

<http://introcs.cs.princeton.edu>

1. Prologue: A Simple Machine

What is this course about?

A broad introduction to **computer science**.

Goals

- Demystify computer systems.
- Empower you to exploit available technology.
- Build awareness of substantial intellectual underpinnings.



Topics

- **Programming** in Java.
- **Design** and architecture of computers.
- **Theory** of computation.
- **Applications** in science and engineering.

and art, music, finance,
and many other fields.

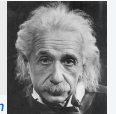
*"Science is everything we understand
well enough to explain to a computer."*

– Don Knuth

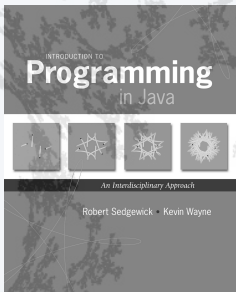


*"Computers are incredibly fast, accurate, and stupid;
humans are incredibly slow, inaccurate, and brilliant;
together they are powerful beyond imagination."*

– Albert Einstein



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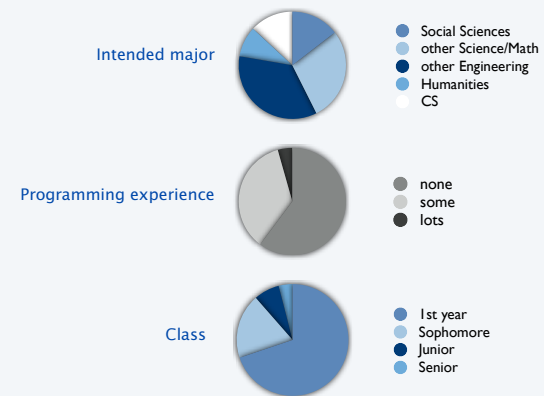
1. Prologue: A Simple Machine

- **Administrivia**
- Secure communication with a one-time pad
- Linear feedback shift registers
- Implications

1a.Prologue.Admin

Who are you?

[data from 2011-12]



Over 60% of all Princeton students take COS 126

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The basics

Lectures. [Sedgewick]

RS office hours.

Precepts. [Pritchard and team]

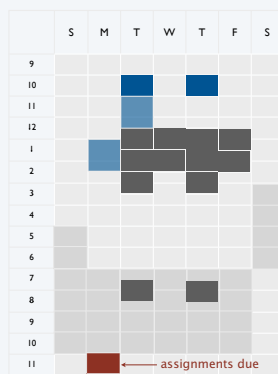
- Tips on assignments / worked examples
- Questions on lecture material.
- Informal and interactive.

Friend 016/017 lab. [undergraduate assistants]

- Help with systems/debugging.
- No help with course material.

Piazza. [online discussion]

- Best chance of quick response to a question.
- Post to class or private post to staff.



See www.princeton.edu/~cos126 for full current details and office hours.

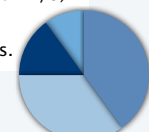
5

Grades

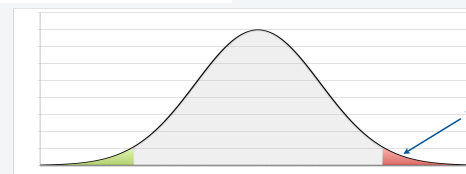
are based on **achievement**.

Opportunities for us to determine your level of achievement:

- 9 programming assignments.
- 2 written exams (in class, 10/10 and 12/12).
- 2 programming exams (evenings, 10/21 or 10/24 and 12/9).
- Final programming project (due Dean's date - 1).
- Extra credit / staff discretion. Adjust borderline cases.



We do **not** grade on a "curve".



| | Due dates | | | | | | |
|-----|-----------|----|----|----|----|----|----|
| | Su | Mo | Tu | We | Th | Fr | Sa |
| SEP | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| | 29 | 30 | | | | | |
| OCT | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| | 13 | 14 | 15 | 16 | 17 | 18 | 19 |
| | 20 | 21 | 22 | 23 | 24 | 25 | 26 |
| | 27 | 28 | 29 | 30 | 31 | | |
| NOV | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| | 17 | 18 | 19 | 20 | 21 | 22 | 23 |
| | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| | 15 | 16 | 17 | 18 | 19 | 20 | 21 |
| DEC | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| | 29 | 30 | 31 | | | | |
| JAN | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| | 19 | 20 | 21 | 22 | 23 | 24 | 25 |
| | 26 | 27 | 28 | 29 | 30 | 31 | |

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Course website

<http://www.princeton.edu/~cos126> ← bookmark this page!

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Textbook and Booksite



Textbook.

- Full introduction to course material.
- Developed for this course.
- For use while learning and studying.

Booksite.

- Summary of content.
- Code, exercises, examples.
- Supplementary material.
- NOT the textbook.
- (also not the course web page).
- For use while online.

<http://introc.cs.princeton.edu> ← bookmark this page, too!

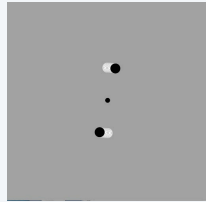
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Programming assignments

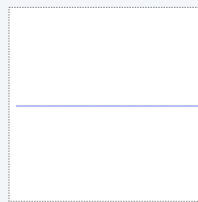
are an essential part of the experience in learning CS.

Desiderata

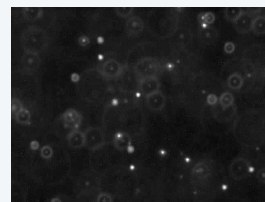
- Address an important scientific or commercial problem.
- Illustrate the importance of a fundamental CS concept.
- You solve the problem from scratch on your own computer!



N-body simulation



pluck a guitar string



estimate Avogadro's number

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What's Ahead?

Coming events

- Lecture 2. Basic programming concepts.
- Precept 1. Meets today/tomorrow.
- Not registered? Go to any precept now; officially register ASAP.
- Change precepts? Use SCORE. ← see Colleen Kenny-McGinley in CS 210 if the only precept you can attend is closed

→ Assignment 0 due Monday 11:59PM ←

Things to do before attempting assignment

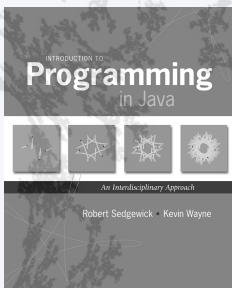
- Read Sections 1.1 and 1.2 in textbook.
- Read assignment carefully.
- Install **introc**s software as per instructions.
- Do a few exercises.
- Lots of help available, don't be bashful.

<http://introc.cs.princeton.edu/assignments.php>

END OF ADMINISTRATIVE STUFF

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COMPUTER SCIENCE
SEDGEWICK / WAYNE



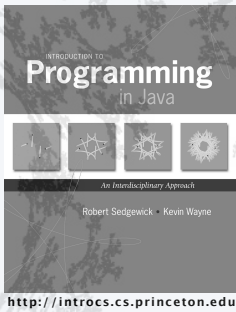
<http://introc.cs.princeton.edu>

0. Prologue: A Simple Machine

- Administrivia
- Secure communication with a one-time pad
- Linear feedback shift registers
- Implications

1a.Prologue.Admin





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0. Prologue: A Simple Machine

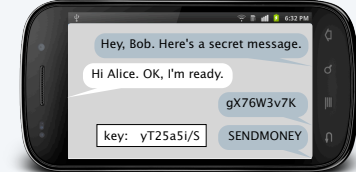
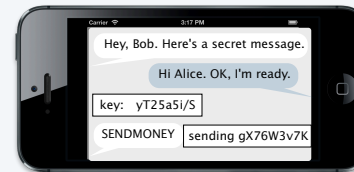
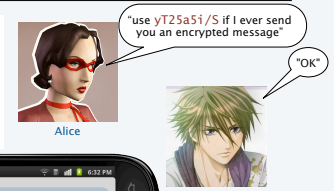
- Administrivia
- **Secure communication with a one-time pad**
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1b.Prologue.OneTime

Sending a secret message with a cryptographic key

Alice wants to send a secret message to Bob.

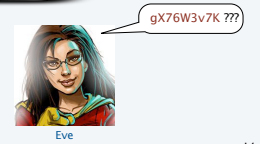
- Sometime in the past, they exchange a **cryptographic key**.
- Alice uses the key to encrypt the message.
- Bob uses the *same* key to decrypt the message.



encrypted message is "in the clear" (anyone can read it)

Critical point: Without the key, Eve cannot understand the message.

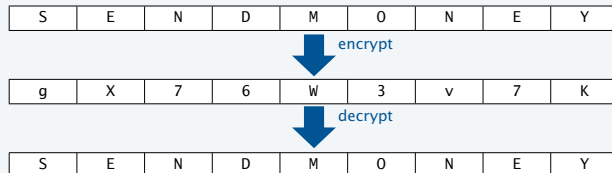
Q. How does the system work?



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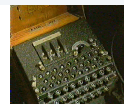
Encrypt/decrypt methods

Goal. Design a method to encrypt and decrypt data.



Example 1. **Enigma encryption machine** [German code, WWII]

- Broken by Turing bombe (one of the first uses of a computer).
- Broken code helped win Battle of Atlantic by providing U-boat locations.



Example 2. **One-time pad** [details to follow]

Example 3. **Linear feedback shift register** [later this lecture]

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A digital world

A *bit* is a basic unit of information.

- Two possible values (0 or 1).
- Easy to represent in the physical world (*on or off*).

In modern computing and communications systems, we represent *everything* as a sequence of bits.

- Text [details to follow in this lecture]
- Numbers
- Sound [details to follow in this course]
- Pictures [details to follow in this course]
- ...
- Programs [profound implications, stay tuned].



0 1 0 0 0 1 0 1

$0100101_2 = 69_{10}$

Bottom line. If we can send and receive bits, we can send and receive *anything*.

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Encoding text as a sequence of bits

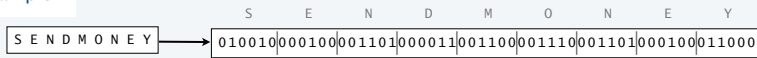
Base64 encoding of character strings

- A simple method for representing text.
- 64 different symbols allowed: A-Z, a-z, 0-9, +, /.
- 6 bits to represent each symbol.
- ASCII and Unicode methods used on your computer are similar.

| | bits | symbols |
|---------|------|---------|
| Base64 | 6 | 64 |
| ASCII | 8 | 256 |
| Unicode | 16 | 65,536+ |

| | | | | | | | | | | | | | | | |
|--------|---|--------|---|--------|---|--------|---|--------|---|--------|---|--------|---|--------|---|
| 000000 | A | 001000 | I | 010000 | Q | 011000 | Y | 100000 | g | 101000 | o | 110000 | w | 111000 | 4 |
| 000001 | B | 001001 | J | 010001 | R | 011001 | Z | 100001 | h | 101001 | p | 110001 | x | 111001 | 5 |
| 000010 | C | 001010 | K | 010010 | S | 011010 | a | 100010 | i | 101010 | q | 110010 | y | 111010 | 6 |
| 000011 | D | 001011 | L | 010011 | T | 011011 | b | 100011 | j | 101011 | r | 110011 | z | 111011 | 7 |
| 000100 | E | 001100 | M | 010100 | U | 011100 | c | 100100 | k | 101100 | s | 110100 | 0 | 111100 | 8 |
| 000101 | F | 001101 | N | 010101 | V | 011101 | d | 100101 | l | 101101 | t | 110101 | 1 | 111101 | 9 |
| 000110 | G | 001110 | O | 010110 | W | 011110 | e | 100110 | m | 101110 | u | 110110 | 2 | 111110 | + |
| 000111 | H | 001111 | P | 010111 | X | 011111 | f | 100111 | n | 101111 | v | 110111 | 3 | 111111 | / |

Example:

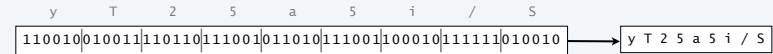
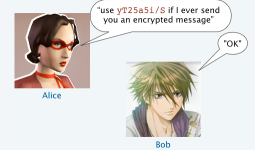


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One-Time Pads

What is a one-time pad?

- A *cryptographic key* known only to the sender and receiver.
- Good choice: A *random* sequence of bits (stay tuned).
- Security depends on each sequence being used only once.



| | | | | | | | | | | | | | | | |
|--------|---|--------|---|--------|---|--------|---|--------|---|--------|---|--------|---|--------|---|
| 000000 | A | 001000 | I | 010000 | Q | 011000 | Y | 100000 | g | 101000 | o | 110000 | w | 111000 | 4 |
| 000001 | B | 001001 | J | 010001 | R | 011001 | Z | 100001 | h | 101001 | p | 110001 | x | 111001 | 5 |
| 000010 | C | 001010 | K | 010010 | S | 011010 | a | 100010 | i | 101010 | q | 110010 | y | 111010 | 6 |
| 000011 | D | 001011 | L | 010011 | T | 011011 | b | 100011 | j | 101011 | r | 110011 | z | 111011 | 7 |
| 000100 | E | 001100 | M | 010100 | U | 011100 | c | 100100 | k | 101100 | s | 110100 | 0 | 111100 | 8 |
| 000101 | F | 001101 | N | 010101 | V | 011101 | d | 100101 | l | 101101 | t | 110101 | 1 | 111101 | 9 |
| 000110 | G | 001110 | O | 010110 | W | 011110 | e | 100110 | m | 101110 | u | 110110 | 2 | 111110 | + |
| 000111 | H | 001111 | P | 010111 | X | 011111 | f | 100111 | n | 101111 | v | 110111 | 3 | 111111 | / |

more convenient than bits for initial exchange

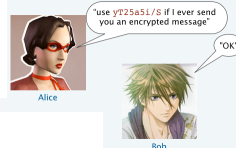
Note: Any sequence of bits can be decoded into a sequence of characters.

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Encryption with a one-time pad

Preparation

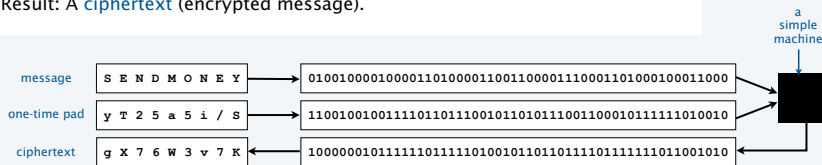
- Create a "random" sequence of bits (a one-time pad).
- Send one-time pad to intended recipient through a secure channel.



Encryption

- Encode text as a sequence of N bits.
- Use the first N bits of the pad.
- Compute a new sequence of N bits (a function of the message and the pad).
- Decode result to get a sequence of characters.

Result: A **ciphertext** (encrypted message).



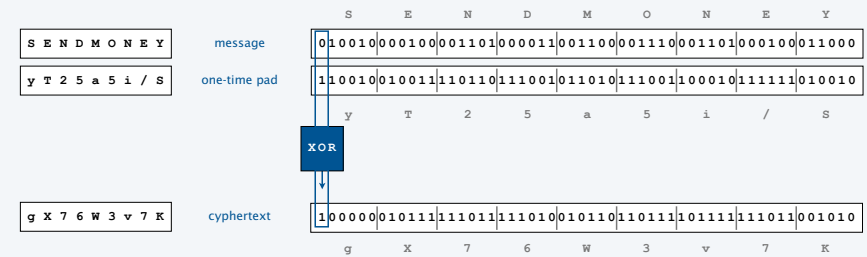
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A (very) simple machine for encryption

To compute a ciphertext from a message and a one-time pad

- Encode message and pad in binary.
- Each ciphertext bit is the *bitwise exclusive or* of corresponding bits in message and pad.

Def. The *bitwise exclusive or* of two bits is 1 if they differ, 0 if they are the same.

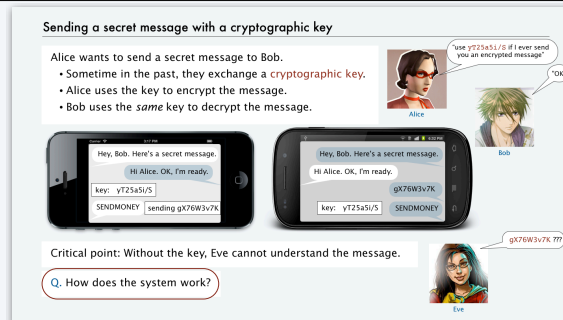


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Typical Exam Question (TEQ) on bitwise XOR encryption

Q. Encrypt the message **E A S Y** with the pad **0 1 2 3**.

Decryption with a one-time pad



A. Alice's device uses a "bitwise exclusive or" machine to encrypt the message.

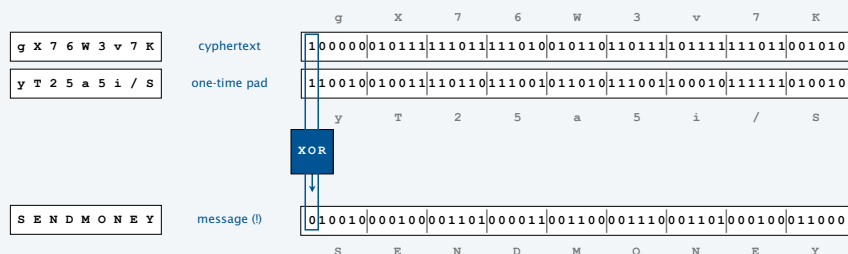
Q. What kind of machine does Bob's device use to *decrypt* the message?

A. The same one (!!)

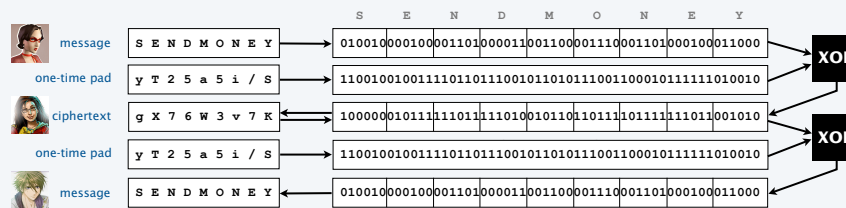
A (very) simple machine for encryption and decryption

To compute a *message* from a *cyphertext* and a *one-time pad*

- Use binary encoding of cyphertext and pad.
- Each message bit is the *bitwise exclusive or* of corresponding bits in cyphertext and pad.



Why does it work?



Crucial property: Decrypted message is the same as the original message.

Let m be a bit of the message and k be the corresponding bit of the one-time pad.

To prove: $(m \wedge k) \wedge k = m$ ← Notation: $m \wedge k$ is equivalent to XOR(m, k)

Approach 1: Truth tables

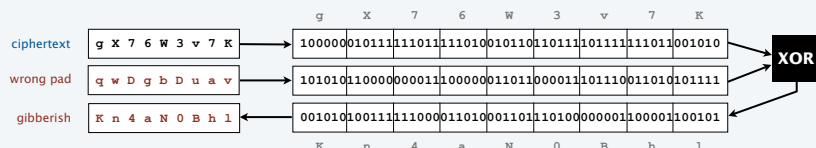
| m | k | $m \wedge k$ | $(m \wedge k) \wedge k$ |
|-----|-----|--------------|-------------------------|
| 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 |
| 1 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 |

Approach 2: Boolean algebra

$$\begin{aligned}
 (k \wedge k) &= 0 \\
 m \wedge 0 &= m \\
 (m \wedge k) \wedge k &= m \wedge (k \wedge k) \\
 &= m \wedge 0 \\
 &= m \quad \checkmark
 \end{aligned}$$

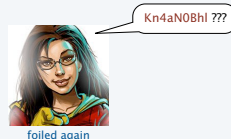
Decryption with the wrong pad

Eve *cannot* read a message without knowing the pad.



One-time pad is **provably secure** [Shannon, 1940s]

- IF each pad is used only once,
- AND the pad bits are random,
- THEN Eve cannot distinguish cyphertext from random bits.



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Eve's problem with one-time pads

Eve has a computer. Why not try all possibilities?



Problem

- 54 bits, so there are 2^{54} possible pad values.
- Suppose Eve could check a million values per second.
- It would still take 570+ years to check all possibilities.

Much worse problem

- There are also 2^{54} possible messages.
- If Eve were to check all the pads, she'd see all the *messages*.
- No way to distinguish the real one from any other.

One-time pad is **provably secure**.

| pad value | message? |
|-----------|-----------|
| AAAAAAAAA | gX76W3v7K |
| AAAAAAAAB | gX76W3v7L |
| AAAAAAAC | gX76W3v7I |
| ... | |
| qwDgbDuav | Kn4aN0Bh1 |
| ... | |
| tTtpwk+1E | NEWTATTOO |
| ... | |
| yT25a5i/S | SENDMONEY |
| ... | |
| ////////+ | fo7FpIQE0 |
| //////// | fo7FpIQE1 |

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Goods and bads of one-time pads



a one-time pad

Goods.

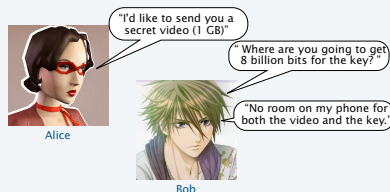
- Very simple encryption method.
- Decrypt with the same method.
- Provably unbreakable if bits are truly random.
- Widely used in practice. [Example: cold war hotline.]



Dallas Morning News, 1963

Bads.

- Easily breakable if seed is re-used.
- Truly random bits are very hard to come by.
- Need separate secure channel to distribute key.
- Pad must be as long as the message.

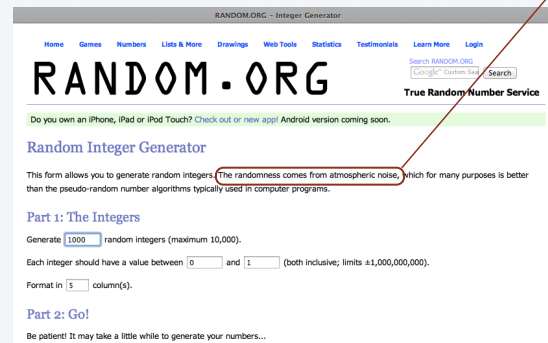


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Random bits are not so easy to find

You might look on the internet.

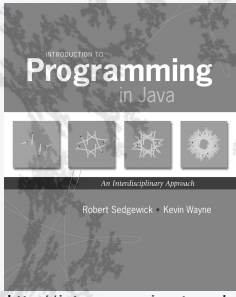
The randomness comes from atmospheric noise



... if you trust the internet.

Next: Creating a (long) sequence of "pseudo-random" bits from a (short) key.

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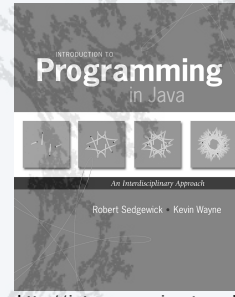


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1b.Prologue.OneTime



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1c.Prologue.LFSR

A pseudo-random number generator

is a *deterministic* machine that produces a long sequence of *pseudo random* bits.

Examples

Enigma.

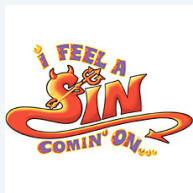
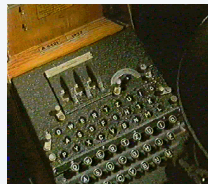
Linear feedback shift register (next).

Blum-Blum-Shub generator.

...

[an early application of computing]

[research still ongoing]



"Anyone who considers arithmetical methods of producing random digits is, of course, in a state of sin."

— John von Neumann



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A pseudo-random number generator

is a *deterministic* machine that produces a long sequence of *pseudo random* bits.

Deterministic: Given the current state of the machine, we know the next bit.

An absolute requirement: Alice and Bob need the same sequence.

Random: We never know the next bit.

Pseudo-random: The sequence of bits *appears to be* random.



10000001011111011
111010010110110111 ???
10111111011001010

Appears to be random??

- A profound and elusive concept.
- For this lecture: "Has enough properties of a random sequence that Eve can't tell the difference".

Ex. 1: No long repeats
Ex. 2: About the same number of 0s and 1s
Ex. 3: About the same number of 00s, 01s, 10s, and 11s.
...

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Typical Exam Question (TEQ) on LFSRs

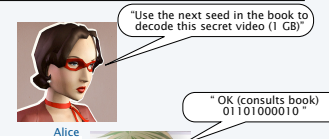
Q. Give first 10 steps of [5,4] LFSR with initial fill 00001.

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Encryption/decryption with an LFSR

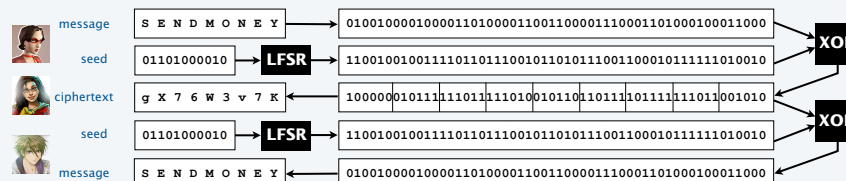
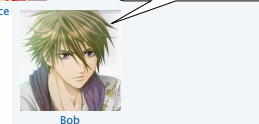
Preparation

- Alice creates a book of "random" (short) seeds.
- Alice sends the book to Bob through a secure channel.



Encryption/decryption

- Alice sends Bob a description of which seed to use.
- They use the specified seed to initialize an LFSR and produce N bits. [and proceed in the same way as for one-time pads]

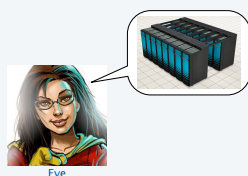


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Eve's opportunity with LFSR encryption

Eve has computers. Why not try all possible seeds?

- Seeds are short, messages are long.
- All seeds give a tiny fraction of all messages.
- Extremely likely that all but real seed will produce gibberish.



Good news (for Eve): This approach can work.

- Ex: 11-bit register implies 2047 possibilities.
- Extremely likely that only *one* of those is not gibberish.
- After this course, *you* could write a program to check whether any of the 2047 messages have words in the dictionary.

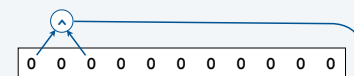
Bad news (for Eve): It is easy for Alice and Bob to use a much longer LFSR.

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Key properties of LFSRs

Property 1.

- Don't use all 0s as a seed!
- Fill of all 0s will not otherwise occur.



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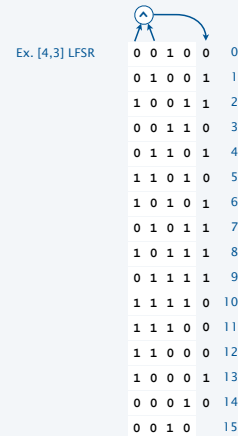
Key properties of LFSRs

Property 1.

- Don't use all 0s as a seed!
- Fill of all 0s will not otherwise occur.

Property 2. Bitstream must eventually cycle.

- $2^N - 1$ nonzero fills in an N -bit register.
- Future output completely determined by current fill.



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Key properties of LFSRs

Property 1.

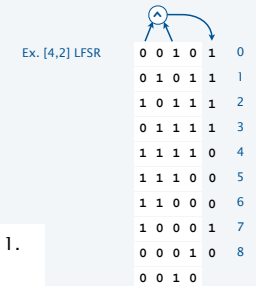
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Property 2. Bitstream must eventually cycle.

- $2^N - 1$ nonzero fills in an N -bit register.
- Future output completely determined by current fill.

Property 3. Cycle length in an N -bit register is *at most* $2^N - 1$.

- Could be smaller; cycle length depends on tap positions.
- Need theory of finite groups to know good tap positions.



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Key properties of LFSRs

Property 1.

- Don't use all 0s as a seed!
- Fill of all 0s will not otherwise occur.

Property 2. Bitstream must eventually cycle.

- $2^N - 1$ nonzero fills in an N -bit register.
- Future output completely determined by current fill.

Property 3. Cycle length in an N -bit register is at most $2^N - 1$.

- Could be smaller; cycle length depends on tap positions.
- Need theory of finite groups to know good tap positions.

Bottom line.

- [11, 9] register generates 2047 bits before repeating.
- [63, 62] register generates $2^{63} - 1$ bits before repeating. ← Definitely preferable: small cost, huge payoff.

Linear Feedback Shift Register Taps

This table lists the approximate taps for maximum-length LFSRs of various sizes. The register dimensions and the tap positions are in hexadecimal. The tap positions are numbered from 1 to N , with 1 being the rightmost bit. The register is assumed to be initialized with the value 1. For a full list of tap positions, see the Appendix in [1].

Table 3. Taps for Maximum Length LFSR Counters

| Register Size (N) | Tap Positions (Hex) |
|-------------------|--|
| 3 | 0, 1, 2 |
| 4 | 0, 1, 2, 3 |
| 5 | 0, 1, 2, 3, 4 |
| 6 | 0, 1, 2, 3, 4, 5 |
| 7 | 0, 1, 2, 3, 4, 5, 6 |
| 8 | 0, 1, 2, 3, 4, 5, 6, 7 |
| 9 | 0, 1, 2, 3, 4, 5, 6, 7, 8 |
| 10 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9 |
| 11 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 |
| 12 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11 |
| 13 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12 |
| 14 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13 |
| 15 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14 |
| 16 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15 |
| 17 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16 |
| 18 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17 |
| 19 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18 |
| 20 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19 |
| 21 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20 |
| 22 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21 |
| 23 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22 |
| 24 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23 |
| 25 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24 |
| 26 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25 |
| 27 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26 |
| 28 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27 |
| 29 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28 |
| 30 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29 |
| 31 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30 |
| 32 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31 |
| 33 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32 |
| 34 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33 |
| 35 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34 |
| 36 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35 |
| 37 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36 |
| 38 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37 |
| 39 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38 |
| 40 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39 |
| 41 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40 |
| 42 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41 |
| 43 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42 |
| 44 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43 |
| 45 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44 |
| 46 | 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45 |

XILINX manual, 1990s

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Eve's problem with LFSR encryption

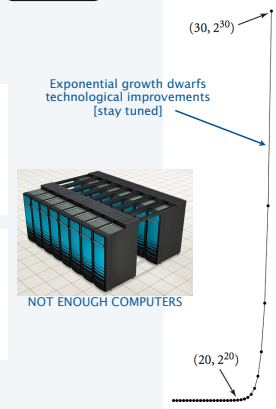
Without the seed, Eve cannot read the message.



gX76W3v7K ???

Eve has computers. Why not try all possible seeds?

- Seeds are short, messages are long.
- All seeds give a tiny fraction of all messages.
- Extremely likely that all but real seed will produce gibberish.



Bad news (for Eve): There are still way too many possibilities.

- Ex: 63-bit register implies $2^{63} - 1$ possibilities.

- If Eve could check 1 million seeds per second, it would take her 2923 centuries to try them all!

Bad news (for Alice and Bob): LFSR output is *not* random.

experts have cracked LFSRs

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Goods and bads of LFSRs

Goods.

- Very simple encryption method.
- Decrypt with the same method.
- Scalable: 20 cells for 1 million bits; 30 cells for 1 billion bits.
- Widely used in practice. [Example: military cryptosystems.]



a commercially available LFSR

Bads.

- Easily breakable if seed is re-used.
- Still need secure key distribution.
- Experts can crack LFSR encryption.

Example.

- CSS encryption widely used for DVDs.
- Widely available DeCSS breaks it!

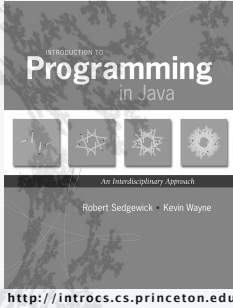
```

/*  efdt.c  Author: Charles M. Hannum <root@ihack.net>  */
/*  Usage is: cat title-key scrambled.vob | efdt >clear.vob  */

#define m(i) (x[i]^m[i+84])<<

unsigned char x[5], y, s[2048]; main(
n){for( read(0,x,5) ;read(0,s,n=2048
); write(1, s,n) ;){if(
{y=s (13)^8+20) /1644 ==1 }){int
i=m( 1)^17 ^256 m(0) 8,k m(2)
0,y= m(4) 17^ m(3) 9^14^ 2^148
^8,a =0,c =26;xor (s[y] ^-16;
--c; } +=2)a= a^2^16 1,s=1 /2^141
<<<<<for( j= 127; ++j;c,rand()
y)
c
==y^1^1/8^1>>4^1>>12,
i=1>>8^y<<17,a^m>>16,y^a^8^a<<6,a=m
>>8^y<<9,k=a^j,k =!7No~'G \216"[k
67]^2^"qr3r4w5v;^k<>/n_ [k>>4]^<^k^257/
8,s[i]=k^ (84k^224)^6^c^y
:)}
    
```

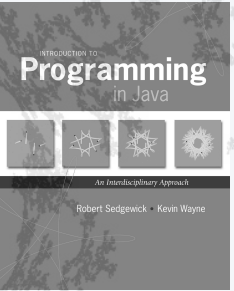
DeCSS DVD decryption code



0. Prologue: A Simple Machine

- Administrivia
- Secure communication with a one-time pad
- Linear feedback shift registers
- Implications

<http://introcs.cs.princeton.edu>



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LFSRs and general-purpose computers



- Important similarities.
- Both are built from simple components.
 - Both scale to handle huge problems.
 - Both require careful study to use effectively.

| component | LFSR | computer |
|-------------|----------------------------|-----------------------------|
| control | start, stop, load | same |
| clock | | same |
| memory | 12 bits | billions of bits |
| input | 12 bits | bit sequence |
| computation | shift, XOR | + - * / ... |
| output | pseudo-random bit sequence | any computable bit sequence |

- Critical differences: Operations, input. ← but the simplest computers differ only slightly from LFSRs!
- General purpose computer can simulate any abstract machine.
 - All general purpose computers have equivalent power (!) [stay tuned].

A Profound Idea

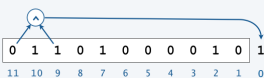
Programming. We can write a Java program to simulate the operation of *any* abstract machine.

- Basis for theoretical understanding of computation.
- Basis for bootstrapping real machines into existence.

Stay tuned (we cover these sorts of issues in this course).

```
public class LFSR
{
    public static void main(String[] args)
    {
        int[] a = { 0, 0, 1, 0, 0, 0, 0, 1, 0, 1, 1, 0 };
        for (int t = 0; t < 2000; t++)
        {
            a[0] = (a[11] ^ a[9]);
            System.out.print(a[0]);
            for (int i = 11; i > 0; i--)
                a[i] = a[i-1];
            System.out.println();
        }
    }
}
```

YOU will be writing code like this within a few weeks.



```
% java LFSR
11001001001111011011100101101011100110001
0111110100100001001101001011110011001001
1111101110000010101100010000111010100110
10000111001001100111011111010100000100
00100010100101010001100000101111000100100
1101011011100011010011011100111101...
```

Note: You will write and apply an LFSR simulator in Assignment 5.

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Profound questions

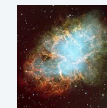
Q. What is a random number?

LFSRs *do not* produce random numbers.

- They are *deterministic*. ← von Neumann's "state of sin": we know that "deterministic" is incompatible with "random"
- It is not obvious how to distinguish the bits LFSRs produce from random,
- BUT experts have figured out how to do so.

Q. Are random processes found in nature?

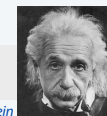
- Motion of cosmic rays or subatomic particles?
- Mutations in DNA?



Q. Is the natural world a (not-so-simple) deterministic machine??

"God does not play dice."

— Albert Einstein



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INTRODUCTION TO
Programming
in Java



An Interdisciplinary Approach
Robert Sedgwick · Kevin Wayne

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1d.Prologue.Implications

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