# Computer Science 341 

Discrete Mathematics
Problem Session 8
Mon, Nov 18, 2002

## Problem 1

Prove the "exchange property" for trees: Let $T$ and $T^{\prime}$ be spanning trees in $G(V, E)$. Given any $e^{\prime} \in T^{\prime}-T$, there exists an edge $e \in T-T^{\prime}$ such that $(T-\{e\}) \cup\left\{e^{\prime}\right\}$ is also a spanning tree.

## Problem 2

Draw $K_{4,5}$ on the surface of a double torus (i.e. sphere with two handles) such that no lines cross.

## Problem 3

Find the number $j$ such that removing any set of $j$ edges from $K_{6}$ yields a non-planar graph (prove this direction), but there exist a set of edges of size $(j+1)$ such that removing it results in a planar graph (give the set of edges and the planar embedding for this direction).

