qw73v/til_oracle_changed_the_internal_string$

Suffix sort

- Q. How to efficiently form (and sort) suffixes in Java 7u6?
- A. Define Suffix class ala Java 7u5 String.

```
public class Suffix implements Comparable<Suffix>
{
   private final String text;
   private final int offset;
   public Suffix(String text, int offset)
   {
      this.text = text;
      this.offset = offset;
   }
   public int length() { return text.length() - offset; }
   public char charAt(int i) { return text.charAt(offset + i); }
   public int compareTo(Suffix that) { /* see textbook */ }
}
```



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Lessons learned

Lesson 1. Put performance guarantees in API.

Lesson 2. If API has no performance guarantees, don't rely upon any!

Corollary. May want to avoid String data type for huge strings.

- Are you sure charAt() and length() take constant time?
- If lots of calls to charAt(), overhead for function calls is large.
- If lots of small strings, memory overhead of String is large.

Ex. Our optimized algorithm for suffix arrays is 5x faster and uses 32x less memory than our original solution in Java 7u5!

Suffix sort

- Q. How to efficiently form (and sort) suffixes in Java 7u6?
- A. Define Suffix class ala Java 7u5 String.

```
String[] suffixes = new String[N];
for (int i = 0; i < N; i++)
    suffixes[i] = new Suffix(s, i);
Arrays.sort(suffixes);</pre>
```



4th printing (2013)

Radix sorting: quiz 3

What is worst-case running time of our suffix array algorithm?

- A. Quadratic.
- B. Linearithmic.
- C. Linear.
- D. None of the above.
- E. I don't know.

```
suffixes
```

•

Radix sorting: quiz 4

What is the worst-case complexity of the suffix array problem?

- A. Quadratic.
- B. Linearithmic.
- C. Linear.
- D. None of the above.
- E. I don't know.

"has no practical virtue... but a historic monument in the area of string processing."

LINEAR PATTERN MATCHING ALGORITHMS

Peter Weine

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Abstract

In 1970, Knuth, Pratt, and Morris [1] showed how to do basic pattern matching in linear time. Related problems, such as those discussed in [4], have previously been solved by efficient but sub-optimal algorithms. In this paper, we introduce an interesting data structure called a bi-tree. A linear time algorithm for obtaining a compacted version of a bi-tree associated with a given string is presented. With this construction as the basic tool, we indicate how to solve several pattern matching problems, including some from [4], in linear time.

elegant N log N algorithm (see video)

Suffix arrays: A new method for on-line string searches

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> May 1989 Revised August 1991

Abstract

A new and conceptually simple data structure, called a suffix array, for on-line string searches is introduced in this paper. Constructing and querying suffix arrays is reduced to a sort and search paradiac employs noved algorithms. The mind avolatage of suffix arrays over suffix teres is that, in practice, they use three to five times less space. From a complexity standpoint, suffix arrays permit on-line string searches of the type, "Is W a substring of A?" to be answered in time $O(P + \log N)$, where P is the length of W and N is the length of A, which is competitive with (and in some cases slightly better than) suffix trees. The only drawback is that in those instances where the underlying alphabet is finite and small, suffix trees can be constructed in O(N) time in the worst case, versus O(N) log N) time for suffix arrays. However, we give an augmented algorithm that, regardless of the alphabet size, constructs suffix arrays in O(N) expected time, albeit with lesser space efficiency. We believe that suffix arrays will prove to be batter in movince to but suffix tree to many ambications.

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String sorting summary

We can develop linear-time sorts.

- · Key compares not necessary for string keys.
- · Use characters as index in an array.

We can develop sublinear-time sorts.

- Input size is amount of data in keys (not number of keys).
- · Not all of the data has to be examined.

3-way string quicksort is asymptotically optimal.

• 1.39 N lg N chars for random data.

Long strings are rarely random in practice.

- · Goal is often to learn the structure!
- · May need specialized algorithms.

Suffix arrays: practice

Applications. Bioinformatics, information retrieval, data compression, ...

Many ingenious algorithms.

- · Memory footprint very important.
- · State-of-the art still changing.

year	algorithm	worst case	memory	
1990	Manber-Myers	$N \log N$	8 N	
1999	Larsson-Sadakane	$N \log N$	8 N	
2003	Kärkkäinen-Sanders	N	13 N	
2003	Ko-Aluru	N	10 N	
2008	divsufsort2	$N \log N$	5 N	good choices
2010	sais	N	6 N	(Yuta Mori)

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