

## COS226 Week 2 Activity

1. *Design an algorithm.* Design a quadratic-time algorithm for the 3-sum problem. Describe your design by giving a crisp and concise English description of your algorithm; don't write Java code.

(a) Given an integer  $x$  and a sorted array  $a[]$  of  $N$  distinct integers, design a linear-time algorithm to find if there exists indices  $i$  and  $j$  such that  $(a[i] + a[j] == x)$ . Hint: start by checking whether  $a[0] + a[N-1]$  is  $<$ ,  $>$ , or  $== x$ .

(b) Given an array  $a[]$  of  $N$  distinct integers, design a quadratic-time algorithm to find if there exists indices  $i$ ,  $j$ , and  $k$  such that  $(a[i] + a[j] + a[k] == 0)$ . Hint: Use the result from (a). You can assume the array is sorted since sorting the array can be done in quadratic (and even linearithmic) time.

2. *Generics, iterators, autoboxing, and mathematical analysis.*

Use the class shown here: <http://algs4.cs.princeton.edu/13stacks/ResizingArrayStack.java.html>

```
ResizingArrayStack<Character> stack = new ResizingArrayStack<Character>();
stack.push('A');
stack.push('C');
stack.push('T');
for (char left : stack)
    for (char right : stack)
        StdOut.println(left + " " + right);
```

(a) What does the above code fragment output to standard output?

(b) If  $N$  characters are pushed onto the stack initially (instead of 3), how many lines of output does the above code fragment produce as a function of  $N$ ?

3. *Unit testing.* Describe three ways to test the correctness of the implementation of `ResizingArrayStack`.

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4. *Memory analysis.* Suppose you have a generic stack implemented using a linked list, as defined below:

```
public class Stack<Item> implements Iterable<Item> {
    private int N;           // size of the stack
    private Node first;     // top of stack

    private class Node {
        private Item item;
        private Node next;
    }
    ...
}
```

- (a) How much memory (in bytes) does a single `Node` object use? Use the 64-bit memory cost model from Section 1.4. Do not include the memory for the item itself—this memory is allocated by the client and depends on the item type.
- (b) How much memory (in bytes) does a `Stack` use to store  $N$  items? Do not include the memory for the items themselves.
- (c) Repeat the previous question, but use tilde notation to simplify your answer.