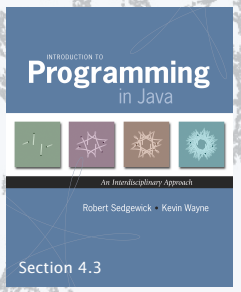

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14. Stacks and Queues

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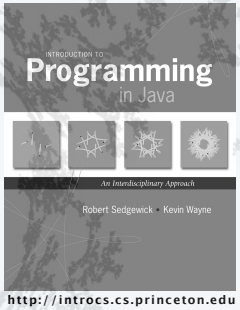

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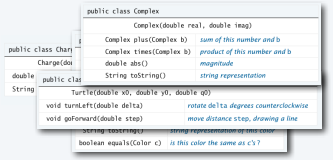
14. Stacks and Queues

- **APIs**
- Clients
- Strawman implementation
- Linked lists
- Implementations

Data types and data structures

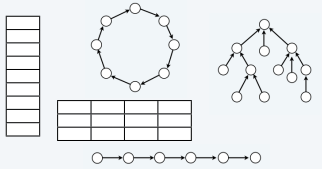
Data types

- Set of values.
- Set of operations on those values.
- Some are built in to Java: `int`, `double`, `String`, . . .
- Most are not: `Complex`, `Picture`, `Charge`, . . .



Data structures

- Represent data.
- Represent relationships among data.
- Some are built in to Java: 1D arrays, 2D arrays, . . .
- Most are not: linked list, circular list, tree, . . .



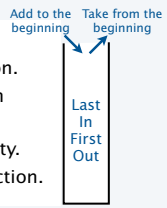
Design challenge for every data type: Which data structure to use?

- Resource 1: How much memory is needed?
- Resource 2: How much time do data-type methods use?

Stack and Queue APIs

A collection is an ADT whose values are a multiset of items, all of the same type.

Two fundamental collection ADTs differ in just a detail of the specification of their operations.



Stack operations

- Add an item to the collection.
- Remove and return the item *most* recently added (LIFO).
- Test if the collection is empty.
- Return the size of the collection.

Queue operations

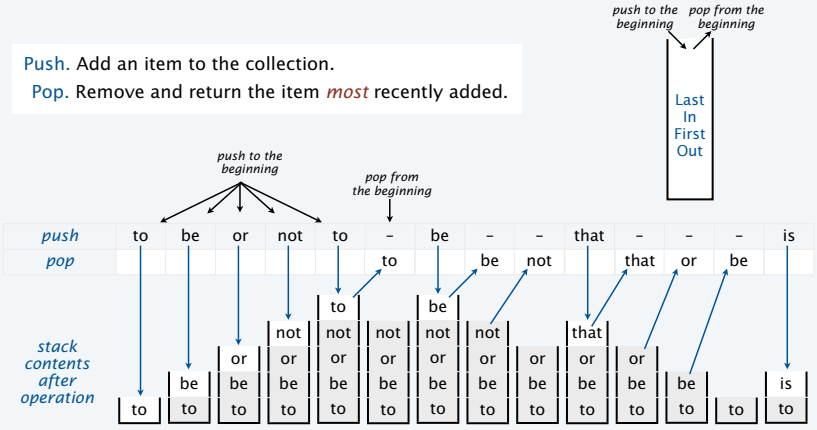
- Add an item to the collection.
- Remove and return the item *least* recently added (FIFO).
- Test if the collection is empty.
- Return the size of the collection.

Stacks and queues both arise naturally in countless applications.

A key characteristic. No limit on the size of the collection.

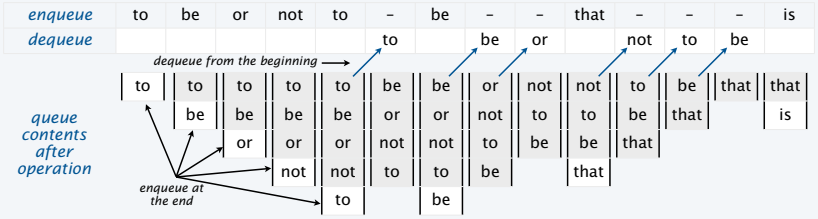
Example of stack operations

Push. Add an item to the collection.
Pop. Remove and return the item *most* recently added.



Example of queue operations

Enqueue. Add an item to the collection.
Dequeue. Remove and return the item *least* recently added.



Parameterized data types

Goal. Simple, safe, and clear client code for collections of any type of data.

Java approach: Parameterized data types (generics)

- Use placeholder type name in definition.
- Substitute concrete type for placeholder in clients. ← stay tuned for examples

Stack API

public class Stack<Item>	
Stack<Item>()	*create a stack of objects, all of type* Item
void push(Item item)	*add* item *to stack*
Item pop()	*remove and return the item most recently pushed*
boolean isEmpty()	*is the stack empty?*
int size()	*# of objects on the stack*

Queue API

public class Queue<Item>	
Queue<Item>()	*create a queue of objects, all of type* Item
void enqueue(Item item)	*add* item *to queue*
Item dequeue()	*remove and return the item least recently enqueued*
boolean isEmpty()	*is the queue empty?*
int size()	*# of objects on the queue*

Performance specifications

Challenge. Provide guarantees on performance.

Goal. Simple, safe, clear, and *efficient* client code.

Typically required for client code to be *scalable*

Performance specifications

- All operations are constant-time.
- Memory use is proportional to the size of the collection, when it is nonempty.
- No limits within the code on the collection size.

Java. Any implementation of the API implements the stack/queue abstractions.

RS+KW. Implementations that do not meet performance specs *do not* implement the abstractions.

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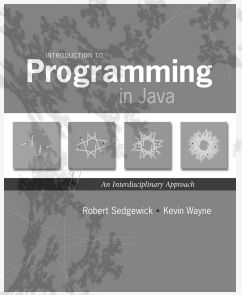

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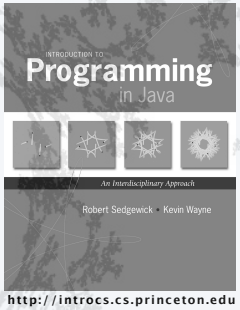

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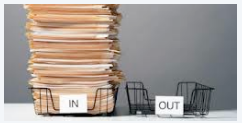
Stack and queue applications

Queues

- First-come-first-served resource allocation.
- Asynchronous data transfer (StdIn, StdOut).
- Dispensing requests on a shared resource (printer, processor).
- Simulations of the real world (guitar string, traffic analysis, ...)

Stacks

- Last-come-first-served processes (browser, e-mail).
- Function calls in programming languages.
- Basic mechanism in interpreters, compilers.
- . . .



Queue client example: Read all strings from StdIn into an array

Challenge
- Can't store strings in array before creating the array.
- Can't create the array without knowing how many strings are in the input stream.
- Can't know how many strings are in the input stream without reading them all.

Solution: Use a Queue<String>.

```
public class QEx
{
    public static String[] readAllStrings()
    { // See next slide. }

    public static void main(String[] args)
    {
        String[] words = readAllStrings();
        for (int i = 0; i < words.length; i++)
            StdOut.println(words[i]);
    }
}
```

Note: StdIn has this functionality

```
% more moby.txt
moby dick
herman melville
call me ishmael some years ago never
mind how long precisely having
little or no money
...
```

```
% java QEx < moby.txt
moby
dick
herman
melville
call
me
ishmael
some
years
...
```


Queue client example: Read all strings from StdIn into an array

Solution: Use a Queue<String>.
- Store strings in the queue.
- Get the size when all have been read from StdIn.
- Create an array of that size.
- Copy the strings into the array.

```
public class QEx
{
    public static String[] readAllStrings()
    {
        Queue<String> q = new Queue<String>();
        while (!StdIn.isEmpty())
            q.enqueue(StdIn.readString());
        int N = q.size();
        String[] words = new String[N];
        for (int i = 0; i < N; i++)
            words[i] = q.dequeue();
        return words;
    }
    public static void main(String[] args)
    {
        String[] words = readAllStrings();
        for (int i = 0; i < words.length; i++)
            StdOut.println(words[i]);
    }
}
```


Stack example: "Back" button in a browser

Typical scenario
- Visit a page.
- Click a link to another page.
- Click a link to another page.
- Click a link to another page.
- Click "back" button.
- Click "back" button.
- Click "back" button.

http://introcs.cs.princeton.edu/java/43stack/

http://introcs.cs.princeton.edu/java/40algorithms/

http://introcs.cs.princeton.edu/java/home/

Autoboxing

Challenge. Use a *primitive* type in a parameterized ADT.

Wrapper types
- Each primitive type has a wrapper reference type.
- Wrapper type has larger set of operations than primitive type. Example: `Integer.parseInt()`.
- Values of wrapper types are objects.
- Wrapper type can be used in a parameterized ADT.

primitive type	*wrapper type*
`int`	`Integer`
`long`	`Long`
`double`	`Double`
`boolean`	`Boolean`

Autoboxing. Automatic cast from primitive type to wrapper type.

Auto-unboxing. Automatic cast from wrapper type to primitive type.

Simple client code (no casts) →

```
Stack<Integer> stack = new Stack<Integer>();
stack.push(17);        // Autobox    (int -> Integer)
int a = stack.pop();   // Auto-unbox (Integer -> int)
```

Stack client example: Postfix expression evaluation

Infix. Standard way of writing arithmetic expressions, using parentheses for precedence.

Example. `( 1 + ( ( 2 + 3 ) * ( 4 * 5 ) ) ) = ( 1 + ( 5 * 20 ) ) = 101`

Jan Łukasiewicz
1878–1956

Postfix. Write operator *after* operands (instead of in between them).

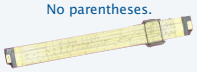
Example. `1 2 3 + 4 5 * * +` ← also called "reverse Polish" notation (RPN)

Remarkable fact. No parentheses are needed!

There is only one way to parenthesize a postfix expression.

```
1 2 3 + 4 5 * * +
1 ( 2 + 3 ) 4 5 * * +      <- find first operator, convert to infix, enclose in ()
1 ( ( 2 + 3 ) * ( 4 * 5 ) ) +
( 1 + ( ( 2 + 3 ) * ( 4 * 5 ) ) )      <- iterate, treating subexpressions in parentheses as atomic
```

HP-35 (1972)
First handheld calculator.
"Enter" means "push".
No parentheses.

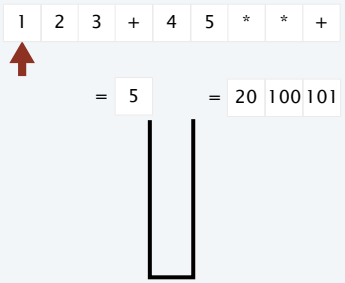


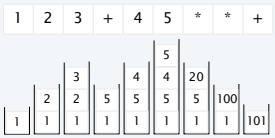
Made slide rule obsolete (!)

Next. With a stack, postfix expressions are easy to evaluate.

Postfix arithmetic expression evaluation

Algorithm
- While input stream is nonempty, read a token.
- Value: Push onto the stack.
- Operator: Pop operand(s), apply operator, push the result.





Stack client example: Postfix expression evaluation

```
public class Postfix
{
   public static void main(String[] args)
   {
      Stack<Double> stack = new Stack<Double>();
      while (!StdIn.isEmpty())
      {
         String token = StdIn.readString();
         if (token.equals("*"))
             stack.push(stack.pop() * stack.pop());
         else if (token.equals("+"))
             stack.push(stack.pop() + stack.pop());
         else if (token.equals("-"))
             stack.push(- stack.pop() + stack.pop());
         else if (token.equals("/"))
             stack.push((1.0/stack.pop()) * stack.pop());
         else if (token.equals("sqrt"))
             stack.push(Math.sqrt(stack.pop()));
         else
             stack.push(Double.parseDouble(token));
      }
      StdOut.println(stack.pop());
   }
}
```

```
% java Postfix
1 2 3 + 4 5 * * +
101
```

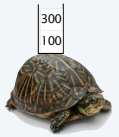
```
% java Postfix
1 5 sqrt + 2 /
1.618033988749895
```

$\frac{1+\sqrt{5}}{2}$

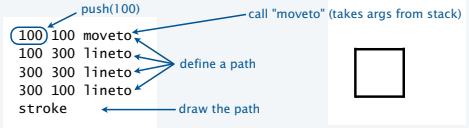
Perspective
- Easy to add operators of all sorts.
- Can do infix with two stacks (see text).
- Could output TOY program.
- Indicative of how Java compiler works.

Real-world stack application: PostScript

PostScript (Warnock-Geschke, 1980s): A turtle with a stack.
- Postfix program code (push literals; functions pop arguments).
- Add commands to drive virtual graphics machine.
- Add loops, conditionals, functions, types, fonts, strings....



PostScript code



A simple virtual machine, but not a toy
- Easy to specify published page.
- Easy to implement on various specific printers.
- Revolutionized world of publishing.

Another stack machine: The JVM (Java Virtual Machine)!

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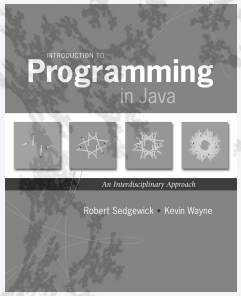

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14. Stacks and Queues

- APIs
- **Clients**
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- Linked lists
- Implementations

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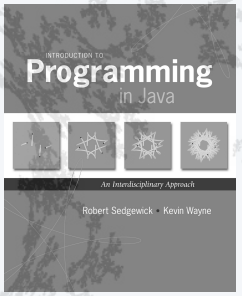

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Strawman ADT for pushdown stacks

Warmup: simplify the ADT

- Implement only for items of type `String`.
- Have client provide a stack *capacity* in the constructor.

values

Strawman API

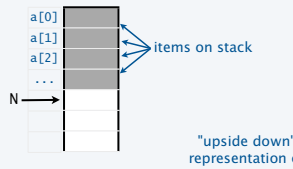
public class StrawStack	
`StrawStack(int max)`	*create a stack of capacity* `max`
`void push(String item)`	*add* `item` *to stack*
`String pop()`	*return the string most recently pushed*
`boolean isEmpty()`	*is the stack empty?*
`int size()`	*number of strings on the stack*

Rationale. Allows us to represent the collection with an array of strings.

Strawman implementation: Instance variables and constructor

Data structure choice. Use an array to hold the collection.

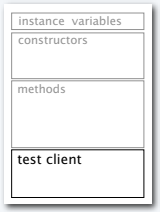
```
public class StrawStack
{
   private String[] a;
   private int N = 0;

   public StrawStack(int max)
   {  a = new String[max];  }
...
}
```



"upside down" representation of

Strawman stack implementation: Test client

```
public static void main(String[] args)
{
   int max = Integer.parseInt(args[0]);
   StrawStack stack = new StrawStack(max);
   while (!StdIn.isEmpty())
   {
      String item = StdIn.readString();
      if (item.equals("-"))
         stack.push(item);
      else
         StdOut.print(stack.pop());
   }
   StdOut.println();
}
```



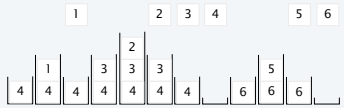

```
% more tobe.txt
to be or not to - be - - that - - - is

% java StrawStack 20 < tobe.txt
to be not that or be
```

What we *expect*, once the implementation is done.

TEQ 1 on stacks

Q. Can we always insert pop() commands to make items come out in sorted order?

Example 1.	6	5	4	3	2	1	-	-	-	-	-	-
Example 2.	1	-	2	-	3	-	4	-	5	-	6	-
Example 3.	4	1	-	3	2	-	-	-	6	5	-	-



TEQ 1 on stacks

Q. Can we always insert pop() commands to make items come out in sorted order?

Example 1.	6	5	4	3	2	1	-	-	-	-	-	-
Example 2.	1	-	2	-	3	-	4	-	5	-	6	-
Example 3.	4	1	-	3	2	-	-	-	6	5	-	-

A. No. Example. 5 6

no way for 5 to be popped before 6

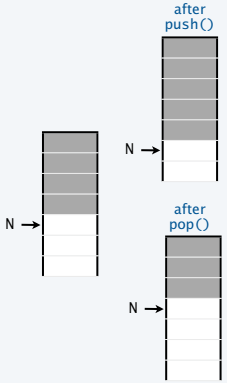
Note. In a *queue*, they always come out in the order they came in.

Strawman implementation: Methods

Methods define data-type operations (implement APIs).

```
public class StrawStack
{
...
   public boolean isEmpty()
   {  return (N == 0); }

   public void push(Object item)
   {  a[N++] = item;  }

   public String pop()
   {  return a[--N];  }

   public int size()
   {  return N;  }
...
}
```

all constant-time one-liners!



Strawman pushdown stack implementation

```
public class StrawStack
{
   private String[] a;
   private int N = 0;

   public StrawStack(int max)
   {  a = new String[max];  }

   public boolean isEmpty()
   {  return (N == 0);   }
   public void push(String item)
   {  a[N++] = item;  }
   public String pop()
   {  return a[--N];  }
   public int size()
   {  return N;  }

   public static void main(String[] args)
   {
      int max = Integer.parseInt(args[0]);
      StrawStack stack = new StrawStack(max);
      while (!StdIn.isEmpty())
      {
         String item = StdIn.readString();
         if (item.compareTo("-") != 0)
            stack.push(item);
         else
            StdOut.print(stack.pop());
      }
      StdOut.println();
   }
}
```

instance variables

constructor

methods

test client

```
% more tobe.txt
to be or not to - be - - that - - - is

% java StrawStack 20 < tobe.txt
to be not that or be
```


Trace of strawman stack implementation (array representation)

push	to	be	or	not	to	-	be	-	-	that	-	-	-	is
pop						to		be	not		that	or	be	

stack contents after operation

a[0]	to	to	to	to	to	to	to	to	to	to	to	to	to	to	to
a[1]		be	be	be	be	be	be	be	be	be	be	be	be	be	is
a[2]	↑		or	or	or	or	or	or	or	or	or	or	or	or	or
a[3]	N			not	not	not	not	not	not	not	that	that	that	that	that
a[4]					to	to	be	be	be	be	be	be	be	be	be
a[5]															
a[6]															
a[7]															
a[8]															
a[9]															
a[10]															
a[11]															
a[12]															
a[13]															
a[14]															
a[15]															
a[16]															
a[17]															
a[18]															
a[19]															

Significant wasted space when stack size is not near the capacity (typical).

Benchmarking the strawman stack implementation

StrawStack implements a *fixed-capacity collection that behaves like a stack* if the data fits.

It does *not* implement the stack API or meet the performance specifications.

StrawStack requires client to provide capacity

Stack API	public class Stack<Item>
	Stack<Item>() ✘	*create a stack of objects, all of type* Item
	void push(Item item)	*add* item *to stack*
StrawStack works only for strings →	✘ Item pop()	*remove and return the item most recently pushed*
	boolean isEmpty()	*is the stack empty?*
	int size()	*# of objects on the stack*

Performance specifications

- All operations are constant-time. ✓
- Memory use is proportional to the size of the collection, when it is nonempty. ✘
- No limits within the code on the collection size. ✘

Nice try, but need a new *data structure.*

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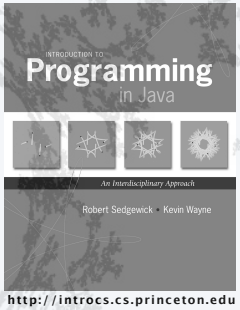

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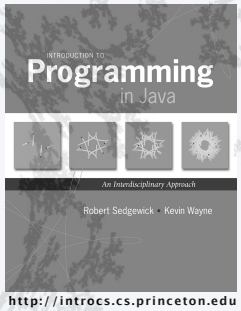

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14. Stacks and Queues

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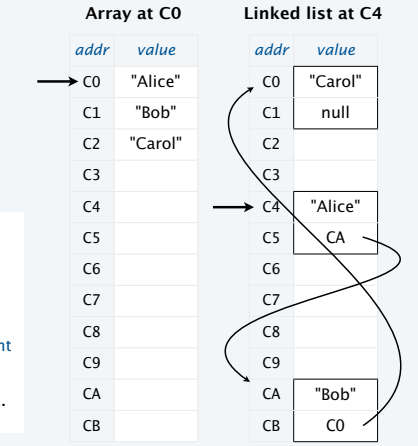
Data structures: sequential vs. linked

Sequential data structure

- Put objects next to one another.
- TOY: consecutive memory cells.
- Java: array of objects.
- Fixed size, arbitrary access. ⟵ *i*th element

Linked data structure

- Associate with each object a link to another one.
- TOY: link is memory address of next object.
- Java: link is reference to next object.
- Variable size, sequential access. ⟵ *next* element
- Overlooked by novice programmers.
- Flexible, widely used method for organizing data.



Simplest singly-linked data structure: linked list

Linked list

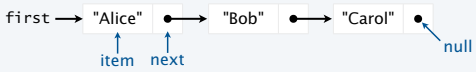
- A recursive data structure.
- Def. A *linked list* is null or a reference to a *node*.
- Def. A *node* is a data type that contains a reference to a node.
- Unwind recursion: A linked list is a sequence of nodes.

```
private class Node
{
  private String item;
  private Node next;
}
```

Representation

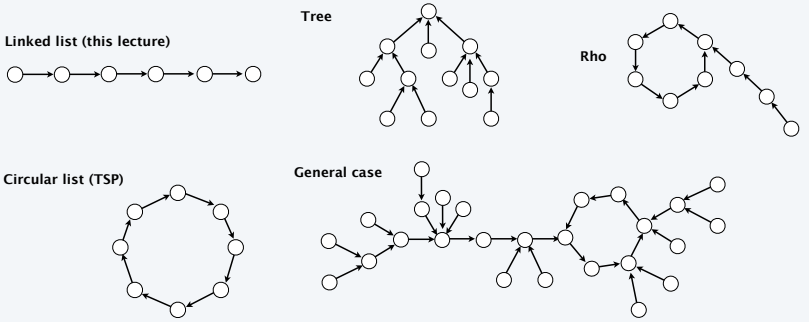
- Use a private nested class Node to implement the node abstraction.
- For simplicity, start with nodes having two values: a `String` and a Node.

A linked list



Singly-linked data structures

Even with just one link (⟶) a wide variety of data structures are possible.



Multiply linked structures: many more possibilities!

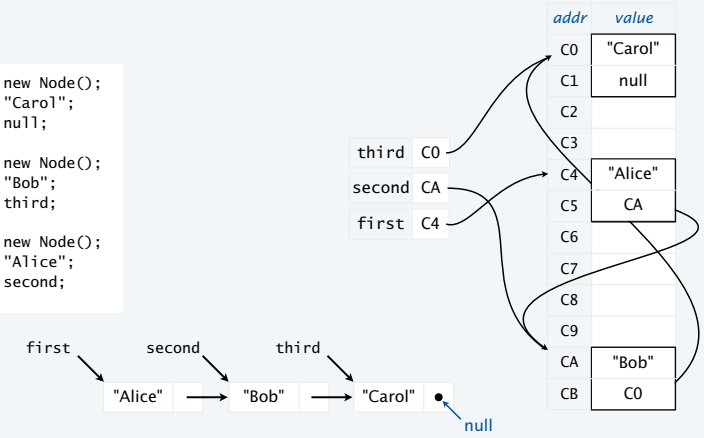
From the point of view of a particular object, all of these structures look the same.

Building a linked list

```
Node third  = new Node();
third.item  = "Carol";
third.next  = null;

Node second = new Node();
second.item = "Bob";
second.next = third;

Node first  = new Node();
first.item  = "Alice";
first.next  = second;
```



List processing code

Standard operations for processing data structured as a singly-linked list

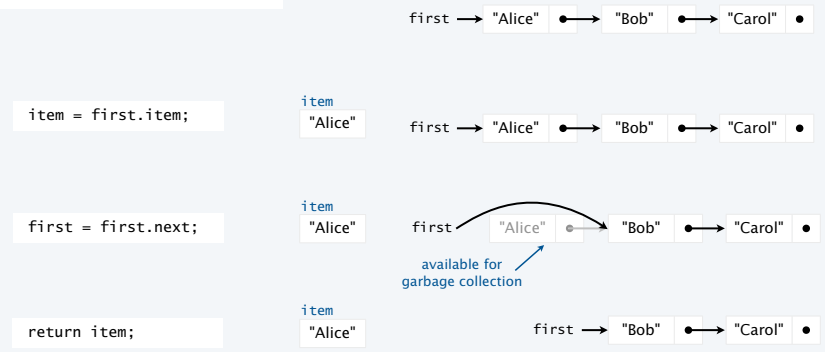
- Add a node at the beginning.
- Remove and return the node at the beginning.
- Add a node at the end (requires a reference to the last node).
- Traverse the list (visit every node, in sequence).

An operation that calls for a *doubly*-linked list (slightly beyond our scope)

- Remove and return the node at the end.

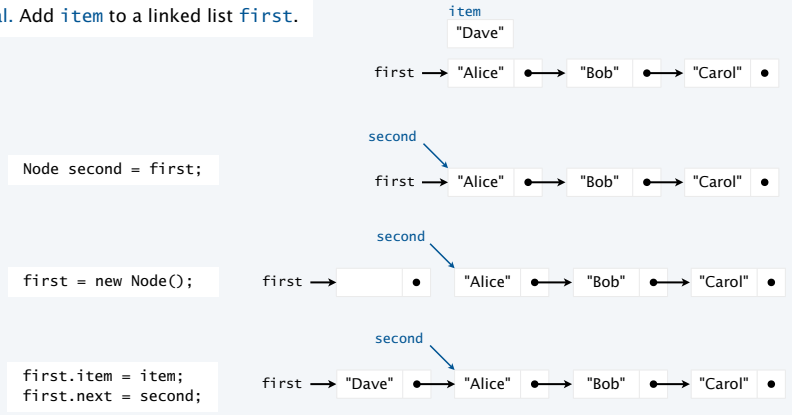
List processing code: Remove and return the first item

Goal. Remove and return the first item in a linked list `first`.



List processing code: Add a new node at the beginning

Goal. Add `item` to a linked list `first`.



List processing code: Traverse a list

Goal. Visit every node on a linked list `first`.

```
Node x = first;
while (x != null)
{
   StdOut.println(x.item);
   x = x.next;
}
```

StdOut

```
Alice
Bob
Carol
```


TEQ 1 on linked lists

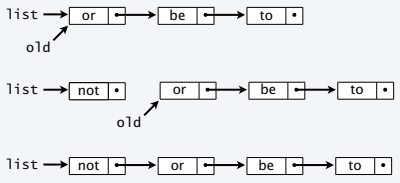
Q. What is the effect of the following code (not-so-easy question)?

```
...
Node list = null;
while (!StdIn.isEmpty())
{
   Node old = list;
   list = new Node();
   list.item = StdIn.readString();
   list.next = old;
}
for (Node t = list; t != null; t = t.next)
   StdOut.println(t.item);
...
```


TEQ 1 on linked lists

Q. What is the effect of the following code (not-so-easy question)?

```
...
Node list = null;
while (!StdIn.isEmpty())
{
   Node old = list;
   list = new Node();
   list.item = StdIn.readString();
   list.next = old;
}
for (Node t = list; t != null; t = t.next)
   StdOut.println(t.item);
...
```



A. Prints the strings from StdIn on StdOut, in reverse order.

Note. Better to use a stack.

TEQ 2 on stacks

Q. Give code that uses a stack to print the strings from StdIn on StdOut, in reverse order.

TEQ 2 on stacks

Q. Give code that uses a stack to print the strings from StdIn on StdOut, in reverse order.

A.

```
Stack<String> stack = new Stack<String>();
while (!StdIn.isEmpty())
   stack.push(StdIn.readString());
while (!stack.isEmpty())
   StdOut.println(stack.pop());
```


TEQ 2 on linked lists

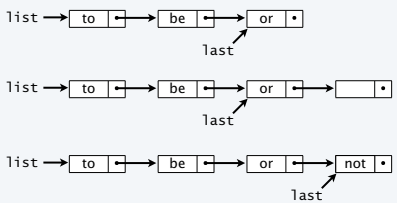
Q. What is the effect of the following code (not-so-easy question)?

```
...
Node list = new Node();
list.item = StdIn.readString();
Node last = list;
while (!StdIn.isEmpty())
{
   last.next = new Node();
   last = last.next;
   last.item = StdIn.readString();
}
...
```


TEQ 2 on linked lists

Q. What is the effect of the following code (not-so-easy question)?

```
...
Node list = new Node();
list.item = StdIn.readString();
Node last = list;
while (!StdIn.isEmpty())
{
   last.next = new Node();
   last = last.next;
   last.item = StdIn.readString();
}
...
```



A. Puts the strings from StdIn on a linked list, in the order they are read (assuming at least one string).

Note. Better to use a *queue*, in most applications.

In this course, we restrict use of linked lists to data-type implementations

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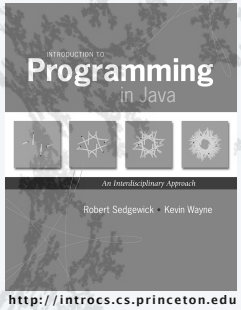

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14. Stacks and Queues

- APIs
- Clients
- Strawman implementation
- **Linked lists**
- Implementations

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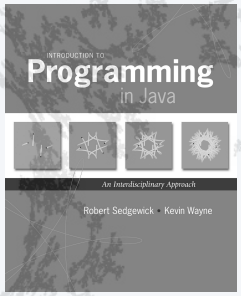

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- **Implementations**

ADT for pushdown stacks: review

A pushdown stack is an idealized model of a LIFO storage mechanism.

An ADT allows us to write Java programs that use and manipulate pushdown stacks.

API

public class Stack<Item>	
Stack<Item>()	*create a stack of objects, all of type* Item
void push(Item item)	*add* item *to stack*
Item pop()	*remove and return the item most recently pushed*
boolean isEmpty()	*is the stack empty?*
int size()	*# of objects on the stack*

Performance specifications

- All operations are constant-time.
- Memory use is proportional to the size of the collection, when it is nonempty.
- No limits within the code on the collection size.

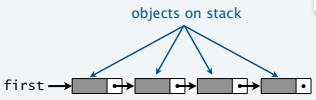
Pushdown stack implementation: Instance variables and constructor

Data structure choice. Use a linked list to hold the collection.

```
public class Stack<Item>
{
   private Node first = null;
   private int N = 0;

   private class Node
   {
      private Item item;
      private Node next;
   }
...
}
```

use in place of concrete type



Annoying exception (not a problem here).
Can't declare an array of Item objects (don't ask why).
Need cast: `Item[] a = (Item[]) new Object[N]`

Stack implementation: Test client

```
public static void main(String[] args)
{
   Stack<String> stack = new Stack<String>();
   while (!StdIn.isEmpty())
   {
      String item = StdIn.readString();
      if (item.equals("-"))
         stack.push(item);
      else
         System.out.print(stack.pop());
   }
   StdOut.println();
}
```


```
% more tobe.txt
to be or not to - be - - that - - - is

% java Stack < tobe.txt
to be not that or be
```

What we *expect*, once the implementation is done.

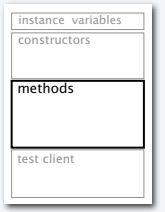
Stack implementation: Methods

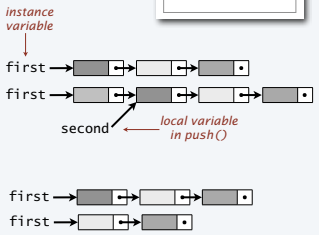
Methods define data-type operations (implement the API).

```
public class Stack<Item>
{
...
   public boolean isEmpty()
   {  return first == null;  }
   public void push(Item item)
   {
      Node second = first;
      first = new Node();
      first.item = item;
      first.next = second;
      N++;
   }
   public Item pop()
   {
      Item item = first.item;
      first = first.next;
      N--;
      return item;
   }
   public int size()
   {  return N;  }
...
}
```

add a new node to the beginning of the list

remove and return first item on list





Stack implementation

```
public class Stack<Item>
{
   private Node first = null;
   private int N = 0;
   private class Node
   {
      private Item item;
      private Node next;
   }
   public boolean isEmpty()
   {  return first == null;  }
   public void push(Item item)
   {
      Node second = first;
      first = new Node();
      first.item = item;
      first.next = second;
      N++;
   }
   public Item pop()
   {
      Item item = first.item;
      first = first.next;
      N--;
      return item;
   }
   public int size()
   {  return N;  }
   public static void main(String[] args)
   { // See earlier slide  }
}
```

instance variables

nested class

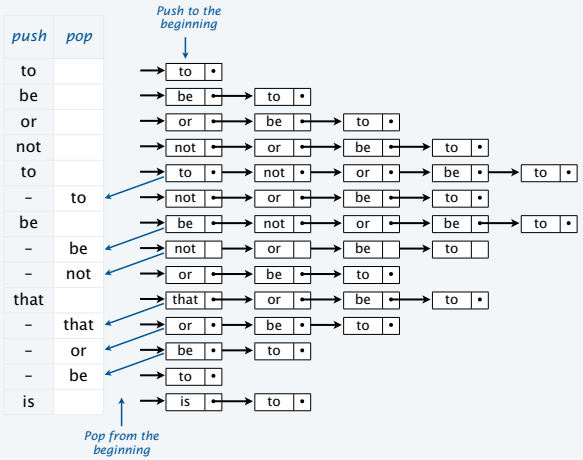
methods

test client

```
% more tobe.txt
to be or not to - be - - that - - - is

% java Stack < tobe.txt
to be not that or be
```


Trace of stack implementation (linked list representation)



Benchmarking the stack implementation

Stack implements the stack abstraction.

It *does* implement the API and meet the performance specifications.

Stack API

public class Stack<Item>	
Stack<Item>()	*create a stack of objects, all of type* Item
void push(Item item)	*add* item *to stack*
Item pop()	*remove and return the item most recently pushed*
boolean isEmpty()	*is the stack empty?*
int size()	*# of objects on the stack*

✓

Performance specifications

- All operations are constant-time. ✓
- Memory use is proportional to the size of the collection, when it is nonempty. ✓
- No limits within the code on the collection size. ✓

Made possible by *linked data structure.*

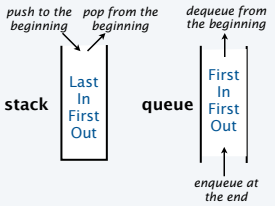
dequeue(): same code as pop()
enqueue(): slightly more complicated, like TEQ 2

Also possible to implement the *queue* abstraction with a singly-linked list (see text).

Summary

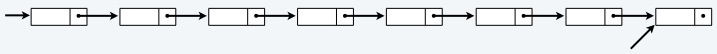
Stacks and queues

- Fundamental collection abstractions.
- Differ only in order in which items are removed.
- Performance specifications: Constant-time for all operations and space proportional to number of objects.



Linked structures

- Fundamental alternative to sequential structures.
- Enable implementations of the stack/queue abstractions *that meet performance specifications.*



Next: *Symbol tables*

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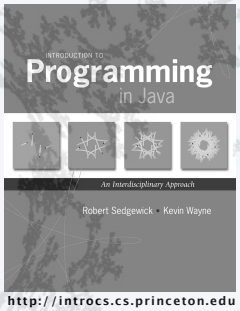

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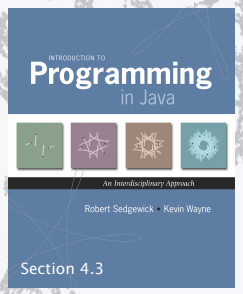

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