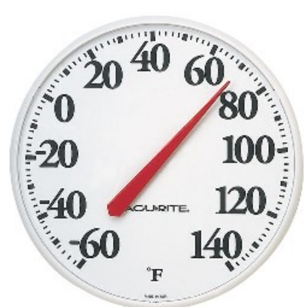
Bits, bytes, and representation of information

- **digital representation means that everything is represented by numbers only**
- **the usual sequence:**
  - something (sound, pictures, text, instructions, ...) is converted into numbers by some mechanism
  - the numbers can be stored, retrieved, processed, transmitted
  - the numbers might be reconstituted into a version of the original
- **for sound, pictures, other real-world values**
  - make accurate measurements
  - convert them to numeric values

Analog versus Digital

- **analog: "analogous" or "the analog of"**
  - smoothly or continuously varying values
  - volume control, dimmer, faucet, steering wheel
  - value varies smoothly with something else
    - no discrete steps or changes in values
      - small change in one implies small change in another
      - infinite number of possible values
  - the world we perceive is largely analog
- **digital: discrete values**
  - only a finite number of different values
  - a change in something results in sudden change from one discrete value to another
    - digital speedometer, digital watch, push-button radio tuner, ...
  - values are represented as <u>numbers</u>



Transducers

- **devices that convert from one representation to another**
  - microphone
  - loudspeaker / earphones
  - camera / scanner
  - printer / screen
  - keyboard
  - mouse
  - touch screen
  - etc.
- **something is usually lost by conversion (in each direction)**
  - the ultimate copy is not as good as the original

Encoding sound

- **need to measure intensity/loudness often enough and accurately enough that we can reconstruct it well enough**
- **higher frequency = higher pitch**
- **human ear can hear ~ 20 Hz to 20 KHz**
  - taking samples at twice the highest frequency is good enough (Nyquist)
- **CD audio usually uses**
  - 44,100 samples / second
  - accuracy of 1 in 65,536 (= 2^16) distinct levels
  - two samples at each time for stereo
  - data rate is 44,100 x 2 x 16 bits/sample
    = 1,411,200 bits/sec = 176,400 bytes/sec ~ 10.6 MB/minute
- **MP3 audio compresses by clever encoding and removal of sounds that won't really be heard**
  - data rate is ~ 1 MB/minute

Discrete values vs continuous values

- **another kind of conversion**
  - letters are converted into numbers when you type on a keyboard
  - the letters are stored (a Word document), retrieved (File/Open...), processed (paper is revised), transmitted (submitted by email)
  - printed on paper
- **letters and other symbols are inherently discrete**
- **encoding them as numbers is just assigning a numeric value to each one, without any intrinsic meaning**

Important ideas

- **number of items and number of digits are tightly related:**
  - one determines the other
  - maximum number of different items = base $^{\text{number of digits}}$
  - e.g., 9-digit SSN: 10^9 = 1 billion possible numbers

  - e.g., to represent up to 100 "characters": 2 digits is enough
  - but for 1000 characters, we need 3 digits
- **interpretation depends on context**
  - without knowing that, we can only guess what things mean
  - what's 81615 ?

What's a bit? What's a byte?

- **a bit is the smallest unit of information**
- **represents one 2-way decision or a choice out of two possibilities**
  - yes / no, true / false, on / off, M / F, ...
- **abstraction of all of these is represented as 0 or 1**
  - enough to tell which of TWO possibilities has been chosen
  - a single digit with one of two values
  - hence "binary digit"
  - hence bit
- **binary is used in computers because it's easy to make fast, reliable, small devices that have only two states**
  - high voltage/low voltage, current flowing/not flowing (chips)
  - electrical charge present/not present (RAM, flash)
  - magnetized this way or that (disks)
  - light bounces off/doesn't bounce off (cd-rom, dvd)
- **all information in a computer is stored and processed as bits**
- **a byte is 8 bits that are treated as a unit**

Using bits to represent information

- **M/F or on/off**
  - 1 bit
- **Fr/So/Jr/Sr**
  - 2 bits
- **add grads, auditors, faculty**
  - 3 bits
- **a number for each student in 109**
  - 7 bits
- **a number for each freshman at PU**
  - 11 bits
- **a number for each undergrad at PU**
  - 13 bits

A review of how decimal numbers work

- **how many digits?**
  - we use 10 digits for counting: "decimal" numbers are natural for us
  - other schemes show up in some areas

    clocks use 12, 24, 60; calendars use 7, 12

    other cultures use other schemes (quatre-vingts)
- **what if we want to count to more than 10?**
  - 0 1 2 3 4 5 6 7 8 9

    1 decimal digit represents 1 choice from 10; counts 10 things; 10 distinct values
  - 00 01 02 … 10 11 12 … 20 21 22 … 98 99

    2 decimal digits represents 1 choice from 100; 100 distinct values

    we usually elide zeros at the front
  - 000 001 … 099 100 101 … 998 999

    3 decimal digits …
- **decimal numbers are shorthands for sums of powers of 10**
  - 1492 = 1 x 1000 + 4 x 100 + 9 x 10 + 2 x 1
  - = $1 \times 10^3 + 4 \times 10^2 + 9 \times 10^1 + 2 \times 10^0$
- **counting in "base 10", using powers of 10**

Binary numbers: using bits to represent numbers

- **just like decimal except there are only <u>two</u> digits: 0 and 1**
- **everything is based on powers of 2 (1, 2, 4, 8, 16, 32, …)**
  - instead of powers of 10 (1, 10, 100, 1000, …)
- **counting in binary or base 2:**

  0 1

  1 binary digit represents 1 choice from 2; counts 2 things; 2 distinct values

  00 01 10 11

  2 binary digits represents 1 choice from 4; 4 distinct values

  000 001 010 011 100 101 110 111

  3 binary digits …
- **binary numbers are shorthands for sums of powers of 2**

  11011 = 1 x 16 + 1 x 8 + 0 x 4 + 1 x 2 + 1 x 1

  = $1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$
- **counting in "base 2", using powers of 2**

Binary (base 2) arithmetic

- **works like decimal (base 10) arithmetic, but simpler**
- **addition:**

  0 + 0 = 0
  0 + 1 = 1
  1 + 0 = 1
  1 + 1 = 10

- **subtraction, multiplication, division are analogous**

Bytes

- **"byte" = group of 8 bits**
  - on modern machines, the fundamental unit of processing and memory addressing
  - can encode any of 2^8 = 256 different values, e.g., numbers 0 .. 255 or a single letter like A or digit like 7 or punctuation like $

    ASCII character set defines values for letters, digits, punctuation, etc.
- **group 2 bytes together to hold larger entities**
  - two bytes (16 bits) holds 2^{16} = 65536 values
  - a bigger integer, a character in a larger character set

    Unicode character set defines values for almost all characters anywhere
- **group 4 bytes together to hold even larger entities**
  - four bytes (32 bits) holds 2^{32} = 4,294,967,296 values
  - an even bigger integer, a number with a fractional part (floating point), a memory address
- **etc.**
  - recent machines use 64-bit integers and addresses (8 bytes)

    2^{64} = 18,446,744,073,709,551,616

Interpretation of bits depends on context

- **meaning of a group of bits depends on how they are interpreted**
- **1 byte could be**
  - 1 bit in use, 7 wasted bits (e.g., M/F in a database)
  - 8 bits storing a number between 0 and 255
  - an alphabetic character like W or + or 7
  - part of a character in another alphabet or writing system (2 bytes)
  - part of a larger number (2 or 4 or 8 bytes, usually)
  - part of a picture or sound
  - part of an instruction for a computer to execute
    - instructions are just bits, stored in the same memory as data
    - different kinds of computers use different bit patterns for their instructions
      - laptop, cellphone, game machine, etc., all potentially different
  - part of the location or address of something in memory
  - ...
- **one program's instructions are another program's data**
  - when you download a new program from the net, it's data
  - when you run it, it's instructions

Powers of two, powers of ten

1 bit = 2 possibilities

2 bits = 4 possibilities

3 bits = 8 possibilities

...

n bits = 2^n

2^{10} = 1,024 is about 1,000 or 1K or 10^3

2^{20} = 1,048,576 is about 1,000,000 or 1M or 10^6

2^{30} = 1,073,741,824 is about 1,000,000,000 or 1G or 10^9

the approximation is becoming less good

but it's still good enough for estimation

- **terminology is often imprecise:**
  - " 1K " might mean 1000 or 1024 (10^3 or 2^{10})
  - " 1M " might mean 1000000 or 1048576 (10^6 or 2^{20})

Converting between binary and decimal (version 1)

- **binary to decimal:**

  $1101 = 1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0$

  $= 1 \times 8 + 1 \times 4 + 0 \times 2 + 1 \times 1$

  $= 13$

- **decimal to binary:**
  - start with largest power of 2 smaller than the number
  - for each power of 2 down to 2^0
  - if you can subtract that power of 2, do so and write "1"
  - otherwise write "0"

  - start with 13, subtract 8, write "1"
  - with 5, subtract 4, write "1"
  - with 1, can't subtract 2, write "0"
  - with 1, subtract 1, write "1"
  - answer is 1101

Converting between binary and decimal (version 2)

- **decimal to binary (from right to left):**
  - repeat while the number is > 0:
  - divide the number by 2
  - write the remainder (0 or 1)
  - use the quotient as the number and repeat
  - answer is the resulting sequence in reverse (right to left) order

  - divide 13 by 2, write "1", number is 6
  - divide 6 by 2, write "0", number is 3
  - divide 3 by 2, write "1", number is 1
  - divide 1 by 2, write "1", number is 0
  - answer is 1101

Hexadecimal notation

- **binary numbers are bulky**
- **hexadecimal notation is a shorthand**
- **it combines 4 bits into a single digit, written in base 16**
  - a more compact representation of the same information
- **hex uses the symbols A B C D E F for the digits 10 .. 15**

0 1 2 3 4 5 6 7 8 9 A B C D E F

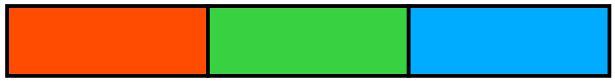
0	0000	1	0001	2	0010	3	0011
4	0100	5	0101	6	0110	7	0111
8	1000	9	1001	A	1010	B	1011
C	1100	D	1101	E	1110	F	1111

ASCII (better representation: uses hex)

	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
0	NUL	SOH	STX	ETX	EOT	ENQ	ACK	BEL	BS	HT	LF	VT	FF	CR	SO	SI
1	DLE	DC1	DC2	DC3	DC4	NAK	SYN	ETB	CAN	EM	SUB	ESC	FS	GS	RS	US
2	SPC	!	"	#	$	%	&	'	(	)	*	+	,	-	.	/
3	0	1	2	3	4	5	6	7	8	9	:	;	<	=	>	?
4	@	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
5	P	Q	R	S	T	U	V	W	X	Y	Z	[	\	]	^	_
6	`	a	b	c	d	e	f	g	h	i	j	k	l	m	n	o
7	p	q	r	s	t	u	v	w	x	y	z	{	|	}	~	DEL

Color

- **TV & computer screens use Red-Green-Blue (RGB) model**



- **each color is a combination of red, green, blue components**
  - R+G = yellow, R+B = magenta, B+G = cyan, R+G+B = white
- **for computers, color of a pixel is usually specified by three numbers giving amount of each color, on a scale of 0 to 255**
- **this is often expressed in hexadecimal so the three components can be specified separately (in effect, as bit patterns)**
  - 000000 is black, FFFFFF is white
- **printers, etc., use cyan-magenta-yellow[-black] (CMY[K])**

Things to remember

- **digital devices represent everything as numbers**
  - discrete values, not continuous or infinitely precise
- **all modern digital devices use binary numbers (base 2)**
  - instead of decimal (base 10)
- **it's all bits at the bottom**
  - a bit is a "binary digit", that is, a number that is either 0 or 1
  - computers ultimately represent and process everything as bits
- **groups of bits represent larger things**
  - numbers, letters, words, names, pictures, sounds, instructions, ...
  - the interpretation of a group of bits depends on their context
  - the representation is arbitrary; standards (often) define what it is
- **the number of digits used in the representation determines how many different things can be represented**
  - number of values = $\text{base}^{\text{number of digits}}$
  - e.g., 10^2 , 2^{10}