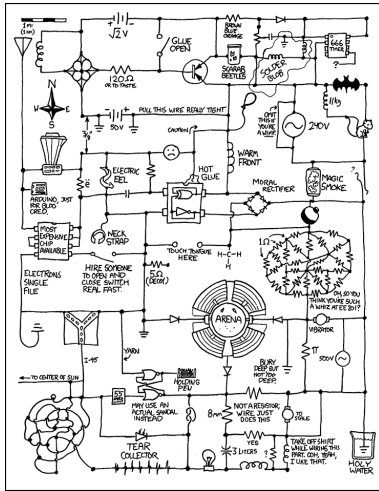


Let's build a computer!

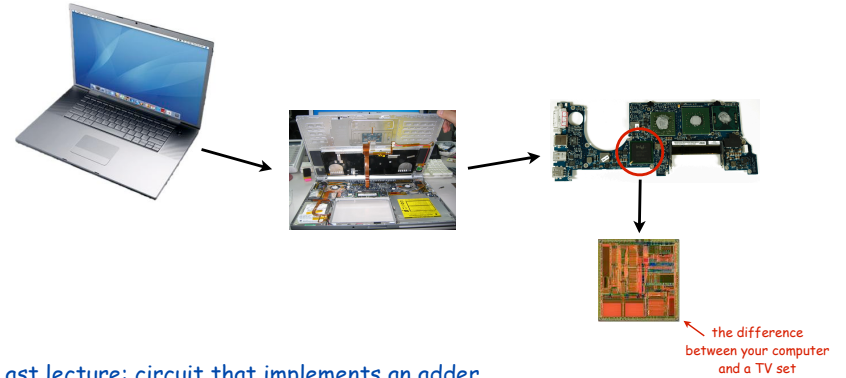
## Designing a CPU



Introduction to Computer Science · Robert Sedgewick and Kevin Wayne · Copyright © 2008 · <http://www.cs.Princeton.EDU/IntroCS>

CPU: "central processing unit"

computer: CPU + display + optical disk + metal case + power supply + ...



Last lecture: circuit that implements an adder

This lecture: circuit that implements a CPU

### TOY Lite

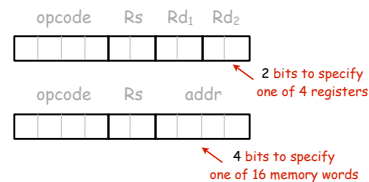
#### TOY machine.

- 256 16-bit words of memory.
- 16 16-bit registers.
- 1 8-bit program counter.
- 2 instruction types
- 16 instructions.



#### TOY-Lite machine.

- 16 10-bit words of memory.
- 4 10-bit registers.
- 1 4-bit program counter.
- 2 instruction types
- 16 instructions.



Goal: CPU circuit for TOY-Lite (same design extends to TOY, your computer)

### Primary Components of Toy-Lite CPU

✓ Arithmetic and Logic Unit (ALU)

Memory

Toy-Lite Registers

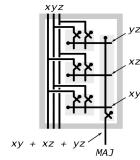
Processor Registers: Program Counter and Instruction Register

"Control"

## A New Ingredient: Circuits With Memory

### Combinational circuits.

- Output determined solely by inputs.
- Ex: majority, adder, decoder, MUX, ALU.

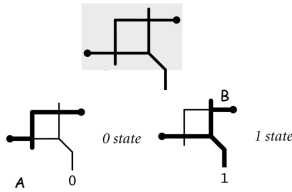


### Sequential circuits.

- Output determined by inputs and current "state".
- Ex: memory, program counter, CPU.

### Ex. Simplest feedback loop.

- Two controlled switches A and B, both connected to power, each blocked by the other.
- State determined by whichever switches first.
- Stable.



### Aside. Feedback with an odd number of switches is a **buzzer** (not stable).

Doorbell: buzzer made with relays.



5

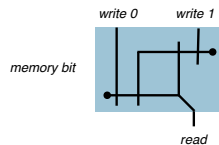
## Memory Overview

### Computers and TOY have several memory components.

- Program counter and other processor registers.
- TOY registers (4 10-bit words in Toy-Lite).
- Main memory (16 10-bit words in Toy-Lite).

### Implementation.

- Use one flip-flop for each bit of memory.
- Use buses and multiplexers to group bits into words.



### Access mechanism: when are contents available?

- Processor registers: enable write.
- Main memory: select and enable write.
- TOY register: dual select and enable write

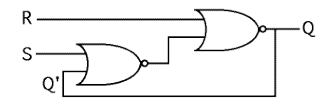
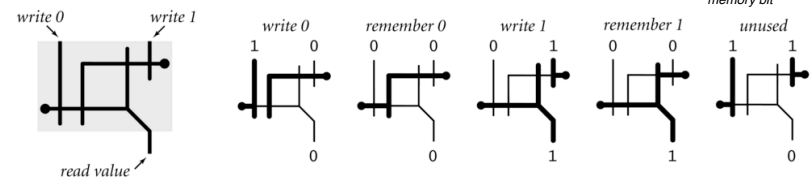
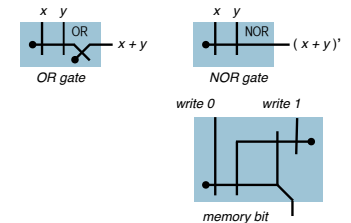
need to be able to read two registers at once

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## SR Flip-Flop

### SR Flip-flop.

- Two cross-coupled NOR gates
- A way to control the feedback loop.
- Abstraction that "remembers" one bit.
- Basic building block for memory and registers.

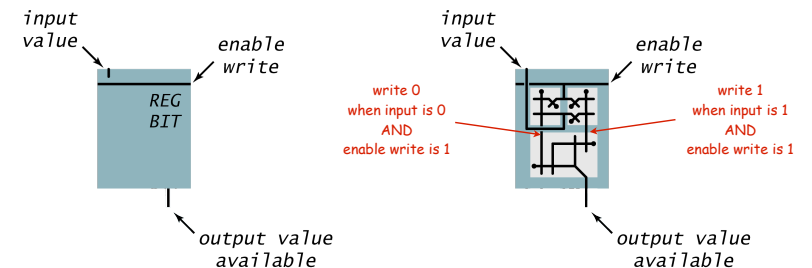


**Caveat.** Timing, switching delay.

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## Processor register Bit

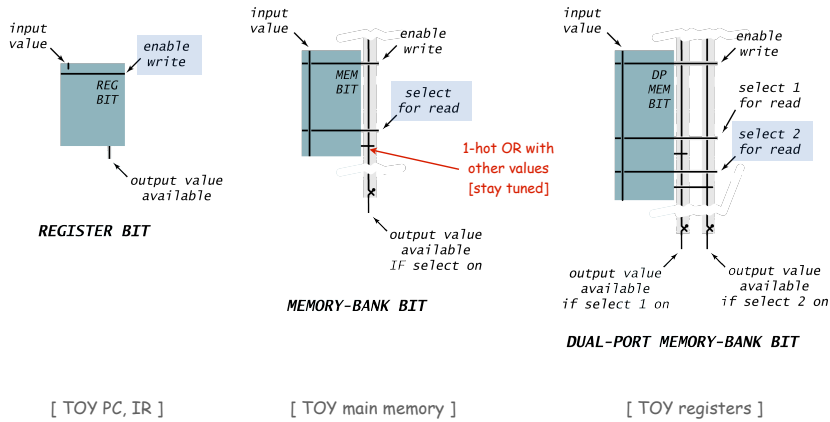
### Processor register bit. Extend a flip-flop to allow easy access to values.



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## Memory Bit Interface

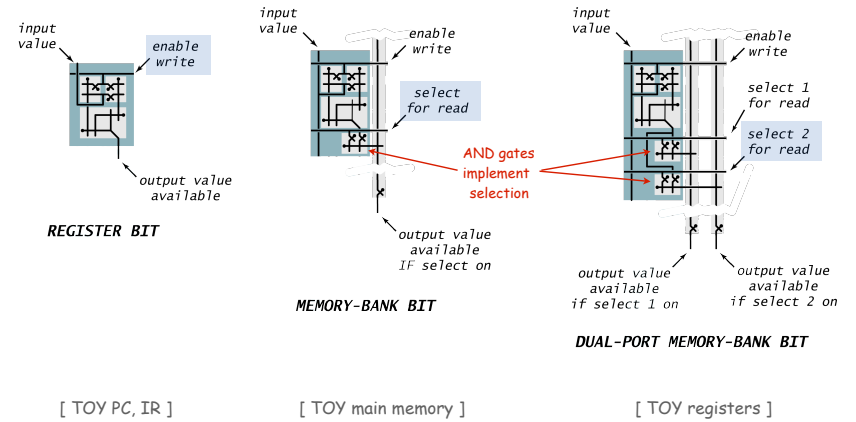
Memory and TOY register bits: Add selection mechanism.



9

## Memory Bit: Switch Level Implementation

Memory and TOY register bits: Add selection mechanism.



10

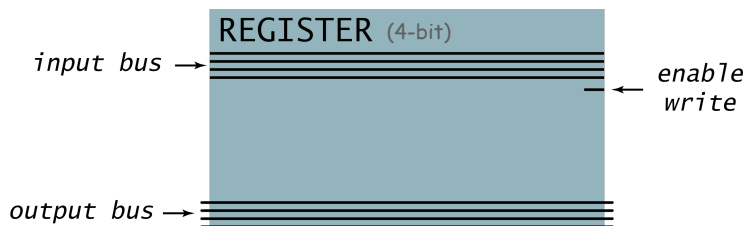
## Processor Register

Processor register. ← don't confuse with TOY register

- Stores k bits.
- Register contents always available on output bus.
- If enable write is asserted, k input bits get copied into register.

Ex 1. TOY-Lite program counter (PC) holds 4-bit address.

Ex 2. TOY-Lite instruction register (IR) holds 10-bit current instruction.



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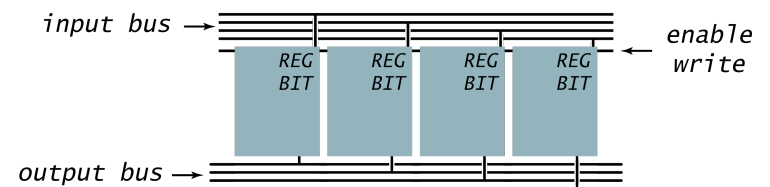
## Processor Register

Processor register. ← don't confuse with TOY register

- Stores k bits.
- Register contents always available on output bus.
- If enable write is asserted, k input bits get copied into register.

Ex 1. TOY program counter (PC) holds 8-bit address.

Ex 2. TOY instruction register (IR) holds 16-bit current instruction.



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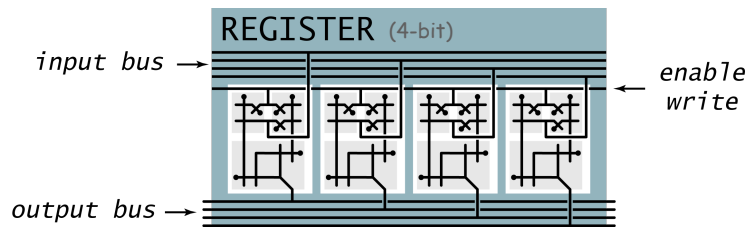
## Processor Register

**Processor register.** — don't confuse with TOY register

- Stores  $k$  bits.
- Register contents always available on output bus.
- If enable write is asserted,  $k$  input bits get copied into register.

**Ex 1.** TOY program counter (PC) holds 8-bit address.

**Ex 2.** TOY instruction register (IR) holds 16-bit current instruction.



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## Memory Bank

**Memory bank.**

- Bank of  $n$  registers; each stores  $k$  bits.
- Read and write information to one of  $n$  registers.
- Address inputs specify which one. —  $\log_2 n$  address bits needed
- Addressed bits always appear on output.
- If write enabled,  $k$  input bits are copied into addressed register.

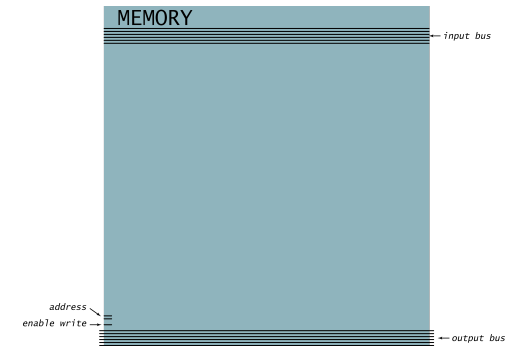
**Ex 0 (for lecture).** 4-by-6  
(four 6-bit words)

**Ex 1.** Main memory bank.

- TOY: 256-by-16
- TOY-Lite: 16-by-10

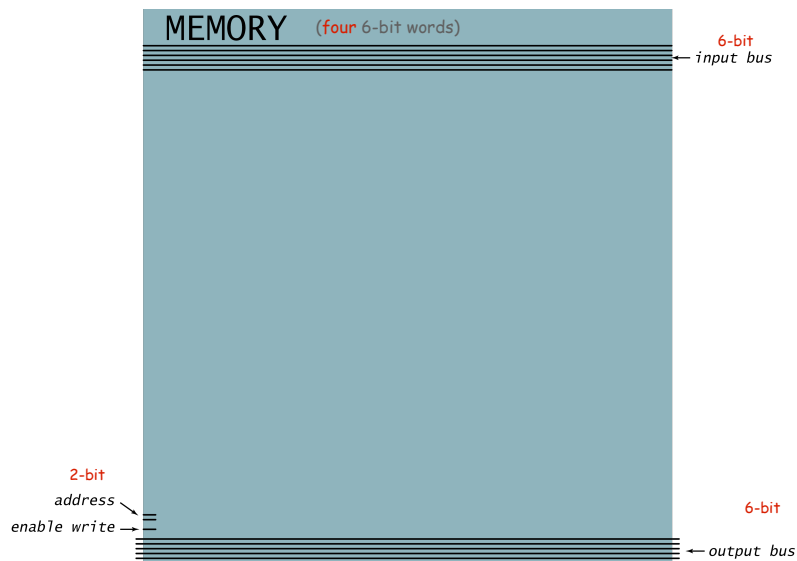
**Ex 2.** Registers.

- TOY: 16-by-16
- TOY Lite: 4-by-10
- Two output buses.



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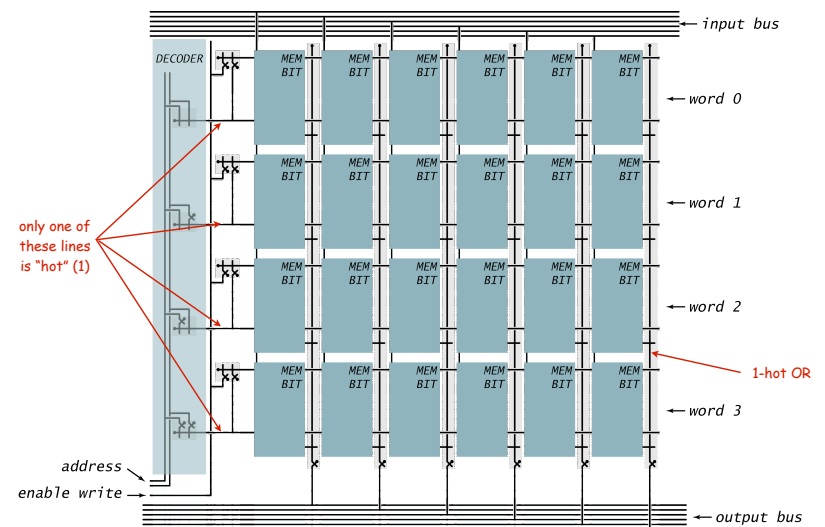
## Memory: Interface



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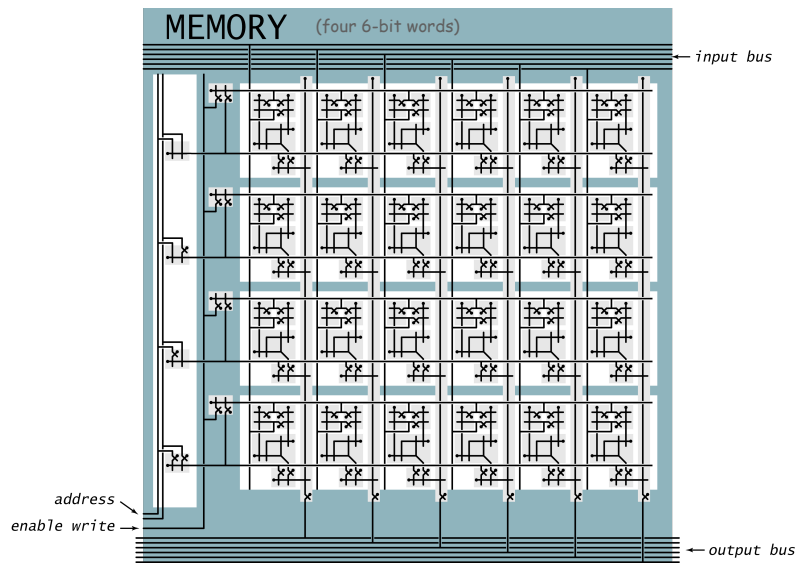
## Memory: Component Level Implementation

**Decoder plus memory selection: connect only to addressed word.**



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## Memory: Switch Level Implementation

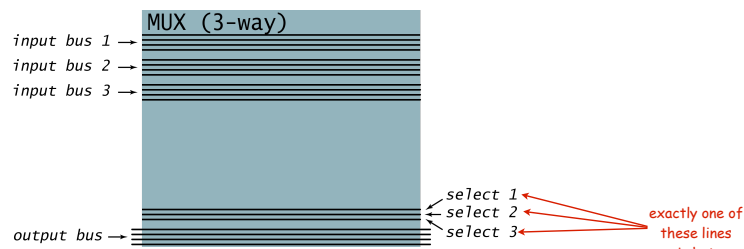


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## Another Useful Combinational Circuit: Multiplexer

**Multiplexer (MUX).** Combinational circuit that selects among input buses.

- Exactly one select line  $i$  is activated.
- Copies bits from input bus  $i$  to output bus.

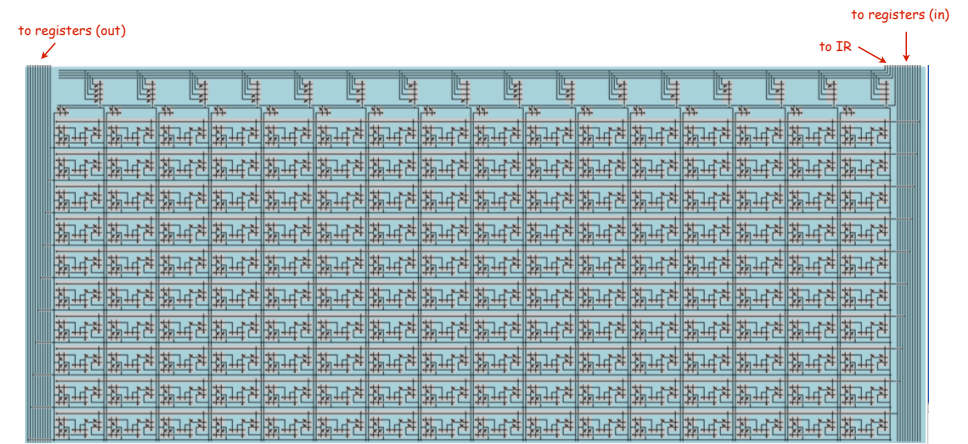


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## TOY-Lite Memory

16 10-bit words

- input connected to registers for "store"
- output connected to registers for "load"
- addr connect to processor Instruction Register (IR)

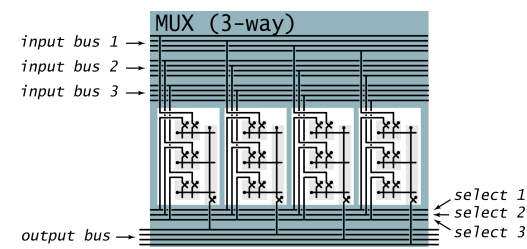


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## Nuts and Bolts: Buses and Multiplexers

**Multiplexer (MUX).** Combinational circuit that selects among input buses.

- Exactly one select line  $i$  is activated.
- Copies bits from input bus  $i$  to output bus.

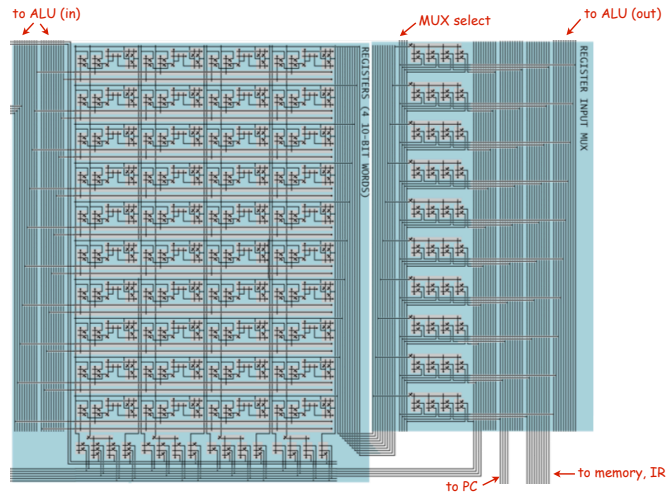


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## Toy-Lite Registers

### 4 10-bit words

- Dual-ported to support connecting two different registers to ALU
- Input MUX to support input connection to ALU, memory, IR, PC



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## Primary Components of Toy-Lite CPU

- ✓ ALU
  - ✓ Memory
  - ✓ Registers
  - ✓ Processor Registers: Program Counter and Instruction Register
- "Control"

Not quite done.  
Need to be able to increment.

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## How To Design a Digital Device

### How to design a digital device.

- Design **interface**: input buses, output buses, control wires.
- Determine **components**.
- Determine **datapath** requirements: "flow" of bits.
- Establish **control sequence**.

**Warmup.** Design a program counter (3 devices, 3 control wires).

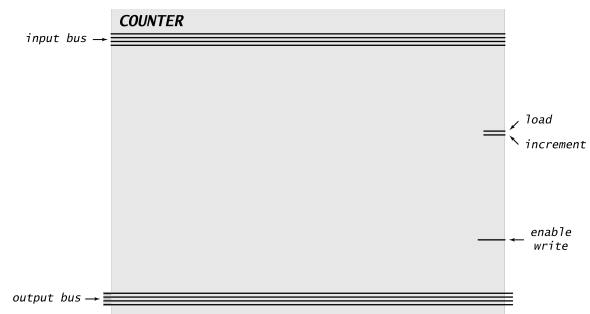
**Goal.** Design TOY-Lite computer (10 devices, 27 control wires).

## Program Counter: Interface

**Counter.** Holds value that represents a binary number.

- Load: set value from input bus.
- Increment: add one to value.
- Enable Write: make value available on output bus.

**Ex.** TOY-Lite program counter (4-bit).



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## Program Counter: Components

### Components.

- Register.
- Incrementer.
- Multiplexer (to provide connections for both load and increment).

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## Program Counter: Datapath and Control

### Datapath.

- Layout and interconnection of components.
- Connect input and output buses.

**Control.** Choreographs the "flow" of information on the datapath.

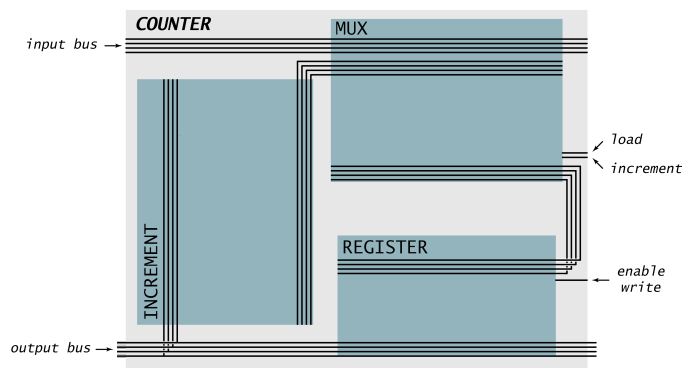
26

## Program Counter: Datapath and Control

### Datapath.

- Layout and interconnection of components.
- Connect input and output buses.

**Control.** Choreographs the "flow" of information on the datapath.



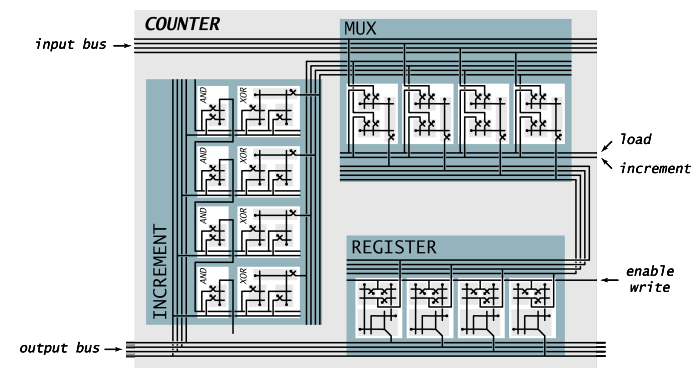
27

## Program Counter: Datapath and Control

### Datapath.

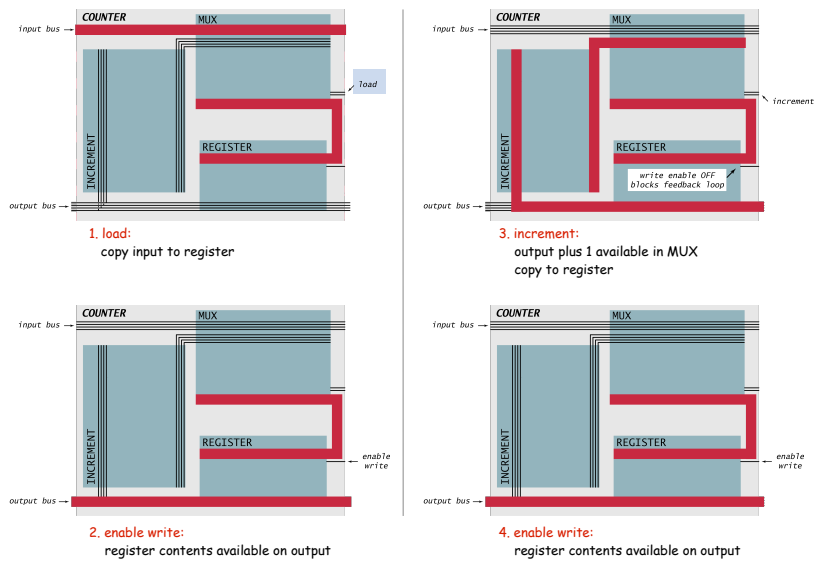
- Layout and interconnection of components.
- Connect input and output buses.

**Control.** Choreographs the "flow" of information on the datapath.



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## Program Counter: Datapath and Control



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## Primary Components of Toy-Lite CPU

- ✓ ALU
- ✓ Memory
- ✓ Toy-Lite Registers
- ✓ Processor Registers: Program Counter and Instruction Register

"Control"

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## How To Design a Digital Device

### How to design a digital device.

- Design **interface**: input buses, output buses, control wires.
- Determine **components**.
- Determine **datapath** requirements: "flow" of bits.
- Establish **control sequence**.

Warmup. Design a program counter (3 devices, 3 control wires).

**Next.** Design TOY-Lite computer (10 devices, 27 control wires).

## TOY-Lite: Interface

CPU is a circuit.

Interface: switches and lights.

- set memory contents
- set PC value
- press RUN
- [details of connection to circuit omitted]

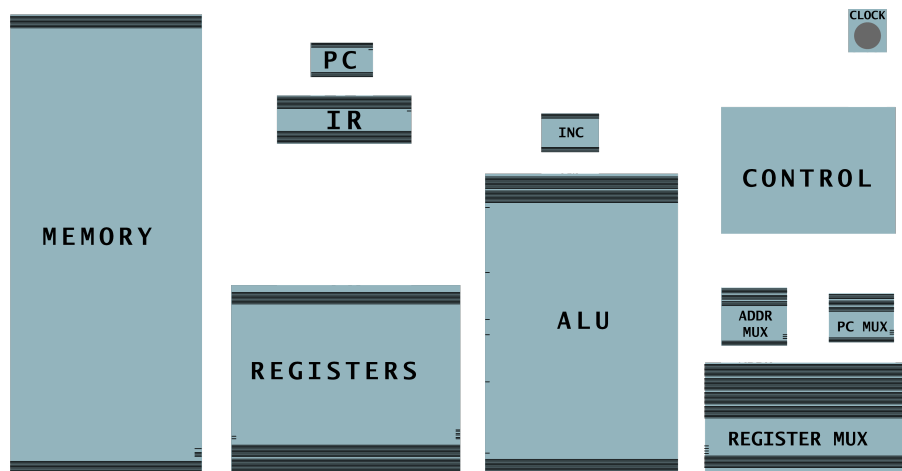


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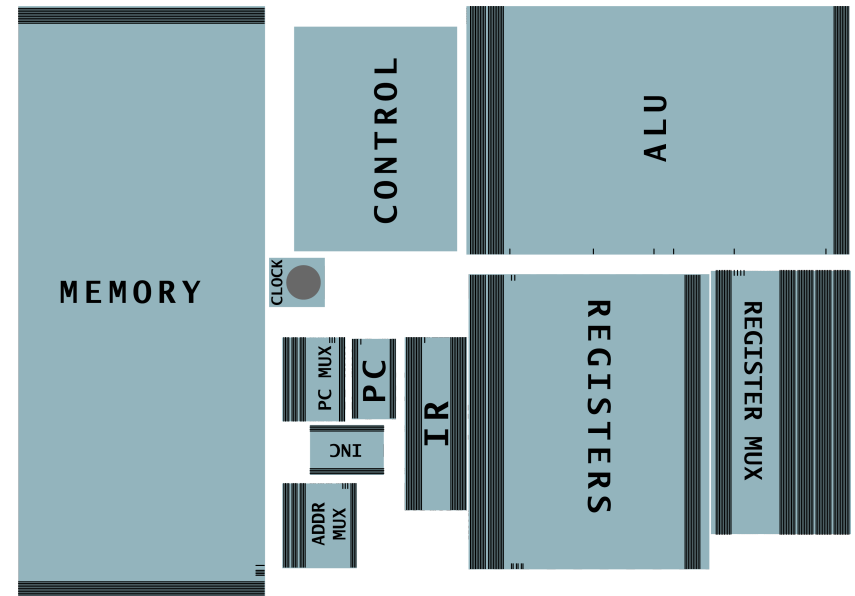


## TOY-Lite: Components



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## TOY-Lite: Layout



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## TOY-Lite Datapath Requirements: Fetch

Basic machine operation is a cycle.

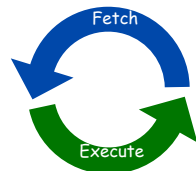
- Fetch
- Execute

### Fetch.

- Memory[PC] to IR
- Increment PC

### Execute.

- Datapath depends on instruction



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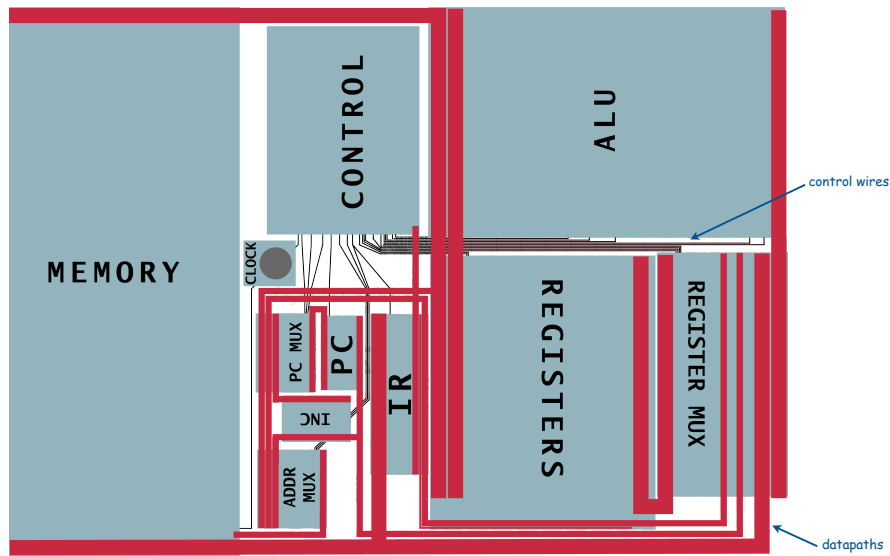
## TOY-Lite Datapath Requirements: Execute

Instructions determine datapaths and control sequences for execute

		...
0	halt	...
1	add	IR opcode to control control to ALU two registers to ALU ALU to register MUX
2	subtract	
3	and	
4	xor	
5	shift left	
6	shift right	
7	load address	...
8	load	...
9	store	...
A	load indirect	...
B	store indirect	...
C	branch zero	...
D	branch positive	
E	jump register	
F	jump and link	

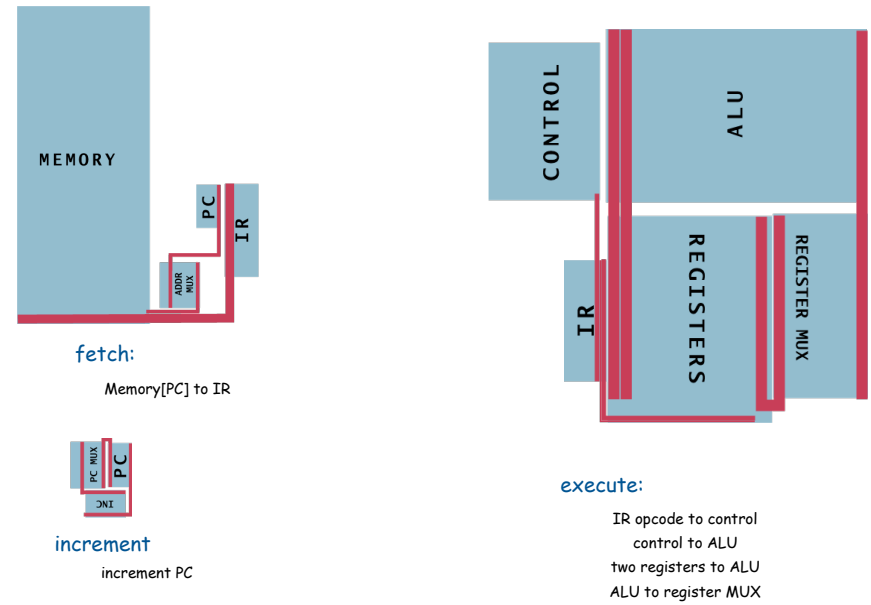
36

# TOY-Lite: Datapaths and Control



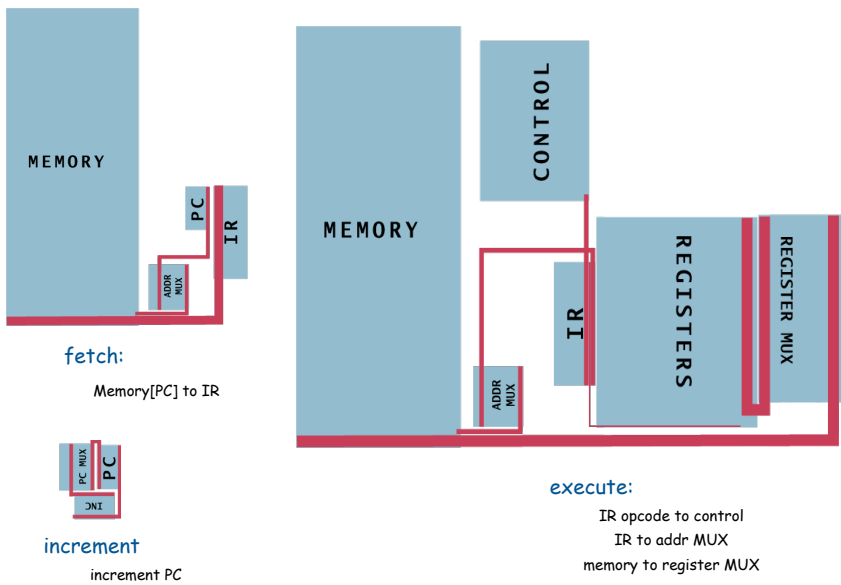
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# Datapath: Add



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# Datapath: Load



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# Last step

**Control.** Each instruction corresponds to a **sequence** of control signals.

**Q.** How do we create the sequence?

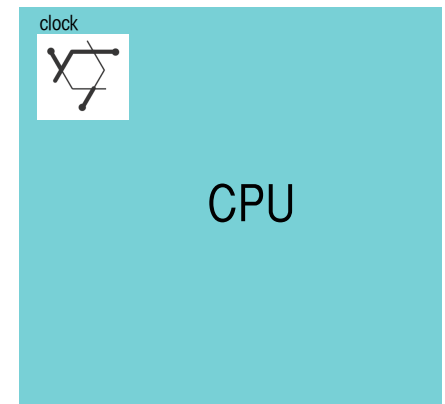
**A.** Need a "physical" clock.

**Solution 2:** Use a buzzer [need sufficiently long cycle to cover CPU switching]

**Solution 1:** Use some other technology



CPU



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## Clock

### Clock.

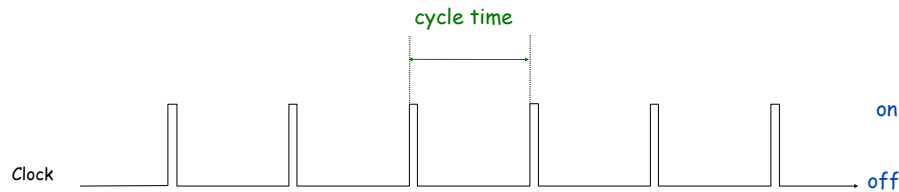
- Fundamental abstraction: regular on-off pulse.
  - on: fetch phase
  - off: execute phase
- "external" device.
- Synchronizes operations of different circuit elements.
- Requirement: clock cycle longer than max switching time.

Solution 3P

Fetch



Execute



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## How much does it Hertz?

### Frequency is inverse of cycle time.

- Expressed in hertz.
- Frequency of 1 Hz means that there is 1 cycle per second.
  - 1 kilohertz (kHz) means 1000 cycles/sec.
  - 1 megahertz (MHz) means 1 million cycles/sec.
  - 1 gigahertz (GHz) means 1 billion cycles/sec.
  - 1 terahertz (THz) means 1 trillion cycles/sec.



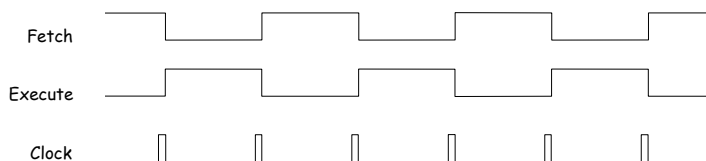
Heinrich Rudolf Hertz  
(1857-1894)

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## Clocking Methodology

### Two-cycle design.

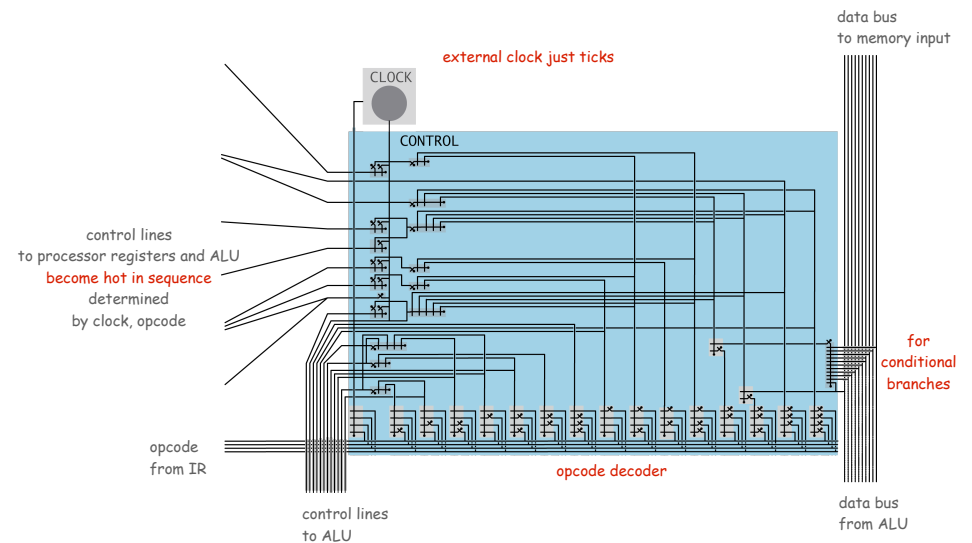
- Each control signal is in one of four epochs.
  - fetch [set memory address from pc]
  - fetch and clock [write instruction to IR]
  - execute [set ALU inputs from registers]
  - execute and clock [write result of ALU to registers]



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## One Last Combinational Circuit: Control

### Control. Circuit that determines control line sequencing.



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## Tick-Tock

CPU is a circuit, driven by a clock.

Switches initialize memory, PC contents

Clock ticks

- **fetch** instruction from memory[PC] to IR
- **increment** PC
- **execute** instruction

[details of instruction execution differ]

- **fetch** next instruction
- ...

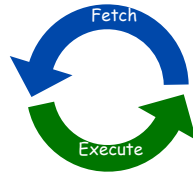
That's all there is to it!



Fetch

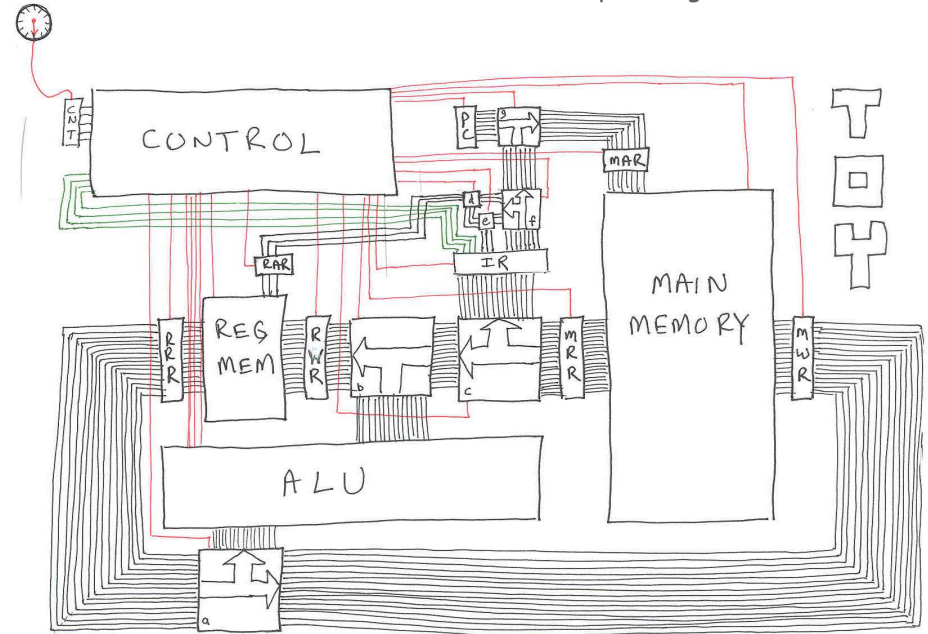


Execute



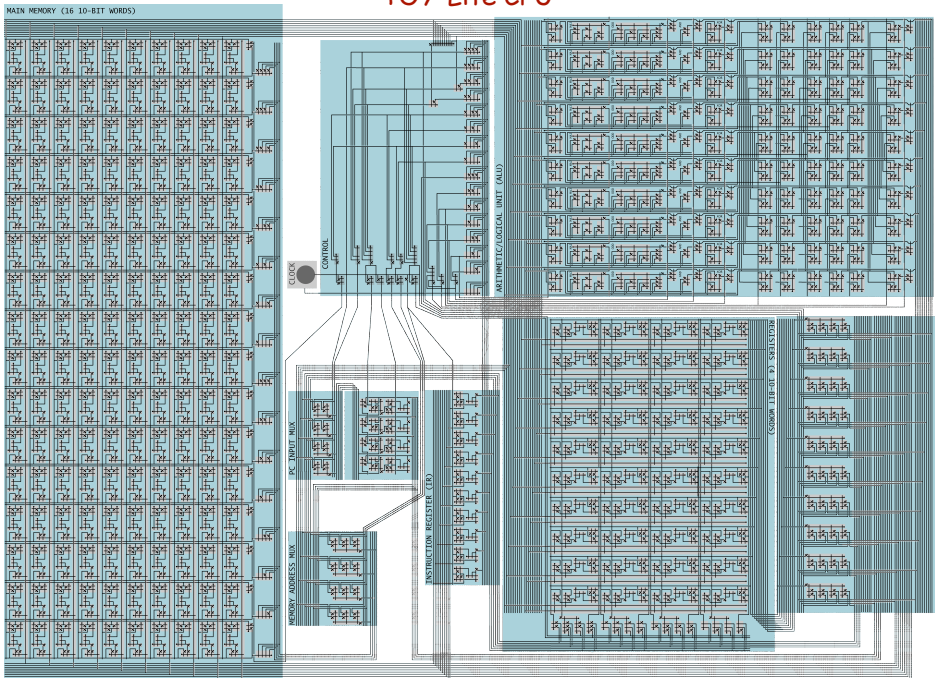
45

## TOY "Classic", Back Of Envelope Design



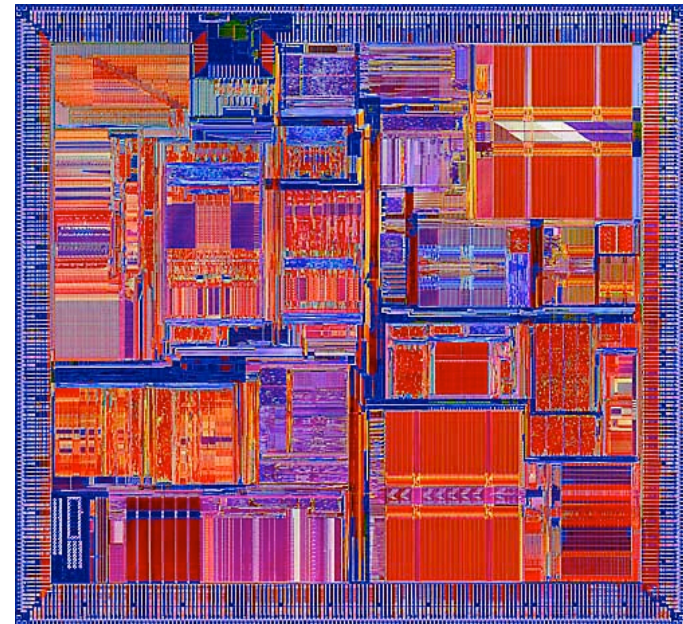
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## TOY-Lite CPU



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## Real Microprocessor (MIPS R1000)



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## Layers of Abstraction

Abstraction	Built From	Examples
Abstract Switch	raw materials	transistor, relay
Connector	raw materials	wire
Clock	raw materials	crystal oscillator
Logic Gates	abstract switches, connectors	AND, OR, NOT
Combinational Circuit	logic gates, connectors	decoder, multiplexer, adder
Sequential Circuit	logic gates, clock, connector	flip-flop
Components	decoder, multiplexer, adder, flip-flop	registers, ALU, counter, control
Computer	components	TOY

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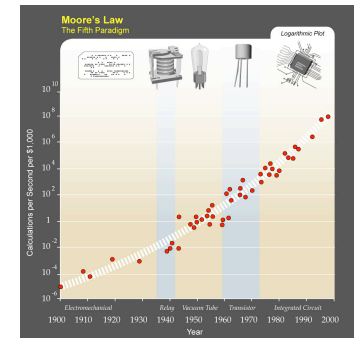
## History + Future

Computer constructed by layering abstractions.

- Better implementation at low levels improves **everything**.
- Ongoing search for better abstract switch!

History.

- 1820s: mechanical switches.
- 1940s: relays, vacuum tubes.
- 1950s: transistor, core memory.
- 1960s: integrated circuit.
- 1970s: microprocessor.
- 1980s: VLSI.
- 1990s: integrated systems.
- 2000s: web computer.
- Future: quantum, optical soliton, ...



Ray Kurzweil  
<http://en.wikipedia.org/wiki/Image:PP2MooreLaw1.jpg>

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