

Princeton University

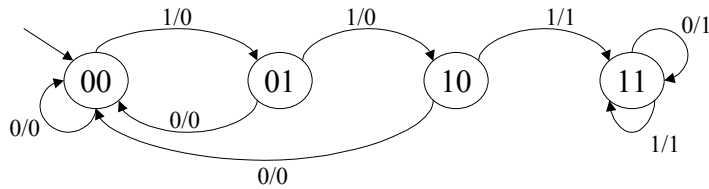
COS 217: Introduction to Programming Systems

A “111” Detector Sequential Circuit

Description

Repeatedly accept one input. Repeatedly produce one output. The output should be 0 until/unless a sequence of three contiguous 1's is detected. Thereafter the output should be 1.

State Machine



Truth Table

A	B	x	next A	next B	y
0	0	0	0	0	0
0	0	1	0	1	0
0	1	0	0	0	0
0	1	1	1	0	0
1	0	0	0	0	0
1	0	1	1	1	1
1	1	0	1	1	1
1	1	1	1	1	1

Boolean Expression

$$\begin{aligned} \text{next A} &= (\sim A \ \& \ B \ \& \ x) \ | \ (A \ \& \ \sim B \ \& \ x) \ | \ (A \ \& \ B \ \& \ \sim x) \ | \ (A \ \& \ B \ \& \ x) \\ \text{next B} &= (\sim A \ \& \ \sim B \ \& \ x) \ | \ (A \ \& \ \sim B \ \& \ x) \ | \ (A \ \& \ B \ \& \ \sim x) \ | \ (A \ \& \ B \ \& \ x) \\ y &= (A \ \& \ \sim B \ \& \ x) \ | \ (A \ \& \ B \ \& \ \sim x) \ | \ (A \ \& \ B \ \& \ x) \end{aligned}$$

Circuit

(See reverse)