



# Representations

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COS 217



## Goals of Today's Lecture

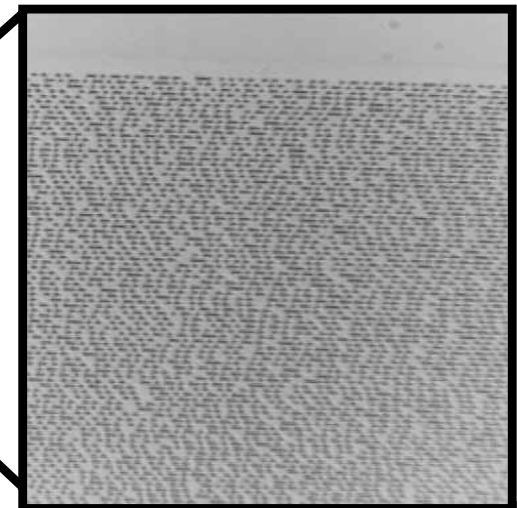
- **Representations**
  - Why binary?
  - Converting base 10 to base 2
  - Octal and hexadecimal
- **Integers**
  - Unsigned integers
  - Integer addition, subtraction
  - Signed integers
- **C bit operators**
  - And, or, not, and xor
  - Shift-left and shift-right
  - Function for counting the number of 1 bits
  - Function for XOR encryption of a message



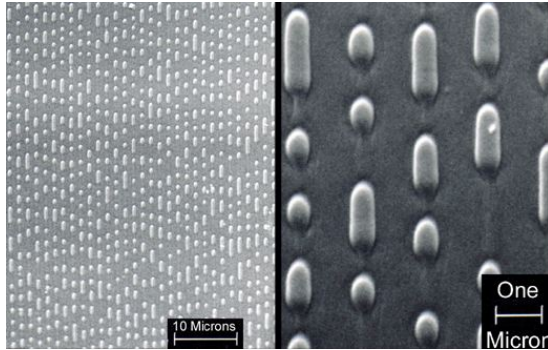
## Radiohead - OK Computer CD



3 Miles of Music

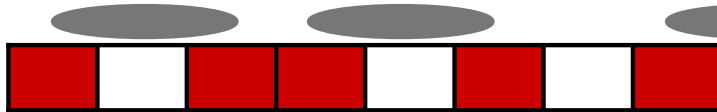


# Pits and Lands

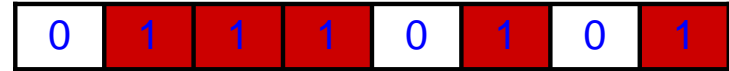


Transition represents a bit state (1/on/red/female/heads)

No change represents other state (0/off/white/male/tails)



# Interpretation



As Music:

$01110101_2 = 117/256$  position of speaker

As Number:

$01110101_2 = 1 + 4 + 16 + 32 + 64 = 117_{10} = 75_{16}$

(Get comfortable with base 2, 8, 10, and 16.)

As Text:

$01110101_2 = 117^{\text{th}}$  character in the ASCII codes = "u"

# Interpretation – ASCII



| ASCII value | Character         | Control character | ASCII value | Character | ASCII value | Character | ASCII value | Character |
|-------------|-------------------|-------------------|-------------|-----------|-------------|-----------|-------------|-----------|
| 000         | (null)            | NUL               | 032         | (space)   | 064         | @         | 096         |           |
| 001         | ☉                 | SOH               | 033         | !         | 065         | A         | 097         | a         |
| 002         | ☼                 | STX               | 034         | "         | 066         | B         | 098         | b         |
| 003         | ▼                 | ETX               | 035         | #         | 067         | C         | 099         | c         |
| 004         | ◆                 | EOT               | 036         | \$        | 068         | D         | 100         | d         |
| 005         | ♣                 | ENQ               | 037         | %         | 069         | E         | 101         | e         |
| 006         | ♠                 | ACK               | 038         | &         | 070         | F         | 102         | f         |
| 007         | (beep)            | BEL               | 039         | '         | 071         | G         | 103         | g         |
| 008         | ■                 | BS                | 040         | (         | 072         | H         | 104         | h         |
| 009         | (tab)             | HT                | 041         | )         | 073         | I         | 105         | i         |
| 010         | (line feed)       | LF                | 042         | *         | 074         | J         | 106         | j         |
| 011         | (home)            | VT                | 043         | +         | 075         | K         | 107         | k         |
| 012         | (form feed)       | FF                | 044         | ,         | 076         | L         | 108         | l         |
| 013         | (carriage return) | CR                | 045         | -         | 077         | M         | 109         | m         |
| 014         | ☺                 | SO                | 046         | .         | 078         | N         | 110         | n         |
| 015         | ☹                 | SI                | 047         | /         | 079         | O         | 111         | o         |
| 016         | ▲                 | DLE               | 048         | 0         | 080         | P         | 112         | p         |
| 017         | ▼                 | DC1               | 049         | 1         | 081         | Q         | 113         | q         |
| 018         | ↺                 | DC2               | 050         | 2         | 082         | R         | 114         | r         |
| 019         | ↻                 | DC3               | 051         | 3         | 083         | S         | 115         | s         |
| 020         | ↷                 | DC4               | 052         | 4         | 084         | T         | 116         | t         |
| 021         | ↶                 | NAK               | 053         | 5         | 085         | U         | 117         | u         |
| 022         | ↵                 | SYN               | 054         | 6         | 086         | V         | 118         | v         |
| 023         | ↹                 | ETB               | 055         | 7         | 087         | W         | 119         | w         |
| 024         | ↻                 | CAN               | 056         | 8         | 088         | X         | 120         | x         |
| 025         | ↷                 | EM                | 057         | 9         | 089         | Y         | 121         | y         |
| 026         | ↶                 | SUB               | 058         | :         | 090         | Z         | 122         | z         |
| 027         | ↵                 | ESC               | 059         | ;         | 091         | [         | 123         | {         |
| 028         | (cursor right)    | FS                | 060         | <         | 092         | \         | 124         |           |
| 029         | (cursor left)     | GS                | 061         | =         | 093         | ]         | 125         | }         |
| 030         | (cursor up)       | RS                | 062         | >         | 094         | ^         | 126         | ~         |
| 031         | (cursor down)     | US                | 063         | ?         | 095         | _         | 127         | ␣         |

# Computer Science Building West Wall





# Interpretation: Code and Data (Hello World!)



- Programs consist of Code and Data
- Code and Data are Encoded in Bits

```
00000000: 7f45 4c46 0201 0100 0000 0000 0000 0000  .ELF.....
...
00000260: 5002 0000 0000 0000 006c 6962 632e 736f  P.....libc.so
00000270: 2e36 2e31 0070 7269 6e74 6600 5f5f 6c69  .6.l.printf._li
00000280: 6263 5f73 7461 7274 5f6d 6169 6e00 474c  bc_start_main.GL
00000290: 4942 435f 322e 3200 0000 0200 0200 0000  IBC_2.2.....
...
00000860: 4865 6c6c 6f20 576f 726c 6421 0d00 0000  Hello world!...
...
40000000000000690 <main>:
40000000000000690: 00 10 15 08 80 05      [MII]    alloc r34=ar.pfs,5,4,0
40000000000000696: 30 02 30 00 42 20      mov r35=r12
4000000000000069c: 04 00 c4 00            mov r33=b0
400000000000006a0: 0a 20 81 03 00 24      [MMI]    addl r36=96,r1;;
400000000000006a6: 40 02 90 30 20 00      ld8 r36=[r36]
400000000000006ac: 04 08 00 84            mov r32=r1
400000000000006b0: 1d 00 00 00 01 00      [MFB]    nop.m 0x0
400000000000006b6: 00 00 00 02 00 00      nop.f 0x0
400000000000006bc: b8 fd ff 58            br.call.sptk.many b0=40000000000000460;;
400000000000006c0: 00 08 00 40 00 21      [MII]    mov r1=r32
400000000000006c6: 80 00 00 00 42 00      mov r8=r0
400000000000006cc: 20 02 aa 00            mov.i ar.pfs=r34
400000000000006d0: 00 00 00 00 01 00      [MII]    nop.m 0x0
400000000000006d6: 00 08 05 80 03 80      mov b0=r33
400000000000006dc: 01 18 01 84            mov r12=r35
400000000000006e0: 1d 00 00 00 01 00      [MFB]    nop.m 0x0
400000000000006e6: 00 00 00 02 00 80      nop.f 0x0
400000000000006ec: 08 00 84 00            br.ret.sptk.many b0;;
```

IA-64 Binary (objdump)

# Interpretation: Numbers



- Base 10
  - Each digit represents a power of 10
  - $4173 = 4 \times 10^3 + 1 \times 10^2 + 7 \times 10^1 + 3 \times 10^0$
- Base 2
  - Each bit represents a power of 2
  - $10110 = 1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 = 22$

Divide repeatedly by 2 and keep remainders

$$\begin{aligned}
 12/2 &= 6 & R &= 0 \\
 6/2 &= 3 & R &= 0 \\
 3/2 &= 1 & R &= 1 \\
 1/2 &= 0 & R &= 1 \\
 \text{Result} &= 1100
 \end{aligned}$$

# Writing Bits is Tedious for People



- Octal (base 8)
  - Digits 0, 1, ..., 7
  - In C: 00, 01, ..., 07
- Hexadecimal (base 16)
  - Digits 0, 1, ..., 9, A, B, C, D, E, F
  - In C: 0x0, 0x1, ..., 0xf

|          |          |
|----------|----------|
| 0000 = 0 | 1000 = 8 |
| 0001 = 1 | 1001 = 9 |
| 0010 = 2 | 1010 = A |
| 0011 = 3 | 1011 = B |
| 0100 = 4 | 1100 = C |
| 0101 = 5 | 1101 = D |
| 0110 = 6 | 1110 = E |
| 0111 = 7 | 1111 = F |

Thus the 16-bit binary number

1011 0010 1010 1001

converted to hex is

B2A9

# Interpretation: Colors



- Three primary colors
  - Red
  - Green
  - Blue
- Strength
  - 8-bit number for each color (e.g., two hex digits)
  - So, 24 bits to specify a color

• In HTML, on the course Web page

- Red: `<font color="#FF0000"><i>Symbol Table Assignment Due</i></font>`
- Blue: `<font color="#0000FF"><i>Fall Recess</i></font>`

• Same thing in digital cameras

- Each pixel is a mixture of red, green, and blue

## Binary Representation of Integers



- Fixed number of bits in memory

- char: 8 bits
- short: usually 16 bits
- int: 16 or 32 bits
- long: 32 bits
- long long: 64 bits

| Binary | Decimal           |
|--------|-------------------|
| 0      | 0                 |
| 1      | 1                 |
| 10     | 2                 |
| 11     | 3                 |
| 100    | 4                 |
| 101    | 5                 |
| 110    | 6                 |
| 111    | 7                 |
| 1000   | 8                 |
| ...    | ...               |
| 1{n}   | 2 <sup>n</sup> -1 |

- Unsigned integers

- Always positive or 0
- All arithmetic is modulo 2<sup>n</sup>
- unsigned char
- unsigned short
- unsigned int
- unsigned long
- unsigned long long

## Size and Overflow in Unsigned Integers



| Bits | Integer Range                  |
|------|--------------------------------|
| 8    | 0 - 255                        |
| 16   | 0 - 65,535                     |
| 32   | 0 - 4,294,967,295              |
| 64   | 0 - 18,446,744,073,709,551,615 |

| Binary | Decimal           |
|--------|-------------------|
| 0      | 0                 |
| 1      | 1                 |
| 10     | 2                 |
| ...    | ...               |
| 1{n}   | 2 <sup>n</sup> -1 |

Number of bits determines unsigned integer range

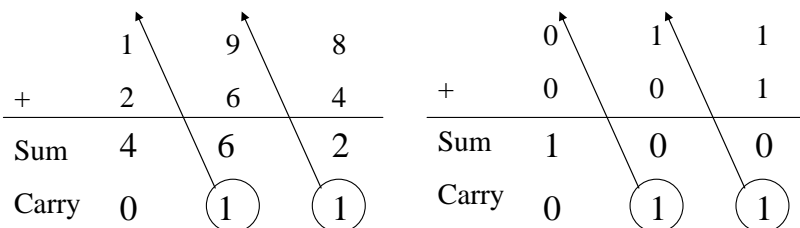
Overflow:

- 8-bit integer → 11111111<sub>2</sub> (255<sub>10</sub>)
- Add 1
- What happens?

## Adding Two Integers: Base 10



- From right to left, we add each pair of digits
- We write the sum, and add the carry to the next column



## Binary Sums and Carries



|   |   |     |
|---|---|-----|
| a | b | Sum |
| 0 | 0 | 0   |
| 0 | 1 | 1   |
| 1 | 0 | 1   |
| 1 | 1 | 0   |

|   |   |       |
|---|---|-------|
| a | b | Carry |
| 0 | 0 | 0     |
| 0 | 1 | 0     |
| 1 | 0 | 0     |
| 1 | 1 | 1     |

XOR

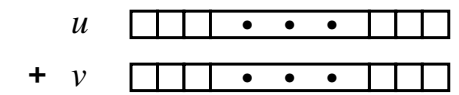
AND

$$\begin{array}{r}
 0100\ 0101 \leftarrow 69 \\
 + 0110\ 0111 \leftarrow 103 \\
 \hline
 1010\ 1100 \leftarrow 172
 \end{array}$$

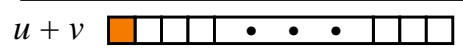
## Overflow in Unsigned Addition



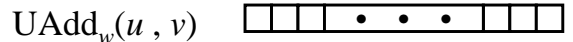
Operands:  $w$  bits



True Sum:  $w + 1$  bits



Discard Carry:  $w$  bits



$$UAdd_w(u, v) = \begin{cases} u + v & u + v < 2^w \\ u + v - 2^w & u + v \geq 2^w \end{cases}$$

Modulo Arithmetic:  $UAdd_w(u, v) = u + v \bmod 2^w$

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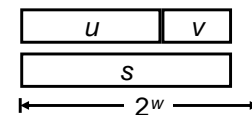
## Detecting Unsigned Overflow



### • Task:

- Given  $s = UAdd_w(u, v)$
- Determine if  $s = u + v$

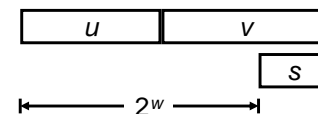
No Overflow:



### • Claim:

- Overflow iff  $s < u$
- ovf =  $(s < u)$
- By symmetry iff  $s < v$

Overflow:



### • Proof:

- $0 \leq v < 2^w$
- No overflow  $\Rightarrow s = u + v \geq u + 0 = u$
- Overflow  $\Rightarrow s = u + v - 2^w < u + 0 = u$

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## Modulo Arithmetic



### • Consider only numbers in a range

- E.g., five-digit car odometer: 0, 1, ..., 99999
- E.g., eight-bit numbers 0, 1, ..., 255

### • Roll-over when you run out of space

- E.g., car odometer goes from 99999 to 0, 1, ...
- E.g., eight-bit number goes from 255 to 0, 1, ...

### • Adding $2^n$ doesn't change the answer

- For eight-bit number,  $n=8$  and  $2^n=256$
- E.g.,  $(37 + 256) \bmod 256$  is simply 37

### • This can help us do subtraction...

- Suppose you want to compute  $a - b$
- Note that this equals  $a + (256 - 1 - b) + 1$

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## Modulo Arithmetic



### Modulo Addition Forms an Abelian Group

#### • Closed under addition

- $0 \leq UAdd_w(u, v) \leq 2^w - 1$

#### • Commutative

- $UAdd_w(u, v) = UAdd_w(v, u)$

#### • Associative

- $UAdd_w(t, UAdd_w(u, v)) = UAdd_w(UAdd_w(t, u), v)$

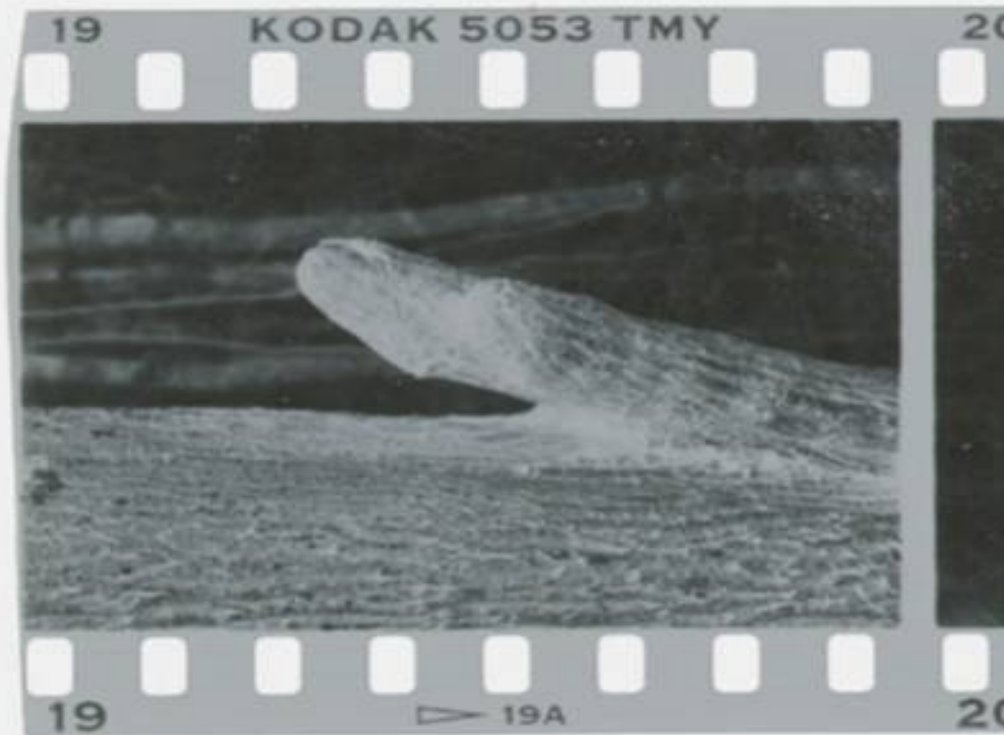
#### • 0 is additive identity

- $UAdd_w(u, 0) = u$

#### • Every element has additive inverse

- Let  $UComp_w(u) = 2^w - u$
- $UAdd_w(u, UComp_w(u)) = 0$

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(negatives...)

## What about Negative Numbers?



| Bits | Patterns                   |
|------|----------------------------|
| 8    | 256                        |
| 16   | 65,536                     |
| 32   | 4,294,967,296              |
| 64   | 18,446,744,073,709,551,616 |

| Binary | Pattern        |
|--------|----------------|
| 0      | 1              |
| 1      | 2              |
| 10     | 3              |
| ...    | ...            |
| 1{n}   | 2 <sup>n</sup> |

- We have been looking at **unsigned numbers**
- What about negative or **signed numbers**?
- Need new interpretation of bits
- Some patterns interpreted as negative numbers

## Key Standard Pattern Assignments



| Bit Pattern | Sign Magnitude | One's Complement | Two's Complement |
|-------------|----------------|------------------|------------------|
| 000         | +0             | +0               | 0                |
| 001         | +1             | +1               | +1               |
| 010         | +2             | +2               | +2               |
| 011         | +3             | +3               | +3               |
| 100         | -0             | -3               | -4               |
| 101         | -1             | -2               | -3               |
| 110         | -2             | -1               | -2               |
| 111         | -3             | -0               | -1               |

- Which one is best?
  - Balance
  - Zeros
  - Ease of operations

## Most Common: Two's Complement



| Bit Pattern | Two's Complement |
|-------------|------------------|
| 000         | 0                |
| 001         | +1               |
| 010         | +2               |
| 011         | +3               |
| 100         | -4               |
| 101         | -3               |
| 110         | -2               |
| 111         | -1               |

- “Invert and Add 1” to negate
- Sign Bit
- Zeros, Range
- What about arithmetic?

# Unsigned and Two's Complement



## Unsigned Values

$$B2U(X) = \sum_{i=0}^{w-1} x_i \cdot 2^i$$

• **UMin** = 0

• **UMax** =  $2^w - 1$

## Two's Complement

$$B2T(X) = -x_{w-1} \cdot 2^{w-1} + \sum_{i=0}^{w-2} x_i \cdot 2^i$$

• **TMin** =  $-2^{w-1}$

• **TMax** =  $2^{w-1} - 1$

Values for  $W = 16$

|      | Decimal | Hex   | Binary            |
|------|---------|-------|-------------------|
| UMax | 65535   | FF FF | 11111111 11111111 |
| TMax | 32767   | 7F FF | 01111111 11111111 |
| TMin | -32768  | 80 00 | 10000000 00000000 |
| -1   | -1      | FF FF | 11111111 11111111 |
| 0    | 0       | 00 00 | 00000000 00000000 |



# Sizes and C Data Types

| C Data Type | MIPS, x86 | Alpha   |
|-------------|-----------|---------|
| char        | 8 bits    | 8 bits  |
| short       | 16 bits   | 16 bits |
| int         | 32 bits   | 32 bits |
| long int    | 32 bits   | 64 bits |

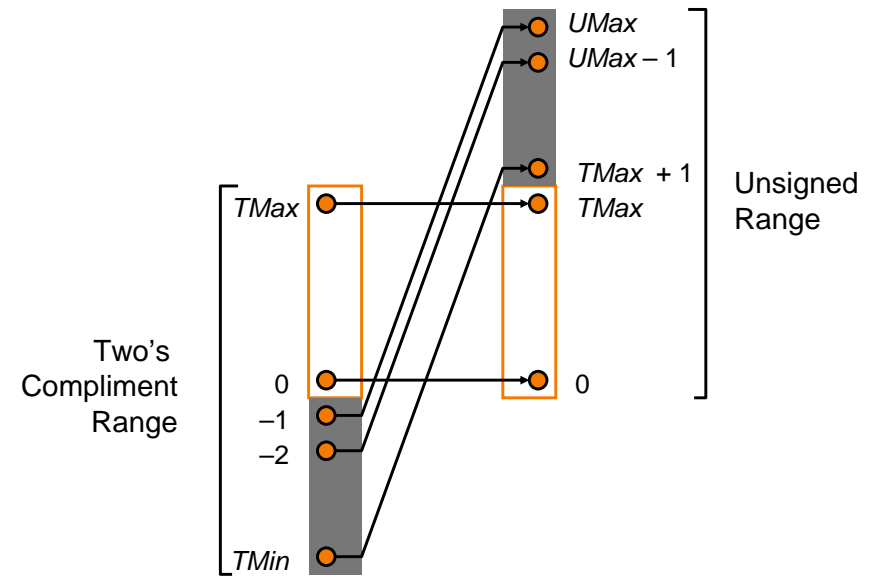
char, short, int, long int

- Refer to number of bits of integer
- Most machines: signed two's complement

unsigned <type>

- Same number of bits as signed counterparts
- Unsigned integer

# Representation Relationship



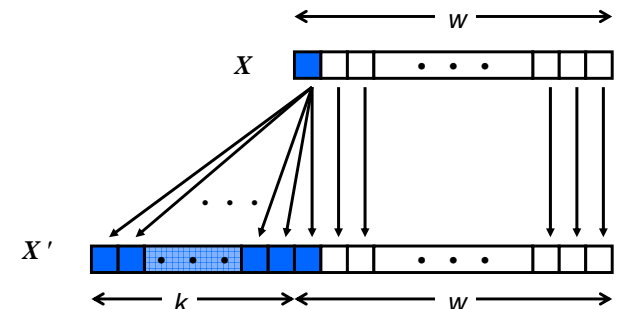
# Sign Extension



```
char minusFour = -4;
short moreBits;
moreBits = (short) minusFour;
```

Given  $w$  bit signed integer, return equivalent  $w+k$  bit signed integer

Sign Extend:

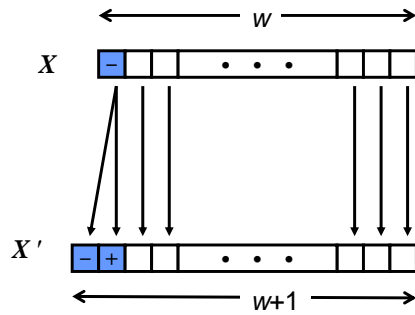


# Sign Extension

## Proof of Correctness Outline



- Prove Correctness by Induction on  $k$
- Induction Step: extending by single bit maintains value

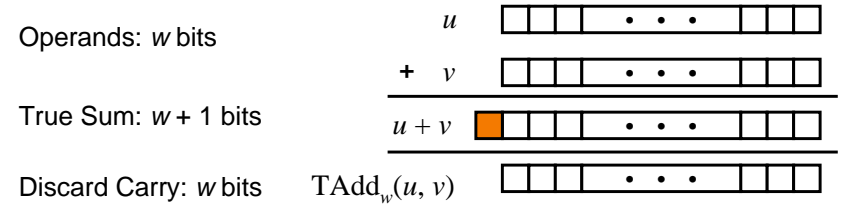


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# Two's Complement Addition



- TAdd and UAdd have identical Bit-Level Behavior!

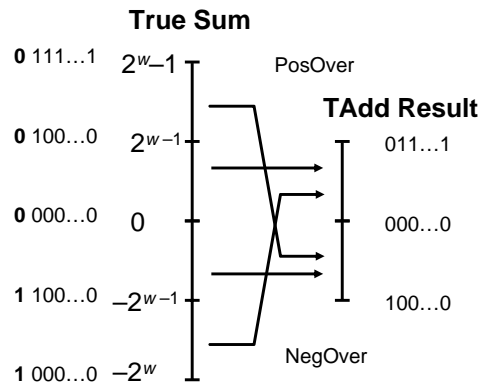
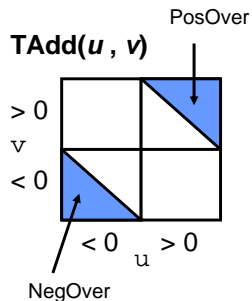


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# Characterizing TAdd



- True sum requires  $w+1$  bits
- Drop MSB



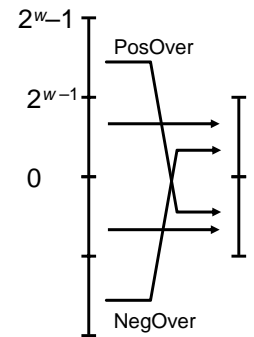
$$TAdd_w(u, v) = \begin{cases} u + v + 2^{w-1} & u + v < TMin_w \text{ (NegOver)} \\ u + v & TMin_w \leq u + v \leq TMax_w \\ u + v - 2^{w-1} & TMax_w < u + v \text{ (PosOver)} \end{cases}$$

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# Detecting Two's Complement Overflow



- Task:
  - Given  $s = TAdd_w(u, v)$
  - Determine if  $s = Add_w(u, v)$
- Claim:
  - Overflow iff either:
    - $u, v < 0, s \geq 0$  (NegOver)
    - $u, v \geq 0, s < 0$  (PosOver)
  - $ovf = (u < 0 == v < 0) \ \&\& \ (u < 0 != s < 0)$ ;



- Proof:
  - Obviously, if  $u \geq 0$  and  $v < 0$ , then  $TMin_w \leq u + v \leq TMax_w$
  - Symmetrically if  $u < 0$  and  $v \geq 0$
  - Other cases from analysis of TAdd

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## Negation vs. Inversion



### Inversion:

- A bit-wise operation
- Flip all 0's to 1's and vice versa: 0011 => 1100
- What does this do to the two's complement value?

### Negation:

- Two's complement: invert all bits and add 1
- Example:

$$3_{10} = 0011$$

$$\text{invert}(0011) + 1 \rightarrow 1100 + 1 \rightarrow 1101$$

$$1101 = -3_{10}$$

## Two's Complement Negation



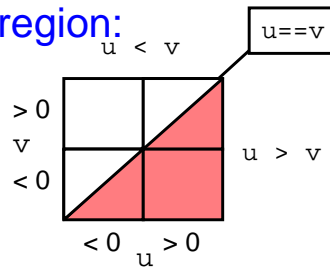
- Mostly like Integer Negation
  - $\text{TComp}(u) = -u$
- TMin is Special Case
  - $\text{TComp}(\text{TMin}) = \text{TMin}$
  - Note Also:  $\text{TComp}(0) = 0$
- Negation in C ( $x = -x;$ ) is Actually TComp

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## Comparing Two's Complements



- Given signed numbers  $u, v$
- Determine whether or not  $u > v$
- Return true for shaded region:



- **Bad Approach:**
  - Test  $(u - v) > 0$
  - Problem: Thrown off by Overflow

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## Representation: A Collection of Bits



- Treat unsigned int as a collection 32 independent bits
- Good for tracking 32 individual binary conditions
  - True/False
  - Yes/No
  - Black/White
- Can also treat unsigned in as:
  - 16 2-bit values
  - 8 4-bit values
  - 4 8-bit values
  - 8 1-bit value, 4 2-bit values, 2 4-bit values, and 1 8-bit value

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## Bitwise Operators: AND and OR



### • Bitwise AND (&)

|   |   |   |
|---|---|---|
| & | 0 | 1 |
| 0 | 0 | 0 |
| 1 | 0 | 1 |

### • Bitwise OR (|)

|   |   |   |
|---|---|---|
|   | 0 | 1 |
| 0 | 0 | 1 |
| 1 | 1 | 1 |

- Mod on the cheap!
  - E.g.,  $h = 53 \& 15$ ;

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|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 0 | 0 | 1 | 1 | 0 | 1 | 0 | 1 |
|---|---|---|---|---|---|---|---|

& 15 

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 |
|---|---|---|---|---|---|---|---|

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|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 |
|---|---|---|---|---|---|---|---|

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## Bitwise Operators: Not and XOR



### • One's complement (~)

- Turns 0 to 1, and 1 to 0
- E.g., set last three bits to 0
  - $x = x \& \sim 7$ ;

### • XOR (^)

- 0 if both bits are the same
- 1 if the two bits are different

|   |   |   |
|---|---|---|
| ^ | 0 | 1 |
| 0 | 0 | 1 |
| 1 | 1 | 0 |

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## Bitwise Operators: Shift Left/Right



### • Shift left (<<): Multiply by powers of 2

- Shift some # of bits to the left, filling the blanks with 0

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|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 0 | 0 | 1 | 1 | 0 | 1 | 0 | 0 |
|---|---|---|---|---|---|---|---|

53<<2 

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 |
|---|---|---|---|---|---|---|---|

### • Shift right (>>): Divide by powers of 2

- Shift some # of bits to the right
  - For unsigned integer, fill in blanks with 0
  - What about signed integers? Varies across machines...
    - Can vary from one machine to another!

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|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 0 | 0 | 1 | 1 | 0 | 1 | 0 | 0 |
|---|---|---|---|---|---|---|---|

53>>2 

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 1 | 1 | 0 | 1 |
|---|---|---|---|---|---|---|---|

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## Count Number of 1s in an Integer



### • Function bitcount(unsigned x)

- Input: unsigned integer
- Output: number of bits set to 1 in the binary representation of x

### • Main idea

- Isolate the last bit and see if it is equal to 1
- Shift to the right by one bit, and repeat

```
int bitcount(unsigned int x) {
    int b;
    for (b = 0; x != 0; x >>= 1)
        if (x & 1)
            b++;
    return b;
}
```

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## XOR Encryption



- Program to encrypt text with a key
  - Input: original text in stdin
  - Output: encrypted text in stdout
- Use the same program to decrypt text with a key
  - Input: encrypted text in stdin
  - Output: original text in stdout
- Basic idea
  - Start with a key, some 8-bit number (e.g., 0110 0111)
  - Do an operation that can be inverted
    - E.g., XOR each character with the 8-bit number

|             |             |
|-------------|-------------|
| 0100 0101   | 0010 0010   |
| ^ 0110 0111 | ^ 0110 0111 |
| -----       | -----       |
| 0010 0010   | 0100 0101   |

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## XOR Encryption, Continued



- But, we have a problem
  - Some characters are control characters
  - These characters don't print
- So, let's play it safe
  - If the encrypted character would be a control character
  - ... just print the original, unencrypted character
  - Note: the same thing will happen when decrypting, so we're okay
- C function `isctr1()`
  - Returns true if the character is a control character

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## XOR Encryption, C Code



```
#define KEY '&'
int main(void) {
    int orig_char, new_char;

    while ((orig_char = getchar()) != EOF) {
        new_char = orig_char ^ KEY;
        if (isctr1(new_char))
            putchar(orig_char);
        else
            putchar(new_char);
    }
    return 0;
}
```

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## Stupid Programmer Tricks



- Where do I use bitwise & most?
  - Bit vectors
- What's a bit vector?
  - Lots of booleans packed into an int/long
  - Often used to indicate some condition(s)
  - Less storage space than lots of fields
  - More explicit storage than compiled-defined bit fields

- Your compiler can do this?

```
typedef struct Blah {
    int b_onoff:1;
    int b_temperature:7;
    char b_someChar;
}
```

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# Example From Real Code



```
• #define DONTCACHE_REQNOSTORE      0x000001
• #define DONTCACHE_AUTHORIZED      0x000002
• #define DONTCACHE_MISSINGVARIANTHDR 0x000004
• #define DONTCACHE_USERORPASS      0x000008
• #define DONTCACHE_BYPASSFILTER     0x000010
• #define DONTCACHE_NONCACHEMETHOD 0x000020
• #define DONTCACHE_CTLPRIVATE       0x000040
• #define DONTCACHE_CTLNOSTORE      0x000080
• #define DONTCACHE_ISQUERY         0x000100
• #define DONTCACHE_EARLYEXPIRE     0x000200
• #define DONTCACHE_NOLASTMOD       0x000400
• #define DONTCACHE_NONEGCACHING    0x000800
• #define DONTCACHE_INSTANTEXPIRE   0x001000
• #define DONTCACHE_FILETOOBIG      0x002000
• #define DONTCACHE_FILEGREWTOOBIG  0x004000
• #define DONTCACHE_ICPPROXYONLY    0x008000
• #define DONTCACHE_LARGEFILEBLAST  0x010000
• #define DONTCACHE_PERSISTLOGLOADING 0x020000
• #define DONTCACHE_NEWERCOPYEXISTS  0x040000
• #define DONTCACHE_BADVARYFIELDS    0x080000
• #define DONTCACHE_SETCOOKIE       0x100000
• #define DONTCACHE_HTTPSTATUSCODE  0x200000
• #define DONTCACHE_OBJECTINCOMPLETE 0x400000
```

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# Conclusions



- Computer represents everything in binary
  - Integers, floating-point numbers, characters, addresses, ...
  - Pixels, sounds, colors, etc.
- Binary arithmetic through logic operations
  - Sum (XOR) and Carry (AND)
  - Two's complement for subtraction
- Binary operations in C
  - AND, OR, NOT, and XOR
  - Shift left and shift right
  - Useful for efficient and concise code, though sometimes cryptic

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