

Exam 1 Solutions

1. Loops and conditionals. (5 points)

```
*****
*+*+*
*****
```

2. Recursion, debugging (6 points)

(a)

```
      func(3)
      |
    2*func(2) + 5*func(1)
      |
    2*func(1) + 5*func(0)
      |
    2*func(-1) + 5*func(-2)
```

(b)

Change “if (j==1) return 1;” to “if (j<=1) return 1;”

3. Arrays. (7 points)

(a)

7942

(b)

{0, 2, 4, 6, 9, 7, 8, 1, 5, 3};

4. Recursion: (9 points)

(a)

```
System.out.println(ping(2));    false
System.out.println(pong(4));   true
```

(b)

ping(n) tells if n is odd and pong(n) tells if n is even.

- (c) stack overflow
- (d) if $(n < 0)$ $n = -n$;
- (e) -1 is represented as $(2^n - 1)$ in 2's complement. $(2^n - 1)$ is odd regardless of the number n of bits. Therefore, `pong(-1)` will return false.

5. Number Representations (4 points)

- (a) 012C
- (b) FFC7
- (c) 163
- (d) -32

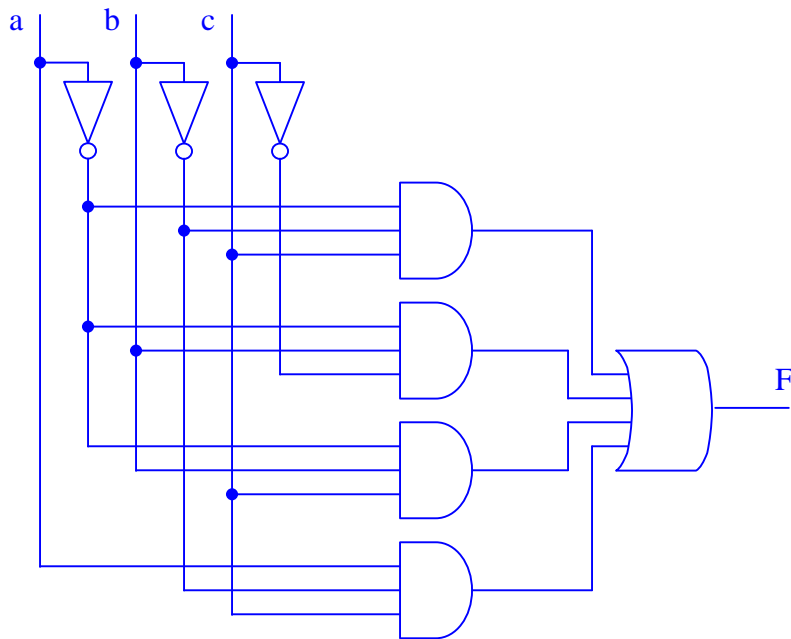
6. Combinational Circuits (8 points)

(a)

a	b	c	F
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	0

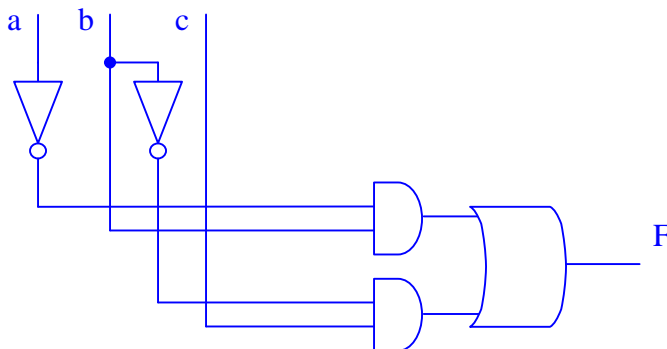
- (b) $F = a'b'c + a'bc' + a'bc + ab'c$

(c)



(d) For a tiny amount of extra credit, simplify the formula and the circuit.

$$F = a\bar{b} + b\bar{c}$$



7. TOY programming (9 points)

(a)

```

1110      R[1] <- R[1] + R[0]
2110      R[1] <- R[1] - R[0]
D010      if (R[0] > 0 ) PC <- 10
3111      R[1] <- R[1] & R[1]
    
```

(b)

(b.1)

```

10: 7101    R[1] <- 01
11: 884F    R[8] <- mem[4F]
12: 7250
13: 1328    R[3] <- R[2] + R[8]
14: 2331    R[3] <- R[3] - R[1]
15: 2423    R[4] <- R[2] - R[3]
16: D41E    if (R[4] > 0) PC <- 1E
17: A502    R[5] <- mem[R[2]]
18: A603
19: B503    mem[R[3]] <- R[5]
1A: B602
1B: 1221    R[2] <- R[2] + R[1]
1C: 2331    R[3] <- R[3] - R[1]
1D: C015    if (R[0] == 0) PC <- 15
1E: 0000    halt

4F: 0005
50: 1141
51: 092C
52: 0653
53: 1EAD
54: 0EEF

```

(b.2)

It reverses the array.

```

4F: 0005          length of array
50: 0EEF          first array element
51: 1EAD
52: 0653
53: 092C
54: 1141          last array element

```