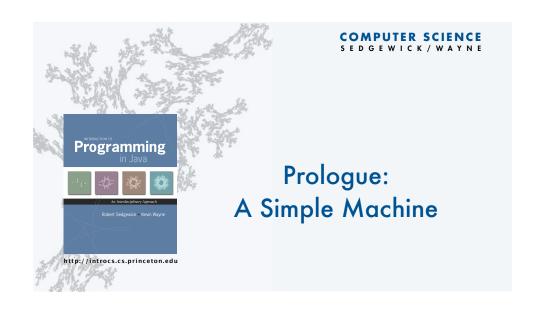
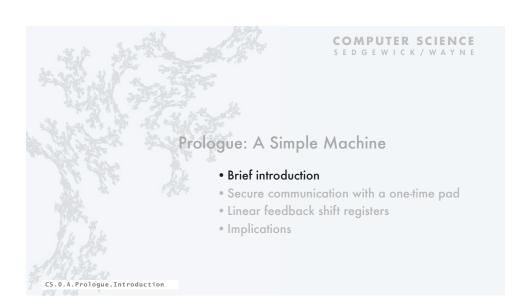
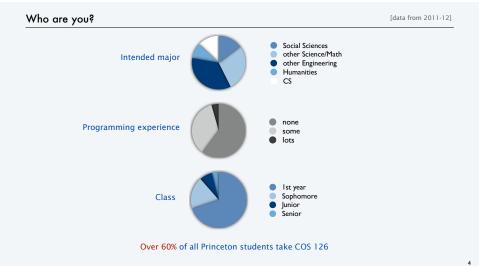
Computer Science 126

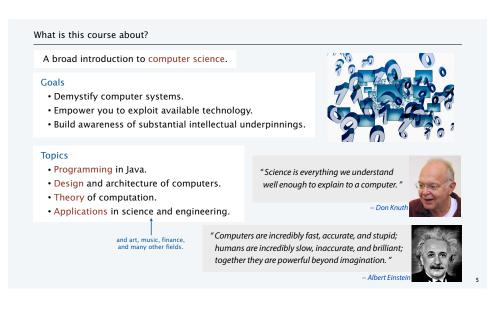
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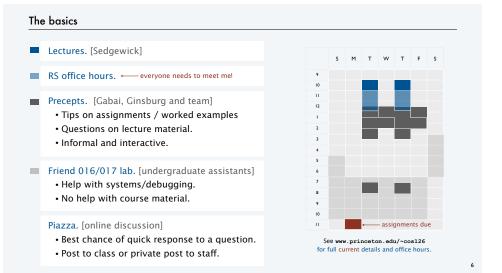
Robert Sedgewick

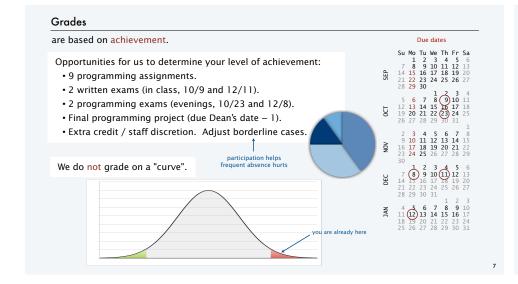


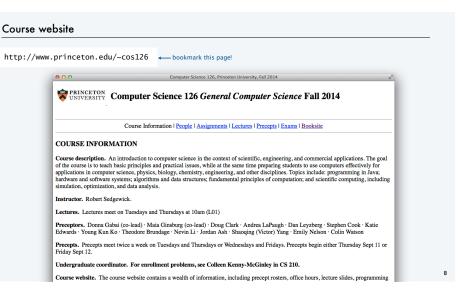












Textbook and Booksite



Textbook.

- Full introduction to course material.
- Developed for this course.
- · For use while learning and studying.

Booksite.

- Summary of content.
- · Code, exercises, examples.
- · Supplementary material.
- NOT the textbook.
- (also not the course web page).
- · For use while online.



Programming assignments

are an essential part of the experience in learning CS.

Desiderata

- · Address an important scientific or commercial problem.
- Illustrate the importance of a fundamental CS concept.
- You solve the problem from scratch on your own computer!



What's Ahead?

Coming events

- Lecture 2. Basic programming concepts.
- · Precept 1. Meets today/tomorrow.
- Not registered? Go to any precept now; officially register ASAP.
- Change precepts? Use SCORE. 👡

see Colleen Kenny-McGinley in CS 210 if the only precept you can attend is closed



Assignment 0 due Monday 11:59PM



Things to do before attempting assignment

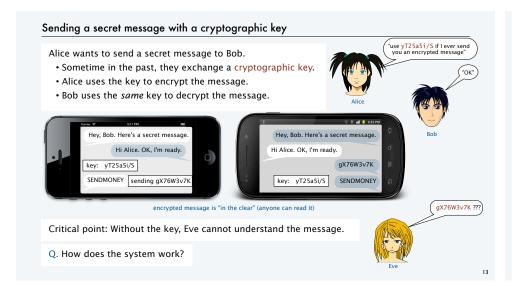
- Read Sections 1.1 and 1.2 in textbook.
- · Read assignment carefully.
- Install introcs software as per instructions.
- · Do a few exercises.
- · Lots of help available, don't be bashful.

 $\verb|http://introcs.cs.princeton.edu/assignments.php|\\$

END OF ADMINISTRATIVE STUFF

1. Prologue: A Simple Machine

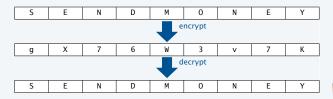
• Brief introduction
• Secure communication with a one-time pad
• Linear feedback shift registers
• Implications



Encrypt/decrypt methods

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Goal. Design a method to encrypt and decrypt data.



Example 1. Enigma encryption machine [German code, WWII]

- Broken by Turing bombe (one of the first uses of a computer).
- Broken code helped win Battle of Atlantic by providing U-boat locations.

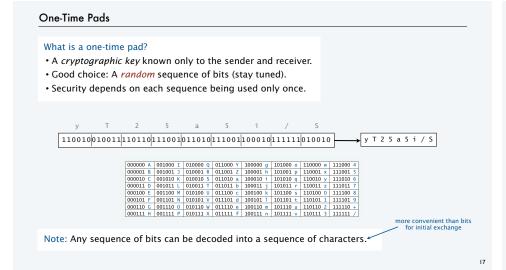
Example 2. One-time pad [details to follow]

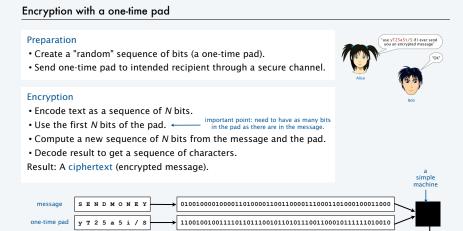
Example 3. Linear feedback shift register [later this lecture]

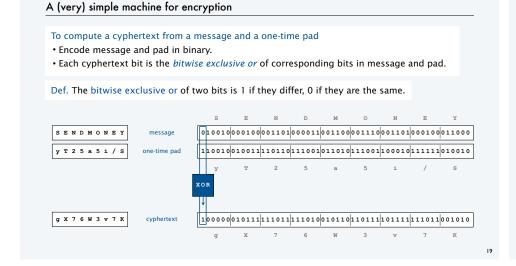
A digital world A bit is a basic unit of information. • Two possible values (0 or 1). • Easy to represent in the physical world (on or off). In modern computing and communications systems, we represent everything as a sequence of bits. • Text [details to follow in this lecture] • Numbers • Sound [details to follow in this course] • Pictures [details to follow in this course] • Programs [profound implications, stay tuned].

Bottom line. If we can send and receive bits, we can send and receive anything.

Encoding text as a sequence of bits Base64 encoding of character strings bits symbols · A simple method for representing text. 64 Base64 • 64 different symbols allowed: A-Z, a-z, 0-9, +, /. · 6 bits to represent each symbol. 65,536+ 16 Unicode · ASCII and Unicode methods used on your computer are similar. 000000 A | 001000 I | 010000 Q | 011000 Y | 100000 g | 101000 o | 110000 w | 111000 4 000001 B 001001 J 010001 R 011001 Z 100001 h 101001 p 110001 x 111001 5 000010 C 001010 K 010010 S 011010 a 100010 101010 q 110010 y 000011 D | 001011 L | 010011 T | 011011 b | 100011 j 101011 r 110011 z | 111011 7 000100 E 001100 M 010100 U 011100 c 100100 101100 110100 0 111100 8 000101 F 001101 N 010101 V 011101 d 100101 7 101101 t 110101 1 111101 9 |000110 G |001110 0 |010110 W |011110 e |100110 m |101110 u |110110 2 |111110 + 000111 H 001111 P 010111 X 011111 f 100111 n Example: SENDMONEY 010010|000100|001101|000011|001100|001110|001101|000100|011000





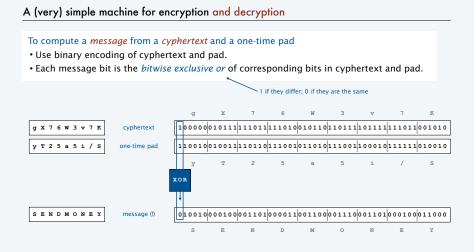


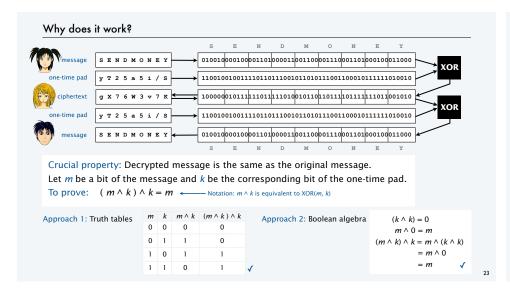
Self-assessment on bitwise XOR encryption

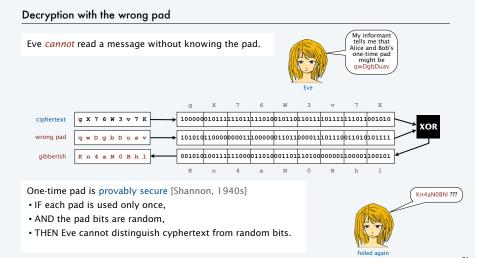
Q. Encrypt the message E A S Y with the pad 0 1 2 3.

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Eve's problem with one-time pads Eve has a computer. Why not try all possibilities? Problem

- 54 bits, so there are 254 possible pad values.
- Suppose Eve could check a million values per second.
- It would still take 570+ years to check all possibilities.

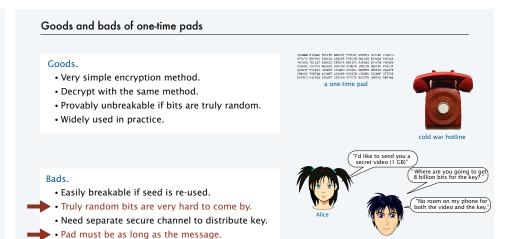
Much worse problem

- There are also 254 possible messages.
- If Eve were to check all the pads, she'd see all the messages.
- · No way to distinguish the real one from any other.

One-time pad is provably secure.

pad value	message?
AAAAAAAA	gX76W3v7K
AAAAAAAAB	gX76W3v7L
AAAAAAAAC	gX76W3v7I
qwDgbDuav	Kn4aN0Bh1
tTtpWk+1E	NEWTATT00
yT25a5i/S	SENDMONEY
//////+	fo7FpIQE0
////////	fo7FpIQE1

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Random bits are not so easy to find

You might look on the internet.

The randomness comes from atmospheric noise

RANDOMONG - Integer Conservator

RANDOMONG - Integer Conservator

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This for allows you to generate random integers (he randomness comes from atmospheric noise)

True Randomy Number Service

This form allows you to generate random integers (he randomness comes from atmospheric noise)

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This form allows you to generate random integers (maximum 10,000).

Each integer should have a value between (in and [in (both inclusive; limits ±1,000,000,000).

Format in [in column(c).

Part 2: Go!

Be patient! It may take a little while to generate your numbers...

Next: Creating a (long) sequence of "pseudo-random" bits from a (short) key.



A pseudo-random number generator

is a *deterministic* machine that produces a long sequence of *pseudo random* bits.

Examples

Enigma.

Linear feedback shift register (next). Blum-Blum-Shub generator.

[an early application of computing] [research still ongoing]







"Anyone who considers arithmetical methods of producing random digits is, of course, in a state of sin."



A pseudo-random number generator

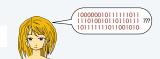
is a *deterministic* machine that produces a long sequence of *pseudo random* bits.

Deterministic: Given the current state of the machine, we know the next bit.

An absolute requirement: Alice and Bob need the same sequence.

Random: We never know the next bit.

Pseudo-random: The sequence of bits appears to be random.



Appears to be random??

· A profound and elusive concept.

Ex. 1: No long repeats
Ex. 2: About the same number of 0s and 1s
Ex. 3: About the same number of 00s, 01s, 10s, and 11s.

• For this lecture: "Has enough properties of a random sequence that Eve can't tell the difference"

Which of these sequences appear to be random?

but # of 00s 01s 10s and 11s are about equa

key for Alice and Bob

√ ciphertext for SENDMONEY

generated by coin flips

typed arbitrarily (no long segs of 0s or 1s)

but # of 0s and 1s

are about equal

SENDMONEY

Note: Any one of them could be random!

Linear feedback shift register

Terminology

• Bit: 0 or 1.

· Cell: storage element that holds one bit.

• Register: sequence of cells.

· Seed: initial sequence of bits.

• Feedback: Compute XOR of two bits and put result at right.

• Shift register: when clock ticks, bits propagate one position to left.

An [11, 9] LFSR



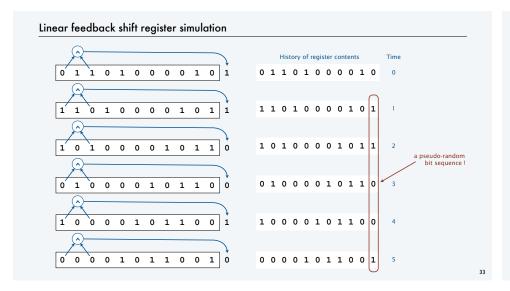
More terminology

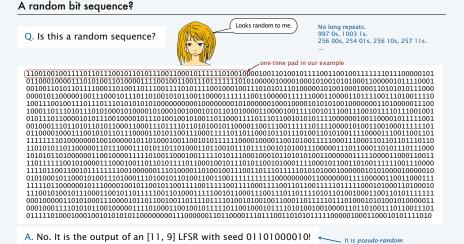
Tap: Bit positions used for XOR (one must be leftmost). ←

-Numbered from right, starting at 1.

• [N, k] LFSR: N-bit register with taps at N and k.

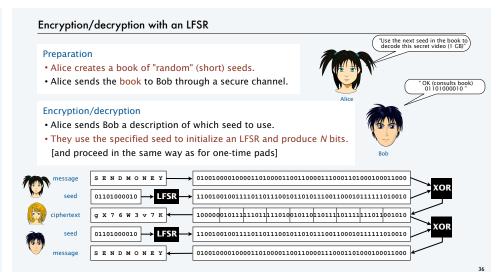
- Not all values of k give desired effect (stay tuned).







Q. Give first 10 steps of [5,4] LFSR with initial fill 00001.



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Eve's opportunity with LFSR encryption

Eve has computers. Why not try all possible seeds?

- · Seeds are short, messages are long.
- All seeds give a tiny fraction of all messages.
- Extremely likely that all but real seed will produce gibberish.

Eve

Good news (for Eve): This approach can work.

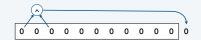
- Ex: 11-bit register implies 2047 possibilities.
- Extremely likely that only one of those is not gibberish.
- After this course, *you* could write a program to check whether any of the 2047 messages have words in the dictionary.

Bad news (for Eve): It is easy for Alice and Bob to use a much longer LFSR.

Key properties of LFSRs

Property 1.

- · Don't use all 0s as a seed!
- Fill of all 0s will not otherwise occur.



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Key properties of LFSRs

Property 1.

- · Don't use all 0s as a seed!
- Fill of all 0s will not otherwise occur.

Property 2. Bitstream must eventually cycle.

- $2^N 1$ nonzero fills in an N-bit register.
- Future output completely determined by current fill.

Ex. [4,3] LFSR

Key properties of LFSRs

Property 1.

- · Don't use all 0s as a seed!
- Fill of all 0s will not otherwise occur.

Property 2. Bitstream must eventually cycle.

- $2^N 1$ nonzero fills in an N-bit register.
- Future output completely determined by current fill.

Property 3. Cycle length in an N-bit register is at most $2^{N}-1$.

- Could be smaller; cycle length depends on tap positions.
- Need theory of finite groups to know good tap positions.

40

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Bottom line.

- [11, 9] register generates 2047 bits before repeating.
- [63, 62] register generates 2⁶³ -1 bits before repeating. Definitely preferable: small cost, huge payoff.

gX76W3v7K ??? Without the seed. Eve cannot read the message. $(30, 2^{30})$ Exponential growth dwarfs technological improvements Eve has computers. Why not try all possible seeds? · Seeds are short, messages are long. · All seeds give a tiny fraction of all messages. · Extremely likely that all but real seed will produce gibberish. Bad news (for Eve): There are still way too many possibilities. • Ex: 63-bit register implies $2^{63} - 1$ possibilities. • If Eve could check 1 million seeds per second, it would take her 2923 centuries to try them all! Bad news (for Alice and Bob): LFSR output is not random. experts have cracked LFSRs

Eve's problem with LFSR encryption

Goods and bads of LFSRs

Goods.

- Very simple encryption method.
- · Decrypt with the same method.
- Scalable: 20 cells for 1 million bits; 30 cells for 1 billion bits.
- Widely used in practice. [Example: military cryptosystems.]



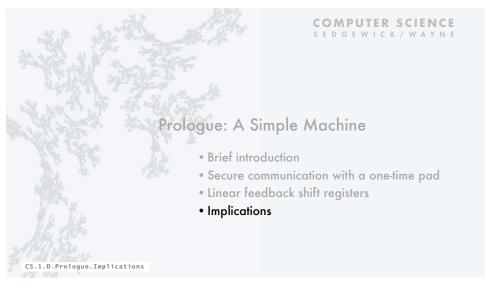
Bads.

- · Easily breakable if seed is re-used.
- Still need secure key distribution.
- · Experts can crack LFSR encryption.

Example.

- · CSS encryption widely used for DVDs.
- · Widely available DeCSS breaks it!





LFSRs and general-purpose computers





component	LFSR
control	start, stop, load
clock	
memory	12 bits
input	12 bits

computation

output

shift, XOR

pseudo-random bit

sequence

Important similarities.

- · Both are built from simple components.
- · Both scale to handle huge problems.
- Both require careful study to use effectively.

Critical differences: Operations, input. ← but the simplest computers differ only slightly from LFSRs!

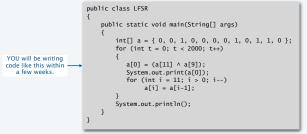
- General purpose computer can simulate any abstract machine.
- All general purpose computers have equivalent power (!) [stay tuned].

A Profound Idea

Programming. We can write a Java program to simulate the operation of any abstract machine.

- · Basis for theoretical understanding of computation.
- Basis for bootstrapping real machines into existence.

Stay tuned (we cover these sorts of issues in this course).





Note: You will write and apply an LFSR simulator in Assignment 5.

Profound questions

O. What is a random number?

LFSRs do not produce random numbers.

- It is not obvious how to distinguish the bits LFSRs produce from random,
- · BUT experts have figured out how to do so.
- Q. Are random processes found in nature?
- Motion of cosmic rays or subatomic particles?
- Mutations in DNA?





Q. Is the natural world a (not-so-simple) deterministic machine??





computer

same

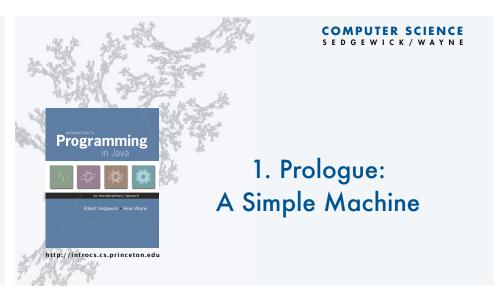
same

billions of bits

bit sequence

+-*/...

any computable



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