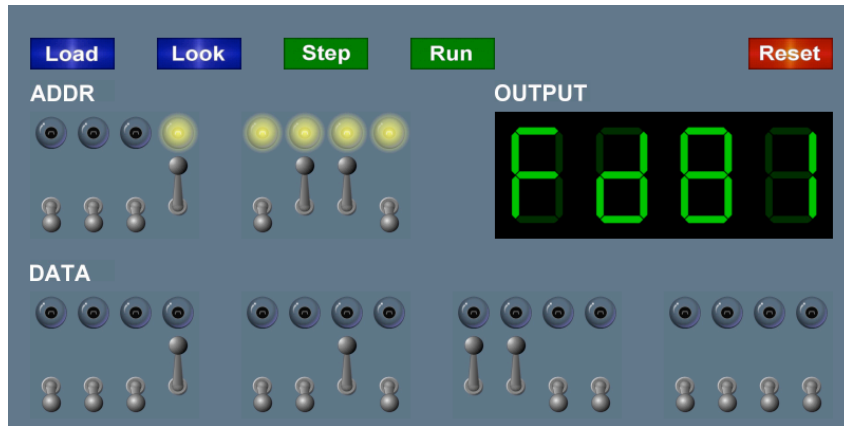


5: The TOY Machine

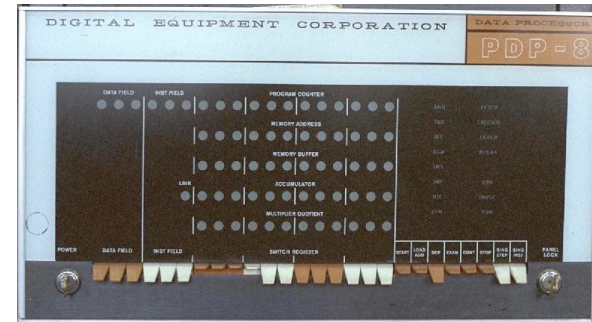


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What is TOY?

An imaginary machine similar to:

- Ancient computers.



2

What is TOY?

An imaginary machine similar to:

- Ancient computers.
- Today's microprocessors.



Pentium

Celeron

5

What is TOY?

An imaginary machine similar to:

- Ancient computers.
- Today's microprocessors.

Why study TOY?

- Machine language programming.
 - how do Java programs relate to computer?
 - key to understanding Java references (and C pointers)
- Computer architecture.
 - how is a computer put together?
 - how does it work?
- Optimized for understandability, not cost or performance.

6

Inside the Box

Switches. Input data and programs.

Lights. View data.

Memory.

- Stores data and programs.
- 256 "words." (16 bits each)
- Special word reserved for stdin / stdout.

Program counter (PC).

- An extra 8-bit register.
- Keeps track of next instruction to be executed.

Registers.

- Fastest form of storage.
- Scratch space during computation.
- 16 registers. (16 bits each)
- Register 0 is always 0.

Arithmetic-logic unit (ALU). Manipulate data stored in registers.

Standard input, standard output.

Interact with outside world.

Data and Programs Are Encoded in Binary

Each bit consists of two states:

- Switch is ON or OFF.
- High voltage or low voltage.
- 1 or 0.
- True or false.

Dec	Bin	Dec	Bin
0	0000	8	1000
1	0001	9	1001
2	0010	10	1010
3	0011	11	1011
4	0100	12	1100
5	0101	13	1101
6	0110	14	1110
7	0111	15	1111

How to represent integers?

- Use binary encoding.
- Ex: $6375_{10} = 0001100011100111_2$

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	0	0	1	1	0	0	0	1	1	1	0	0	1	1	1

$$\begin{aligned}
 6375_{10} &= +2^{12} +2^{11} && +2^7 +2^6 +2^5 && +2^2 +2^1 +2^0 \\
 &= 4096 +2048 && +128 +64 +32 && +4 +2 +1
 \end{aligned}$$

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Shorthand Notation

Use hexadecimal (base 16) representation.

- Binary code, four bits at a time.
- Ex: $6375_{10} = 0001100011100111_2 = 18E7_{16}$

Dec	Bin	Hex	Dec	Bin	Hex
0	0000	0	8	1000	8
1	0001	1	9	1001	9
2	0010	2	10	1010	A
3	0011	3	11	1011	B
4	0100	4	12	1100	C
5	0101	5	13	1101	D
6	0110	6	14	1110	E
7	0111	7	15	1111	F

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	0	0	1	1	0	0	0	1	1	1	0	0	1	1	1
1				8				E				7			

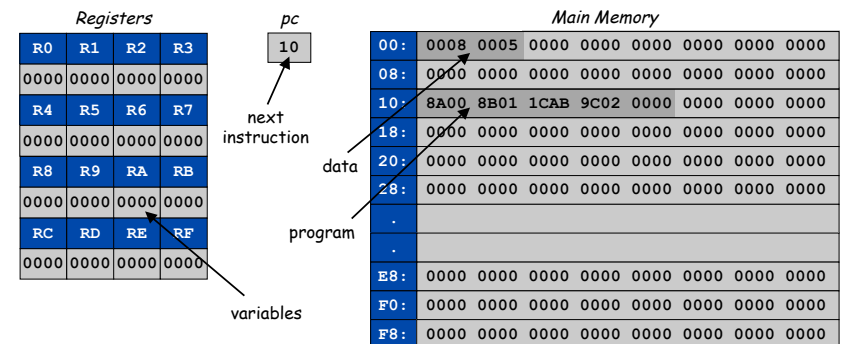
$$\begin{aligned}
 6375_{10} &= 1 \times 16^3 + 8 \times 16^2 + 14 \times 16^1 + 7 \times 16^0 \\
 &= 4096 + 2048 + 224 + 7
 \end{aligned}$$

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Machine "Core" Dump

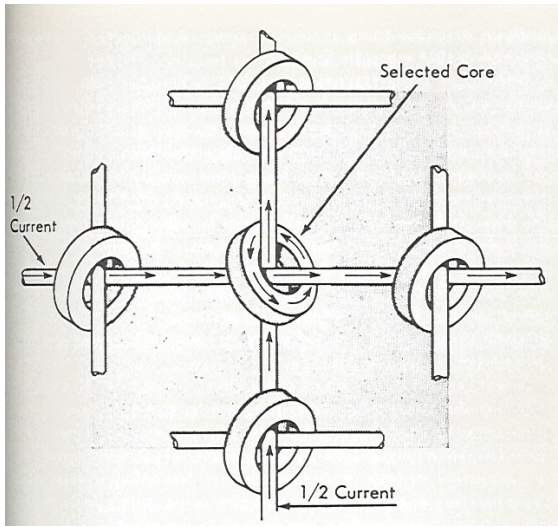
Machine contents at a particular place and time.

- Record of what program has done.
- Completely determines what machine will do.



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Why do they call it "core"?



Reference: <http://www.columbia.edu/acis/history/core.html>

A Sample Program

A sample program.

- Adds $8 + 5 = D$.

RA	RB	RC
0000	0000	0000

Registers

pc
10

00:	0008	8	add.toy
01:	0005	5	
02:	0000	0	
10:	8A00	RA	← mem[00]
11:	8B01	RB	← mem[01]
12:	1CAB	RC	← RA + RB
13:	9C02	mem[02]	← RC
14:	0000	halt	

Memory

Since PC = 10, machine interprets 8A00 as an instruction.

Load

Load. (opcode 8)

- Loads the contents of some memory location into a register.
- 8A00 means load the contents of memory cell 00 into register A.

RA	RB	RC	pc
0000	0000	0000	10

Registers

00:	0008	8	add.toy
01:	0005	5	
02:	0000	0	
10:	8A00	RA	← mem[00]
11:	8B01	RB	← mem[01]
12:	1CAB	RC	← RA + RB
13:	9C02	mem[02]	← RC
14:	0000	halt	

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
1	0	0	0	1	0	1	0	0	0	0	0	0	0	0	0
8 ₁₆				A ₁₆				00 ₁₆							
opcode				dest d				addr							

Load

Load. (opcode 8)

- Loads the contents of some memory location into a register.
- 8B01 means load the contents of memory cell 01 into register B.

RA	RB	RC	pc
0008	0000	0000	11

Registers

00:	0008	8	add.toy
01:	0005	5	
02:	0000	0	
10:	8A00	RA	← mem[00]
11:	8B01	RB	← mem[01]
12:	1CAB	RC	← RA + RB
13:	9C02	mem[02]	← RC
14:	0000	halt	

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
1	0	0	0	1	0	1	1	0	0	0	0	0	0	0	1
8 ₁₆				B ₁₆				01 ₁₆							
opcode				dest d				addr							

Add

Add. (opcode 1)

- Add contents of two registers and store sum in a third.
- 1CAB means add the contents of registers A and B and put the result into register C.

RA	RB	RC	pc
0008	0005	0000	12

Registers

00: 0008	8	add.toy
01: 0005	5	
02: 0000	0	
10: 8A00	RA ← mem[00]	
11: 8B01	RB ← mem[01]	
12: 1CAB	RC ← RA + RB	
13: 9C02	mem[02] ← RC	
14: 0000	halt	

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0	0	0	1	1	1	0	0	1	0	1	0	1	0	1	1
1 ₁₆				C ₁₆				A ₁₆				B ₁₆			
opcode				dest d				source s				source t			

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Store

Store. (opcode 9)

- Stores the contents of some register into a memory cell.
- 9C02 means store the contents of register C into memory cell 02.

RA	RB	RC	pc
0008	0005	000D	13

Registers

00: 0008	8	add.toy
01: 0005	5	
02: 0000	0	
10: 8A00	RA ← mem[00]	
11: 8B01	RB ← mem[01]	
12: 1CAB	RC ← RA + RB	
13: 9C02	mem[02] ← RC	
14: 0000	halt	

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
1	0	0	1	1	1	0	0	0	0	0	0	0	0	1	0
9 ₁₆				C ₁₆				02 ₁₆							
opcode				dest d				addr							

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Halt

Halt. (opcode 0)

- Stop the machine.

RA	RB	RC	pc
0008	0005	000D	14

Registers

00: 0008	8	add.toy
01: 0005	5	
02: 000D	D	
10: 8A00	RA ← mem[00]	
11: 8B01	RB ← mem[01]	
12: 1CAB	RC ← RA + RB	
13: 9C02	mem[02] ← RC	
14: 0000	halt	

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Program and Data

Program: Sequence of instructions.

16 instruction types:

- 16-bit word (interpreted one way).
- Changes contents of registers, memory, and PC in specified, well-defined ways.

Data:

- 16-bit word (interpreted other way).

Program counter (PC):

- Holds memory address of "next instruction."

Instructions

→ 0:	halt
→ 1:	add
2:	subtract
3:	and
4:	xor
5:	shift left
6:	shift right
7:	load address
→ 8:	load
→ 9:	store
A:	load indirect
B:	store indirect
C:	branch zero
D:	branch positive
E:	jump register
F:	jump and link

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TOY Instruction Set Architecture

TOY instruction set architecture (ISA).

- Interface that specifies behavior of machine.
- 16 register, 256 words of main memory, 16-bit words.
- 16 instructions.

Each instruction consists of 16 bits.

- Bits 12-15 encode one of 16 instruction types or opcodes.
- Bits 8-11 encode destination register *d*.
- Bits 0-7 encode:
 - Format 1: source registers *s* and *t*
 - Format 2: 8-bit memory address or constant

	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	
Format 1	1	0	1	1	1	0	1	0	0	0	0	0	0	0	1	0	0
	opcode				dest <i>d</i>			source <i>s</i>				source <i>t</i>					
Format 2	opcode				dest <i>d</i>			addr									

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Interfacing with the TOY Machine

To enter a program or data:

- Set 8 memory address switches.
- Set 16 data switches.
- Press LOAD.
 - data written into addressed word of memory

To view the results of a program:

- Set 8 memory address switches.
- Press LOOK: contents of addressed word appears in lights.



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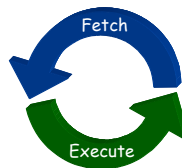
Using the TOY Machine: Run

To run the program:

- Set 8 memory address switches to address of first instruction.
- Press LOOK to set PC to first instruction.
- Press RUN button to repeat fetch-execute cycle until halt opcode.

Fetch-execute cycle.

- FETCH:** get instruction from memory.
- EXECUTE:** update PC, move data to or from memory and registers, perform calculations.



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Programming in TOY

Hello, World. Add two numbers.

To harness the power of TOY, need loops and conditionals.

- Manipulate PC to control program flow.

Branch if zero. (opcode C)

- Changes PC depending of value of some register.
- Used to implement: `for`, `while`, `if-else`.

Branch if positive. (opcode D)

- Analogous.

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An Example: Multiplication

Multiply.

- No direct support in TOY hardware.
- Load in integers a and b, and store $c = a \times b$.
- Brute-force algorithm:
 - initialize $c = 0$
 - add b to c, a times

```
int a = 3;
int b = 9;
int c = 0;

while (a != 0) {
    c = c + b;
    a = a - 1;
}
```

Java

Issues ignored: slow, overflow, negative numbers.

Multiply

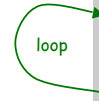
```
0A: 0003 3 ← inputs
0B: 0009 9 ← inputs
0C: 0000 0 ← output

0D: 0000 0 ← constants
0E: 0001 1 ← constants

10: 8A0A RA ← mem[0A]      a
11: 8B0B RB ← mem[0B]      b
12: 8C0D RC ← mem[0D]      c = 0

13: 810E R1 ← mem[0E]      always 1

14: CA18 if (RA == 0) pc ← 18
15: 1CCB RC ← RC + RB
16: 2AA1 RA ← RA - R1
17: C014 pc ← 14
18: 9C0C mem[0C] ← RC
19: 0000 halt
```



multiply.toy

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Step-By-Step Trace

		R1	RA	RB	RC
10: 8A0A	RA ← mem[0A]		0003		
11: 8B0B	RB ← mem[0B]			0009	
12: 8C0D	RC ← mem[0D]				0000
13: 810E	R1 ← mem[0E]	0001			
14: CA18	if (RA == 0) pc ← 18				
15: 1CCB	RC ← RC + RB				0009
16: 2AA1	RA ← RA - R1		0002		
17: C014	pc ← 14				
14: CA18	if (RA == 0) pc ← 18				
15: 1CCB	RC ← RC + RB				0012
16: 2AA1	RA ← RA - R1		0001		
17: C014	pc ← 14				
14: CA18	if (RA == 0) pc ← 18				
15: 1CCB	RC ← RC + RB				001B
16: 2AA1	RA ← RA - R1		0000		
17: C014	pc ← 14				
14: CA18	if (RA == 0) pc ← 18				
18: 9C0C	mem[0C] ← RC				
19: 0000	halt				

multiply.toy

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An Efficient Multiplication Algorithm

Inefficient multiply.

- Brute force multiplication algorithm loops a times.
- In worst case, 65,535 additions!

"Grade-school" multiplication.

- Always 16 additions to multiply 16-bit integers.

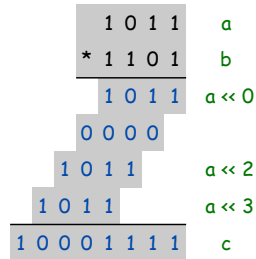
Decimal	<pre> 1 2 3 4 * 1 5 1 2 ----- 2 4 6 8 6 1 7 0 1 2 3 4 ----- 0 1 8 6 5 8 0 8</pre>	Binary	<pre> 1 0 1 1 * 1 1 0 1 ----- 1 0 1 1 0 0 0 0 1 0 1 1 1 0 1 1 ----- 1 0 0 0 1 1 1 1</pre>
---------	--	--------	--

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Binary Multiplication

Grade school binary multiplication algorithm to compute $c = a \times b$.

- Initialize $c = 0$.
- Loop over i bits of b . $\leftarrow b_i = i^{\text{th}}$ bit of b
 - if $b_i = 0$, do nothing
 - if $b_i = 1$, shift a left i bits and add to c



Implement with built-in TOY shift instructions.

```

int c = 0;
for (int i = 15; i >= 0; i--)
    if (((b >> i) & 1) == 1)
        c = c + (a << i);
  
```

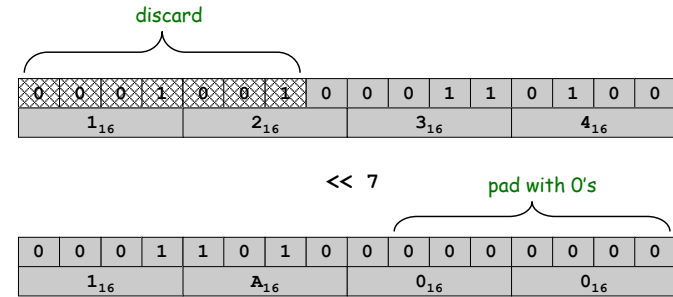
$\leftarrow b_i = i^{\text{th}}$ bit of b

29

Shift Left

Shift left. (opcode 5)

- Move bits to the left, padding with zeros as needed.
- $1234_{16} \ll 7_{16} = 1A00_{16}$

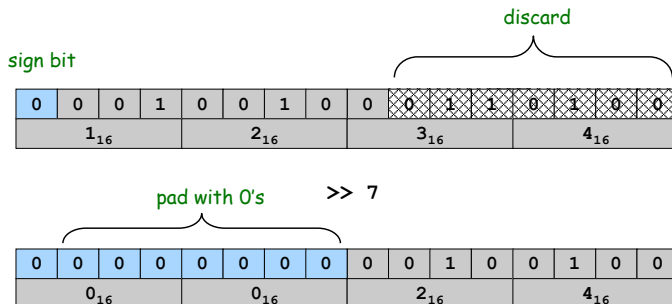


30

Shift Right

Shift right. (opcode 6)

- Move bits to the right, padding with sign bit as needed.
- $1234_{16} \gg 7_{16} = 0024_{16}$



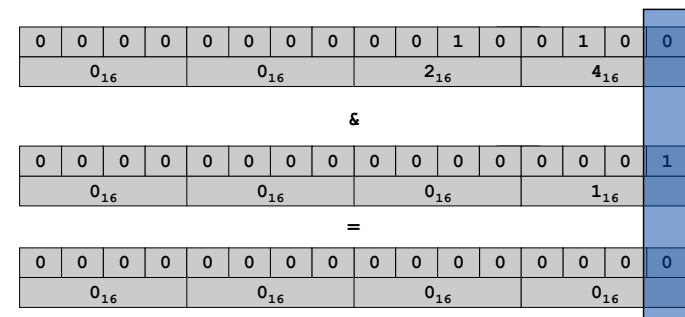
31

Bitwise AND

Logical AND. (opcode B)

- Logic operations are BITWISE.
- $0024_{16} \& 0001_{16} = 0000_{16}$

x	y	AND
0	0	0
0	1	0
1	0	0
1	1	1

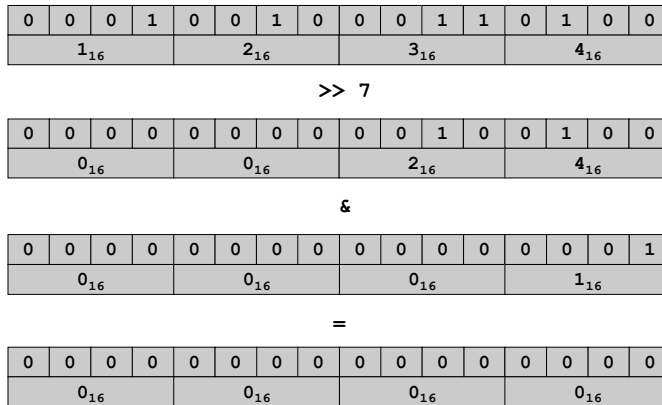


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Shifting and Masking

Shift and mask: get the 7th bit of 1234.

- Compute $1234_{16} \gg 7_{16} = 0024_{16}$.
- Compute $0024_{16} \&\& 1_{16} = 0_{16}$.



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Binary Multiplication

0A: 0007	3		← inputs	
0B: 0008	9		← output	
0C: 0000	0			
0D: 0000	0			
0E: 0001	1		← constants	
0F: 0010	16			
10: 8A0A	RA	← mem[0A]		a
11: 8B0B	RB	← mem[0B]		b
12: 8C0D	RC	← mem[0D]		c = 0
13: 810E	R1	← mem[0E]		always 1
14: 820F	R2	← mem[0F]		i = 16 ← 16 bit words
15: 2221	R2	← R2 - R1		do {
16: 53A2	R3	← RA << R2		i--
17: 64B2	R4	← RB >> R2		a << i
18: 3441	R4	← R4 & R1		b >> i
19: C41B		if (R4 == 0) goto 1B		<i>b_i</i> = <i>i</i> th bit of b
1A: 1CC3	RC	← RC + R3		if <i>b_i</i> is 1
1B: D215		if (R2 > 0) goto 15		add a << i to sum
				} while (i > 0);
1C: 9C0C	mem[0C]	← RC		multiply-fast.toy

Note: In the original image, a 'loop' arrow points from instruction 15 to 1B, and a 'branch' arrow points from 1B to 15.

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TOY Reference Card

	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
Format 1	opcode				dest d				source s				source t			
Format 2	opcode				dest d				addr							

#	Operation	Fmt	Pseudocode
0:	halt	1	exit(0)
1:	add	1	R[d] ← R[s] + R[t]
2:	subtract	1	R[d] ← R[s] - R[t]
3:	and	1	R[d] ← R[s] & R[t]
4:	xor	1	R[d] ← R[s] ^ R[t]
5:	shift left	1	R[d] ← R[s] << R[t]
6:	shift right	1	R[d] ← R[s] >> R[t]
7:	load addr	2	R[d] ← addr
8:	load	2	R[d] ← mem[addr]
9:	store	2	mem[addr] ← R[d]
A:	load indirect	1	R[d] ← mem[R[t]]
B:	store indirect	1	mem[R[t]] ← R[d]
C:	branch zero	2	if (R[d] == 0) pc ← addr
D:	branch positive	2	if (R[d] > 0) pc ← addr
E:	jump register	2	pc ← R[d]
F:	jump and link	2	R[d] ← pc; pc ← addr

Register 0 always 0.
Loads from mem[FF] from stdin.
Stores to mem[FF] to stdout.

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Useful TOY "Idioms"

Jump absolute.

- Jump to a fixed memory address.
 - branch if zero with destination
 - register 0 is always 0

17: C014 pc ← 14

Register assignment.

- No instruction that transfers contents of one register into another.
- Pseudo-instruction that simulates assignment:
 - add with register 0 as one of two source registers

17: 1230 R[2] ← R[3]

No-op.

- Instruction that does nothing.
- Plays the role of whitespace in C programs.
 - numerous other possibilities!

17: 1000 no-op

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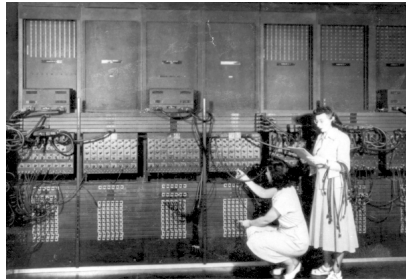
A Little History

Electronic Numerical Integrator and Calculator (ENIAC).

- First widely known general purpose electronic computer.
- 30 tons, 30 x 50 x 8.5 ft, 17,468 vacuum tubes, 300 multiply/sec.
- Conditional jumps, programmable.
- Programming: change switches and cable connections.
- Data: enter numbers using punch cards.



John Mauchly (left) and J. Presper Eckert (right)
http://cs.swau.edu/~durkin/articles/history_computing.html



ENIAC, Ester Gerston (left), Gloria Gordon (right)
US Army photo: <http://ftp.arl.mil/ftp/historic-computers>

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Basic Characteristics of TOY Machine

TOY is a general-purpose computer.

- Sufficient power to perform ANY computation.
- Limited only by amount of memory and time.

Stored-program computer. (von Neumann memo, 1944)

- Data and instructions encoded in binary.
- Data and instructions stored in SAME memory.
- Can change program without rewiring.

Outgrowth of Alan Turing's work. (stay tuned)

All modern computers are general-purpose computers and have same (von Neumann) architecture.



John von Neumann



Maurice Wilkes (left)
EDSAC (right)

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