## COS 597A, Fall 08: Problem Set 5, Problem 2 Solution

Initially:


Leaf. Only key value is shown.

Part A - Remove 29:
Follow root to interior node with key 27 to leaf containing 29
Remove 29 from leaf. B+ tree properties preserved. Done


## Part B- Remove 27:

Follow root to interior node with key 27 to leaf containing 27
Remove 27 from leaf. Leaf is too small.
Check sibling containing 20 for redistribution - sibling not full enough Merge siblings, deleting parent key 27


## Remove 27, continued:

Parent node $P$ is too small after deletion of key 27
Check sibling for redistribution. Either sibling is full enough. This solution assumes check right sibling first and redistribute with it.
Redistribution:
key 30 moves from parent of $P$ to $P$
leaf containing 30,38 shifts from being child of right sibling to be child of $P$
Key 40 moves up from right sibling of $P$ to parent
Done.


