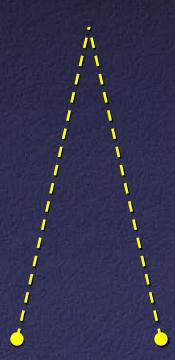
## Multiview Reconstruction

#### Why More Than 2 Views?

#### Baseline

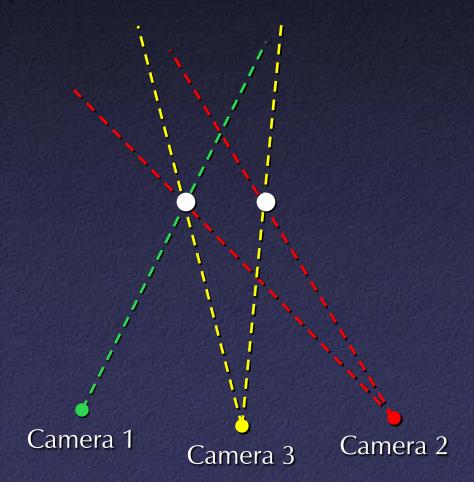
- Too short low accuracy
- Too long matching becomes hard





#### Why More Than 2 Views?

Ambiguity with 2 views



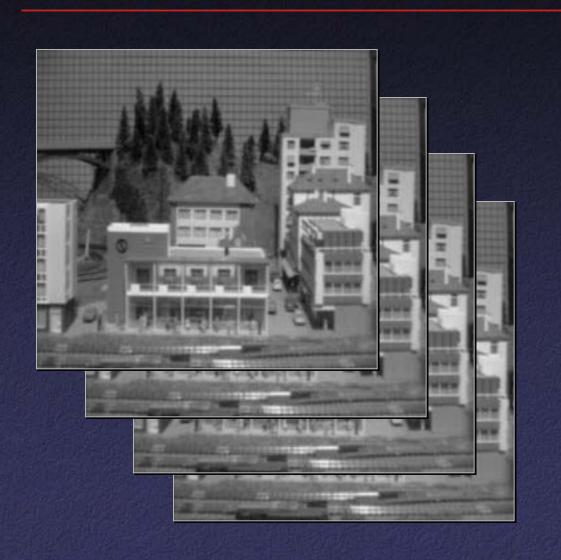
#### Trinocular Stereo

- Straightforward approach to eliminate bad correspondences
  - Pick 2 views, find correspondences
  - For each matching pair, reconstruct 3D point
  - Project point into 3<sup>rd</sup> image
  - If can't find correspondence near predicted location, reject

#### Trinocular Stereo

- Trifocal geometry: relations between points in three camera views
- Trifocal tensor: analogue of essential matrix
  - 3x3x3 trilinear tensor (3D cube of numbers)
  - Given lines in 2 views, predict lines in the 3<sup>rd</sup>

- Slightly different algorithm for n cameras:
- Pick one reference view
- For each candidate depth
  - Compute sum of squared differences to all other views, assuming correct disparity for view
- Resolves ambiguities: only correct depths will "constructively interfere"



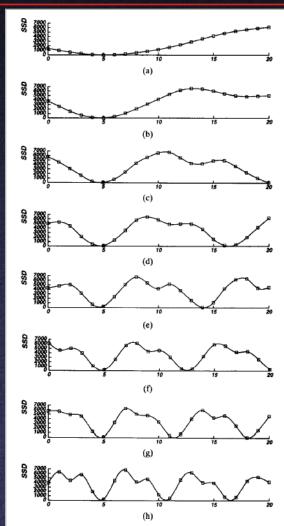
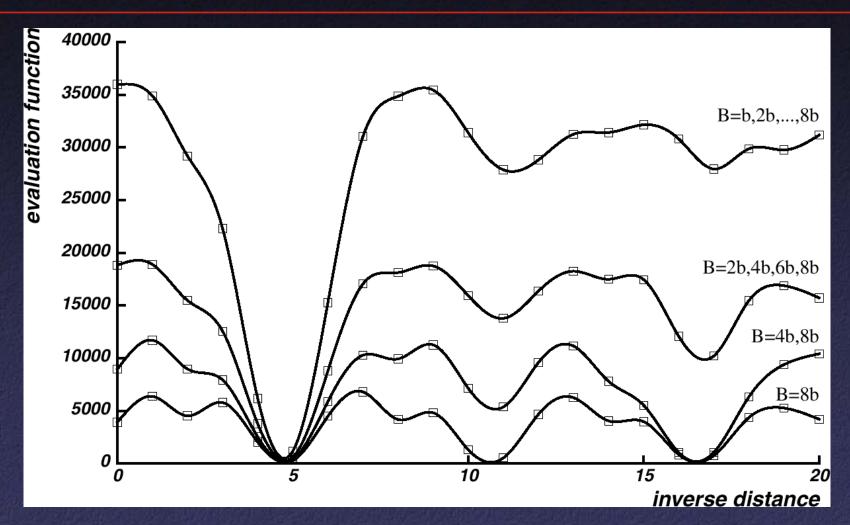
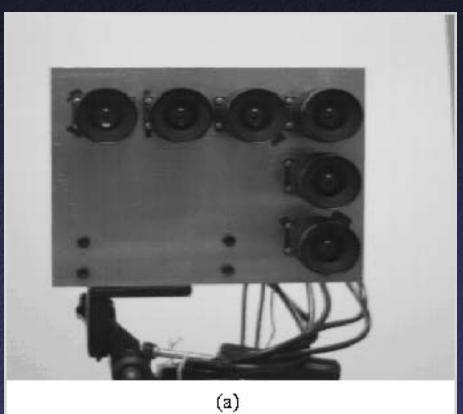


Fig. 5. SSD values versus inverse distance: (a) B=b; (b) B=2b; (c) B=3b; (d) B=4b; (e) B=5b; (f) B=6b; (g) B=7b; (h) B=8b. The horizontal axis is normalized such that 8bF=1.



### Multibaseline Stereo Reconstruction









(b)

Figure 7: The CMU Video-Rate Stereo Machine Prototype System: (a) camera head; (b) processor boards

#### Problems with Multibaseline Stereo

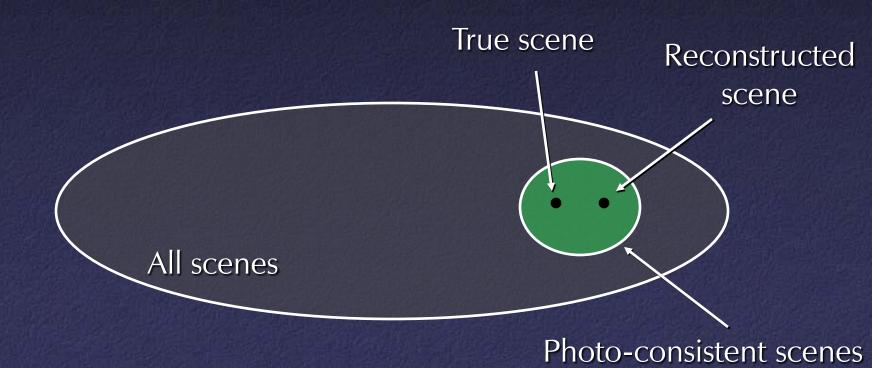
- Have to pick a reference view
- Occlusion
  - With many cameras / large baseline, occlusion becomes likely
  - Contributes incorrect values to error function

#### Volumetric Multiview Approaches

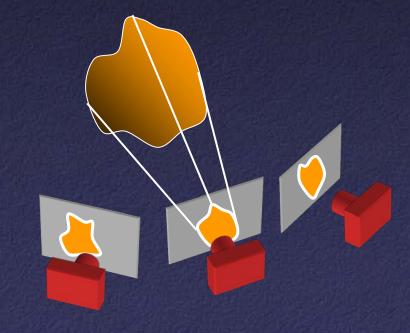
- Goal: find a model consistent with images
- "Model-centric" (vs. image-centric)
- Typically use discretized volume (voxel grid)
- For each voxel, compute occupied / free (for some algorithms, also color, etc.)

#### Photo Consistency

- Result: not necessarily correct scene
- Many scenes produce the same images

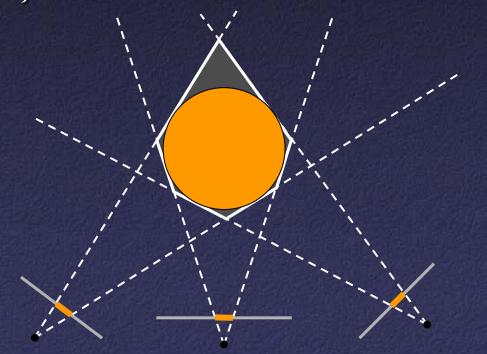


- Find silhouettes in all images
- Exact version:
  - Back-project all silhouettes, find intersection



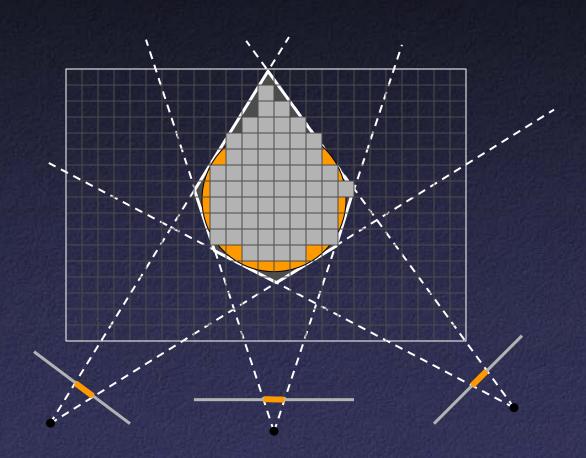
Binary Images —

- Find silhouettes in all images
- Exact version:
  - Back-project all silhouettes, find intersection



- Limit of silhouette carving is *visual hull* or *line hull*
- Complement of lines that don't intersect object
- In general not the same as object
  - Can't recover "pits" in object
- Not the same as convex hull

- Discrete version:
  - Loop over all voxels in some volume
  - If projection into images lies inside all silhouettes, mark as occupied
  - Else mark as free



### Voxel Coloring

- Seitz and Dyer, 1997
- In addition to free / occupied, store color at each voxel
- Explicitly accounts for occlusion

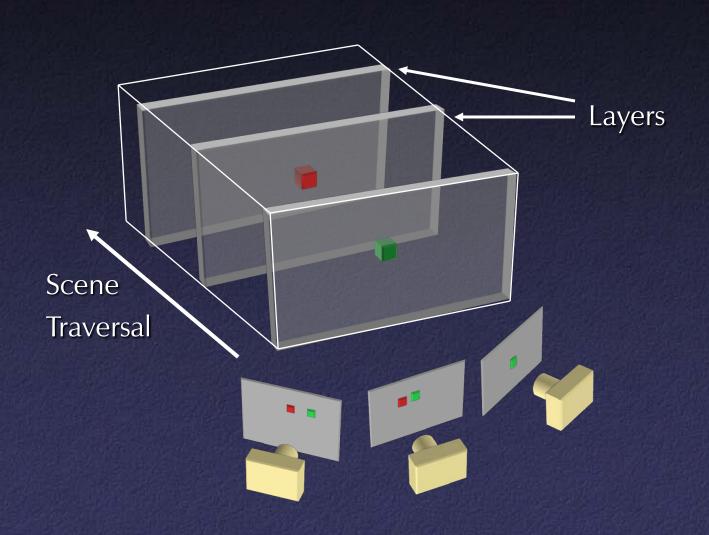
#### Voxel Coloring

- Basic idea: sweep through a voxel grid
  - Project each voxel into each image in which it is visible
  - If colors in images agree, mark voxel with color
  - Else, mark voxel as empty
- Agreement of colors based on comparing standard deviation of colors to threshold

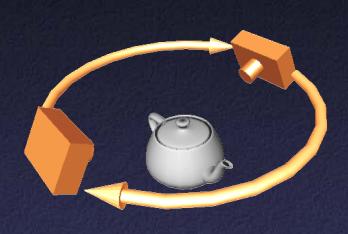
#### Voxel Coloring and Occlusion

- Problem: which voxels are visible?
- Solution, part 1: constrain camera views
  - When a voxel is considered, necessary occlusion information must be available
  - Sweep occluders before occludees
  - Constrain camera positions to allow this sweep

# Voxel Coloring Sweep Order

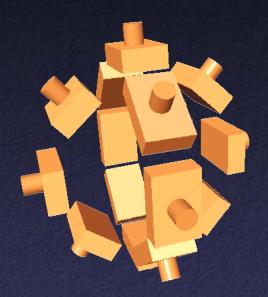


### Voxel Coloring Camera Positions



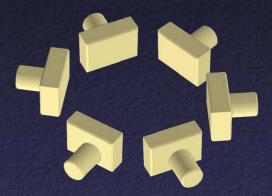
Inward-looking

<u>Cameras above scene</u>

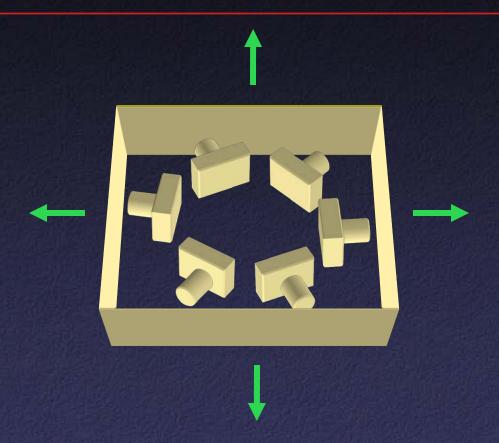


Outward-looking

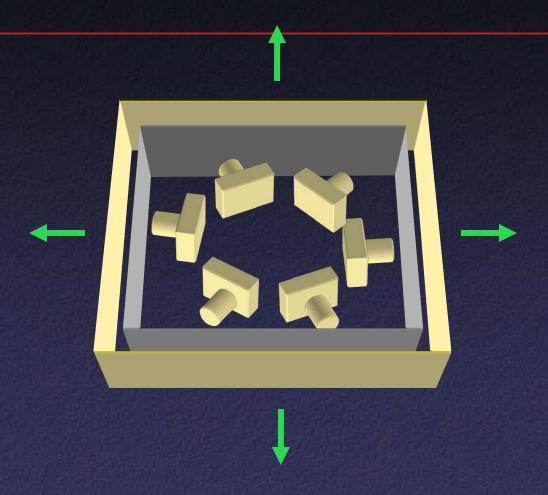
Cameras inside scene



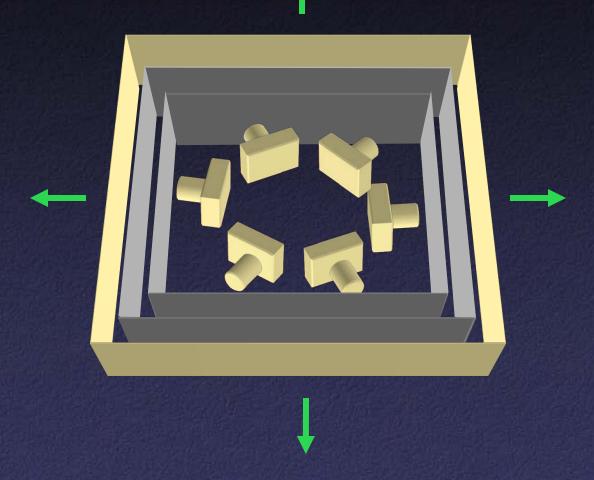
- Cameras oriented in many different directions
- Planar depth ordering does not apply



Layers radiate outwards from cameras



Layers radiate outwards from cameras



Layers radiate outwards from cameras

### Voxel Coloring and Occlusion

- Solution, part 2: per-image mask of which pixels have been used
  - Each pixel only used once
  - Mask filled in as sweep progresses

# Image Acquisition





Selected Dinosaur Images





Selected Flower Images



- Calibrated Turntable
- ■360° rotation (21 images)

## Voxel Coloring Results



Dinosaur Reconstruction
72 K voxels colored
7.6 M voxels tested
7 min. to compute
on a 250MHz SGI



Flower Reconstruction
70 K voxels colored
7.6 M voxels tested
7 min. to compute
on a 250MHz SGI

#### Voxel Coloring Results

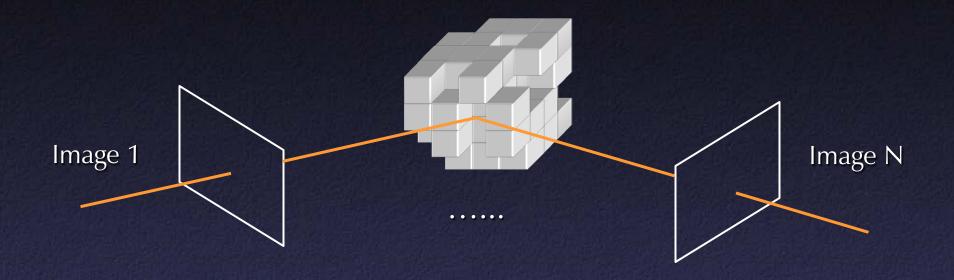
- With texture: good results
- Without texture: regions tend to "bulge out"
  - Voxels colored at earliest time at which projection into images is consistent
  - Model good for re-rendering: image will look correct for viewpoints near the original ones

## Limitations of Voxel Coloring



- A view-independent depth order may not exist
- Need more powerful general-case algorithms
  - Unconstrained camera positions
  - Unconstrained scene geometry/topology

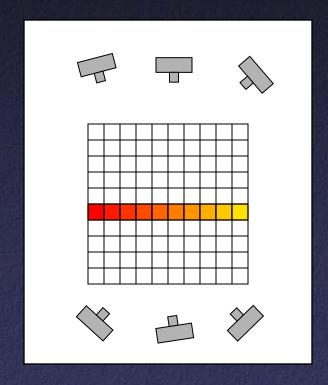
### Space Carving



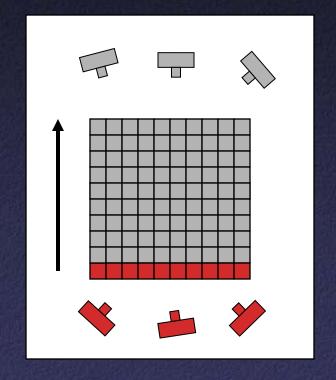
Initialize to a volume V containing the true scene Choose a voxel on the current surface Project to visible input images Carve if not photo-consistent Repeat until convergence

Kutulakos & Seitz

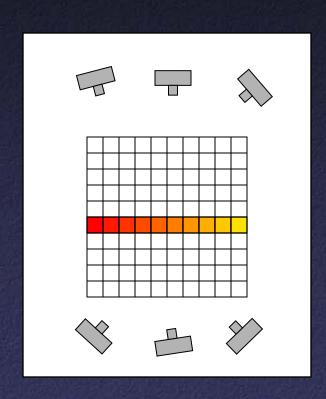
- Faster alternative:
  - Sweep plane in each of 6 principal directions
  - Consider cameras on only one side of plane
  - Repeat until convergence

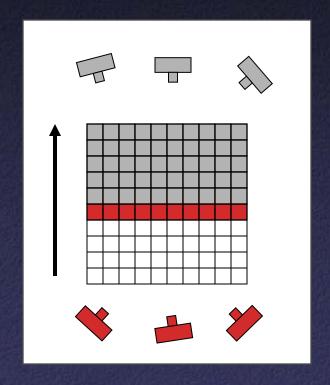


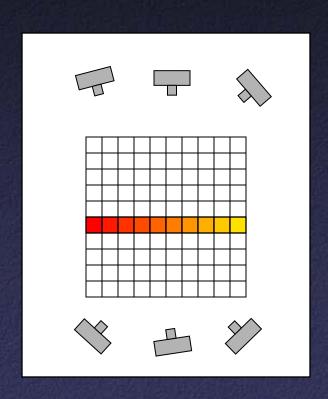
True Scene

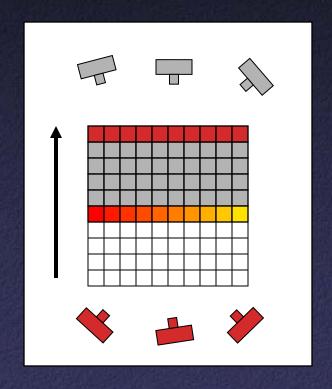


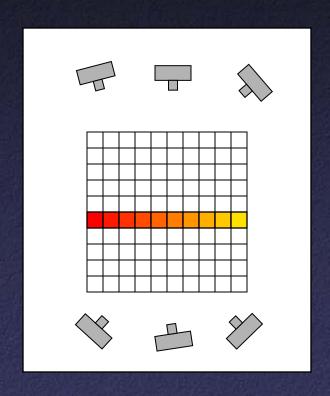
Reconstruction

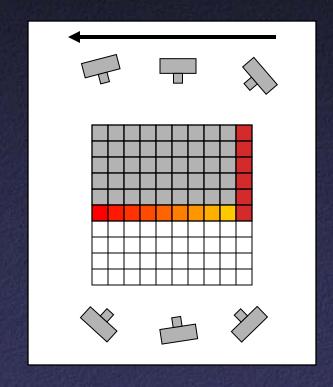


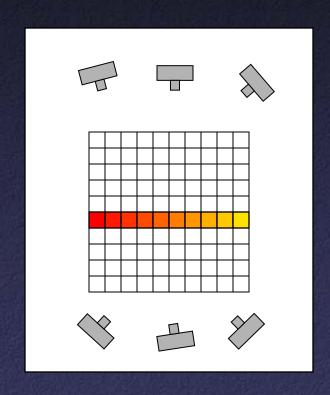


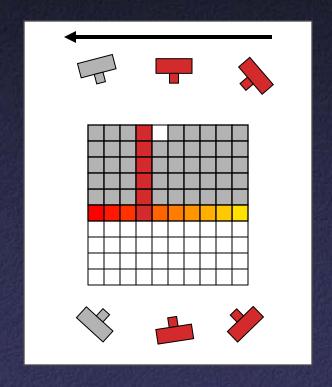


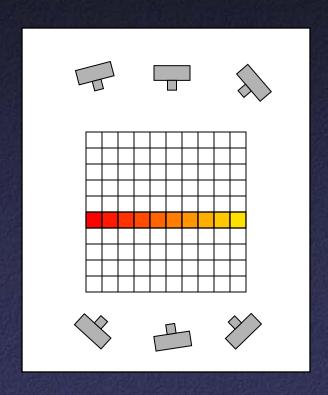


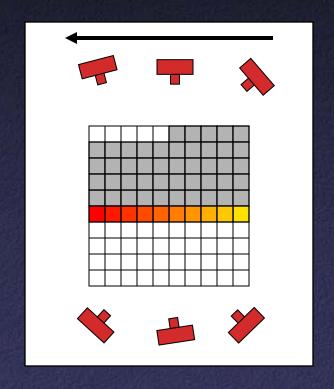












# Space Carving Results: African Violet



Input Image (1 of 45)



Reconstruction



Reconstruction



Reconstruction

# Space Carving Results: Hand



Input Image (1 of 100)





Views of Reconstruction